

### **Constraints**

Martha Hoffmann Session 4 RLI, 18.09.2019







#### **Introducing words**



# Inner workings of oemof: Linear optimization and constraints

All workshop contents at: <a href="https://github.com/smartie2076/oemof\_workshop">https://github.com/smartie2076/oemof\_workshop</a>
Todays jupyter notebooks are stored in <a href="mailto:\_Oemof\_workshop">\_Oemof\_workshop</a>



Introduction to linear optimization Linear equation systems of oemof models **In-build oemof constraints Introducing own constraints Further examples for constraints** 



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#### An introduction to linear optimization



- Example: <u>./3\_LP\_general\_example.ipynb</u>
- ► Linear Problem (LP) / Mixed Integer (Linear) Problem (MI(L)P) consists of :
  - a target function
  - a set of constraints and balances
- Solver searches on the edges of the solutions space for the optimal solution
- Available solvers: CBC, GLPK, Gurobi, ...
- ► Time steps adjustable (e.g. 15 mins, hourly)



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#### Linear equation system generated by oemof



## A set of linear equations fully describes an energy system model as a whole

#### The "lp-file"



- ► Linear equation system describes energy system fully
  - generated using Pyomo package
  - can be stored in "lp-file"
- ► The "Ip-file" is transferred to solver for optimization
  - Recommended solver: coinor-cbc
  - Same file can be optimized with different solvers
- ► Lp-file can help to verify and debug your code
- Example: <u>./micro\_grid\_fixed\_cap\_basic.ipynb</u>

#### The "lp-file": Objective value



► The objective value should be minimized:

```
min
objective:
+0.03955047913155272 GenericInvestmentStorageBlock_invest(storage)
+0.022175440918742569 InvestmentFlow_invest(genset_electricity_bus)
+0.034350422598754829 InvestmentFlow_invest(pv_electricity_bus)
+0.091601126930012891 InvestmentFlow_invest(wind_electricity_bus)
+0.063761955366631234 flow(diesel_fuel_bus_0)
+0.063761955366631234 flow(diesel_fuel_bus_1)
+0.063761955366631234 flow(diesel_fuel_bus_2)
+0.063761955366631234 flow(diesel_fuel_bus_3)
+0.063761955366631234 flow(diesel_fuel_bus_4)
```

#### Optimizing with oemof - Objective value



- Oemof generates a linear equation system describing the energy system model
- Solves for the minimal objective value (costs)
- Target function:

$$\min \sum_{i} (Capex(i) * CRF(i) + Opex_{fix}(i)) * P_{inst}(i) + \sum_{i} \sum_{t} Opex_{var}(i) * E_{gen}(i,t)$$

$$i \in \{WEA, PV, BHKW, Speicher\}$$
  
 $t \in \{1...8760\}$ 

Capex	Capital expenditure	EUR/kW
$\operatorname{CRF}$	Capital recovery factor	-
$Opex_{fix}$	Fixed operational expenditure	EUR/(kW*a)
$Opex_{var}$	Variable operational expenditure	EUR/kWh
$P_{inst}$	Capacity of component	kW
$E_{gen}$	Generated electricity per timestep	$\mathrm{kWh}$
i	Index of system components	-
t	Index of time steps	-

#### The "lp-file": Bus balances



- ► Each bus is by default balanced:
  - $\blacktriangleright \sum inputs = \sum outputs \ \forall \ t$
  - ▶ le. no energy can be lost or generated from nowhere
  - ▶ Can require "shortage"-Source or "excess"-Sink

```
c_e_Bus_balance(fuel_bus_0)_:
+1 flow(diesel_fuel_bus_0)
-1 flow(fuel_bus_genset_0)
= 0
```

#### The "lp-file": Bus balances



- ► Each bus is by default balanced:
  - $\sum inputs = \sum outputs \ \forall \ t$
  - ▶ le. no energy can be lost or generated from nowhere
  - ▶ Can require "shortage"-Source or "excess"-Sink

```
c_e_Transformer_relation(genset_fuel_bus_electricity_bus_0)_:
+1 flow(fuel_bus_genset_0)
-3.030303030303030303 flow(genset_electricity_bus_0)
= 0

c_e_InvestmentFlow_fixed(wind_electricity_bus_0)_:
-0.31556899999999999 InvestmentFlow_invest(wind_electricity_bus)
+1 flow(wind_electricity_bus_0)
= 0
```

#### The "lp-file": Bus balances



- ► Each bus is by default balanced:
  - $\sum inputs = \sum outputs \ \forall \ t$
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```
c_e_Bus_balance(electricity_bus_0)_:
-1 flow(electricity_bus_excess_0)
-1 flow(electricity_bus_storage_0)
+1 flow(genset_electricity_bus_0)
+1 flow(pv_electricity_bus_0)
+1 flow(storage_electricity_bus_0)
+1 flow(wind_electricity_bus_0)
= 279.53099120000002
```



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**Further examples for constraints** 

#### In-build bounds of flows



- ▶ Bounds limit Flows to an interval
- ► Decreases search area for valid optimization results
- ► Examples:
  - ► Component parameters: min\_storage\_capacity, max\_storage capacity
  - ▶ Flow parameters: nominal value
  - ▶ Investment parameters: maximum

Example: ./micro\_grid\_system\_inbuilt\_bounds.ipynb

#### The "lp-file": Bounds



```
0 <= flow(wind_electricity_bus_4) <= +inf
0 <= InvestmentFlow_invest(electricity_bus_storage) <= +inf
0 <= InvestmentFlow_invest(genset_electricity_bus) <= +inf
0 <= InvestmentFlow_invest(pv_electricity_bus) <= 800
0 <= InvestmentFlow_invest(storage_electricity_bus) <= +inf
0 <= InvestmentFlow_invest(wind_electricity_bus) <= 500
0 <= GenericInvestmentStorageBlock_capacity(storage_0) <= +inf</pre>
```

```
c_u_GenericInvestmentStorageBlock_min_capacity(storage_0)_:
-1 GenericInvestmentStorageBlock_capacity(storage_0)
+0.20000000000000000 GenericInvestmentStorageBlock_invest(storage)
<= 0</pre>
```

#### **In-built constraints**



- ▶ Limit the sum of a Flow:  $\sum Flow \cdot variable = const$
- ► Indirectly decreases search area of optimization, acts like a "exit criterion of a loop"
- ► Examples:
  - ▶summed max
  - ▶emission\_limit

Example: ./micro\_grid\_fixed\_inbuild\_sum.ipynb

#### The "lp-file": Constraints





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#### **Guidelines for own constraints**



- ► Rules for own constraints:
  - Linearized behaviour
  - ▶ No no "if-then-relation" with other decision variables
- ► If-then relations can be implemented when accessing a definite timeseries of actual value

#### **Process of writing constraints**



- 1. Simplify real-world boundary to valid constraint
- 2. Determine structure of constraint:
  - Does the constraint have to be applied each time step individually?
  - ▶ Does the constraint concern Investment objects?
- 3. Create a constraint with a constraint rule, add directly to the linear model of the energy system using Pyomo
- 4. Verify your constraint by checking...
  - ▶ ...the lp-file (for few timesteps)
  - ...the results (fow a higher number of timesteps)

#### Renewable share constraint



- ► Type: Summed minimum
- ► Based on: Minimum renewable share limit (constant)

$$\sum P_{PV} + \sum P_{Wind} - r_{lim} \cdot \sum P_{demand} \ge 0$$

#### Micro grid stability constraint



- ► Type: Minimum bound per timestep
- ▶ Based on: Minimum stability limit (constant)

$$P_{DG}(t) + P_{pcc,cons} + (SOC(t) - SOC_{min}) \cdot CAP_{storage,kWh} \cdot Crate \cdot \eta_{discharge} \cdot \eta_{inv}$$

$$>= L_s \cdot (P_D(t) - P_{short}(t)) \quad \forall t$$

$$P_{DG}(t) + P_{pcc,cons} + CAP_{storage,kW} \cdot \eta_{inv} > = L_s \cdot (P_D(t) - P_{short}(t)) \quad \forall t$$

Custom constraint with bounded flows:
\_/micro\_grid\_custom\_constraint\_flows.ipynb

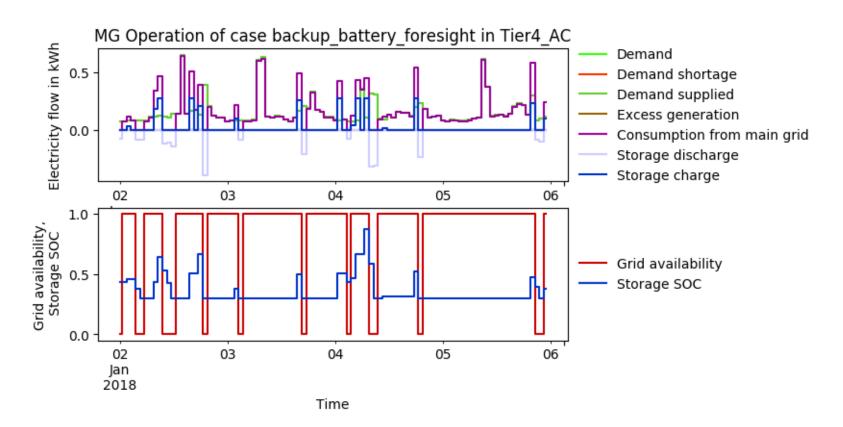


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#### Intermittantly switching off a component



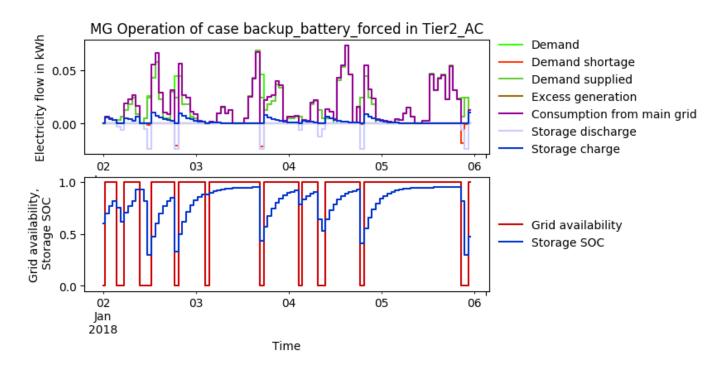
- ► Type: Setting flow value in timesteps
- ► Based on: External boolean timeseries



#### Forced battery charge



- ► Type: Setting flow per timestep
- ► Based on:
  - External boolean timeseries
  - Linerarized formular for value of flow





#### THANK YOU FOR YOUR ATTENTION!

#### How to follow Oemof's activities?

Website: https://oemof.org/

Github: https://github.com/oemof

Or join our mailing list!



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