

Logarithmic < polynomial < Exponential < Fact < Double exp

$$\sqrt{\log n}$$

$$(\log n)^2$$

$$2^{\log n} = n$$

$$2^n$$

$$(n!)!$$

$$2^{2^n}$$

$$\log(n!) = n \log n$$

$$n \log n$$

$$n^2$$

$$n^3$$

$$\log n \log^2 n = n^2$$

$$n \log \log n$$

$$(\log n)!$$

$$\log^{\log n} n$$

$$\log(n!) = \log(n(n-1) \dots 1)$$

$$= \log n + \log(n-1) + \dots + \log 1$$

$$\approx n \log n$$

$$\sqrt{\log n} < (\log n)^2 < \log(n!) < n \log n < n^2 < n^3 < 2^{\log n} < 2^n < (n!) < 2^{2^n}$$

$$(\log n)! < 2^n < (n!) < 2^{2^n}$$

$$\log n < n^2 < n^3 < 2^{\log n} < 2^n < \log n < n < \log \log n$$