

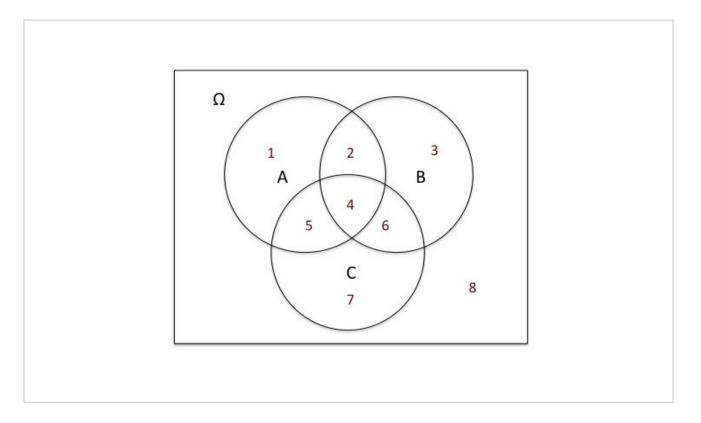
课程 > Unit 1: ... > Proble... > 1. Ven...

1. Venn diagrams

Problem 1. Venn diagrams

5.0/5.0 points (graded)

In this problem, you are given descriptions in words of certain events (e.g., "at least one of the events A, B, C occurs"). For each one of these descriptions, identify the correct symbolic description in terms of A,B,C from Events E1-E7 below. Also identify the correct description in terms of regions (i.e., subsets of the sample space Ω) as depicted in the Venn diagram below. (For example, Region 1 is the part of A outside of B and C.)



Symbolic descriptions:

• Event E1: $A \cap B \cap C$

• Event E2: $(A\cap B\cap C)^c$

• Event E3: $A\cap B\cap C^c$

- Event E4: $B \cup (B^c \cap C^c)$
- Event E5: $A^c \cap B^c \cap C^c$
- Event E6: $(A \cap B) \cup (A \cap C) \cup (B \cap C)$
- Event E7: $(A\cap B^c\cap C^c)\cup (A^c\cap B\cap C^c)\cup (A^c\cap B^c\cap C)$
 - 1. At least two of the events A, B, C occur.

Regions: 2 4 5 6 ▼ ✓ Answer: Regions: 2 4 5 6

2. At most two of the events A, B, C occur.

3. None of the events A, B, C occurs.

Event E5 ▼ **✓ Answer:** Event E5

Region: 8 ✓ Answer: Region: 8

4. All three events $\emph{\textbf{A}}$, $\emph{\textbf{B}}$, $\emph{\textbf{C}}$ occur.

Event E1 ▼ **✓ Answer:** Event E1

Region: 4 ✓ Answer: Region: 4

5. Exactly one of the events A, B, C occurs.

Regions: 1 3 7 **✓ Answer:** Regions: 1 3 7

6. Events $oldsymbol{A}$ and $oldsymbol{B}$ occur, but $oldsymbol{C}$ does not occur.

Event E3 ▼ **✓ Answer:** Event E3 Region: 2 ✓ Answer: Region: 2

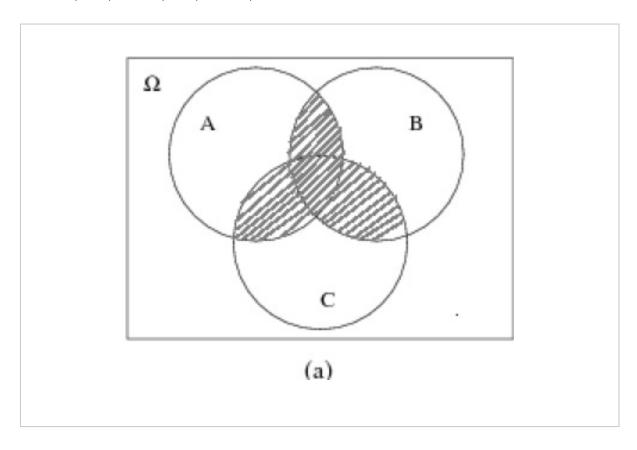
7. Either (i) event $oldsymbol{B}$ occurs, or (ii) neither $oldsymbol{B}$ or $oldsymbol{C}$ occurs.

Event E4 ▼ **✓ Answer:** Event E4

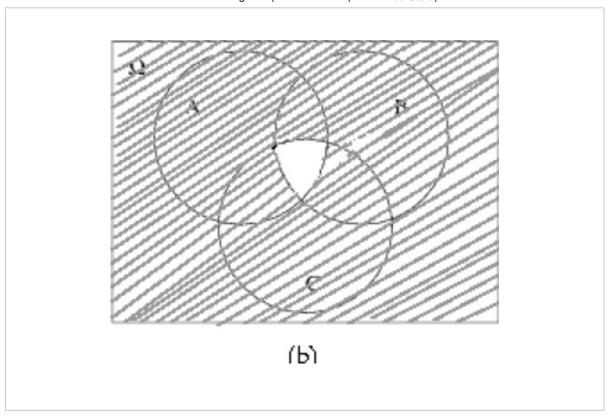
Regions: 1 2 3 4 6 8 **✓ Answer:** Regions: 1 2 3 4 6 8

Solution:

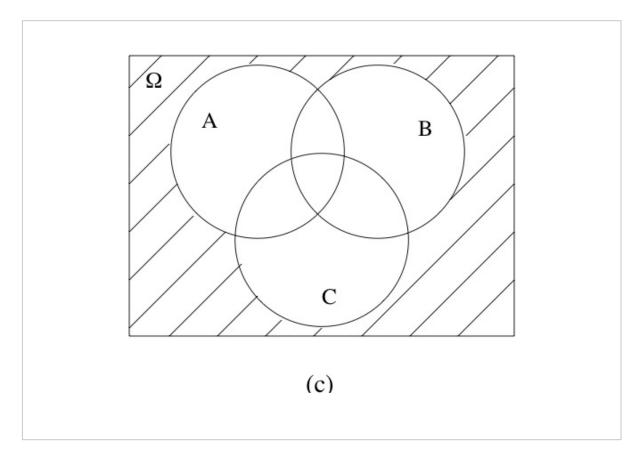
1. At least two of the events $\emph{\textbf{A}}$, $\emph{\textbf{B}}$, $\emph{\textbf{C}}$ occur: $(A \cap B) \cup (A \cap C) \cup (B \cap C)$



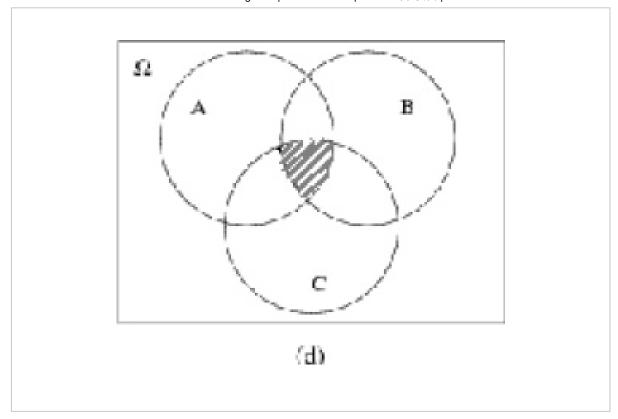
2. At most two of the events $\emph{\textbf{A}}$, $\emph{\textbf{B}}$, $\emph{\textbf{C}}$ occur: $(A\cap B\cap C)^c$



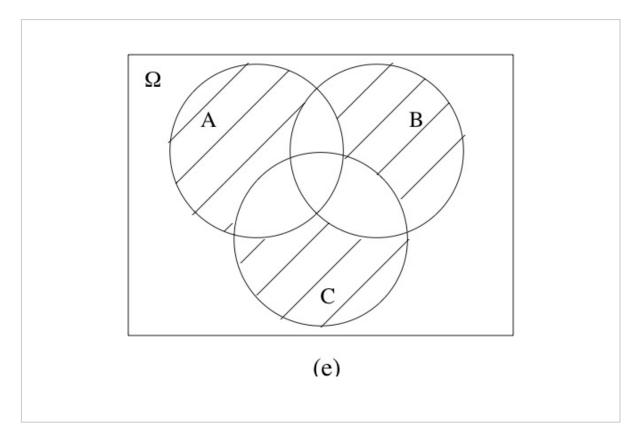
3. None of the events A, B, C occurs: $A^c \cap B^c \cap C^c$



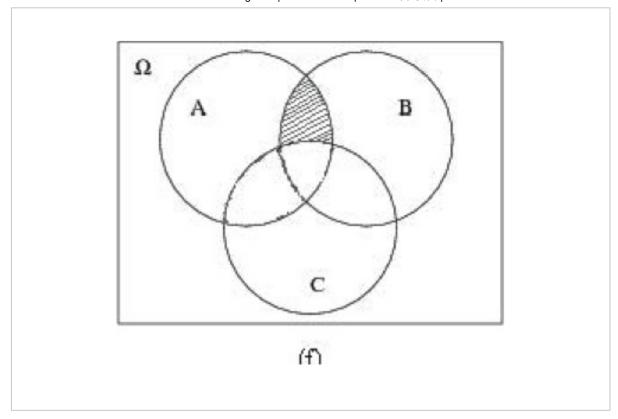
4. All three events $\emph{\textbf{A}}$, $\emph{\textbf{B}}$, $\emph{\textbf{C}}$ occur: $A \cap B \cap C$



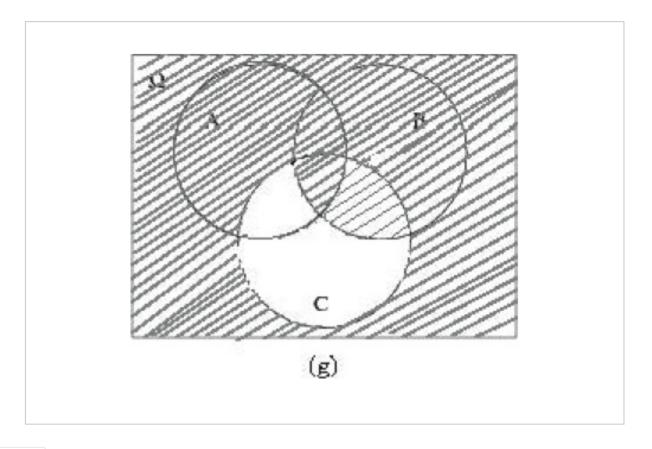
5. Exactly one of the events $\emph{\textbf{A}}$, $\emph{\textbf{B}}$, $\emph{\textbf{C}}$ occurs: $(A\cap B^c\cap C^c)\cup (A^c\cap B\cap C^c)\cup (A^c\cap B^c\cap C)$



6. Events A and B occur, but C does not occur: $A\cap B\cap C^c$



7. Either event B occurs or, if not, then C also does not occur: $B \cup (B^c \cap C^c)$



提交

You have used 1 of 3 attempts

