

## 5. Stochastic Gradient Descent

### Stochastic Gradient Descent



### Stochastic gradient descent (SGD)

$$J(\theta) = \frac{1}{n} \sum_{i=1}^n \left[ \text{Loss}_h(y^{(i)} \theta \cdot x^{(i)}) + \frac{\lambda}{2} \|\theta\|^2 \right]$$

Select  $i \in \{1, \dots, n\}$  at random

$$\theta \leftarrow \theta - \eta_t \nabla_{\theta} \left[ \text{Loss}_h(y^{(i)} \theta \cdot x^{(i)}) + \frac{\lambda}{2} \|\theta\|^2 \right]$$



And that update looks like the perceptron update,

but it is actually made even if we correctly classify the example.

If the example is within the margin boundaries,

you would get a non-zero loss.

So here, we have just a better way

of writing what that stochastic gradient descent update or SGD

update looks like.

update looks like.

8:06 / 8:06 1.25x

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### SGD and Hinge Loss

1/1 point (graded)

As we saw in the lecture above,

$$J(\theta, \theta_0) = \frac{1}{n} \sum_{i=1}^n \text{Loss}_h(y^{(i)} (\theta \cdot x^{(i)} + \theta_0)) + \frac{\lambda}{2} \|\theta\|^2 = \frac{1}{n} \left[ \sum_{i=1}^n \text{Loss}_h(y^{(i)} (\theta \cdot x^{(i)} + \theta_0)) + \frac{\lambda}{2} \|\theta\|^2 \right]$$

With stochastic gradient descent, we choose  $i \in \{1, \dots, n\}$  at random and update  $\theta$  such that

$$\theta \leftarrow \theta - \eta \nabla_{\theta} [\text{Loss}_h(y^{(i)} (\theta \cdot x^{(i)} + \theta_0)) + \frac{\lambda}{2} \|\theta\|^2]$$

What is  $\nabla_{\theta} [\text{Loss}_h(y^{(i)} (\theta \cdot x^{(i)} + \theta_0))]$  if  $\text{Loss}_h(y^{(i)} (\theta \cdot x^{(i)} + \theta_0)) > 0$ ?

☐  $y^{(i)} x^{(i)}$

☒  $-y^{(i)} x^{(i)}$  ✓

☐ 0

☐  $\lambda\theta$

☐  $-\lambda\theta$

Solution:

If  $\text{Loss}_h(y^{(i)}(\theta \cdot x^{(i)} + \theta_0)) > 0$ ,

$$\text{Loss}_h(y^{(i)}(\theta \cdot x^{(i)} + \theta_0)) = 1 - y^{(i)}(\theta \cdot x^{(i)} + \theta_0)$$


. Thus

$$\nabla_{\theta} \text{Loss}_h(y^{(i)}(\theta \cdot x^{(i)} + \theta_0)) = -y^{(i)}x^{(i)}$$

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You have used 1 of 3 attempts

 Answers are displayed within the problem


## Comparison with Perceptron

1/1 point (graded)  
Observing the update step of SGD,

$$\theta \leftarrow \theta - \eta \nabla_{\theta} [\text{Loss}_h(y^{(i)}(\theta \cdot x^{(i)} + \theta_0)) + \frac{\lambda}{2} ||\theta||^2]$$

Which of the following is true?

☐ As in perceptron,  $\theta$  is not updated when there is no mistake

☒ Differently from perceptron,  $\theta$  is updated even when there is no mistake 

Solution:


We can see from

$$\theta \leftarrow \begin{cases} (1 - \lambda\eta) \theta & \text{if Loss}=0 \\ (1 - \lambda\eta) \theta + \eta y^{(i)} x^{(i)} & \text{if Loss}>0 \end{cases}$$

that  $\theta$  is updated even when the sum of losses is 0. This is different from perceptron.

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## Discussion

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