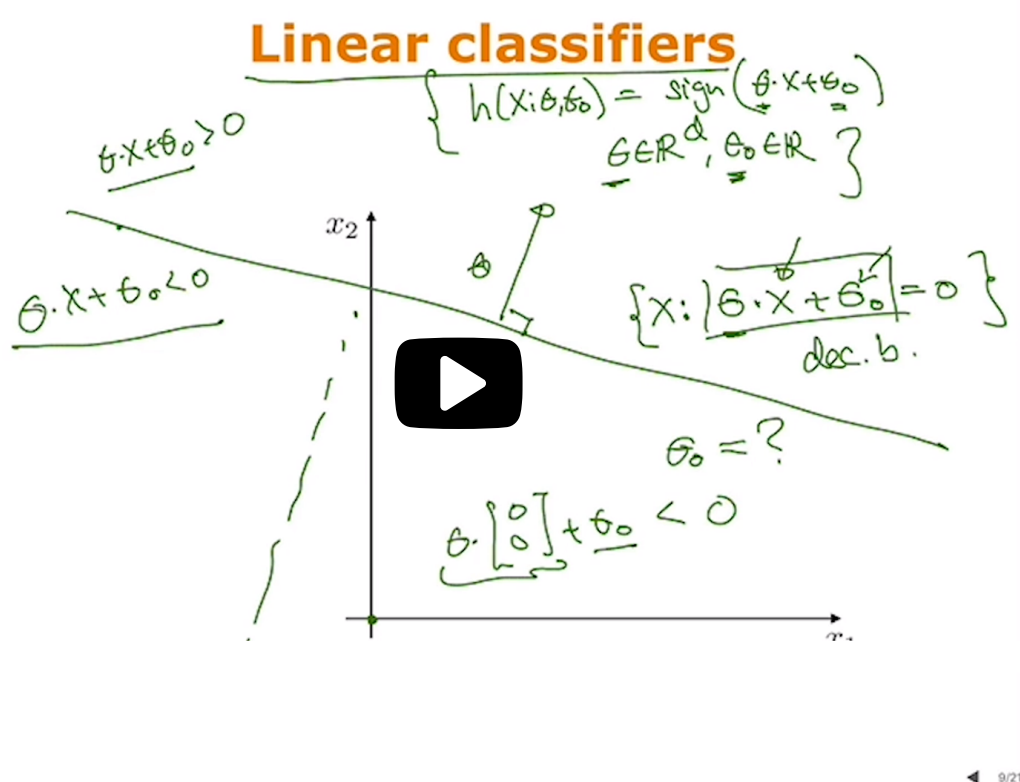


## 3. Linear Classifiers Mathematically Revised

### Linear Classifiers Mathematically Revised



lies on the negative side.

So this has to be negative, which implies, since this is now 0, that  $\theta_0$  itself is negative.

If we move this boundary in this direction past the origin,

$\theta_0$  would become positive.

That is the set of linear classifiers through origin

earlier and now the full set of linear classifiers.

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### Inner product and Orthogonal vectors

1/1 point (graded)

What is the inner product of  $[0, 1, 1]$  and  $[1, 1, 1]$ ?

✓ Answer: 2

#### Solution:

$$0 \cdot 1 + 1 \cdot 1 + 1 \cdot 1 = 2$$

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You have used 1 of 3 attempts

❗ Answers are displayed within the problem

### Linear Classifier Practice

1/1 point (graded)

We saw in the lecture above that for a linear classifier  $h$ ,  $h(x; \theta) = \text{sign}(\theta \cdot x)$ , i.e. the sign of the dot product of  $\theta$  and  $x$ . Now consider  $\theta$  which is given by

$$\theta = (1, -1)$$

(3.1)

Which of the following points would be classified as positive by  $\theta$ ? Please choose all correct answers.

☒  $(1, -1)$  ✓

☒  $(1, 0)$  ✓

☐  $(0, 1)$

☐  $(0, 0)$



Solution:

$X$  is positively classified by the classifier if and only if  $x \cdot \theta > 0$ . The dot product of  $(1, -1)$  with  $\theta$  is positive. Also,  $(1, 0) \cdot \theta$  is positive. On the other hand,  $(0, 1) \cdot \theta$  and  $(0, 0) \cdot \theta$  are nonpositive. Thus the first and second points are positively classified by  $\theta$ .

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You have used 1 of 3 attempts

**i** Answers are displayed within the problem

Offset Added

1/1 point (graded)  
Again, we have a linear classifier with  $\theta$  given by

$$\theta = (1, -1)$$

(3.2)

and the offset,  $\theta_0$  given by  $\theta_0 = -1$  Now which of the following points would be classified as positive by  $\theta$ ? Please choose all correct answers.

☒  $(1, -1)$  ✓

☐  $(1, 0)$

☐  $(0, 1)$

☐  $(0, 0)$



Solution:

$X$  is positively classified by the classifier if and only if  $x \cdot \theta + \theta_0 > 0$ . The dot product of  $(1, -1)$  with  $\theta$  is 2, and adding  $-1$  makes it still positive. However,  $x \cdot \theta + \theta_0 \leq 0$  for other data points.

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You have used 3 of 3 attempts

**i** Answers are displayed within the problem

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