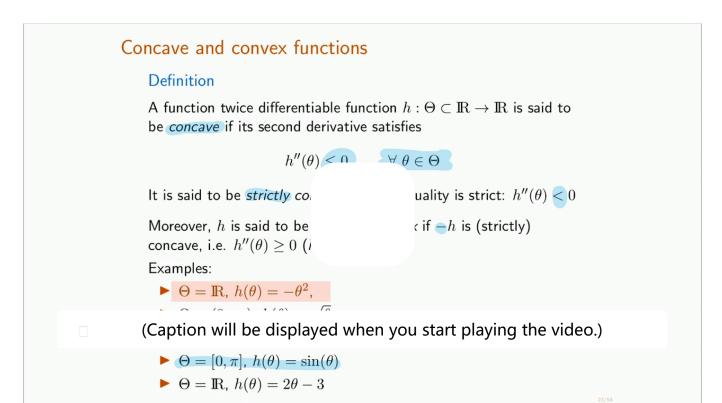


## 7. Worked examples: Concavity in 1 dimension Worked Examples: Concavity in 1 dimensions



Start of transcript. Skip to the end.

OK, so let's see some examples.

If I think of theta as being R, so now I think of the function, which is negative theta

what does this function look like?

1, 2, 3, 4, 5--

squared,

and let's get some space here--

6.

And what of those six shapes is negative theta squared?

## 视频

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## Review: 1D Optimization via Calculus

4/4 points (graded)

(For this problem, you are welcome to use any computational tools that would be helpful.)

Let 
$$f(x)=rac{1}{3}x^3-x^2-3x+10$$
 defined on the interval  $[-4,4]$ .

Let  $x_1$  and  $x_2$  be the critical points of f, and let's impose that  $x_1 < x_2$ . Fill in the next two boxes with the values of  $x_1$  and  $x_2$ , respectively: (Recall that the **critical points** of f are those f0 such that f'(f) = f1.)

$$x_1 = \boxed{ -1 }$$

$$x_2 = \boxed{3}$$

Fill in the next two boxes with the values of f "  $(x_1)$  and f "  $(x_2)$ , respectively:

$$f^{\prime\prime}\left( x_{2}
ight) =oxed{4}$$

提交

你已经尝试了1次 (总共可以尝试3次)

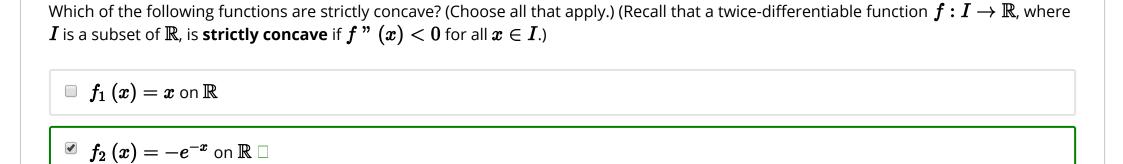
## (For this problem, you are welcome to use any computational tools that would be helpful.) Recall that $x_1$ and $x_2$ are the critical points of the function $f(x)=rac{1}{3}x^3-x^2-3x+10$ . According to the second derivative test, $m{x_1}$ is a ... Local Maximum Local Minimum None of the above and $oldsymbol{x_2}$ is a Local Maximum Local Minimum None of the above Where is the (global) minimum value of f(x) attained on the interval [-4,4]? -4 ☐ Answer: -4 Where is the (global) maximum value of f(x) attained on the interval [-4,4]? -1 ☐ Answer: -1 **Solution:** The previous problem implies that f is concave at $x_1$ and convex at $x_2$ , so $x_1$ is a **local maximum** and $x_2$ is a **local minimum**. To figure out the *global* extrema, we need to test the critical points as well as the endpoints: -4 and 4. We compute that $f(x_1) = rac{35}{3} pprox 11.6666, \quad f(x_2) = 1$ $f(-4) = -rac{46}{3} pprox -15.33333, \quad f(4) = 10/3 pprox 3.3333$ Hence the maximum value of f on [-4,4] is $\frac{35}{3} pprox 11.6666$ and the minimum value is $-\frac{46}{3} pprox -15.33333$ . **Remark:** It is very important to remember to test the endpoints when doing optimization. 你已经尝试了2次(总共可以尝试2次) 提交 Answers are displayed within the problem

Review: 1D Optimization via Calculus (Continued)

4/4 points (graded)

**Strict Concavity** 

1/1 point (graded)



**Solution:** 

 $lacksquare f_4\left(x
ight)=x^2$  on  $\mathbb R$ 

•  $f_{1}\left(x
ight)=x$  is **not** strictly concave because  $f_{1}$  "  $\left(x
ight)=0$ .

 $ilde{oldsymbol{arphi}} \; f_3\left(x
ight) = x^{0.99} \; ext{on the interval} \left(0,\infty
ight) \; \Box$ 

- $f_{2}\left(x
  ight)=-e^{-x}$  is strictly concave because  $f_{2}$  "  $\left(x
  ight)=-e^{-x}<0$  for all  $x\in\mathbb{R}.$
- $f_3\left(x
  ight)=x^{0.99}$  is strictly concave because  $f_3$  "  $\left(x
  ight)=\left(0.99
  ight)\left(-.01
  ight)x^{-1.01}<0$  for all  $x\in\left(0,\infty
  ight)$ .
- $f_4\left(x
  ight)=x^2$  is **not** strictly concave because  $f_4$  "  $\left(x
  ight)=2>0$ . In fact, this function is strictly *convex*.

提交

你已经尝试了1次 (总共可以尝试2次)

Answers are displayed within the problem

讨论

显示讨论

主题: Unit 3 Methods of Estimation:Lecture 9: Introduction to Maximum Likelihood Estimation / 7. Worked examples: Concavity in 1 dimension

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