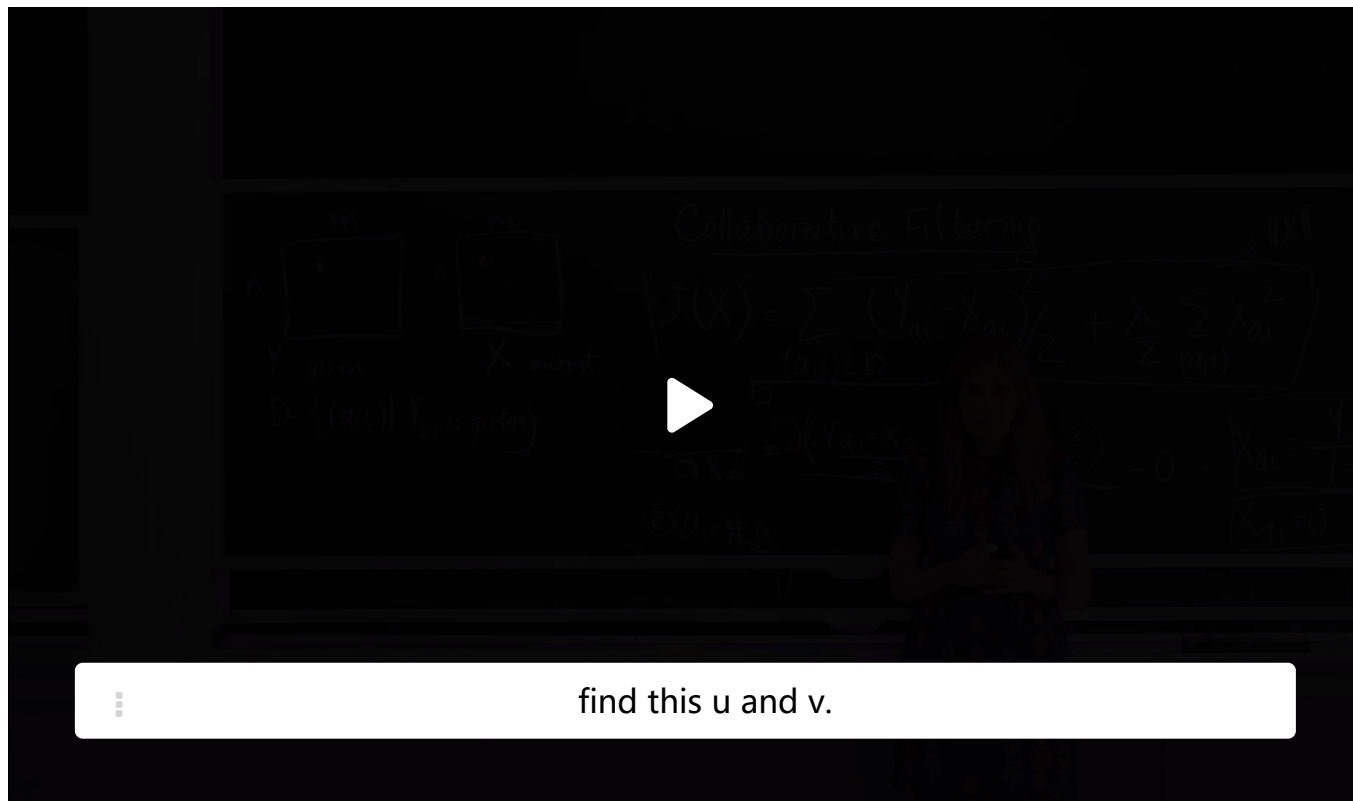


## 5. Collaborative Filtering with Matrix Factorization

### Collaborative Filtering with Matrix Factorization



same.

So now we will start by taking our objective, the original objective that we had, which is written over here--

we will take this objective and rewrite it for the case where our  $x$  is just the multiplication of two

vectors  $u$  and  $v$ . And once we've done that, our next question will be how we can actually

find this  $u$  and  $v$ .



[End of transcript. Skip to the start.](#)

#### Video

[Download video file](#)

#### Transcripts

[Download SubRip \(.srt\) file](#)

[Download Text \(.txt\) file](#)



## Matrix Factorization Practice

1/1 point (graded)

We now use **collaborative filtering** to solve the movie recommender system problem.

As we saw in the previous problem, we ended up with an unsatisfactory and trivial solution of  $X$  by minimizing the objective alone:

$$J(X) = \sum_{a,i \in D} \frac{(Y_{ai} - X_{ai})^2}{2} + \frac{\lambda}{2} \sum_{(a,i)} X_{ai}^2.$$

In the collaborative filtering approach, we impose an additional constraint on  $X$ :

$$X = UV^T$$

for some  $n \times d$  matrix  $U$  and  $d \times m$  matrix  $V^T$ . The number  $d$  is the **rank** of the matrix  $X$ .

Suppose

$$X = \begin{bmatrix} 3 & 6 & 3 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix},$$

then what is the minimum possible  $d$ ?

$d =$   ✔ Answer: 1

**Solution:**

$X$  can be decomposed as

$$X = \begin{bmatrix} 3 \\ 2 \\ 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 1 \end{bmatrix}$$

**Remark:** Note that imposing that a  $n$  by  $m$  matrix  $X$  has rank  $k < \min(m, n)$  means that some of its rows (*resp.* columns) are linearly dependent on other rows (*resp.* columns).

Submit

You have used 1 of 3 attempts

**i** Answers are displayed within the problem

### Intuition on the Vector Factors

1/1 point (graded)  
Assume we have a 3 by 2 matrix  $X$  i.e. we have 3 users and 2 movies. Also,  $X$  is given by

$$X = \begin{bmatrix} \text{User 1's rating on movie 1} & \text{User 1's rating on movie 2} \\ \text{User 2's rating on movie 1} & \text{User 2's rating on movie 2} \\ \text{User 3's rating on movie 1} & \text{User 3's rating on movie 2} \end{bmatrix} = UV^T$$

for some  $3 \times d$  matrix  $U$  and  $d \times 2$  matrix  $V^T$ .

Now which of the following is true about  $U$  and  $V^T$ ? (Choose all those apply. )

- ☒ The first row of  $U$  represents information on user 1's rating tendency ✔
- ☐ The first row of  $U$  represents information on movie 1
- ☐ The first column of  $V^T$  represents information on user 1's rating tendency
- ☒ The first column of  $V^T$  represents information on movie 1 ✔

✔

**Solution:**

$U$  encodes information about the users, and  $V$  about the movies.

Submit

You have used 1 of 3 attempts

**i** Answers are displayed within the problem

### Discussion

Show Discussion