Dependence - exercises

Exercise 1: Causal and statistical dependency.

For each of the following programs:

- Draw the dependency diagram (Bayes net). If you don't have software on your computer for doing this, Google Docs has a decent interface for creating drawings.
- Use informal evaluation order reasoning and the intervention method to determine causal dependency between A and B.
- Use conditioning to determine whether A and B are statistically dependent.

a)

```
var a = flip()

var b = flip()

var c = flip(a && b ? .8 : .5)
```

run ▼

b)

```
var a = flip()

var b = flip(a ? .9 : .2)

var c = flip(b ? .7 : .1)
```

run ▼

c)

```
var a = flip()

var b = flip(a ? .9 : .2)
```

```
var c = flip(a ? .7 : .1)
run ▼
d)
 var a = flip(.6)
 var c = flip(.1)
 var z = flip() ? a : c;
 var b = z ? 'foo' : 'bar'
run ▼
e)
 var examFairPrior = Bernoulli({p: .8})
 var doesHomeworkPrior = Bernoulli({p: .8})
 var examFair = mem(function(exam) {return sample(examFairPrior)})
 var doesHomework = mem(function(student) {return sample(doesHomeworkPrior)});
 var pass = function(student, exam) {
   return flip(examFair(exam) ?
                (doesHomework(student) ? .9 : .5) :
               (doesHomework(student) ? .2 : .1));
 }
 var a = pass('alice', 'historyExam');
 var b = pass('bob', 'historyExam');
```