

1. We expect  $\mathbf{E}[X]$  to be higher than  $\mathbf{E}[Y]$  since if we choose the student, we are more likely to pick a bus with more students.
2. To solve this problem formally, we first compute the PMF of each random variable and then compute their expectations.

The PMF of  $X$  is

$$p_X(x) = \begin{cases} 40/148, & x = 40, \\ 33/148, & x = 33, \\ 25/148, & x = 25, \\ 50/148, & x = 50, \\ 0, & \text{otherwise,} \end{cases}$$

$$\text{and } \mathbf{E}[X] = 40 \frac{40}{148} + 33 \frac{33}{148} + 25 \frac{25}{148} + 50 \frac{50}{148} = 39.28.$$

Similarly, the PMF of  $Y$  is

$$p_Y(y) = \begin{cases} 1/4, & y \in \{40, 33, 25, 50\}, \\ 0, & \text{otherwise,} \end{cases}$$

$$\text{and } \mathbf{E}[Y] = 40 \frac{1}{4} + 33 \frac{1}{4} + 25 \frac{1}{4} + 50 \frac{1}{4} = 37.$$

Clearly,  $\mathbf{E}[X] > \mathbf{E}[Y]$ .