

4. Parametric Hypothesis Testing - Clinical Trials

Clinical Trials

[Start of transcript. Skip to the end.](#)

Clinical trials

Let us go through an example to remind the main notions of hypothesis testing.

- ▶ Pharmaceutical companies use hypothesis testing to test if a new drug is efficient.
- ▶ To do so, they administer a group of patients (test group) and a placebo group (control group).
- ▶ We consider testing a drug that is supposed to lower LDL (low-density lipoprotein), a.k.a "bad cholesterol" among patients with a high level of LDL (above 200 mg/dL).

☐ (Caption will be displayed when you start playing the video.)

4/47

So let's start with parametric hypothesis testing, which is essentially the one that we've seen before.

And just to remind ourselves how we just go through the maneuver of building a test, let's start with a very concrete example which

is clinical trials.

All right.

视频

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Note : The following are problems we will use to prepare for the upcoming video.

Clinical Trials: Hypothesis Test

0/1 point (graded)

We consider the clinical trials set-up of the above video. Let X_1, \dots, X_n be i.i.d. test group samples distributed according to $\mathcal{N}(\Delta_d, \sigma_d^2)$ and let Y_1, \dots, Y_m be i.i.d. control group samples distributed according to $\mathcal{N}(\Delta_c, \sigma_c^2)$. Assume that $X_1, \dots, X_n, Y_1, \dots, Y_m$ are independent.

Select from the following all valid hypothesis test formulations to know if the drug has an effect on cholesterol levels (that is, we wish to know whether the drug has a statistically significant effect on the decrease in cholesterol levels when compared to the decrease in the cholesterol levels due to the placebo).

☐ $H_0 : \Delta_d = \Delta_c, H_1 : \Delta_d > \Delta_c$ ☐

☒ $H_0 : \Delta_d \leq \Delta_c, H_1 : \Delta_d > \Delta_c$ ☐

☐

Solution:

Both are valid formulations for this specific question that will lead to the same test.

提交

你已经尝试了1次 (总共可以尝试1次)

☐ Answers are displayed within the problem

Clinical Trials: Consequence of Gaussian Samples

0/1 point (graded)
We consider the same set-up as the above problem. Let X_1, \dots, X_n be i.i.d. test group samples distributed according to $\mathcal{N}(\Delta_d, \sigma_d^2)$ and let Y_1, \dots, Y_m be i.i.d. control group samples distributed according to $\mathcal{N}(\Delta_c, \sigma_c^2)$. Assume that $X_1, \dots, X_n, Y_1, \dots, Y_m$ are independent.

Select from the following all statements that are correct or true.

- ☒ $\overline{X}_n = \frac{X_1+X_2+\dots+X_n}{n}$ is a gaussian random variable ☐
- ☒ $\overline{Y}_m = \frac{Y_1+Y_2+\dots+Y_m}{m}$ is a gaussian random variable ☐
- ☒ $\overline{X}_n - \overline{Y}_m = \frac{X_1+X_2+\dots+X_n}{n} - \frac{Y_1+Y_2+\dots+Y_m}{m}$ is a gaussian random variable ☐
- ☐ $X_i + Y_j$ is a gaussian random variable for any $i = 1, \dots, n$ and $j = 1, \dots, m$. ☐
- ☒ The variance of $\overline{X}_n - \overline{Y}_m$ is $\frac{\sigma_d^2+\sigma_c^2}{n+m}$.

☐

Solution:

The first four choices are true because of a basic principle of gaussian random variables. The linear combination of any two gaussian random variables (independent or not) is a gaussian random variable.

The last choice is not correct because the variance of $\overline{X}_n - \overline{Y}_m$ is $\frac{\sigma_d^2}{n} + \frac{\sigma_c^2}{m}$.

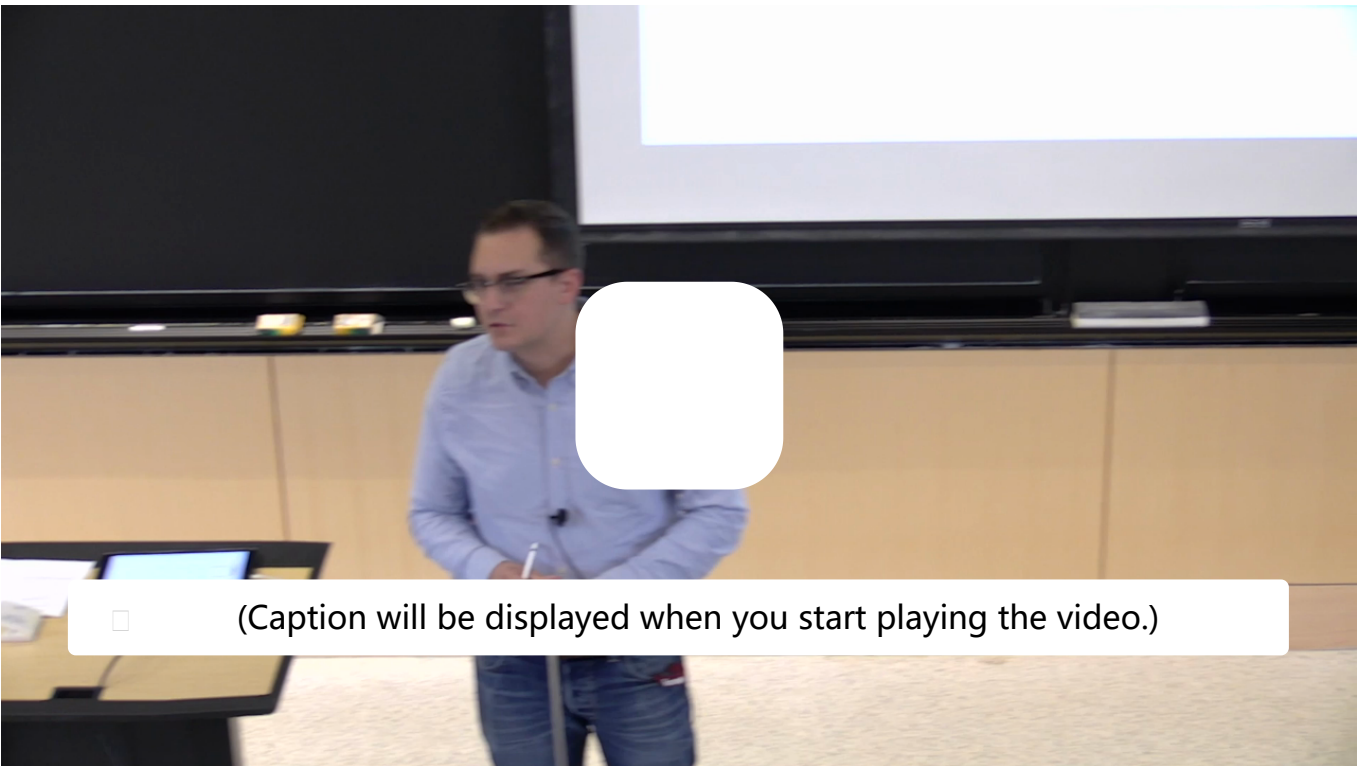
提交

你已经尝试了2次（总共可以尝试2次）

☐ Answers are displayed within the problem

Clinical Trials - Setting up the Hypothesis Test

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So now I want to--
I have a framework.
I have a mathematical language.
I'm no longer a pharmaceutical company.
I'm on the fourth floor.
I've talked to statisticians.
Now they have some Greek letters,
and they can actually formulate everything
into mathematical language.