

# Linear Algebra HW4

## Page Rank

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# Outline

- Introduction
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# Introduction - PageRank

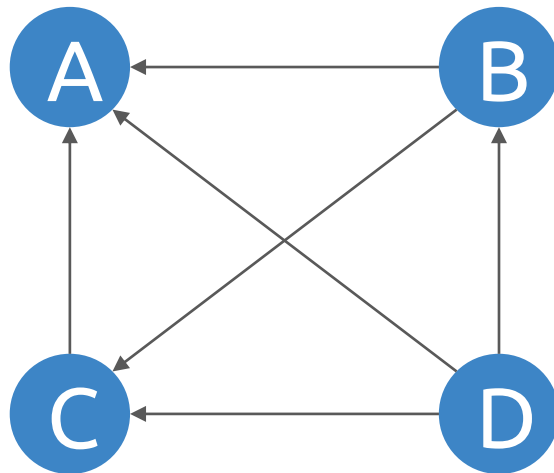
- PageRank is an algorithm to measure the importance of a website.
- It was developed by Larry Page and Sergey Brin in 1996.
- The more links a website received from other websites, the more important it is.
- The algorithm iteratively calculate the importance of a website according to the websites that have links to it and their importance.

# Introduction

$$PR(A) = PR(B) + PR(C) + PR(D)$$

$$PR(A) = \frac{PR(B)}{2} + \frac{PR(C)}{1} + \frac{PR(D)}{3}$$

$$PR(A) = \left( \frac{PR(B)}{2} + \frac{PR(C)}{1} + \frac{PR(D)}{3} \right) d + \frac{1-d}{4}$$



# Introduction

$$\text{PageRank}(p_i) = \frac{1-d}{N} + d \sum_{p_j \in M(p_i)} \frac{\text{PageRank}(p_j)}{L(p_j)}$$

$$\mathbf{R} = \begin{bmatrix} \text{PageRank}(p_1) \\ \text{PageRank}(p_2) \\ \vdots \\ \text{PageRank}(p_N) \end{bmatrix}$$

$$\mathbf{R}' = \begin{bmatrix} (1-d)/N \\ (1-d)/N \\ \vdots \\ (1-d)/N \end{bmatrix} + d \begin{bmatrix} \ell(p_1, p_1) & \ell(p_1, p_2) & \cdots & \ell(p_1, p_N) \\ \ell(p_2, p_1) & \ddots & & \\ \vdots & & \ell(p_i, p_j) & \\ \ell(p_N, p_1) & & & \ell(p_N, p_N) \end{bmatrix} \mathbf{R}, \text{ repeat until } \mathbf{R}' \approx \mathbf{R}$$

$\ell(p_i, p_j): 1 \text{ if } p_j \text{ has a link to } p_i, \text{ else } 0$   
 $\ell(p_i, p_j)$   
 $\ell(p_N, p_N)$

transition matrix

# ToDo

- Download hw4.zip [here](#).
- Write hw4.py that can
  - Make the transition matrix.
  - Calculate the rank of every node.
- Answer the question [here](#).

# ToDo

- Finish 3 ToDos in hw4.py
  - `get_tran()` -> get the transition matrix
  - `cal_rank()` -> calculate the rank of every node
    - `d = 0.85`
  - `save()` -> save the transition matrix, ranks to 1.txt, 2.txt
- Run the code to get 1.txt, 2.txt
  - `python3 hw4.py graph.txt`
  - use `graph_n.txt` according to last number of your student ID (b01234567 -> `graph_7.txt`)
  - 1.txt and 2.txt should be in the same directory as where `hw4.py` is

# ToDo - cal\_rank()

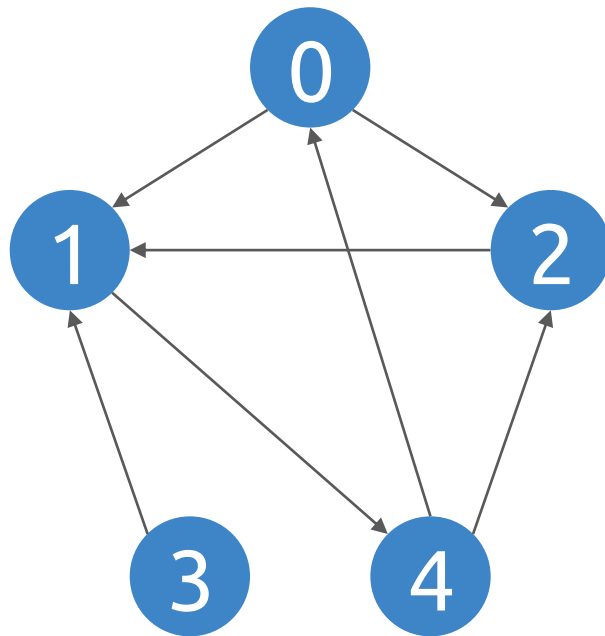
- Step 1: Initiala all PageRank in  $R_0$  with  $1/N$ . (N: the number of nodes)
- Step 2: Use  $R_t$  and transition matrix to calculate  $R_{t+1}$
- Step 3: Repeat Step 2 until:
  - $\| R_{t+1} - R_t \|_1 \leq \text{alpha}$  (Use the funcion  $\text{dist}(R_{t+1}, R_t)$  to calculate  $\| R_{t+1} - R_t \|_1$ )
  - or when  $t \geq \text{max iterations}$
  - $\text{max iterations} = 1000, \text{alpha} = 0.001$



# Data Format

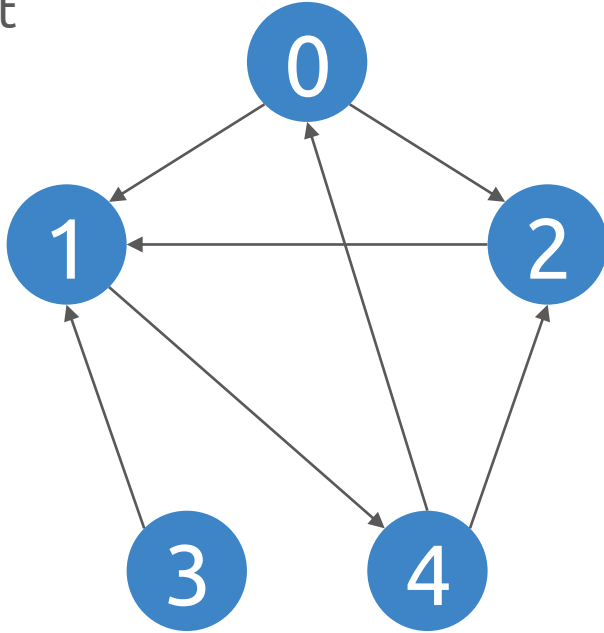
- graph.txt

```
0,1,2  
1,4  
2,1  
3,1  
4,0,2
```



# Data Format

- 1.txt



0	0	0	0	1
1	0	1	1	0
1	0	0	0	1
0	0	0	0	0
0	1	0	0	0

0.0	0.0	0.0	0.0	0.5
0.5	0.0	1.0	1.0	0.0
0.5	0.0	0.0	0.0	0.5
0.0	0.0	0.0	0.0	0.0
0.0	1.0	0.0	0.0	0.0

this is the transition matrix we want

# Data Format

- 2.txt

```
0.15346  
0.30688  
0.21873  
0.03  
0.29093
```

- Note: don't worry about the number of the digits, small deviation is allowable

# Grading

- Save the transition matrix of the graph in 1.txt. (1%)
  - Check ex/1.txt to make sure that your submission is in correct format.
- Save the rank score of every node in 2.txt. (3%)
  - Check ex/2.txt to make sure that your submission is in correct format.
- Q: If we initial  $R_0$  with random numbers and keep  $\text{SUM}(R_0) = 1$ , will the ranking be different ? Try to explain it. (2%)
  - Write your answer in report.pdf.
  - No template for report.pdf, but write the answer in 1 page.

# Submission

- You should put all your files in a folder and compress it in a zip file.

b01234567\_hw4.zip

|—./b01234567\_hw4.zip

|—hw4.py

|—1.txt

|—2.txt

|—report.pdf

- Note: **do not** upload any graph.txt or other files

# Rules

- Plagiarism = 0 point
- Upload b01234567\_hw4.zip to CEIBA
- **DEADLINE: 2018/12/11 (Tue.) 23:59 (GMT+8:00)**
- Late submission: total score x 0.8 (per day)
- Any other error: total score x 0.8
- Python packages: numpy, pandas, and any built-in package
- **請確定投影片中出現的紅字都注意看過：)**

# FAQ