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10. Exercise: Using the formula for the monotonic case

Exercise: Using the formula for the monotonic case

6/6 points (graded)

The random variable X is exponential with parameter $\lambda=1$. The random variable Y is defined by Y=g(X)=1/(1+X).

a) The inverse function h, for which h(g(x))=x, is of the form ay^b+c . Find a, b, and c.

$$a = \begin{bmatrix} 1 \\ b = \begin{bmatrix} -1 \\ c = \end{bmatrix}$$
 Answer: 1

Answer: -1

Answer: -1

b) For $y \in (0,1]$, the PDF of Y is of the form $f_Y(y) = y^a e^{(b/y) + c}$. Find a, b, and c.

$$a = \begin{bmatrix} -2 \\ b = \begin{bmatrix} -1 \\ c = \end{bmatrix}$$
 Answer: -2

Answer: -1

Answer: -1

Solution:

a) If x and y obey the relation y=g(x)=1/(1+x), then y+yx=1, so that

$$x=h(y)=\frac{1-y}{y}=\frac{1}{y}-1.$$

Note that we are interested in $x \ge 0$ which restricts y to the range (0,1]. Notice also that the functions g and h are monotonically decreasing on the relevant ranges of values.

b) Note that

$$rac{dh}{dy}(y) = -rac{1}{y^2}.$$

Therefore,

$$f_Y(y) = f_Xig(h(y)ig)\Big|rac{dh}{dy}(y)\Big| = e^{-(1/y)+1}\cdotrac{1}{y^2}.$$

提交

You have used 2 of 3 attempts

1 Answers are displayed within the problem

讨论

显示讨论

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