

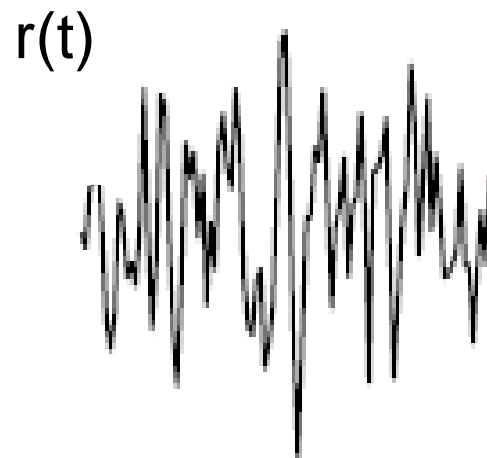
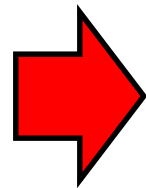
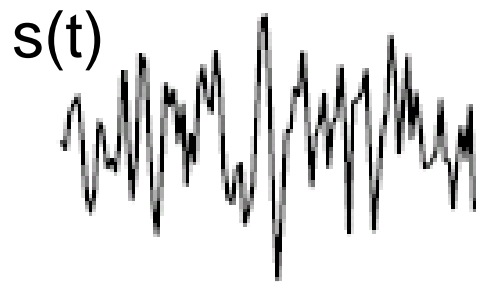
Constructing response models

$P(\text{response} \mid \text{stimulus}) \rightarrow r(t)$ given a stimulus s

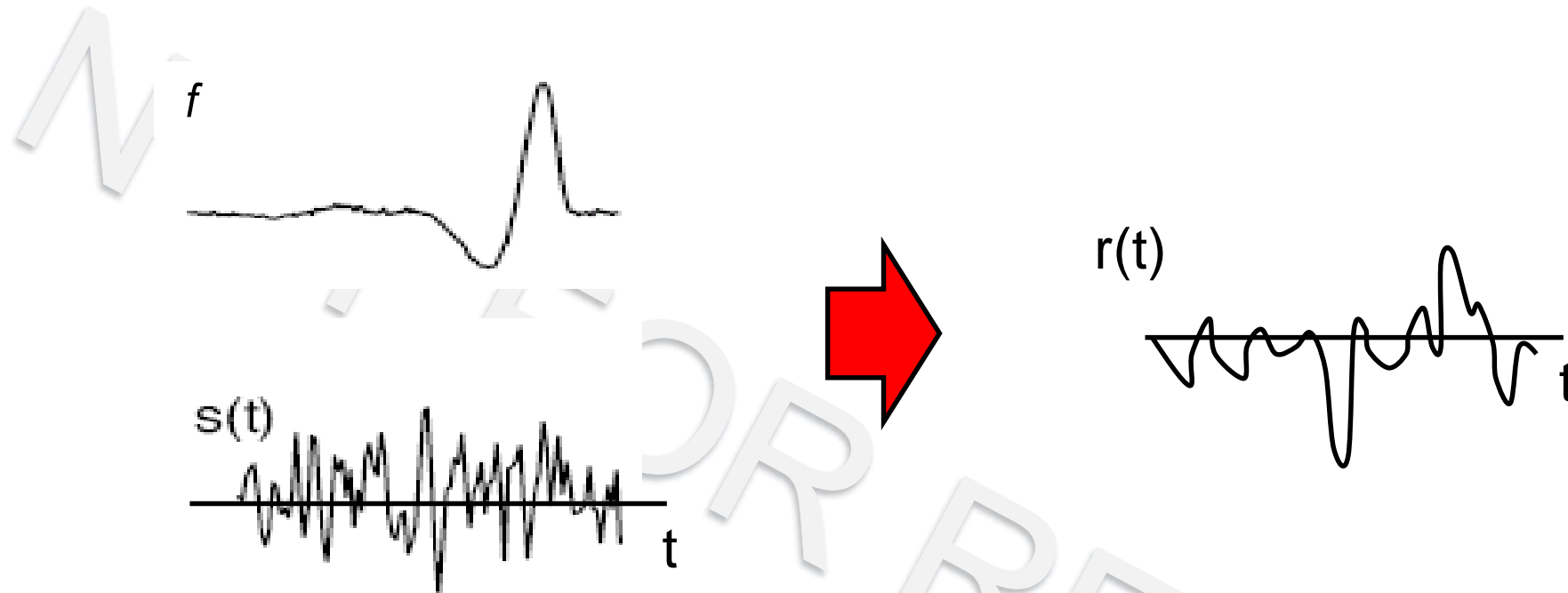
$P(\text{response} \mid \text{stimulus})$

Basic coding model: linear response

$$r(t) = \phi s(t)$$



Basic coding model: temporal filtering

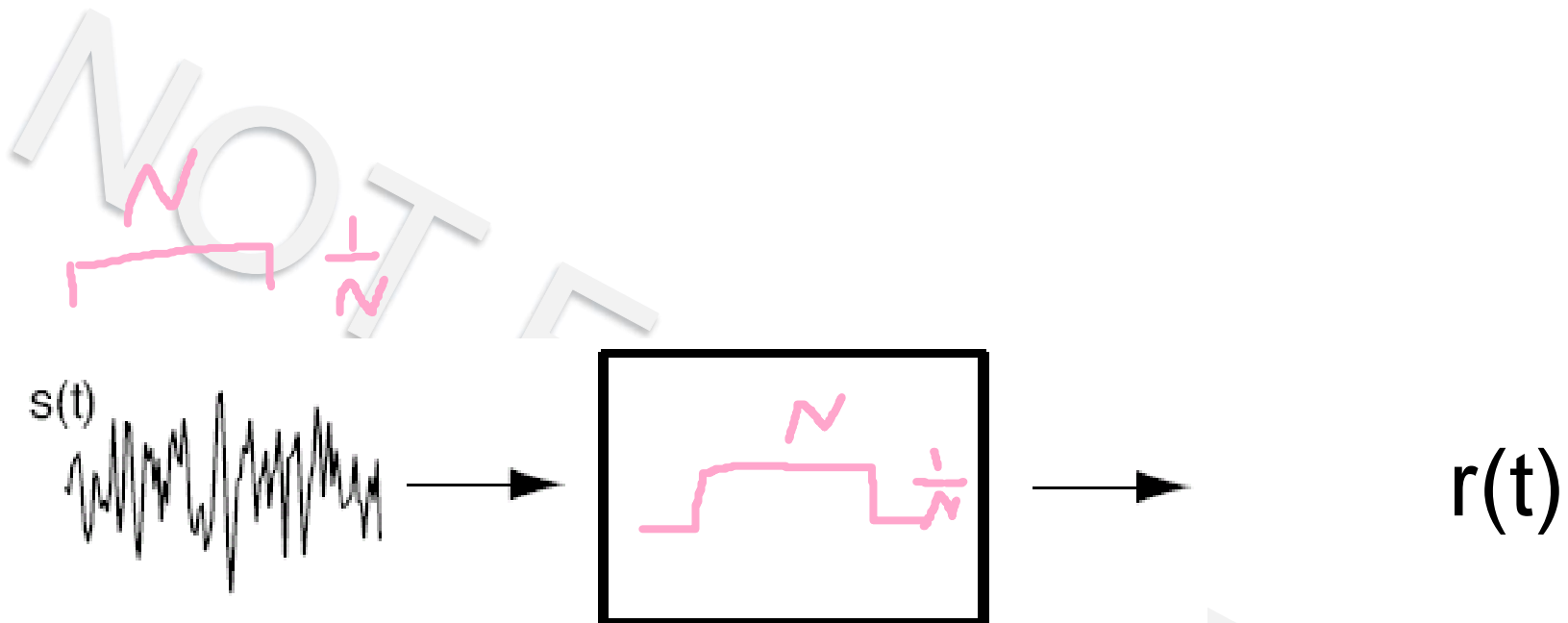


Linear filter:

$$r(t) = \sum_{k=0}^n s_{t-k} f_k$$

$$r(t) = \int_{-\infty}^t d\tau s(t - \tau) f(\tau)$$

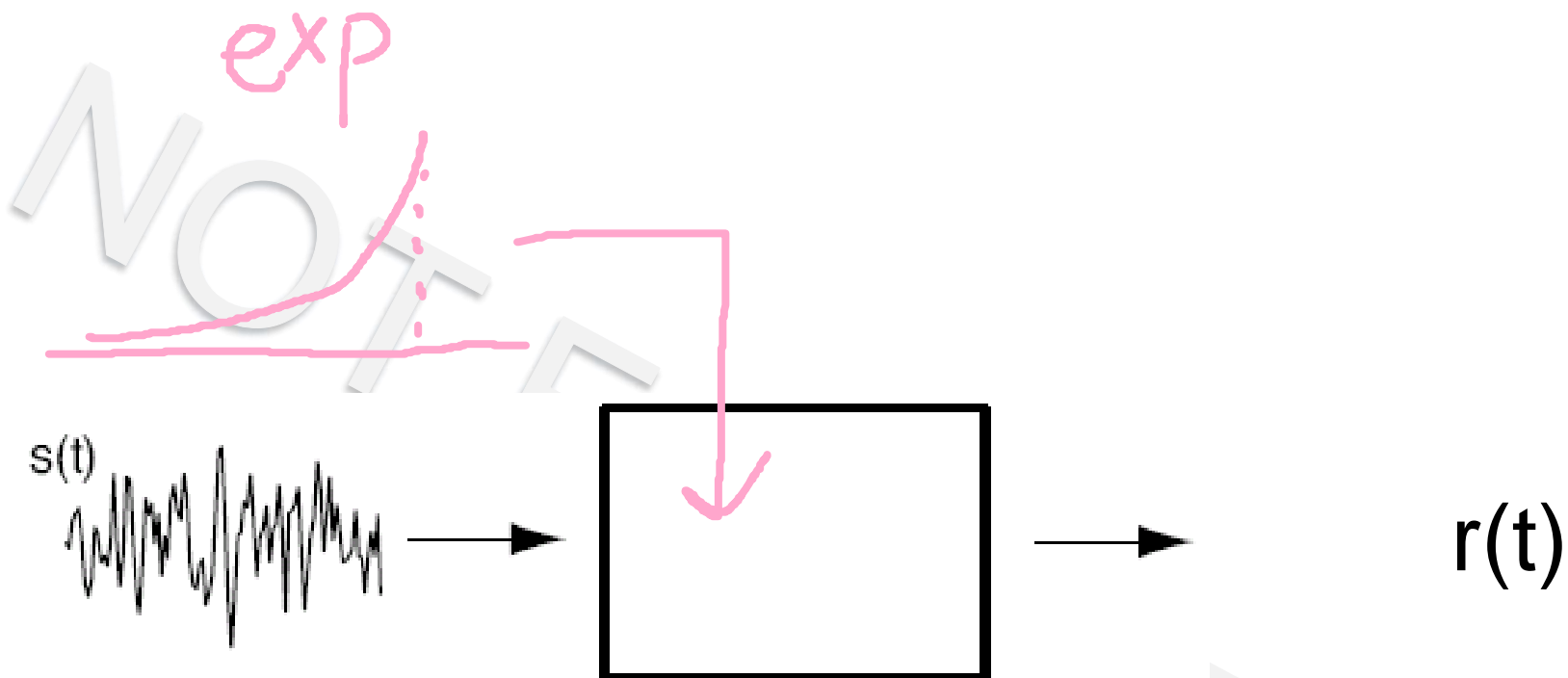
Example I: running average



Linear filter:

$$r(t) = \sum_{k=0}^n s_{t-k} f_k$$

Example II: leaky average



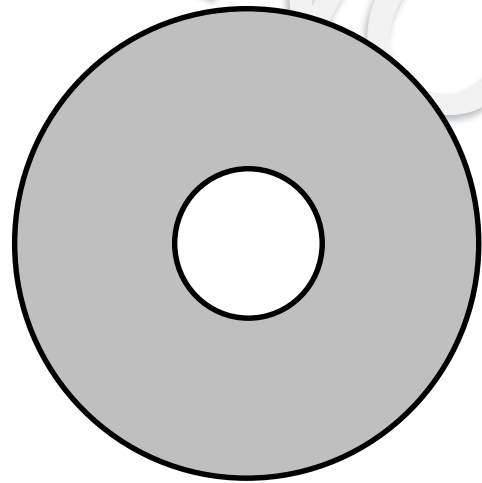
Linear filter:

$$r(t) = \sum_{k=0}^n s_{t-k} f_k$$

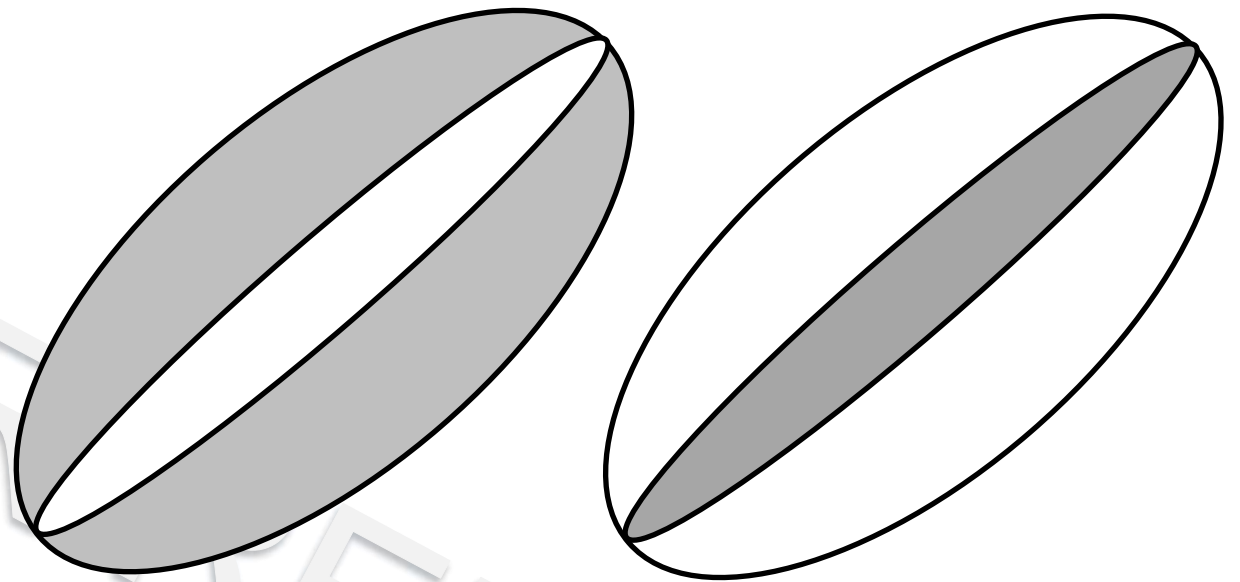
Basic coding model: spatial filtering

NOT FOR REUSE

Basic coding model: spatial filtering



retina



Visual cortex

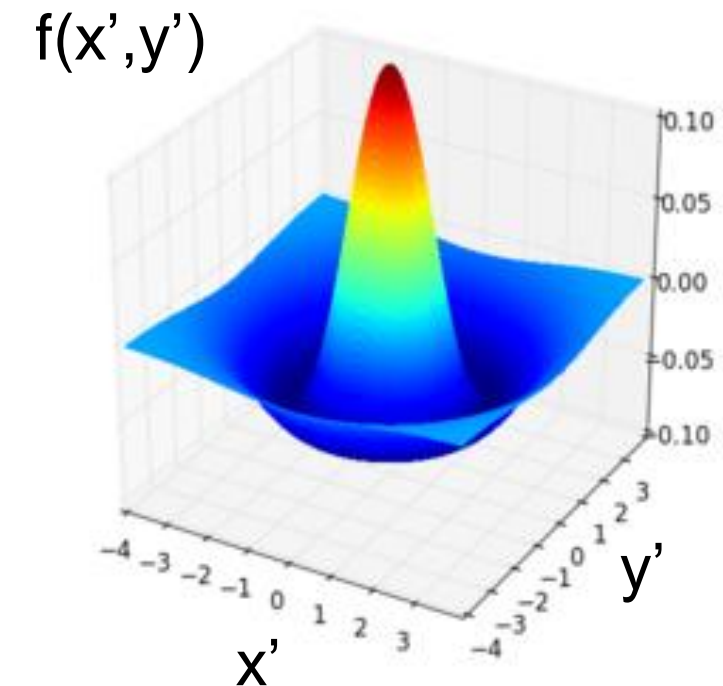
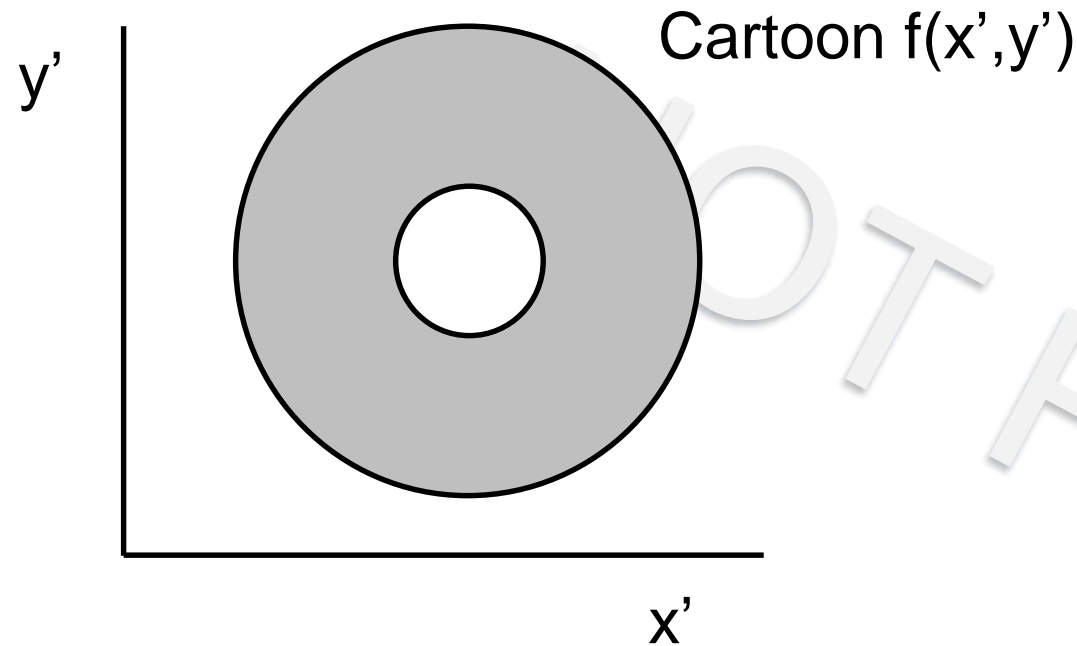
Basic coding model: spatial filtering

$$r(t) = \sum_{k=0}^n s_{t-k} f_k$$

Temporal filter

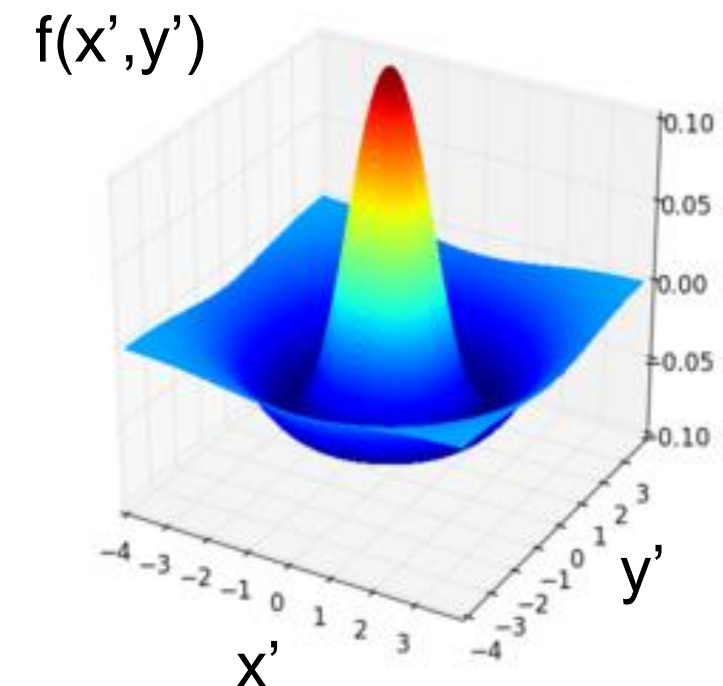
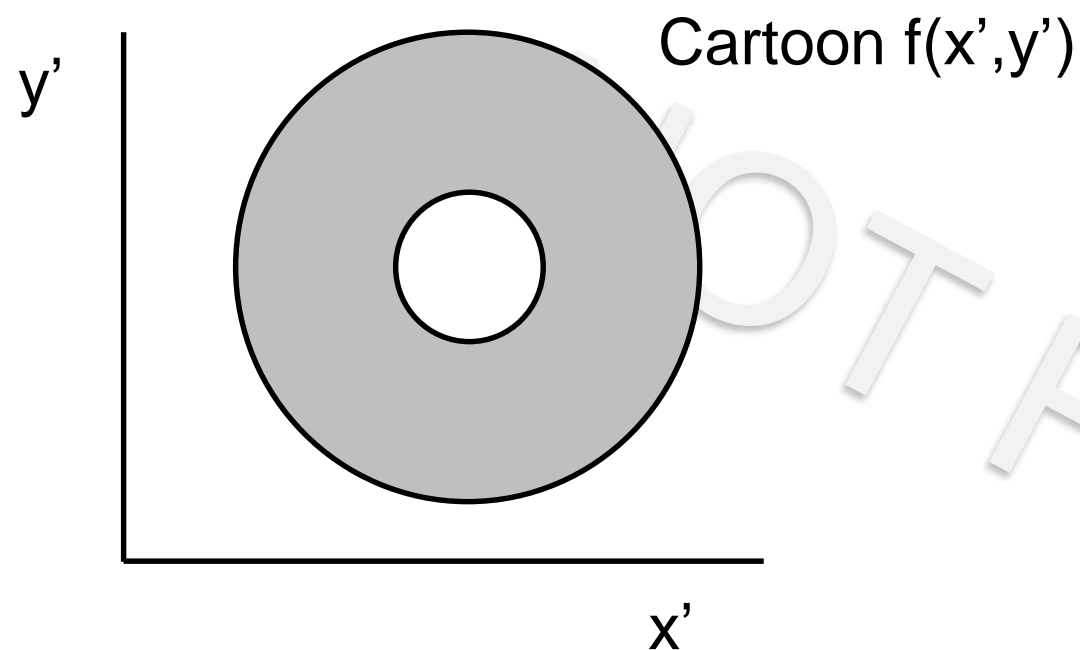
$$r(x, y) = \sum_{x'=-n, y'=-n}^n s_{x-x', y-y'} f_{x', y'}$$
$$= \int_{-\infty}^{\infty} dx' dy' s(x - x', y - y') f(x', y')$$

Spatial filtering and retinal receptive fields



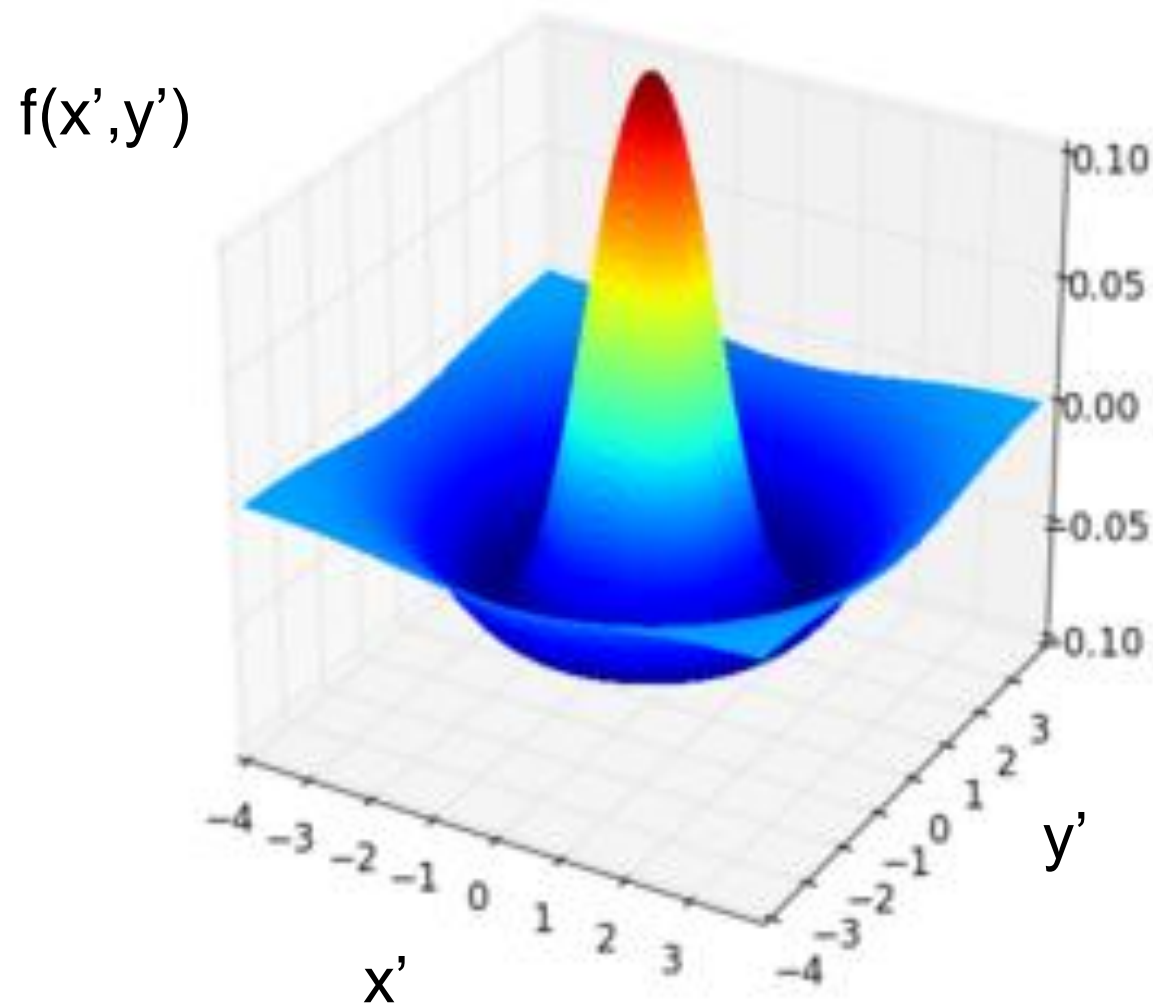
$$r(x, y) = \sum_{x'=-n, y'=-n}^n s_{x-x', y-y'} f_{x', y'}$$

Spatial filtering and receptive fields



$$r(x, y) = \sum_{x'=-n, y'=-n}^n s_{x-x', y-y'} f_{x', y'}$$

Spatial filtering and receptive fields



Spatial filtering

7.2.1. Overview

Figure 16.136. Applying example for the “Difference of Gaussians” filter

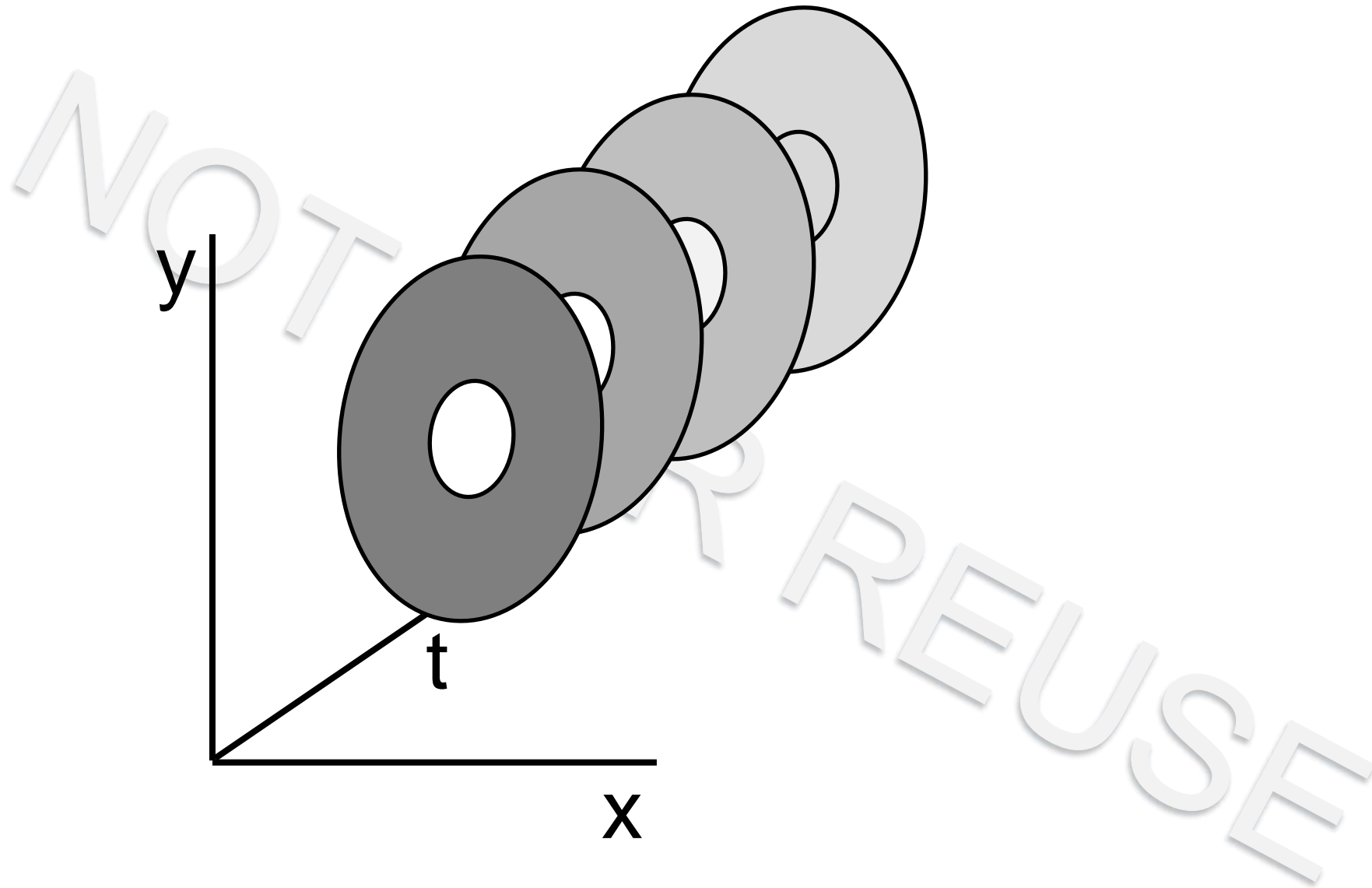


Original image



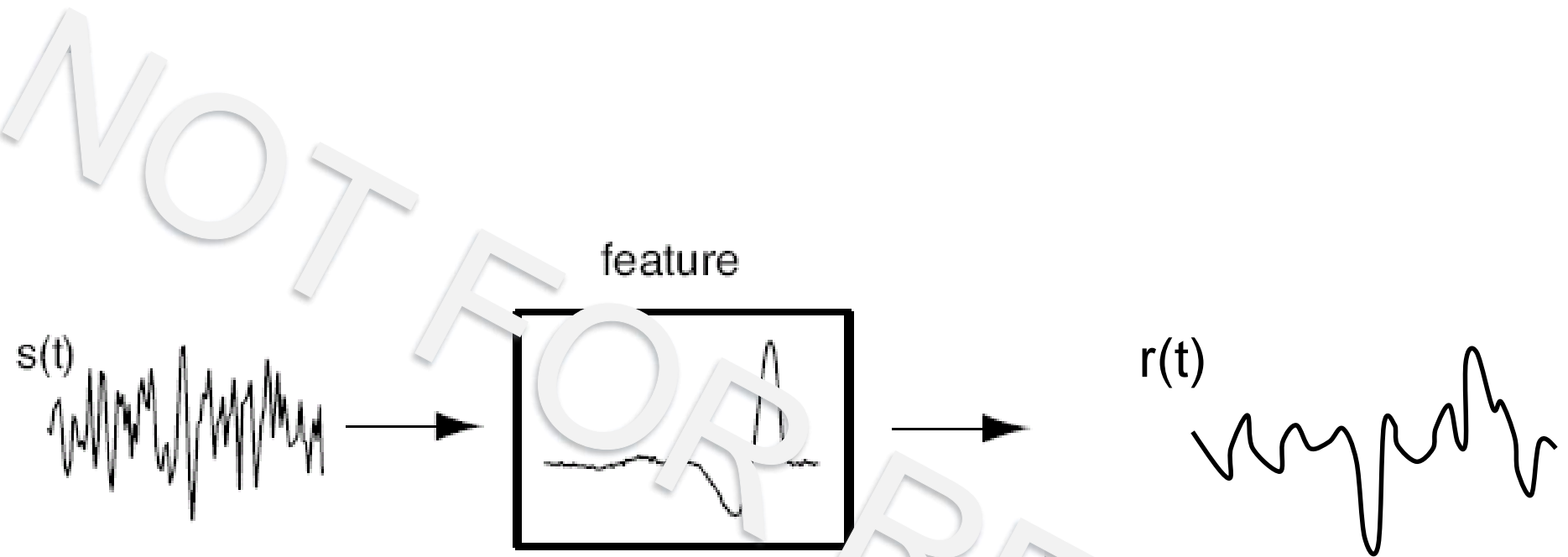
Filter “Difference of Gaussians” applied

Basic coding model: *spatiotemporal* filtering



$$r_{x,y}(t) = \iiint dx' dy' d\tau f(x',y',\tau) s(x-x',y-y',t-\tau)$$

Basic coding model: temporal filtering

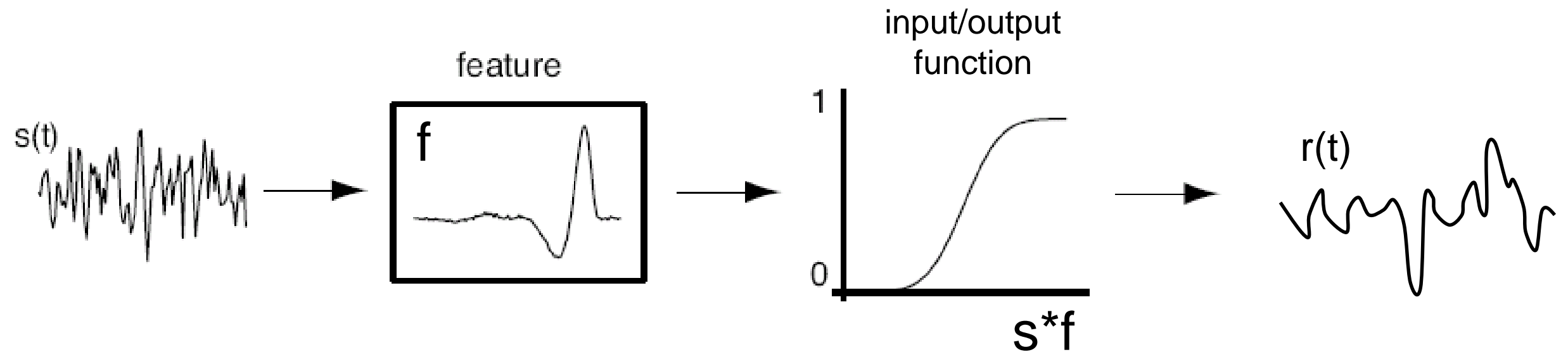


Linear filter:
$$r(t) = \int s(t-\tau) f(\tau) d\tau$$

Can firing rates be negative? Can they increase indefinitely as the input increases?
Both of those are a possible result from a linear filtering operation like this.

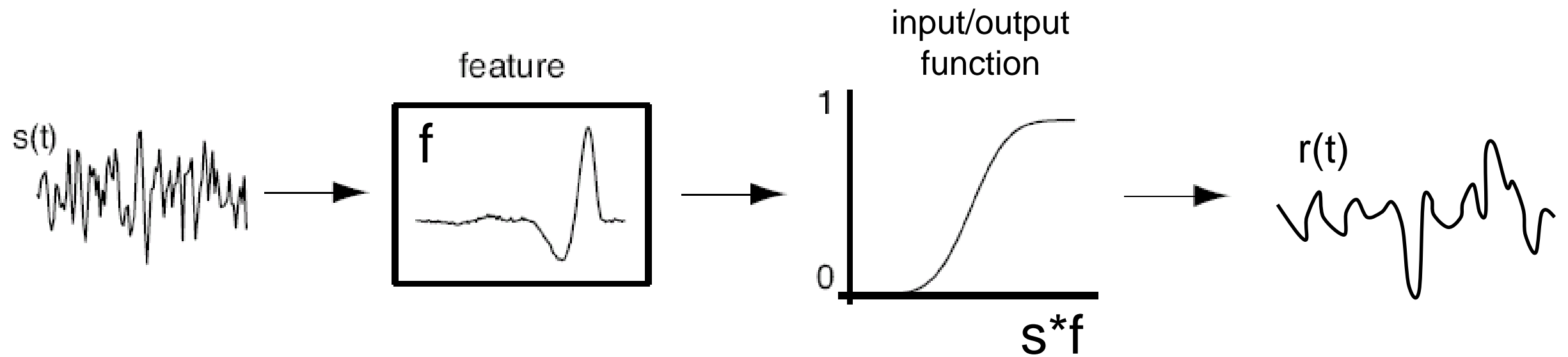
...shortcomings?

Next most basic coding model

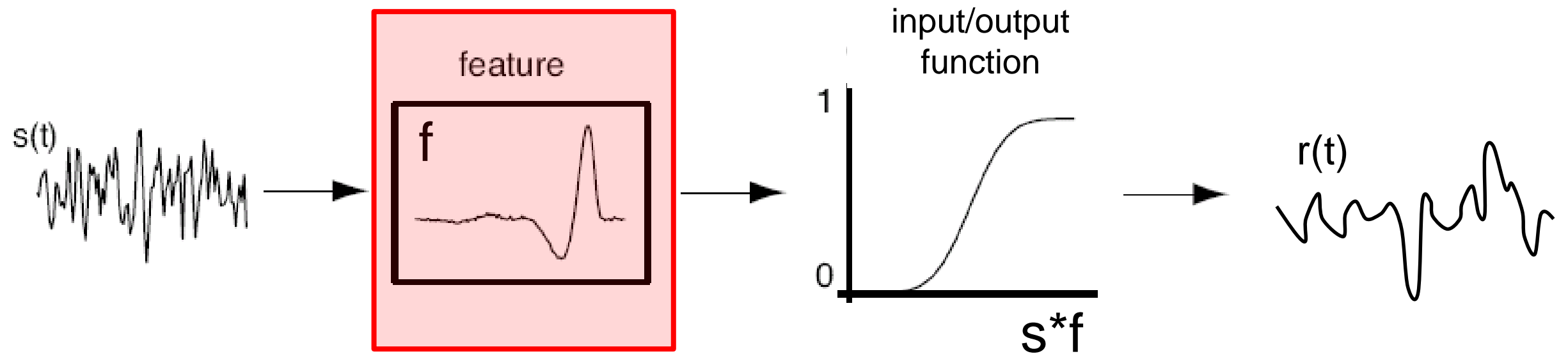


Linear filter & nonlinearity: $r(t) = g(\int s(t-\tau) f(\tau) d\tau)$

How to find the components of this model



How to find the components of this model



How to proceed?

$P(\text{response} \mid \text{stimulus})$

Our problem is one of dimensionality!

Time points \times pixels = 非常多的维度
导致没法sample出整个distribution
所以我们只能降维

We want to sample the responses of the system to many stimuli so we can characterize what it is about the input that triggers responses.

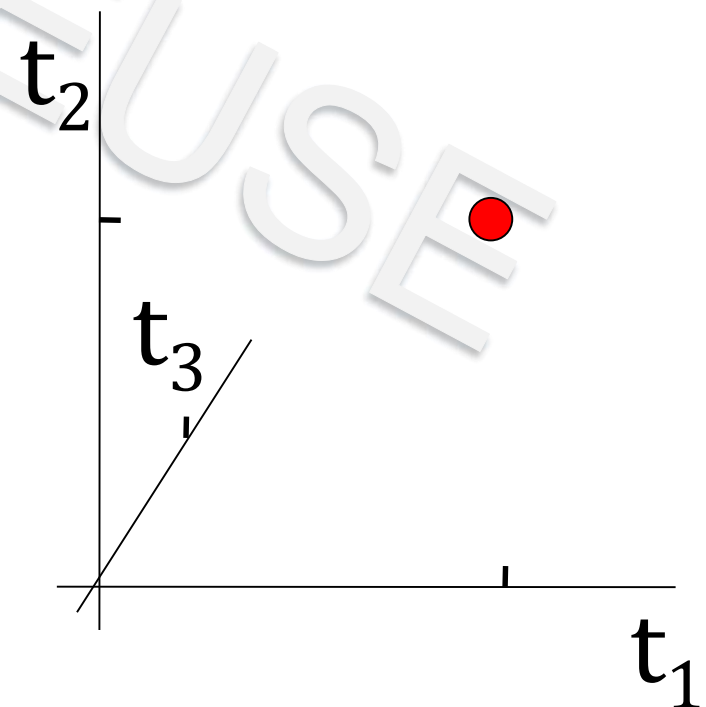
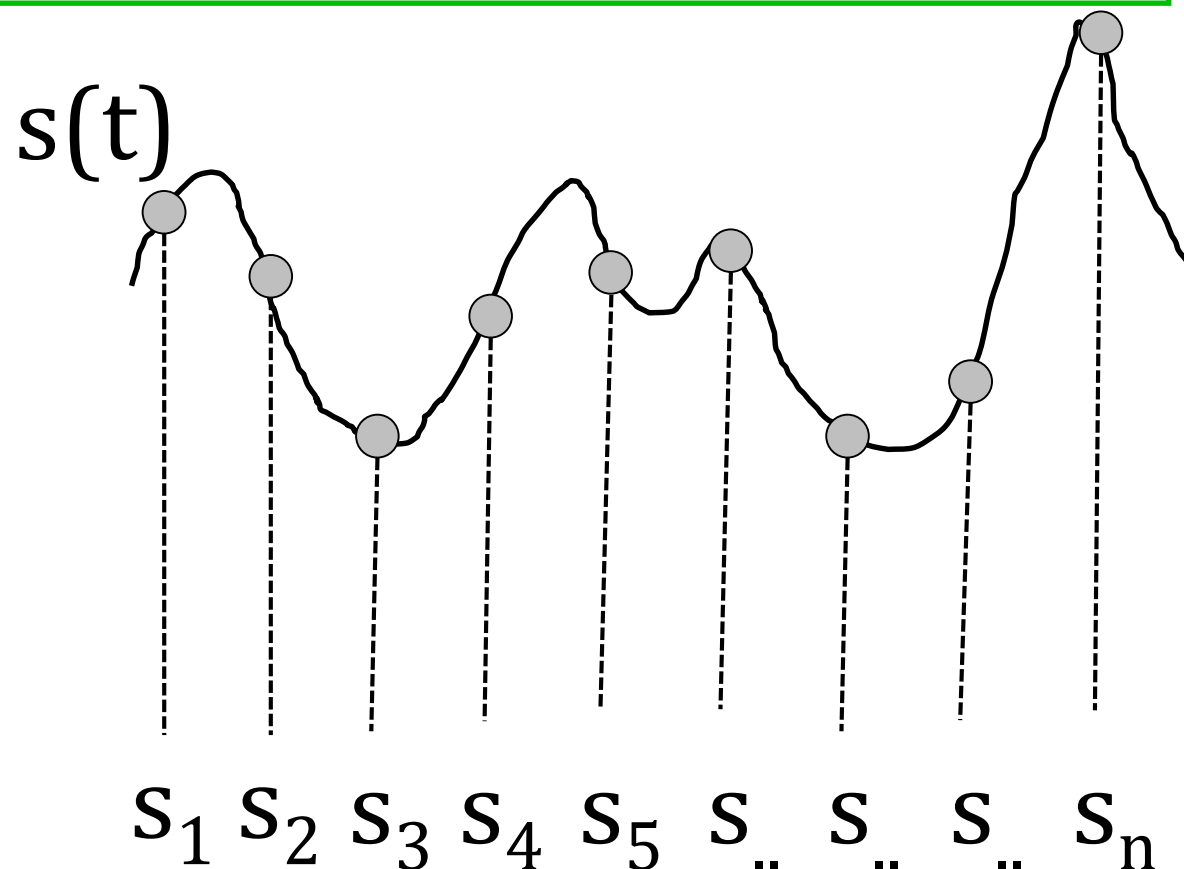
$P(\text{response} \mid \text{stimulus}) \rightarrow P(\text{response} \mid s_1)$

Dimensionality reduction

我们想知道 s 是什么。我们可以用 s 随着时间的概率分布来刻画它。但是我们不知道 s 随着时间的概率分布，所以我们通过采样不同时间的刺激，来刻画这个刺激 s 。

Start with a very high dimensional description (eg. an image or a time-varying waveform) and pick out a small set of relevant dimensions.

这里对不同时间的刺激 s 进行采样，得到了的刺激在不同时间的特征。
We discretize a stimulus waveform in time, we can represent it as a vector in some vector space.
The dimensionality of this vector space is the number of points used in the discretization.



$$s(t) = (s_{t1}, s_{t2}, s_{t3}, \dots, s_{tn})$$

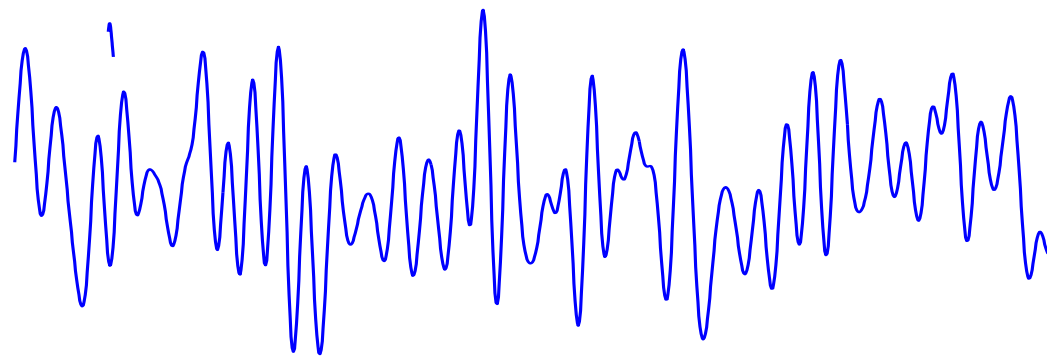
What is the right stimulus to use?

We want to sample the responses of the system to a variety of stimuli so we can characterize what it is about the input that triggers responses.

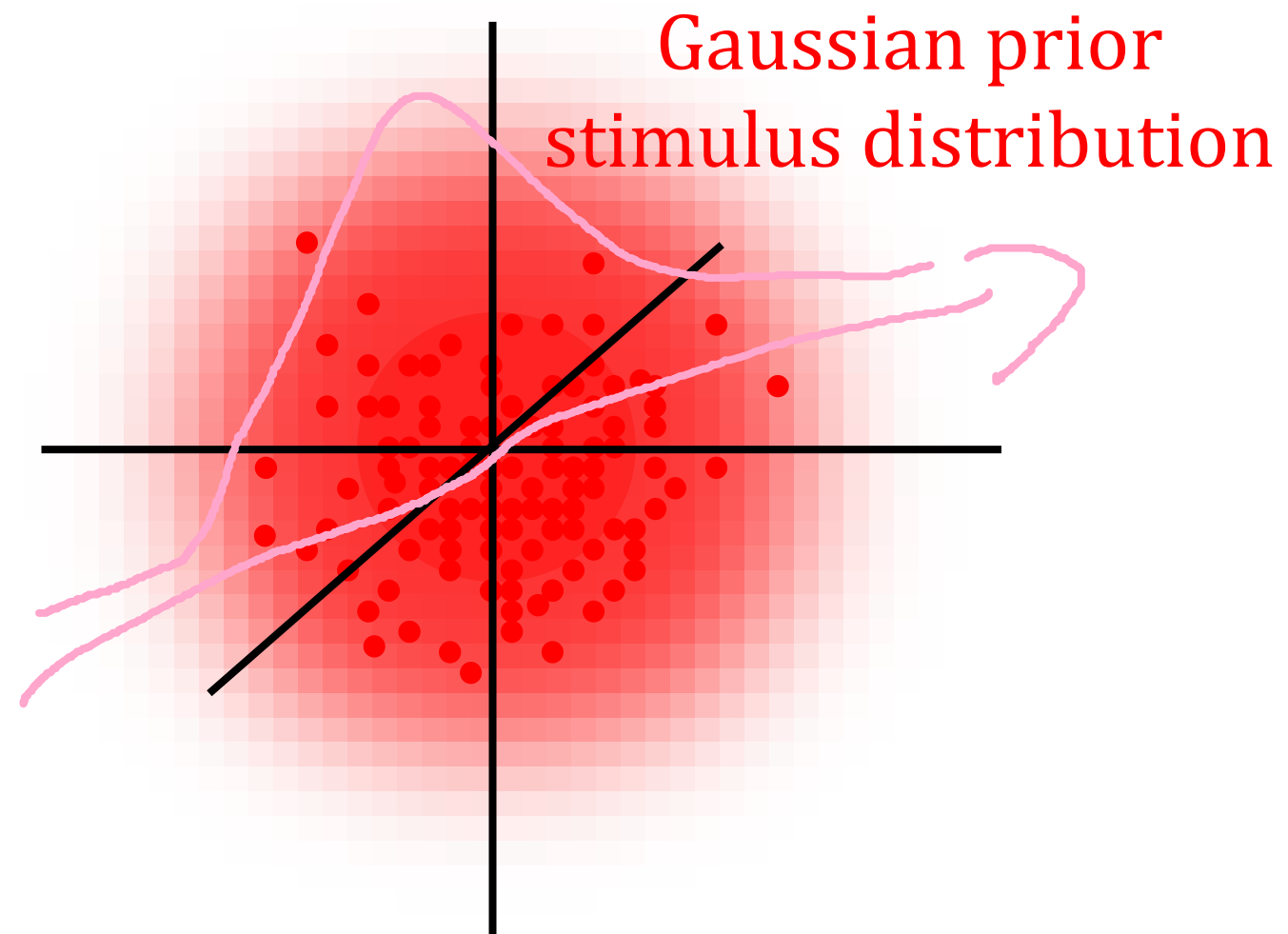
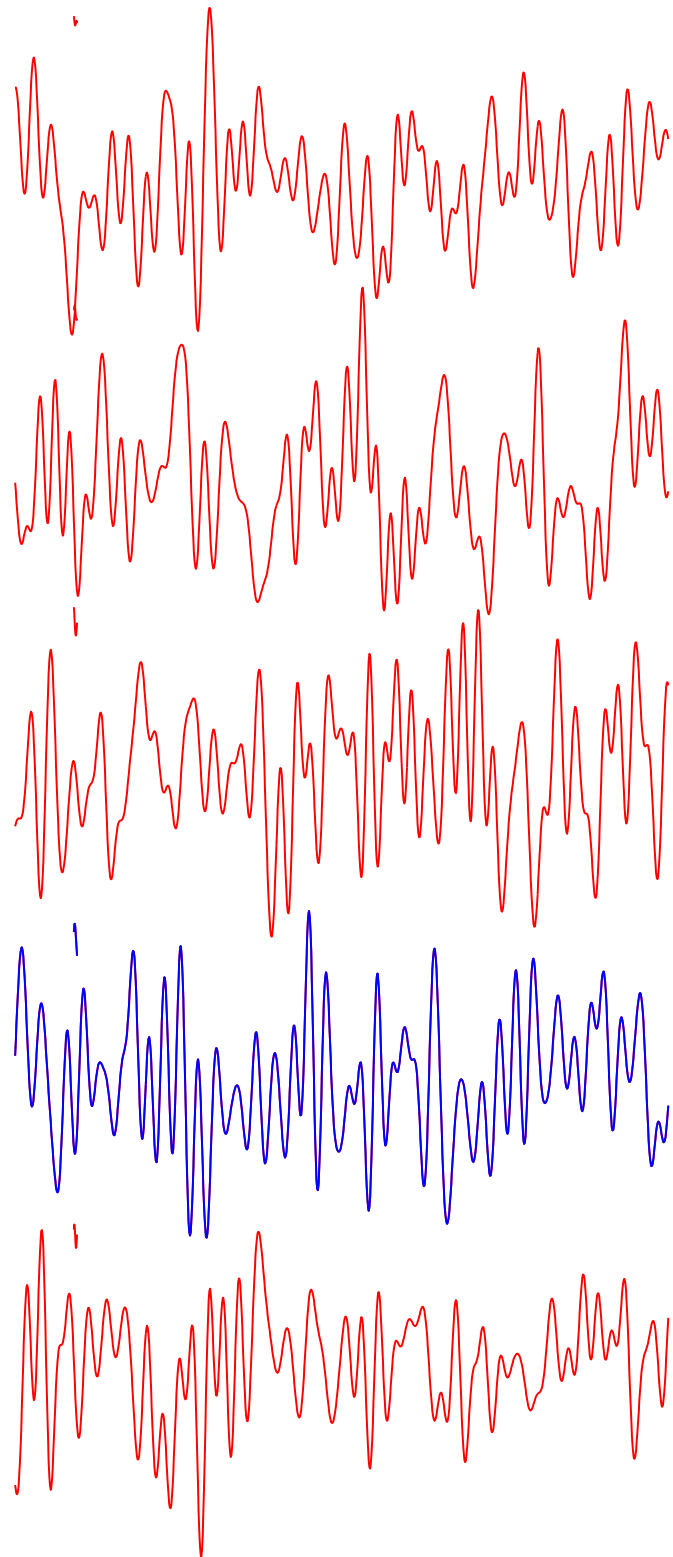
$$P(\text{response} \mid \text{stimulus}) \rightarrow P(\text{response} \mid s_1, s_2, \dots, s_n)$$

One common and useful method is to use

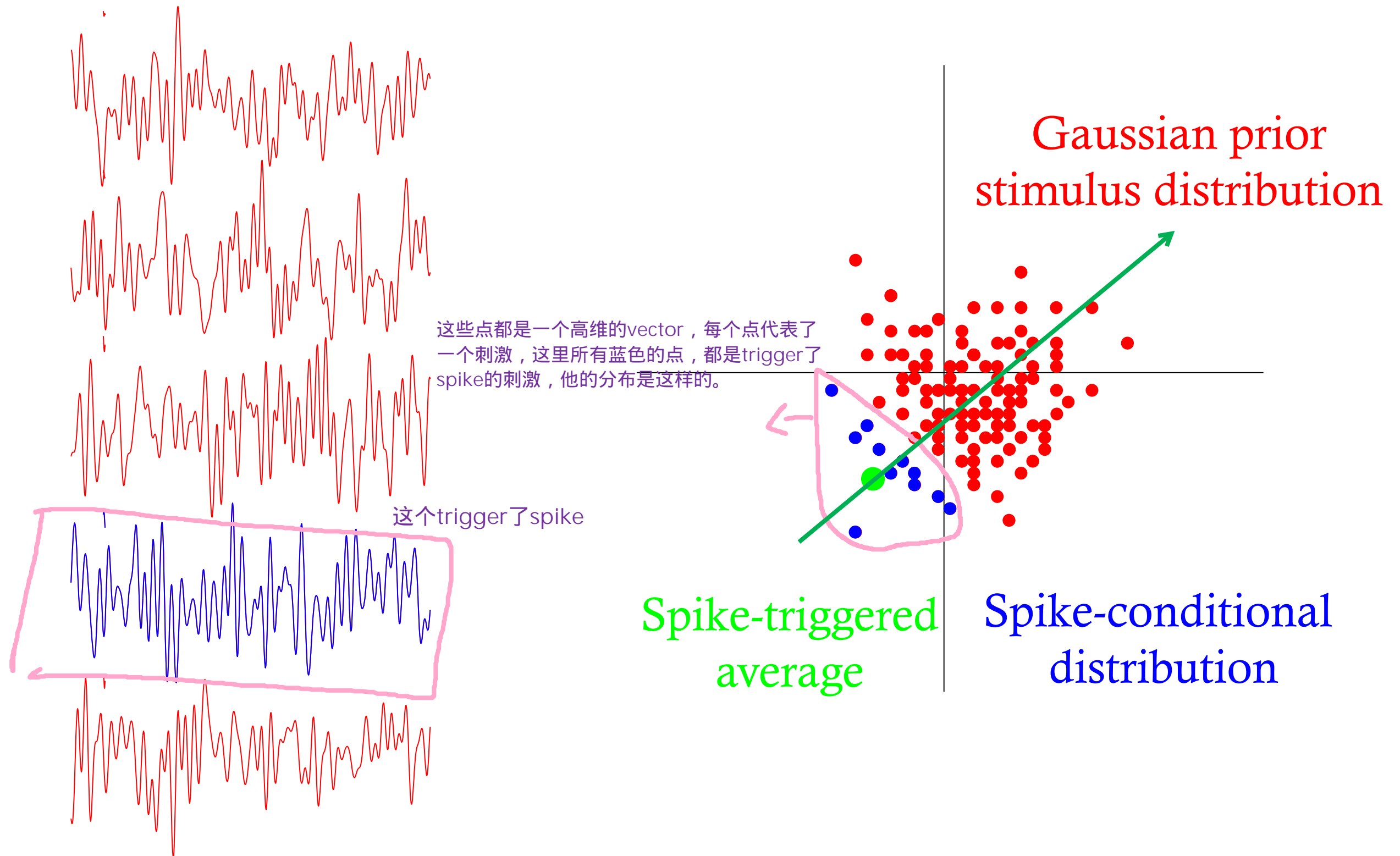
Gaussian **white noise**



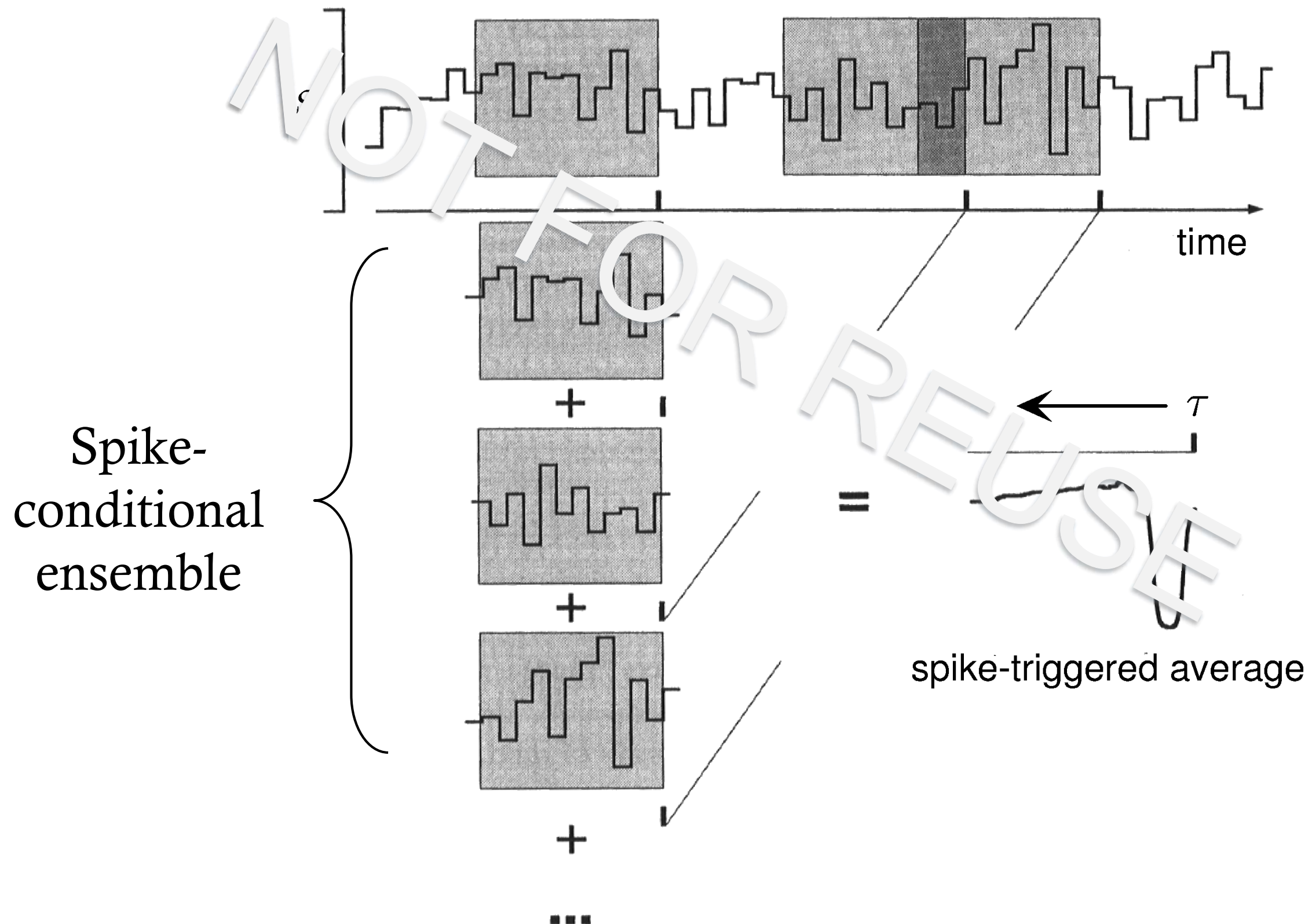
Determining multiple features from white noise



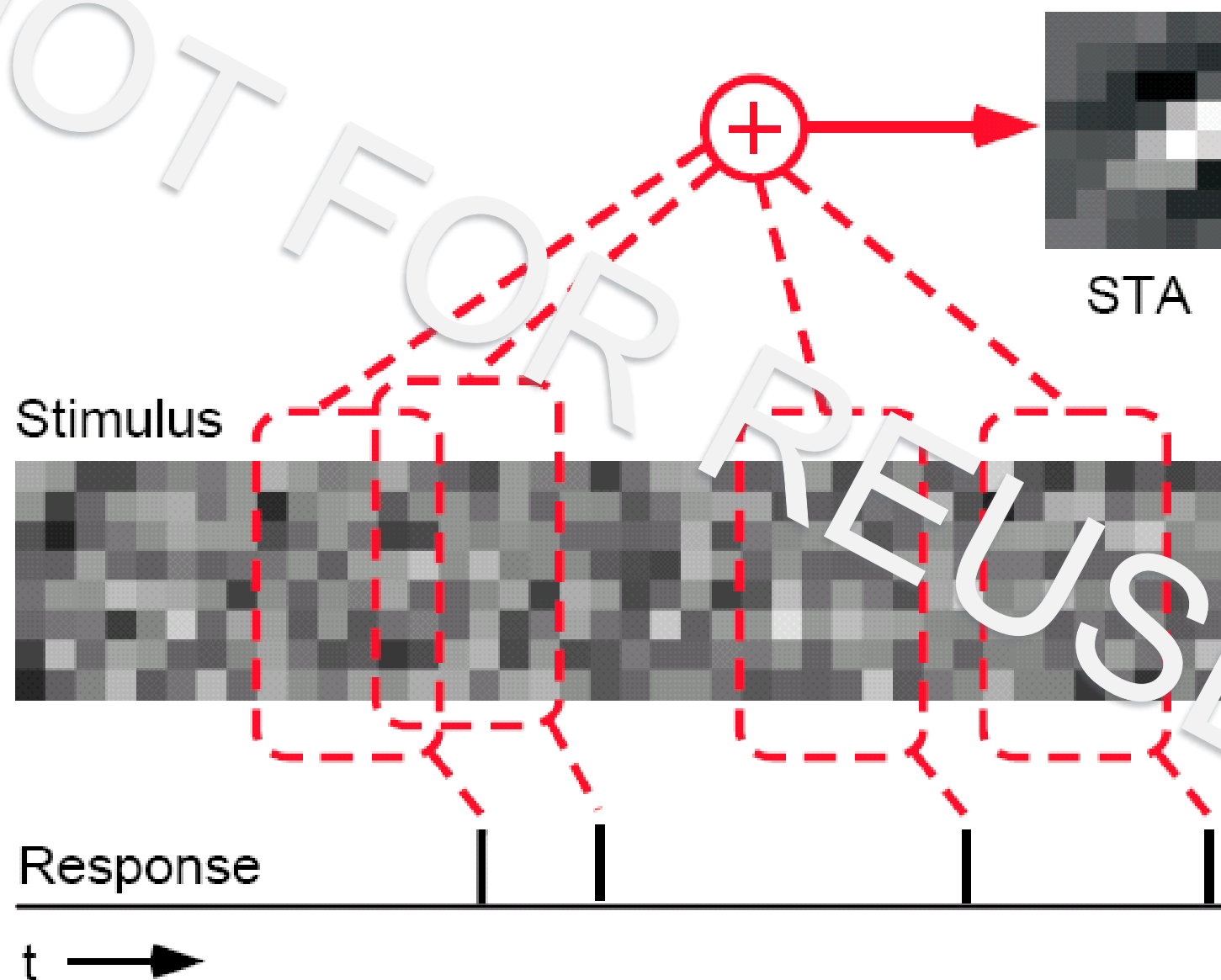
Determining linear features from white noise



Reverse correlation: the spike-triggered average

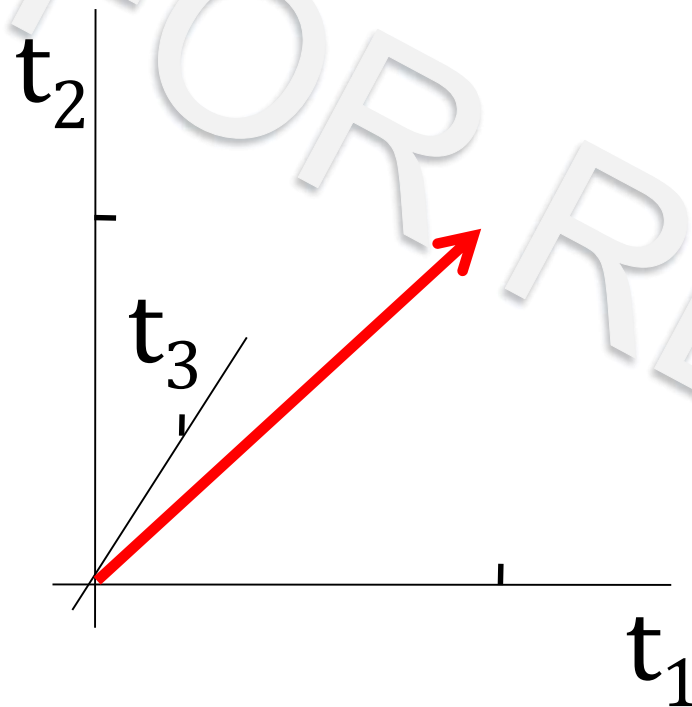


The spike-triggered average



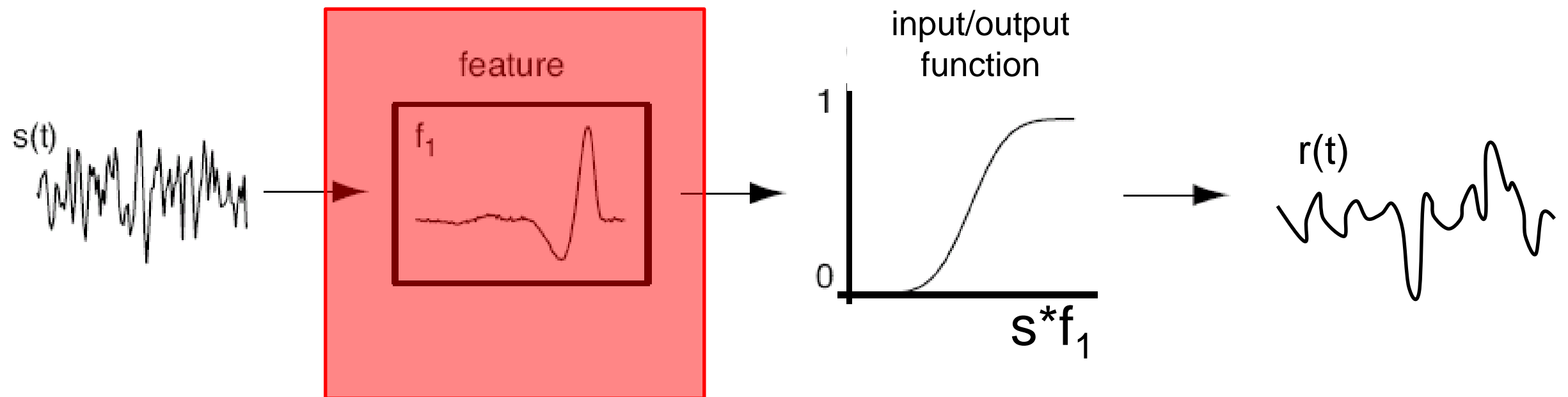
Linear filtering

Stimulus feature f is a vector in a high-dimensional stimulus space



Linear filtering = convolution = projection

How to find the components of this model



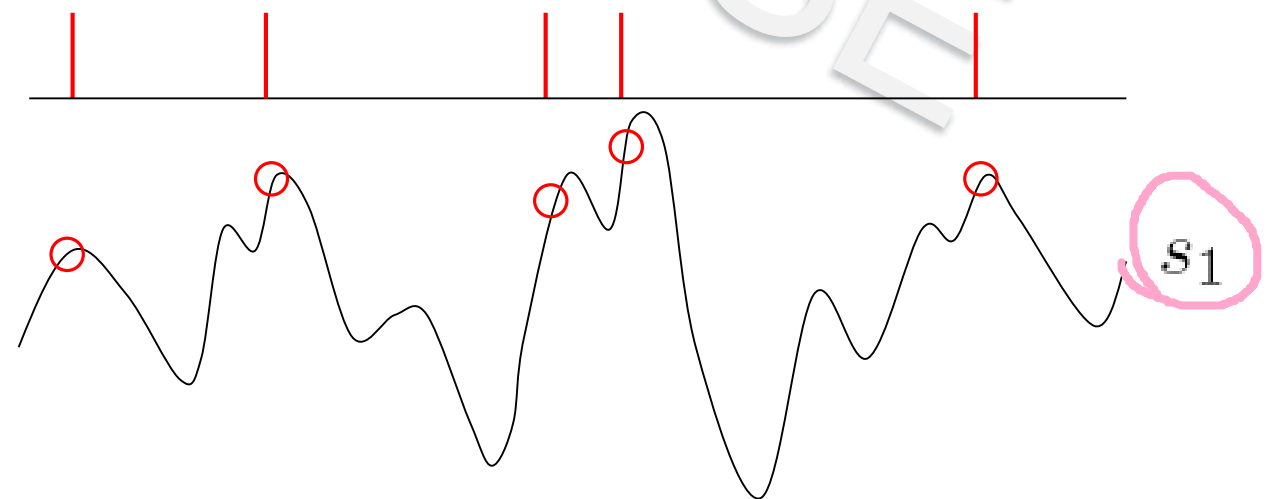
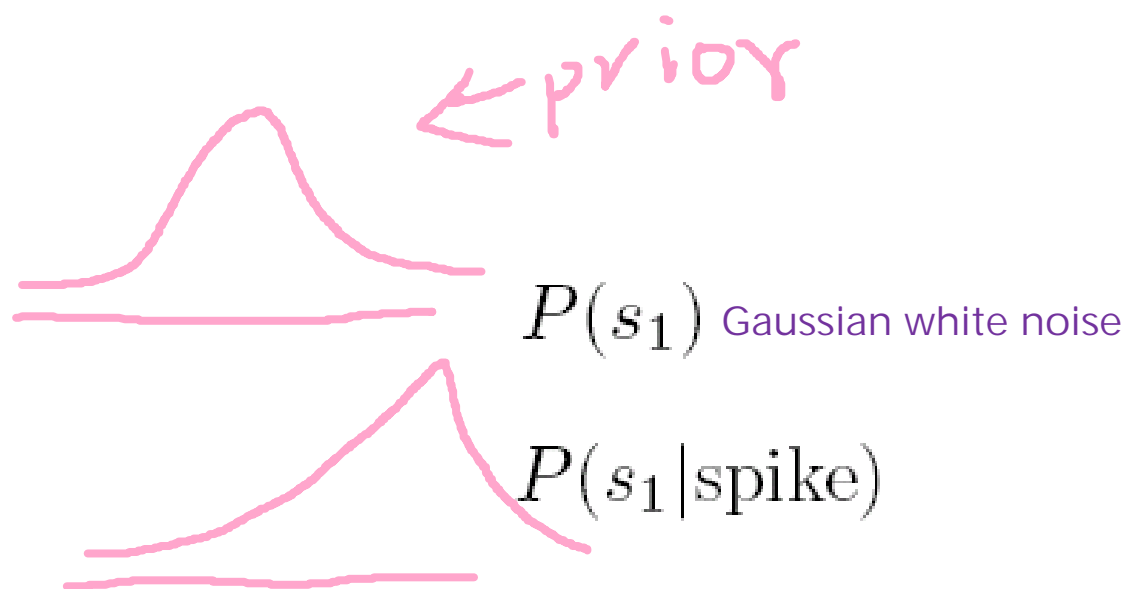
Determining the nonlinear input/output function

The input/output function is:

$$P(\text{spike}|\text{stimulus}) \xrightarrow{\text{red arrow}} P(\text{spike}|s_1)$$

This can be found from data using Bayes' rule:

$$P(\text{spike}|s_1) = \frac{\overset{\text{spike-conditional distribution}}{P(s_1|\text{spike})} \cdot \overset{\text{prior}}{P(\text{spike})}}{P(s_1)}$$

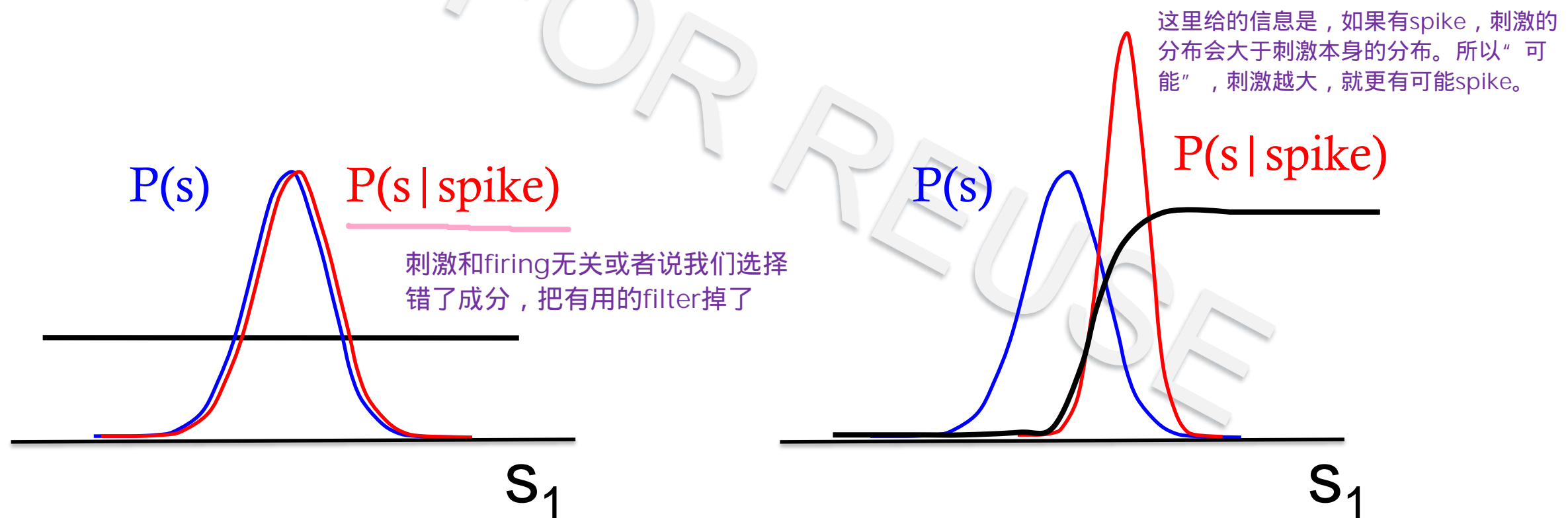


Given spike, s_1 会比较大。
换句话说就是有spike的刺激曲线会比没有spike的值更大。

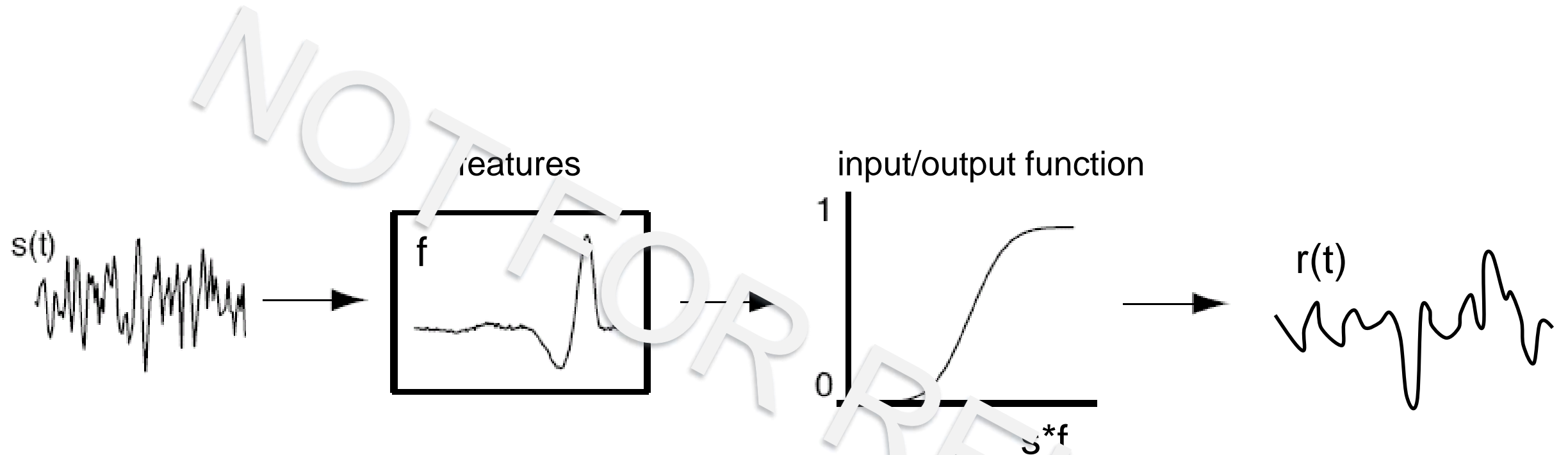
Nonlinear input/output function

$$P(\text{spike} | s_1) = P(s_1 | \text{spike}) P(\text{spike}) / P(s_1)$$

Assumed random
Uniformly distributed



Linear/nonlinear models



Linear filter & nonlinearity: $r(t) = g(\int f(t-\tau) s(\tau) dt)$

High-dimensional feature selection



Featured Members

Auntie_Sassy



Age: 35
Location: Greenwood

Woman seeking

- Man for Dating
- Man for Friendship

Worst Haiku Ever

This is my first dip into the online dating pool and quite frankly, I have no idea what I'm doing.... [learn more about me »](#)

JohnnyX



Age: 47
Location: Capitol Hill

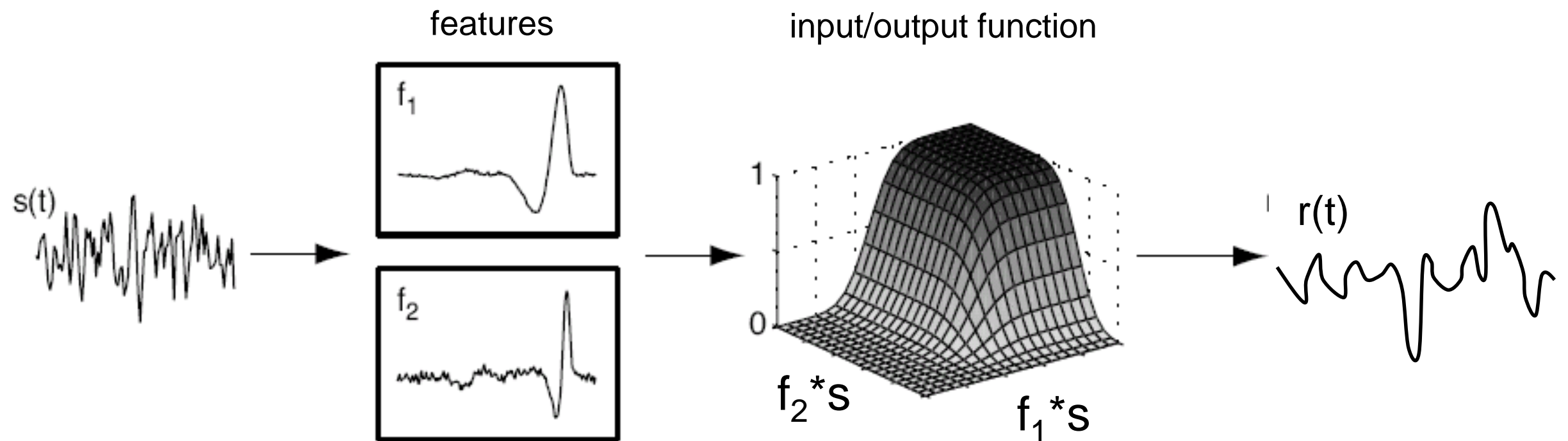
Man seeking

- Woman for Dating
- Woman for Friendship

Sex, Love and Rock-n-Roll

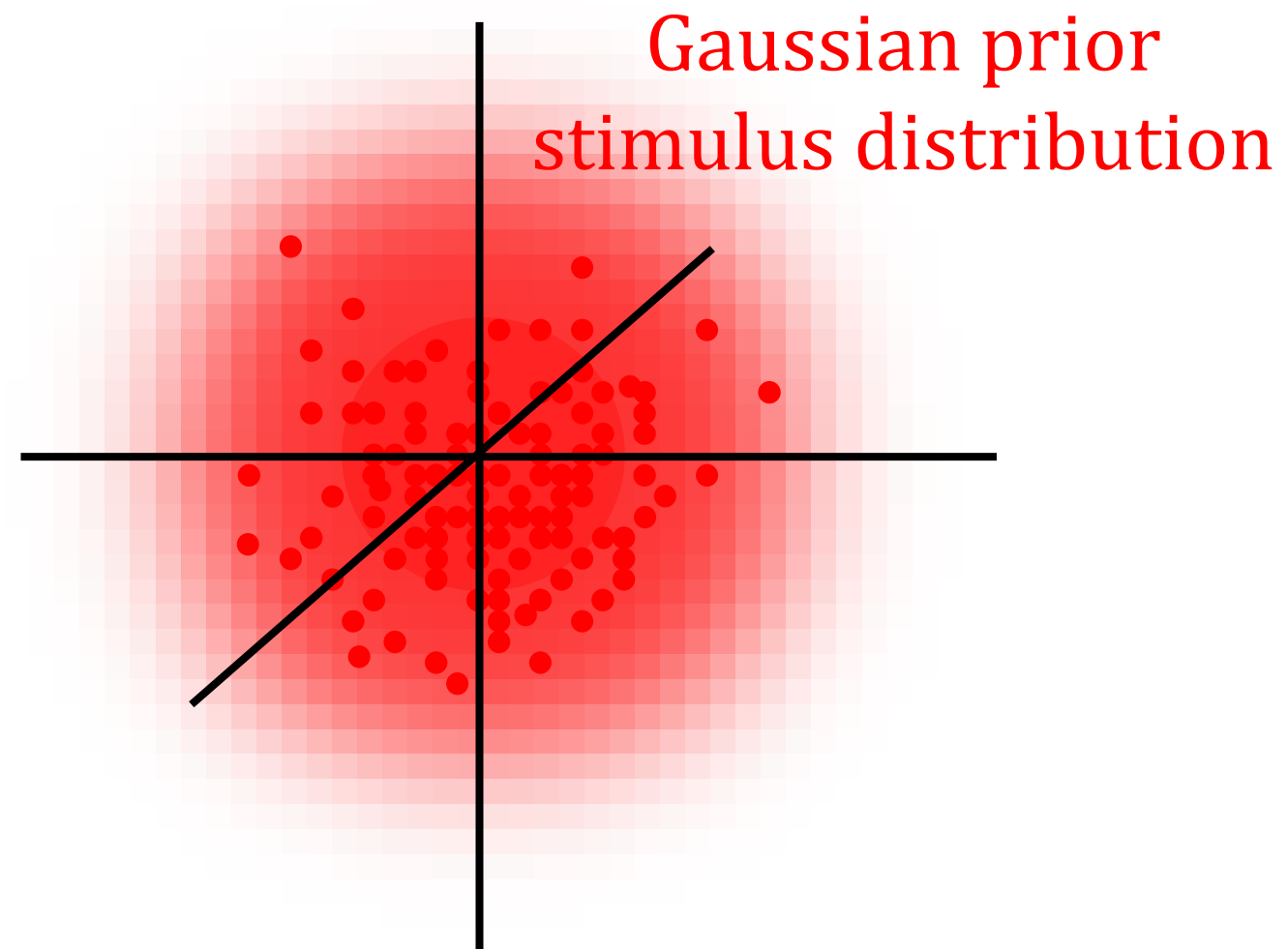
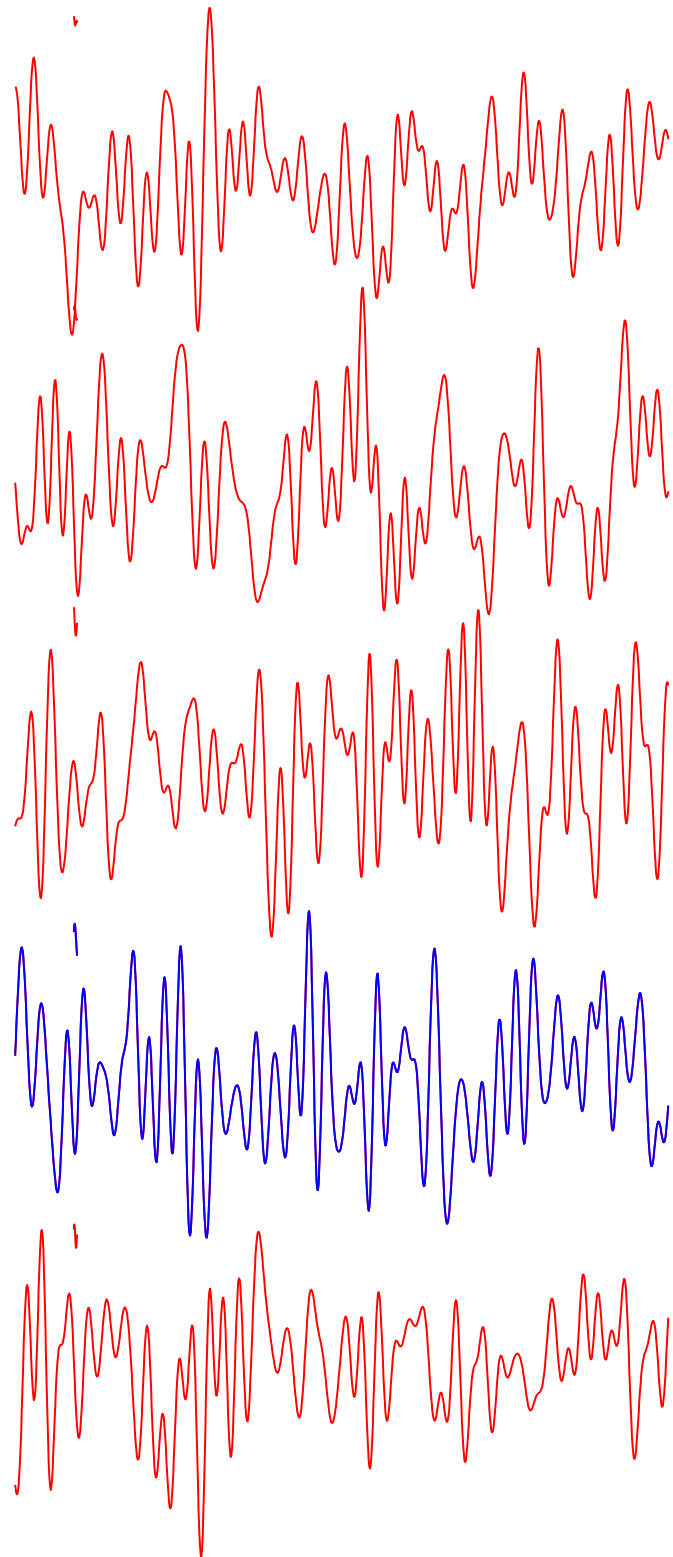
If you don't see how it possible for an older guy to be sexy and exciting, stop reading now because... [learn more about me »](#)

Less basic coding models

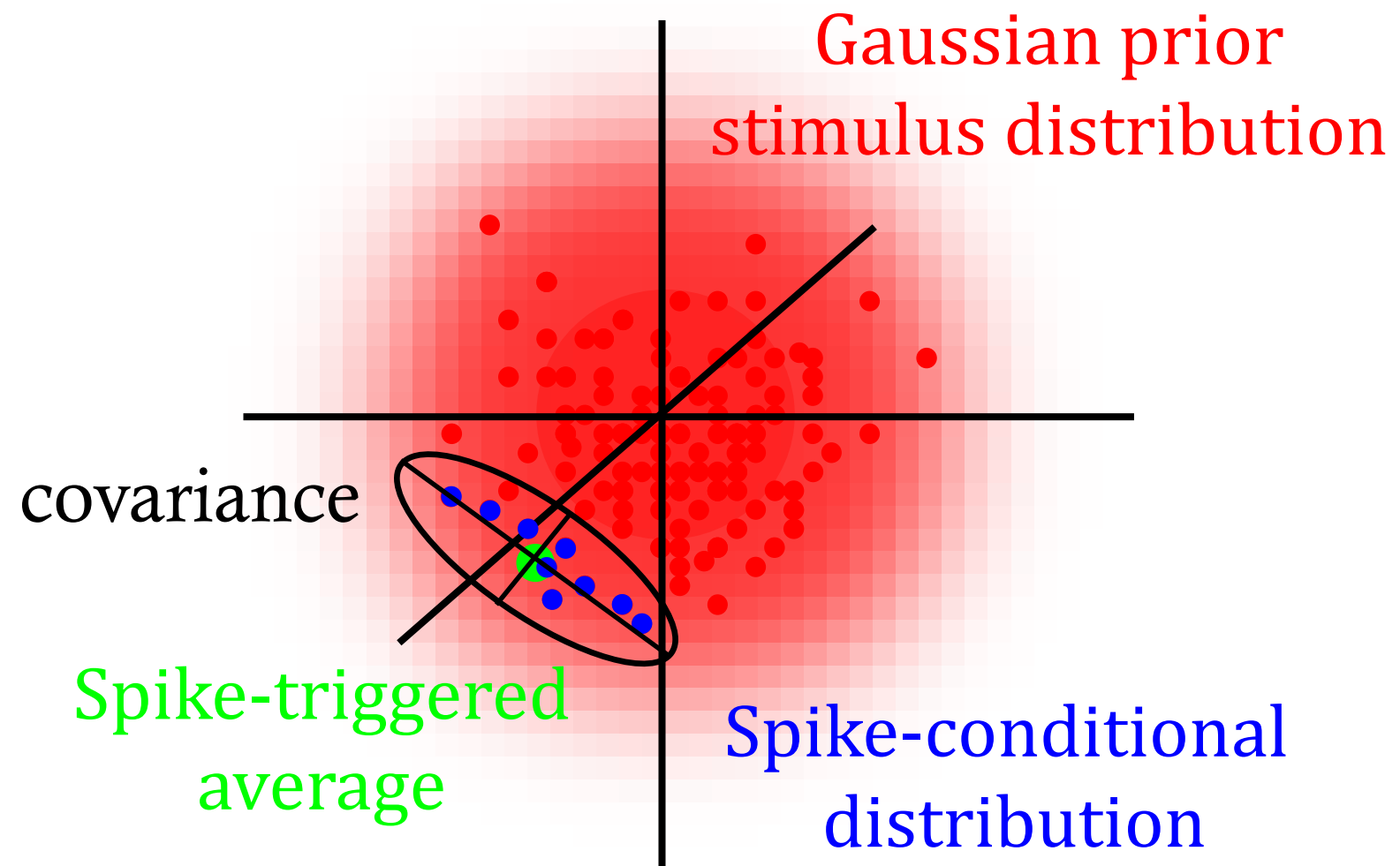
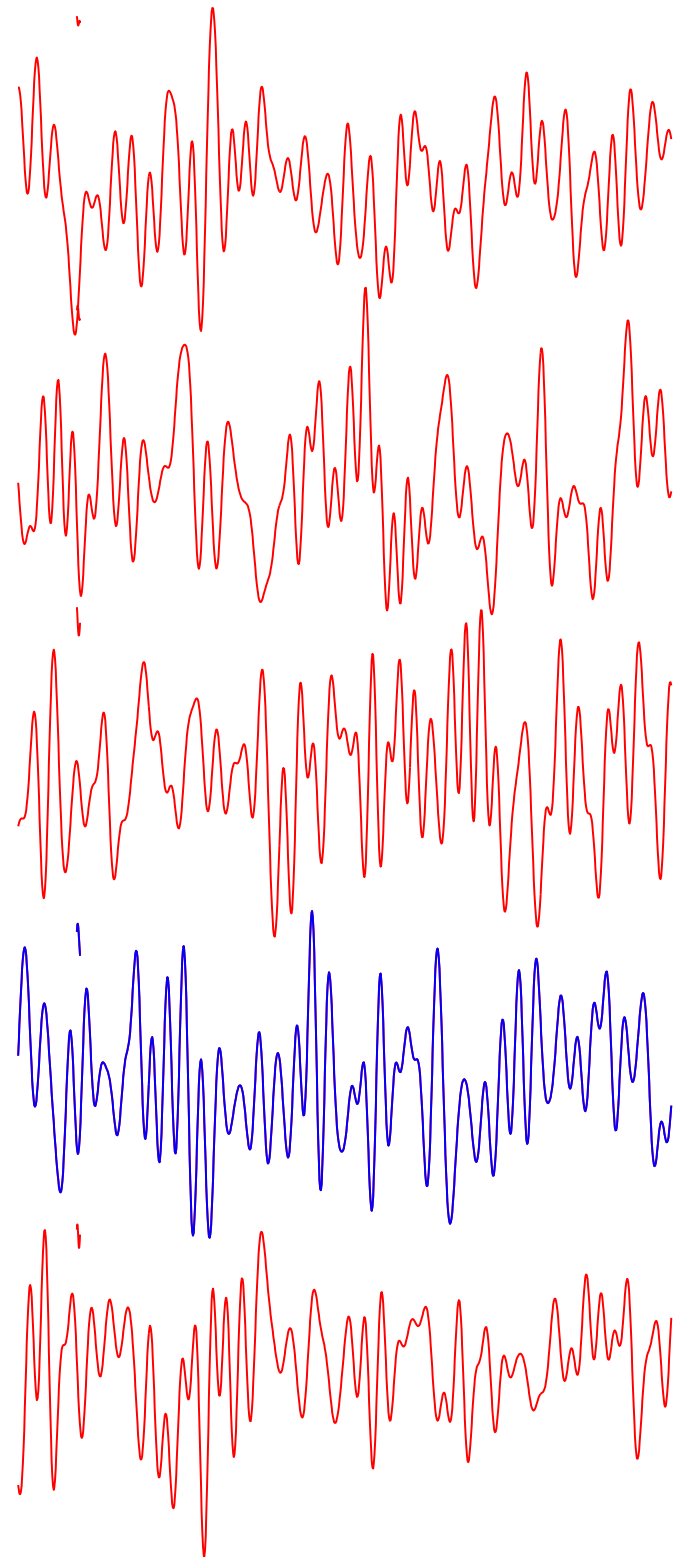


Linear filters & nonlinearity: $r(t) = g(f_1 * s, f_2 * s, \dots, f_n * s)$

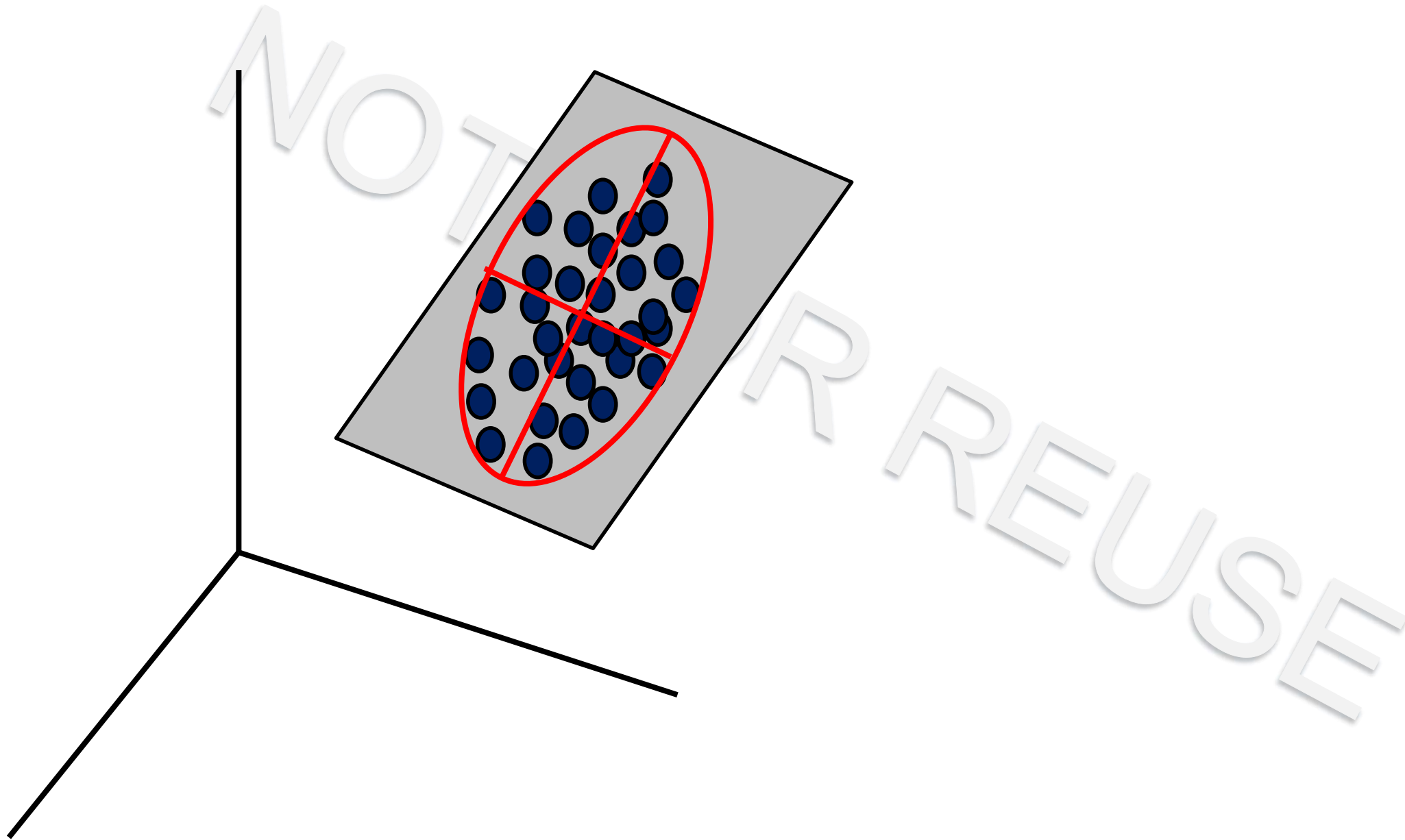
Determining multiple features from white noise



Determining multiple features from white noise



Principal component analysis



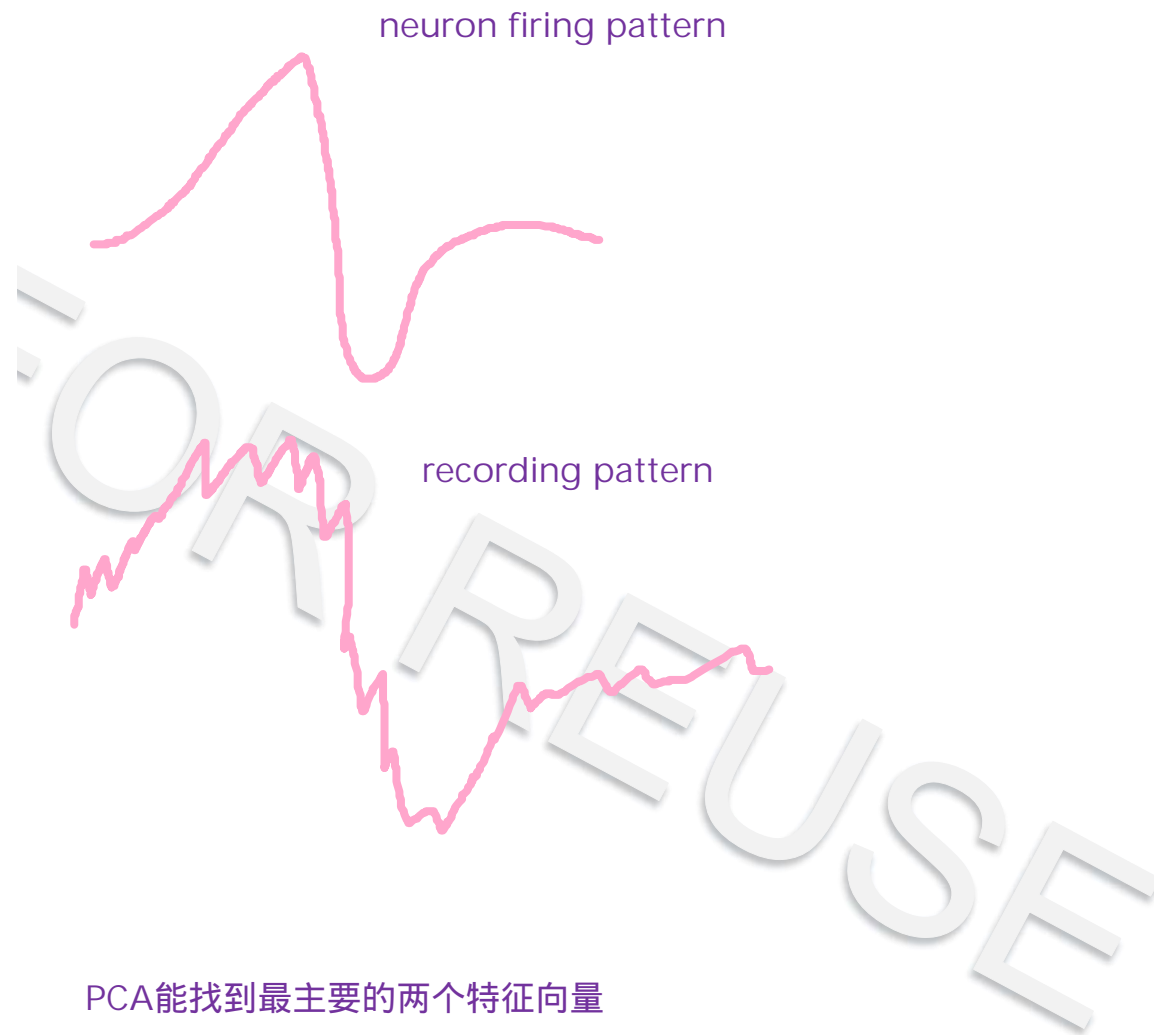
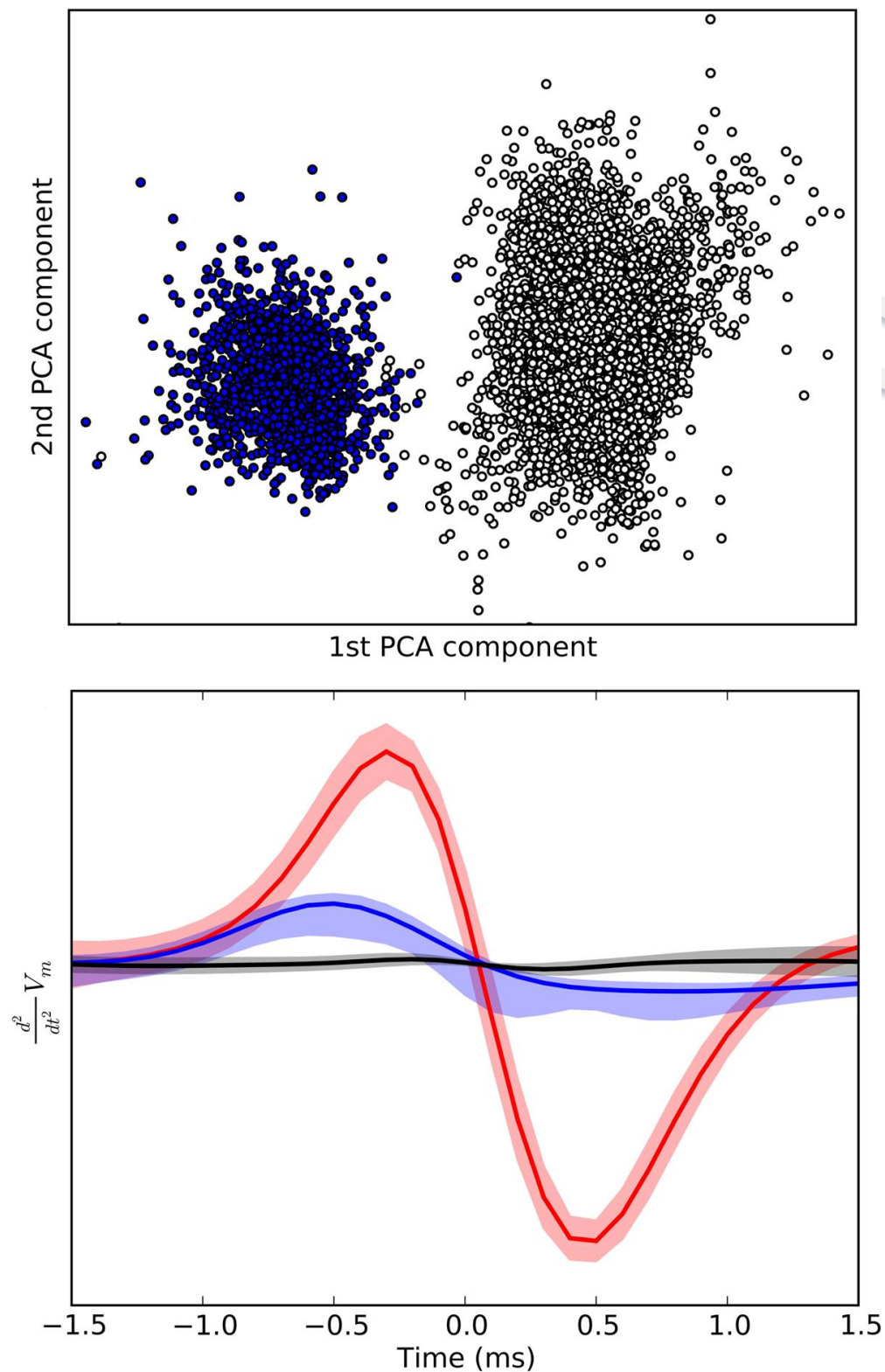
Principal component analysis: eigenfaces

NC



SE

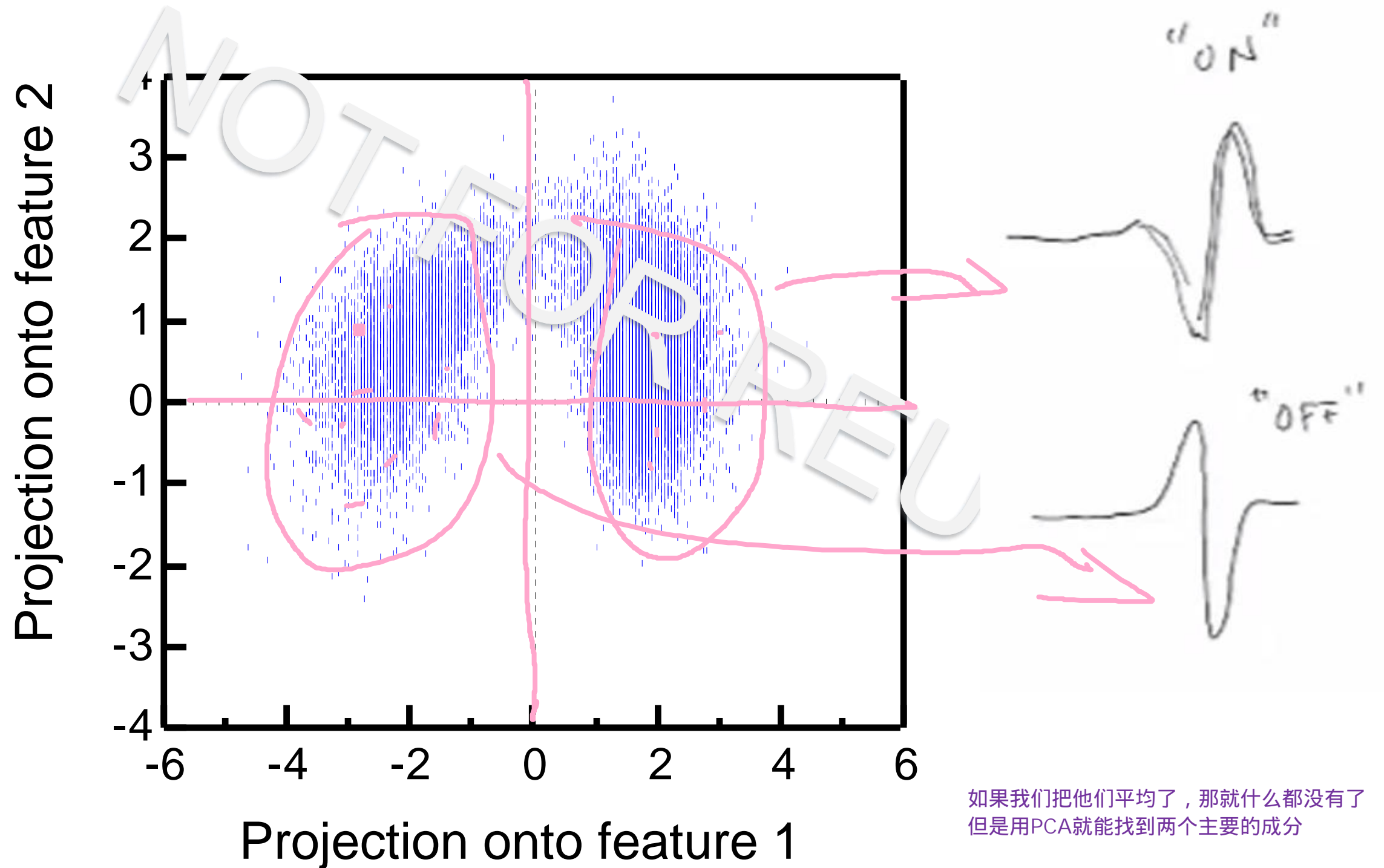
Principal component analysis: spike sorting



PCA能找到最主要的两个特征向量

Finding interesting features in the retina

看一下cluster里面的点是什么样的



NOT FOR REUSE

