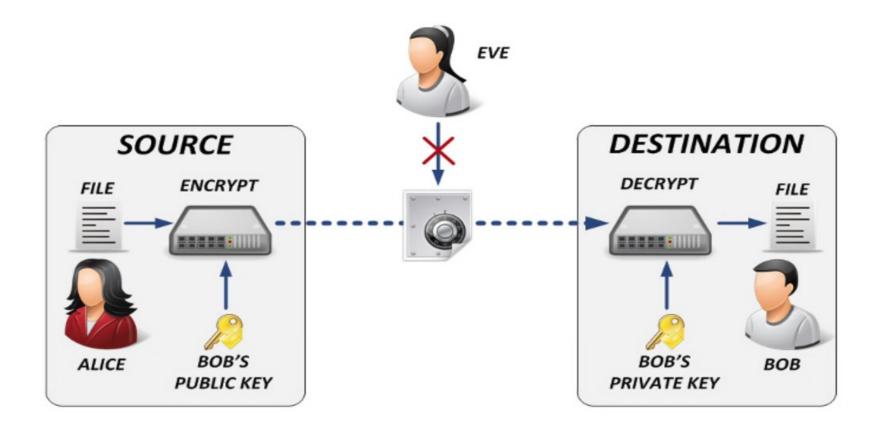
# HW2 Hill cipher

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## Cryptography



## Hill cipher

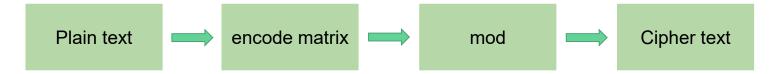
- Hill cipher 是一種簡單的加密方式,利用矩陣的乘法就可以達到線性加密的效果。
- 首先要確定字母集S(=31)

	数照表																													
Α	В	С	D	Е	F	G	Н	I	J	K	L	М	N	0	Р	Q	R	s	Т	U	٧	W	Χ	Υ	Z	_		,	?	!
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30

- Plain text: THIS IS AN APPLE.
- if n = 3
- THI S\_I S\_A N\_A PPL E.. (最後一個不足n則重複末字母補齊)
- Key:
  [ 4 9 -2]
  [ 3 5 7]
  [ 1 -6 11]
- 經過加密之後: WPK\_FJEIIXZ.OQFPM\_

### Flow chart

#### encode stage:



#### decode stage:



#### Crack password:

[encode matrix] \* [Plain] = [Cipher]

[encode matrix] = [Cipher] \* [Plain]^-1

#### How to do

#### Encode

1. Tranform "THI S\_I S\_A N\_A PPL E.." into matrix



2. Cipher = key\*Plain (mod S)



- Decode
  - 1. Find modular inverse of a matrix (a little different to inverse matrix)
  - 2. Plain = mod\_inv\_key \* Cipher (mod S)

#### util.py (在ceiba的檔案裡)

- a. inv\_key(key) may help, import it and use it.
- b. key is a numpy array.

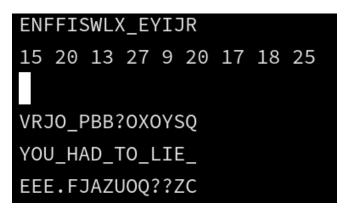
# 破解Hill Cipher

● 利用線性獨立的Plain-Cipher pair 解 Key

明文: POT TOP OPT 密文: DQY ?AN ISR

- 將明文、密文化成矩陣,若線性獨立則可逆。
  - o 加密式子 AP = C (mod S)
  - $\circ$  反推key  $A=CP^{-1}$  (mod S)
- 利用線性獨立之P推出Key之後,則可反推所有密文之明文。

## 作業規定



- 1. 每個人依據學號得到密文和明文(https://goo.gl/nyCKFN),請依照自己的學號作答。
  - a. 第一行為問題一的密文,第二行為問題一的public key,第四、五行分別為問題二的" a pair of cipher text(第四行) and plain text(第五行)",第六行為需要問題二解密的密文(the other cipher text)
- 2. 請將答案存成「學號\_ans.txt」上傳到CEIBA.
  - a. 第1行請輸入學號,第2行輸入第一題答案,3~4行第二題答案,其中第3行為KEY,第4行是 decode的結果。
  - b. ex: (非第一項說明圖片的解答)
    - 3 b02901137 2 IF\_I\_HAD\_THE\_NE 1 25 24 23 2 6 18 20 14 26 4 AFTER\_A\_WHILE\_,
- 1. 題目請見LinearAlgebraHW#2.pdf
- 2. deadline: 10/26(五) 3:00 遲交每24小時: 分數\*0.8

# key, text轉換成矩陣

無論是key還是plain text, cipher text,請用numpy.reshape來轉換成矩陣

numpy.reshape(a, (3, 4))是將 a 這個numpy array轉換成 3x4 的矩陣

#### ex:

key: 11 12 13 14 15 16 17 18 19

plain text: ABCDEFGHIJKLMNO

key會變成[[11, 12, 13], [14, 15, 16], [17, 18, 19]]

plain text會變成[[1, 2, 3, 4, 5], [6, 7, 8, 9, 10], [11, 12, 13, 14,

15]]

測資:

cipher: VJWUV,EDI

plain: IS\_THAT\_W

key: 25 8 25 9 9 16 28 21 18

請注意<u>臉書社團的Q&A</u>

作業的一些補充規定會在上面和ceiba上做更新

### Reference

李宏毅老師的說明影片: <a href="https://www.youtube.com/watch?v=G\_dATE22UqY">https://www.youtube.com/watch?v=G\_dATE22UqY</a>

現代啟示錄: Hill Cipher

https://ccjou.wordpress.com/2013/09/10/%E5%B8%8C%E7%88%BE%E5%AF%8

6%E7%A2%BC/?fbclid=IwAR175SK34eqCXJfhOsDnlk 0cEQ4bLSDG1BSSsd36

JQSMaq436LxlpJolok

# **Appendix**

#### modular inverse of a matrix

 The principle is the same, but one has to calculate the modular inverse of the matrix determinant.

$$A^{-1} = (\det A)^{-1} \operatorname{adj} A$$
  
 $\det(A) = 200$ ;  $(\det(A))^{-1} = 1/200 = 20 \pmod{31}$ 

$$A^{-1} = 20 \begin{bmatrix} \begin{vmatrix} 5 & 7 \\ -6 & 11 \end{vmatrix} & -\begin{vmatrix} 9 & -2 \\ -6 & 11 \end{vmatrix} & \begin{vmatrix} 9 & -2 \\ 5 & 7 \end{vmatrix} \\ -\begin{vmatrix} 3 & 7 \\ 1 & 11 \end{vmatrix} & \begin{vmatrix} 4 & -2 \\ 1 & 11 \end{vmatrix} & -\begin{vmatrix} 4 & -2 \\ 3 & 7 \end{vmatrix} \\ \begin{vmatrix} 3 & 5 \\ 1 & -6 \end{vmatrix} & -\begin{vmatrix} 4 & 9 \\ 1 & -6 \end{vmatrix} & \begin{vmatrix} 4 & 9 \\ 3 & 5 \end{vmatrix} \end{bmatrix}$$
 (mod 31)

not 1/200

hint: when you call np.linalg.inv(), you will get  $A^{-1}=(\det A)^{-1}\operatorname{adj} A$  but what you  $\operatorname{ne}_A^{-1}=(\det A)^{-1}\operatorname{adj} A$ 

In this case, not 1/200, replace it by det(A)^-1 mod(31)

## modular inverse of the matrix determinant

- What is 1/200 mod 31?
  - o 200 \* 20 (mod 31) = 1
  - $\circ$  1/200 (mod 31) = 20