

3. Likelihood of an Exponential Distribution

Likelihood of an Exponential Distribution

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Exercises

Let $(E, (\mathbb{P}_\theta)_{\theta \in \Theta})$ be a statistical model associated with $X_1, \dots, X_n \sim \text{Exp}(\lambda)$.

a) What is E ?

b) What is Θ ?

c) Find the likelihood of the model.

☐ (Caption will be displayed when you start playing the video.)

OK, so now let's do it for the--
sorry, let's do it for the exponential distribution.
What is E?
Yes.
Positive numbers.
Yeah, so it's 0, infinity.
Or I mean, I could put in a 0 or not, but it's 0, infinity.
What is theta?

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Product of Indicators

1/1 point (graded)
Rewrite the product $\mathbf{1}(x_1 \leq 5) \mathbf{1}(x_2 \leq 5)$ as a single indicator function. That is, find $f(x_1, x_2)$ in the following equation:

$$\mathbf{1}(x_1 \leq 5) \mathbf{1}(x_2 \leq 5) = \mathbf{1}(f(x_1, x_2) \leq 5).$$

(Choose all that apply.)

- ☐ $f(x_1, x_2) = x_1 x_2$
- ☐ $f(x_1, x_2) = \frac{x_1 + x_2}{2}$
- ☐ $f(x_1, x_2) = \text{sign}(x_1) \text{sign}(x_2)$
- ☒ $f(x_1, x_2) = \max(x_1, x_2)$ ☐
- ☐ $f(x_1, x_2) = \min(x_1, x_2)$

☐

Solution:

We need to find $f(x_1, x_2)$ such that

$f(x_1, x_2) \leq 5 \iff x_1 \leq 5 \text{ and } x_2 \leq 5$

We go through the choices in order. We leave it to you to find counter examples:

- 1. $x_1, x_2 \leq 5$ does not imply $x_1 x_2 \leq 5$;
- 2. $\frac{x_1 + x_2}{2} \leq 5$ does not imply $x_1, x_2 \leq 5$;
- 3. $\text{sign}(x_1) \text{sign}(x_2) \leq 5$ for all x_1, x_2 , and in particular does not imply $x_1, x_2 \leq 5$;
- 4. $\max(x_1, x_2) \leq 5$ if and only if both $x_1, x_2 \leq 5$, so this is a valid choice for $f(x_1, x_2)$;
- 5. $\min(x_1, x_2) \leq 5$ implies one of x_1, x_2 to be at most 5 but not necessarily both.

提交

你已经尝试了1次（总共可以尝试2次）

☐ Answers are displayed within the problem

讨论

显示讨论

主题： Unit 3 Methods of Estimation:Lecture 9: Introduction to Maximum Likelihood Estimation / 3.
Likelihood of an Exponential Distribution