

# Neural Network Summary

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# Introduction

- Activation Function
  - I. Sigmoid Function
  - II. Rel
- Optimizer
  - I. Adam
  - II. SigmoidPrime
- Loss function
  - I. Mean Squared Error

## 1 Sigmoid Function

An activation function. It is a key part of Neural Network and it can be differentiable. It can make the Neural Network unliner.

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

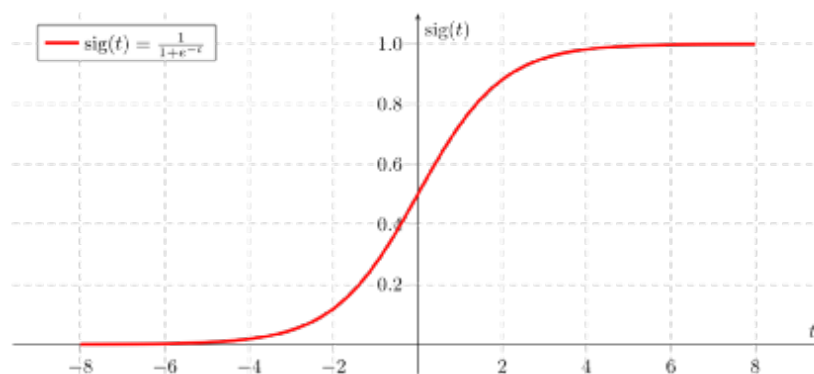


fig 1: Sigmoid; from: Toward Data Science

## 2 SigmoidPrime Function

It is an differential Sigmoid Funtion. It can reduce error of gradient so it is some kind of loss function and Let's take a look the proof of SigmoidPrime

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

$$\sigma'(x) = \frac{d}{dx}\sigma(x) = \frac{d}{dx} \frac{1}{1 + e^{-x}} = \frac{d}{dx}(1 + e^{-x})^{-1}$$

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Tip: find  $f'(x)$  if  $f(x) = \frac{A}{B+Ce^x}$   
Answer:

$$\frac{d}{dx} \left[ \frac{1}{g(x)} \right] = \frac{1'g(x) - 1g'(x)}{g(x)^2} = \frac{g'(x)}{[g(x)]^2}$$

if  $g(x)=\text{constant}$

$$\frac{d}{dx} \left[ \frac{g(x)}{h(x)} \right] = \frac{g'(x)h(x) - g(x)h'(x)}{h(x)^2} = \frac{-kh'(x)}{[h(x)]^2}$$

$$f'(x) = \frac{-A \left[ \frac{d}{dx}(B + Ce^x) \right]}{(B + Ce^x)^2} = \frac{-A(0 + Ce^x)}{(B + Ce^x)^2} = \frac{-ACe^x}{(B + Ce^x)^2}$$

-----skip-----

Hence:

$$= -(1 + e^{-x})^{-2} \frac{d}{dx}(1 + e^{-x}) = -(1 + e^{-x})^{-2} \left[ \frac{d}{dx}(1) + \frac{d}{dx}(e^{-x}) \right]$$

$$= -(1 + e^{-x})^{-2} [0 + \frac{d}{dx}(e^{-x})] = -(1 + e^{-x})^{-2} \left[ \frac{d}{dx}(e^{-x}) \right] = -(1 + e^{-x})^{-2} [e^{-x} \frac{d}{dx}(-x)]$$

$$-(1 + e^{-x})^{-2} [e^{-x}(-1)] = -(1 + e^{-x})^{-2} (-e^{-x}) = \frac{e^{-x}}{(1 + e^{-x})^2} = \frac{1(e^{-x})}{(1 + e^{-x})(1 + e^{-x})}$$

$$= \frac{1}{1+e^{-x}} \frac{e^{-x}}{1+e^{-x}} = \frac{1}{1+e^{-x}} \frac{e^{-x} + 1 - 1}{1+e^{-x}} = \frac{1}{1+e^{-x}} \left( \frac{1+e^{-x}}{1+e^{-x}} - \frac{1}{1+e^{-x}} \right)$$

$$= \sigma(x)[1 - \sigma(x)]$$

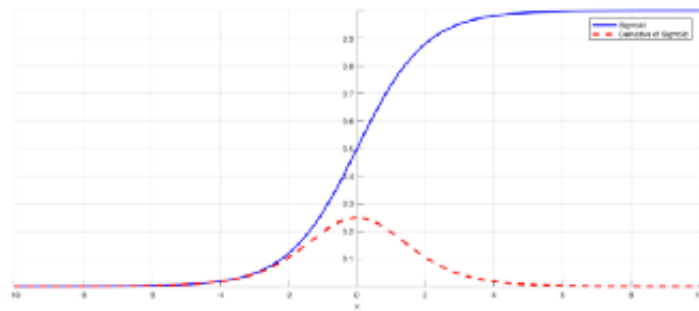


fig 2: SigmoidPrime; from: Toward Data Science

### 3 Relu Function

This is the most commonly used activation function in neural network. It also can solve the Gradient Descent problem.

$$f(x) = \max(0, x)$$

$$\begin{aligned} \text{if } x < 0, f(x) &= 0 \\ \text{else } f(x) &= x \end{aligned}$$

### 4 Adam Function

Combine the advantage of Adagrad and RMSprop. The paper contained some very promising diagrams, showing huge performance gains in terms of speed of training but in some cases Adam

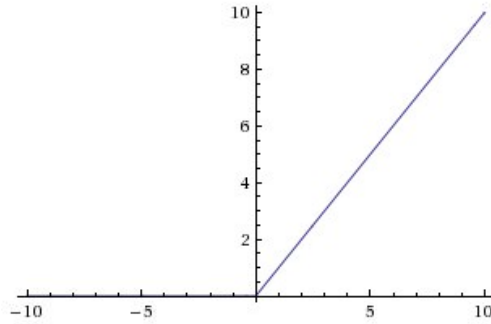


fig 3: Relu; from : [kaggle](#)

actually finds worse solution than stochastic gradient descent. Let's take a look at calculation process

$$g_t = \delta_{\theta} f(\theta)$$

First moment exponentially moving averages :  $m_t = \beta(m_{t-1}) + (1 - \beta_1)(\nabla w_t)$

$$\hat{m}_t = \frac{m_t}{1 - \beta_1^t}$$

Second moment exponentially moving averages :  $v_t = \beta_2(v_{t-1}) + (1 - \beta_2)(\nabla w_t)^2$

$$\hat{v}_t = \frac{v_t}{1 - \beta_2^t}$$

Hence, Adam Function:

$$\omega_{t-1} = \omega_t - \frac{\eta}{\sqrt{\hat{v}_t} + \epsilon} \hat{m}_t$$

## 5 Mean Squared Error

It tells you how close a regression line is to a set of points. It does this by taking the distances from the points to the regression line (these distances are the "errors") and squaring them. The squaring is necessary to remove any negative signs. It also gives more weight to larger differences. (Extracted from here).

regression line : It is a line of the minimize distance of data points.

n : number of data points

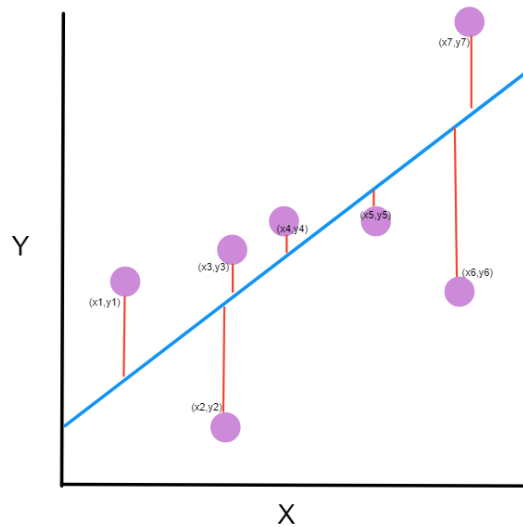


fig 4: regression line

$y_i$  : observed values

$\hat{y}_i$  : predicted values

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - \bar{y}_i)^2$$

## 6 Example Program

This is XOR in neural network program. [Checkout in Notion.](#)  
Two Layer Neural Network:

```
# numpy 建構兩層的神經網路
import numpy as np
# X = input of our 3 input XOR gate
# X=輸入三個 XOR gate 值當作 input
# set up the inputs of the neural network
  (right from the table)
#設置神經網路的輸入
X = np.array([[0,0,0],[0,0,1],[0,1,0],/
[0,1,1],[1,0,0],[1,0,1],[1,1,0],[1,1,1]], dtype=float)
#建立輸入為一維的 array，裡面元素型態為 float
# y = our output of our neural network
#y= 神經網路的輸出
```

```

#建立輸出為一維的 array，裡面元素類型為 float
y = np.array([1], [0], [0],
[0], [0],[0], [0], [1]), dtype=float)
# what value we want to predict
#我們想預測的值
#建立預測值為一維的 array，裡面元素類型為 float
xPredicted=np.array([0,0,1]), dtype=float)
# maximum of X input array # 一維X輸入數組或
最大數組通過axis指定為行
X = X/np.amax(X, axis=0)
# maximum of xPredicted (our input datafor the prediction)
#最大的 xPredicted(用於預測的輸入數據)
# 一維預測值或最大預測值，通過axis指定為行
xPredicted = xPredicted/np.amax(xPredicted, axis=0)
# set up our Loss file for graphing
#設置 Loss file 以作圖
#設置 loss 結果圖檔案為 "SumSquaredLossList.csv"
lossFile = open("SumSquaredLossList.csv", "w")
#網路中每層的 python代碼(物件導向)
#建立類別 Neural_Network，屬性 object
class Neural_Network (object):
#定義初始化物件的屬性值，並告訴類別目前是在設定哪一個物件的屬性
    def __init__(self):
        #parameters
#此物件的 inputLayerSize 屬性等於傳入的 inputLayerSize 屬性值
#隱藏層大小=3
# X1,X2,X3
        self.inputLayerSize = 3
# Y1
#此物件的 outputLayerSize 屬性等於傳入的 outputLayerSize 屬性值
#隱藏層大小=1
        self.outputLayerSize = 1
# Size of the hidden layer
#此物件的 hiddenLayerSize 屬性等於傳入的 hiddenLayerSize 屬性值
#隱藏層大小=4
        self.hiddenLayerSize = 4
# build weights of each layer
#建立每層的權重
# set to random values
#將所有權重設置為隨機值，即為互聯圖
# look at the interconnection diagram to make sense of this
# 3x4 matrix for input to hidden #用於input到hidden layer的3X4矩陣
#權重#keras的kernel
        self.W1 = \
            np.random.randn\
            (self.inputLayerSize, self.hiddenLayerSize) #0,1

```

```

# 4x1 matrix for hidden layer to output
#用於hidden layer到output的4x1矩陣
self.W2 = \
    np.random.randn
    (self.hiddenLayerSize, self.outputLayerSize) #0,1
    def activationSigmoid(self, s):
# activation function
# simple activationSigmoid curve as in the book
    return 1 / (1 + np.exp(-s))#sigmoid函数

    def feedForward(self, X):#X放入函数
# feedForward propagation傳播 through our network
# dot product of X (input) and first set of 3x4 weights
#第一個設置的3x4權重和X(input)點積
    self.z = np.dot(X, self.W1)
# the activationSigmoid activation function – neural magic
    self.z2 = self.activationSigmoid(self.z)#激勵函数
# dot product of hidden layer (z2) and second set of 4x1 weights
    self.z3 = np.dot(self.z2, self.W2)
# final activation function – more neural magic
    o = self.activationSigmoid(self.z3)#激勵函数
    return o

    def activationSigmoidPrime(self, s):#修正斜率誤差
# First derivative of activationSigmoid
#activationSigmoid的倒數
# calculus time!
#微分時間
    return s * (1 - s)

    def backwardPropagate(self, X, y, o):
# backward propagate through the network
# calculate the error in output#計算output錯誤
#計算輸出誤差
    self.o_error = y - o
# apply derivative of activationSigmoid to error
#應用 activationSigmoidPrime於錯誤
    self.o_delta = self.o_error*self.activationSigmoidPrime(o)
# z2 error: how much our hidden layer weights contributed to output
# error
#多少的隱藏層權重到output
    self.z2_error = self.o_delta.dot(self.W2.T)#轉置矩陣
# applying derivative of activationSigmoid to z2 error
#將ActivationSigmoid的導數應用於z2錯誤
    self.z2_delta =
    self.z2_error*self.activationSigmoidPrime(self.z2)

```



```

# adjusting first set (inputLayer --> hiddenLayer) weights
#調整第一組（輸入圖層->隱藏圖層）權重
    self.W1 += X.T.dot(self.z2_delta)
#adjusting second set (hiddenLayer --> outputLayer) weights
#調整第二組（隱藏層->輸出層）權重
    self.W2 += self.z2.T.dot(self.o_delta)

    def trainNetwork(self, X, y):
# feed forward the loop
#feed forward迴圈
        o = self.feedForward(X)
# and then back propagate the values (feedback)
#然後向後傳播值（反饋）
        self.backwardPropagate(X, y, o)
#將損失函數值保存到 excel 和神經網路權重文件中
#\\n 代表換行，print 出來一個新行
        def saveSumSquaredLossList(self, i, error):
            lossFile.write(str(i)+", "+str(error.tolist())+'\\n')

        def saveWeights(self):
            # save this in order to reproduce our cool network
            np.savetxt("weightsLayer1.txt", self.W1, fmt="%s")
            #將 self.W1 反向存成 txt 檔，fmt="%s" 導致數字格式化
            np.savetxt("weightsLayer2.txt", self.W2, fmt="%s")

        def predictOutput(self):
            print ("Predicted XOR output data based on
            trained weights:")
            print ("Expected (X1-X3):\\n" + str(xPredicted))
            print ("Output (Y1):\\n" + str(self.feedForward(xPredicted)))
myNeuralNetwork = Neural_Network()
trainingEpochs = 1000
#trainingEpochs = 1000
for i in range(trainingEpochs):
# train myNeuralNetwork 1,000 times
    print ("Epoch#"+ str(i) + "\\n")
    print ("Network Input:\\n" + str(X))
    print ("Expected Output of XOR Gate Neural Network:\\n"
    + str(y))
    print ("Actual Output from XOR Gate Neural Network:\\n"
    + str(myNeuralNetwork.feedForward(X)))
    # mean sum squared loss
    #平均平方損失值
    Loss = np.mean(np.square(y - myNeuralNetwork.feedForward(X)))
    myNeuralNetwork.saveSumSquaredLossList(i, Loss)
    print ("Sum Squared Loss:\\n" + str(Loss))

```

```

    print ("\n")
    myNeuralNetwork.trainNetwork(X, y)
myNeuralNetwork.saveWeights()
myNeuralNetwork.predictOutput()

```

## XOR Tensorflow in Nerual Network:

```

import tensorflow as tf

from tensorflow.keras import layers

from tensorflow.keras.layers import Activation, Dense

import numpy as np

# X = input of our 3 input XOR gate
# set up the inputs of the neural network (right from the table)
X = np.array([[0,0,0],[0,0,1],[0,1,0],
              [0,1,1],[1,0,0],[1,0,1],[1,1,0],[1,1,1]], dtype=float)
# y = our output of our neural network
y = np.array([[1], [0], [0], [0], [0],
              [0], [0], [1]], dtype=float)

#define -->compile-->fit-->evaluate-->make Predictions
model = tf.keras.Sequential()#多個網路層線性堆疊的序貫模型

model.add(Dense(4, input_dim=3, activation='relu',
use_bias=True))#Dense: output =
activation(dot(input, kernel( 權重矩陣))+bias)
#model.add(Dense(4, activation='relu', use_bias=True))
model.add(Dense(1, activation='sigmoid', use_bias=True))

model.compile(loss='mean_squared_error',optimizer='adam',
metrics=['binary_accuracy'])
#loss: 損失函數 optimizer: 優化器 metrics: 判定model的準確率(評估); 計算預測值與use_bias的符合頻率

print (model.get_weights())

history = model.fit(X, y, epochs=200, validation_data = (X,
y))#modle.fit() 用以訓練模型 ; validation_data: 在每次訓練結束時,
評估損失數據和 metrics 值

model.summary()#method to display sequential contents

```

```

# printing out to file
#. history 紀錄連續迭代的 loss 值
loss_history = history.history["loss"]

numpy_loss_history = np.array(loss_history)
np.savetxt("loss_history.txt",
numpy_loss_history, delimiter="\n") # 字串或字符的分隔列

binary_accuracy_history =
history.history["binary_accuracy"]#. history 紀錄連續迭代的 metrics 值
numpy_binary_accuracy = np.array(binary_accuracy_history)
np.savetxt("binary_accuracy.txt", numpy_binary_accuracy,
delimiter="\n")
print(np.mean(history.history["binary_accuracy"],
dtype=np.float64))
#print 出每次 metrics 的平均值

result = model.predict(X).round() # 結果預測

print (result)

```