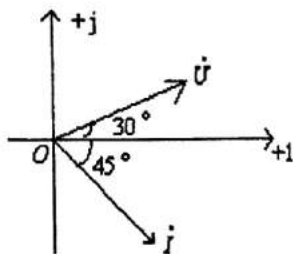


北工大电工习题专题-交流电路

4-2 非客观题(48 小题)

1. 已知 $t=0$ 时正弦量的值分别为 $u(0)=110\text{V}$, $i(0)=-5\sqrt{2}\text{A}$ 。它们的相量图如图所示, 试写出正弦量的瞬时表达式及相量。



Handwritten calculations for problem 1:

$$u = 110\sqrt{2} \sin(314t + 30^\circ) \text{ V}$$

$$i = -5\sqrt{2} \sin(314t + 45^\circ) \text{ A}$$

$$u_m = 220\text{V}$$

$$u = 220\sqrt{2} \sin(\omega t + 30^\circ)$$

$$i_m = 10\text{A}$$

$$i = 10\sqrt{2} \sin(\omega t - 45^\circ)$$

2. 已知电路中某元件的电压 u 和电流 i 分别为 $u=141\cos(314t+60^\circ)\text{V}$, $i=7\sin(314t-120^\circ)\text{A}$ 。问: (1) 元件的性质; (2) 元件的复阻抗; (3) 储存能量的最大值。

Handwritten notes for problem 2:

$u = 141\cos(314t+60^\circ)$

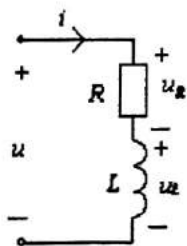
$i = 7\sin(314t-120^\circ)$

电流电压相位差 90°

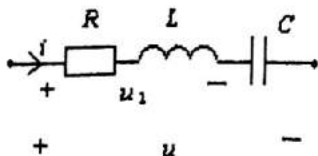
电感元件

3. 某感性电路施加一正弦交流电压 $u=220\sqrt{2}\sin 314t\text{V}$, 有功功率 $P=7.5\text{kW}$, 无功功率 $Q=5.5\text{kvar}$ 。求: (1) 电路的功率因数 λ ; (2) 若电路为 R, L 并联, R, L 值为多少?

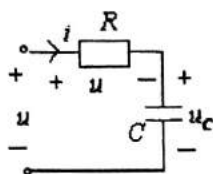
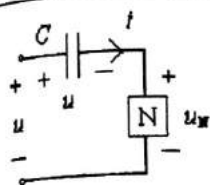
4. 在图示电路中, 电源电压 $u=220\sqrt{2}\sin 314t\text{V}$, 有功功率 $P=8.8\text{kW}$, 无功功率 $Q=6.6\text{kvar}$ 。求: 该电路的 R, L 电流 i , 电压 u_R, u_L 及功率因数 λ , 并画出相量图 ($\dot{U}, \dot{U}_R, \dot{U}_L, \dot{I}$)。



5. 图示电路中, 已知 $R=30\Omega$, $L=382\text{mH}$, $C=40\mu\text{F}$, 电源电压 $u=250\sqrt{2}\sin 314t\text{V}$ 。求电流 i 电压 u_1 , 有功功率 P 和功率因数 λ , 并画出相量图 ($\dot{U}, \dot{U}_R, \dot{U}_L, \dot{U}_C$)。

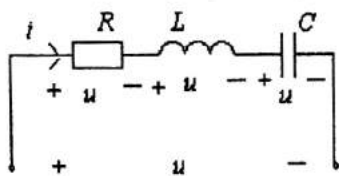
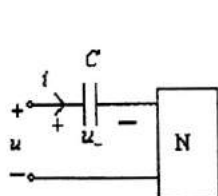


6. 左下图示电路中, $u=10\sqrt{2}\sin(1000t+60^\circ)\text{V}$, $u_C=5\sqrt{2}\sin(1000t-30^\circ)\text{V}$, 容抗 $X_C=10\Omega$ 。求无源二端网络 N 的复阻抗 Z 及有功功率 P , 并画出相量图(含电流及各电压)。



7. 在右上图示电路中, $u = 100 \cos 1000t$ V, $i = 10 \cos(1000t + \frac{\pi}{3})$ A。求: (1) R , C 及电路有功功率 P ; (2) 当 $t = \frac{\pi}{1000}$ s 时的 u_R 及 u_C 的值及实际方向; (3) 画出含 \dot{U} , \dot{I} , \dot{U}_R , \dot{U}_C 的相量图。

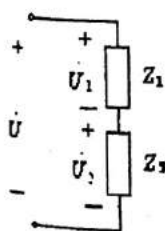
8. 在左下图示正弦交流电路中, 已知: $C = 100 \mu\text{F}$, $u = 10 \sin(10^3 t + 60^\circ)$ V, $u_C = 5 \sin(10^3 t - 30^\circ)$ V。试求电路的有功功率 P 。



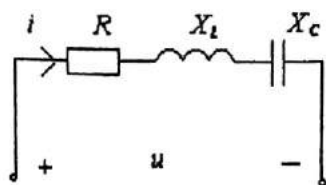
9. 在右上图示电路中, 已知: $i = 0.2 \sin(600t + 45^\circ)$ A, $R = 20 \Omega$, 感抗 $X_L = 20 \Omega$, 容抗 $X_C = 30 \Omega$ 。求: (1) L , C , u ; (2) 画出相量图 (\dot{U} , \dot{I} , \dot{U}_R , \dot{U}_L , \dot{U}_C)。

10. 在 R , L , C 串联电路中, 已知电源电压 $u = 70.7 \sin(100t + 30^\circ)$ V, 电流 $i = 1.5 \sin 100t$ A, 电容 $C = 400 \mu\text{F}$ 。试求电路的电阻 R 和电感 L 。

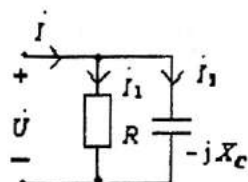
11. 阻抗 $Z_1 = 3 + j4 \Omega$, $Z_2 = 6 + j8 \Omega$ 串联于 $\dot{U} = 225 \angle 53.1^\circ$ V 的电源上工作。求: (1) Z_1 , Z_2 上的电压 u_1 , u_2 ; (2) 有功功率 P , 无功功率 Q 及功率因数 λ , 该电路呈何性质?



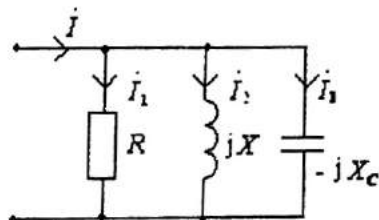
12. 在图示电路中, 已知 $i = 0.2 \sin(600t + 45^\circ)$ A, $R = 20 \Omega$, 感抗 $X_L = 20 \Omega$, 容抗 $X_C = 30 \Omega$ 。求: (1) 电压 u ; (2) 电路的有功功率, 无功功率, 视在功率和功率因数; (3) 此电路呈何性质。



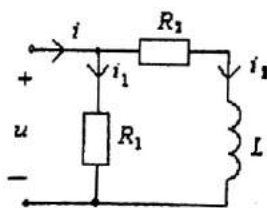
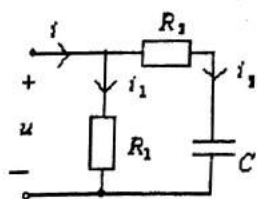
13. 在图示电路中, 电流有效值 $I = 5\text{A}$, $I_2 = 3\text{A}$, $R = 25\Omega$. 求电路的复阻抗 Z .



14. 在图示电路中, $R=8\Omega$, $X_L=22.2\Omega$, $X_C=3.13\Omega$, 总电流相量 $\dot{I}=12\angle 65.4^\circ$. 求: (1) 电流相量 \dot{I}_1 , \dot{I}_2 , \dot{I}_3 ; (2) 电路的功率因数 λ ; (3) 该电路呈何性质。

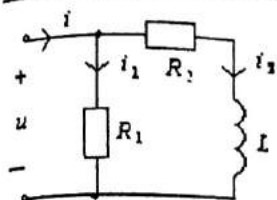


15. 在左下图示电路中, 已知 $u = 220\sqrt{2}\sin 314t\text{V}$, i_1 支路有功功率 $P_1=100\text{W}$, i_2 支路有功功率 $P_2=40\text{W}$, 功率因数 $\lambda_2=0.8$. 求电路的电流 i , 总功率 P 及功率因数 λ , 并画出 \dot{U} , \dot{I} , \dot{I}_1 , \dot{I}_2 的相量图。

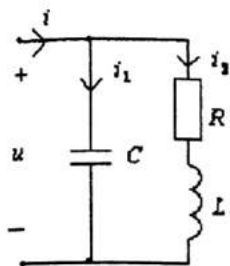


16. 在右上图所示电路中, 已知 $R_2=30\Omega$, $L=0.4\text{H}$, 两支路消耗的有功功率 $P_1=P_2=7.5\text{W}$, 电源角频率 $\omega=100\text{Rad/s}$. 求 R_1 , i , 并画相量图 (\dot{U} , \dot{I} , \dot{I}_1 , \dot{I}_2).

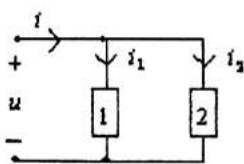
17. 在图示电路中, 已知 $u = 220\sqrt{2}\sin(314t)\text{V}$, i_1 支路有功功率 $P_1=100\text{W}$, i_2 支路 $P_2=40\text{W}$, 功率因数 $\lambda_2=0.8$. 求电流 i , 总功率 P 及总功率因数 λ , 并画相量图 (\dot{U} , \dot{I} , \dot{I}_1 , \dot{I}_2).



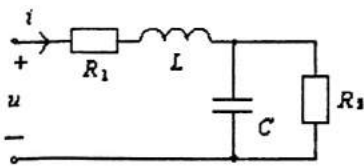
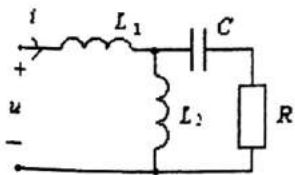
18. 在图示电路中, 已知 $u = 100\sqrt{2} \sin 1000t \text{ V}$, $R = 3\Omega$, $L = 4\text{mH}$, $C = 200\mu\text{F}$ 。求电流 i , i_1 , i_2 及总有功功率 P , 并画相量图 (\dot{U} , \dot{I} , \dot{I}_1 , \dot{I}_2)。



19. 在图示电路中, 已知 $u = 1000\sqrt{2} \sin \omega t \text{ V}$; 负载 1, 2 的功率、功率因数分别为 $P_1 = 10\text{kW}$, $\lambda = 0.8$ (容性); $P_2 = 15\text{kW}$, $\lambda = 0.6$ (感性)。(1) 求电流 i_1 , i_2 , i ; (2) 问全电路呈何性质? (3) 画相量图 (含电压及各电流)。

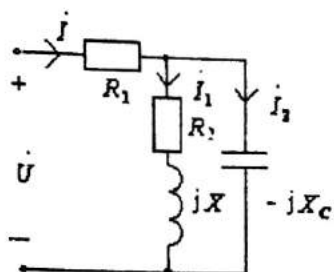


20. 在左下图示电路中, $L_1 = \frac{1}{3}\text{H}$, $L_2 = \frac{5}{6}\text{H}$, $C = \frac{1}{3}\text{F}$, $R = 2\Omega$, $i = \sin(3t + 45^\circ)\text{A}$ 。求: (1) 电压 u ; (2) 电路有功功率 P ; (3) 该电路呈何性质?

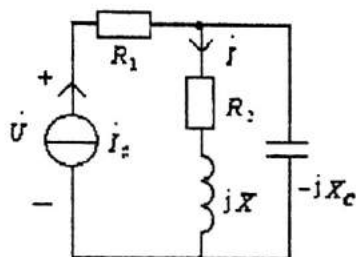


21. 在右上图所示电路中, $u = 318\sqrt{2} \sin(10000t)\text{V}$, $R_1 = R_2 = 1\Omega$, $L = 0.1\text{mH}$, $C = 100\mu\text{F}$ 。求电流 i , 总有功功率 P 及功率因数 λ 。

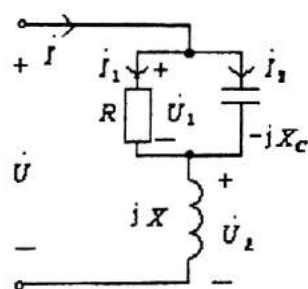
22. 在图示电路中, 已知: $R_1 = 5\Omega$, $R_2 = 3\Omega$, $X_L = X_C = 4\Omega$, $\dot{P} = 30 \angle 30^\circ$ 。求电流 \dot{I}_1 , \dot{I}_2 , 电压 \dot{U} 及总有功功率 P 。



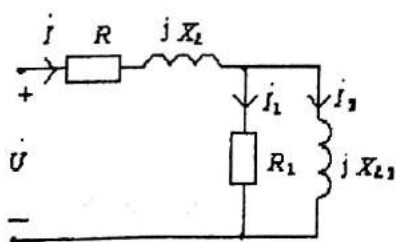
23. 在图示电路中, $R_1=5\Omega$, $R_2=3\Omega$, $X_L=X_C=4\Omega$, $\dot{I}=40\angle-60^\circ\text{A}$ 。求 \dot{I}_1 , \dot{I}_2 及电路的有功功率 P 。



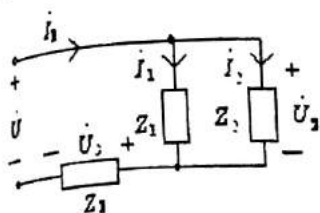
24. 在图示电路中, 电流有效值 $I_1=I_2=10\text{A}$, $\dot{U}=100\angle120^\circ\text{V}$, $\dot{U}_1=36.6\angle0^\circ\text{V}$ 。求 X_L 及总功率因数 λ 。



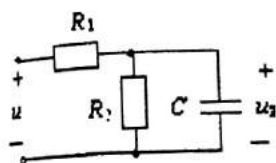
25. 在图示电路中, $R_1=5\Omega$, $R=20\Omega$, $X_L=40\Omega$, $I_1=9\text{A}$, $I_2=12\text{A}$ 。试求: (1) 电源电压的有效值 U ; (2) 电路消耗的功率及电路的功率因数 λ 。



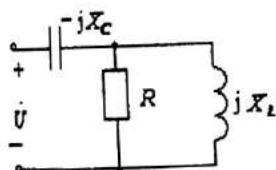
26. 在图示电路中, 已知 $Z_3=3+j3\Omega$, $\dot{I}_1=40\angle-90^\circ\text{A}$, $\dot{I}_2=40\angle0^\circ\text{A}$, $\dot{U}_2=400\angle-53.1^\circ\text{V}$ 。求: (1) Z_1 , Z_2 , \dot{U} ; (2) Z_3 消耗的有功功率 P_3 及功率因数 λ_3 ; (3) 画相量图 (\dot{I}_1 , \dot{I}_2 , \dot{I}_3 , \dot{U}_1 , \dot{U}_2 , \dot{U})。



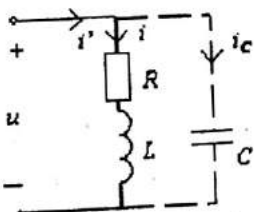
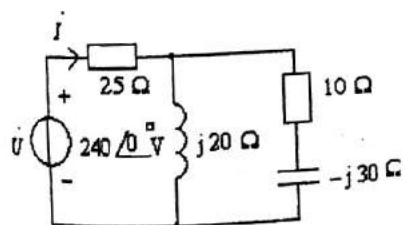
27. 在图示正弦交流电路中, $R_1=86.5\Omega$, $R_2=173\Omega$, $\frac{1}{\omega C}=100\Omega$, $U_2=17.3V$, 若以电压 u_2 为参考正弦量。试求 u 和电路的有功功率 P , 并画出关于各电压, 电流的相量图。



28. 在图示电路中, $R=X_L=X_C=1\Omega$, 电路消耗的功率 $P=1W$ 。求电压 U 及电路功率因数 λ , 并画出含支路电流及各部分电压的相量图。



29. 求左下图示电路中, 电压源 \bar{u} 供出的有功功率。



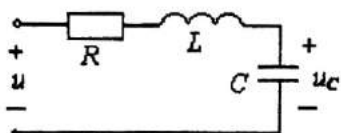
30. 在右上图示 R, L 串联电路中, 已知: $i = 2.82\sqrt{2}\sin 314t A$, $R=60\Omega$, $L=0.255H$ 。求:
(1) 若在电路两端并联 $C=11.3\mu F$ 的电容, 电源供出电流的有效值变化了多少? (2) 并联电容后的功率因数?

31. 某 R, L 串联电路, 施加正弦交流电压 $u = 220\sqrt{2}\sin 314t V$, 测得有功功率 $P=40W$, 电阻上电压 $U_R=110V$ 。试求电路的功率因数? 若将电路的功率因数提高到 0.85, 则应并联多大电容?

32. R, L, C 串联电路外加电压 $u = 100\sqrt{2} \sin 314t \text{ V}$ 时发生串联谐振, 电流 $i = \sqrt{2} \sin 314t \text{ A}$, 且 $U_C = 180 \text{ V}$ 。求电路元件的参数 R, L, C 。

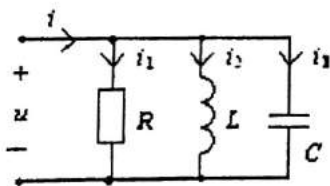
33. R, L, C 并联电路接于 $U_S = 10 \text{ V}$ 的正弦交流电源上, 已知 $R = 1 \text{ k}\Omega, L = 31.8 \text{ mH}, C = 3.18 \mu\text{F}$ 。试求: (1) 要使电路产生并联谐振, 其谐振频率 $f_0 = ?$ (2) 电路谐振时各元件通过的电流和总电流的有效值。

34. 在图示电路中, 已知 $u = 100\sqrt{2} \sin 314t \text{ V}$, 调节电容 C , 使电流 i 与电压 u 同相, 并得电容电压 $U_C = 180 \text{ V}$, 电流 $I = 1 \text{ A}$ 。(1) 求参数 R, L, C ; (2) 若 R, L, C 及 u 的有效值不变, 但将 u 的频率变为 $f = 100 \text{ Hz}$, 求电路中的电流 i 及有功功率 P , 此时电路呈何性质?

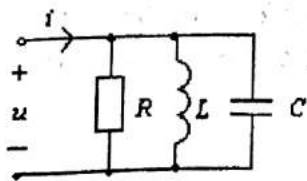


35. 某 R, L, C 串联电路中, 已知: $R = 50 \Omega, C = 10 \mu\text{F}$ 。(1) 若电源频率 $f = 1000 \text{ Hz}$ 时, 电路出现谐振, $L = ?$ (2) 若电路参数保持不变, 求 $f_1 = 500 \text{ Hz}$ 和 $f_2 = 1500 \text{ Hz}$ 时电路的复阻抗, 说明该电路各呈何性质?

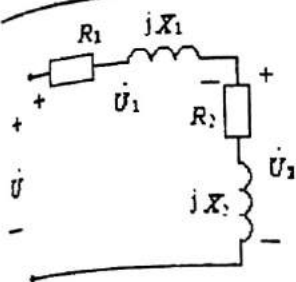
36. 在图示电路中, $R = 2.5 \text{ k}\Omega, C = 2 \mu\text{F}$, 该电路在 $f = 1000 \text{ Hz}$ 时发生谐振, 且谐振时的电流 $I_0 = 0.1 \text{ A}$ 。(1) 求 L 及 i_1, i_2, i_3 ; (2) 若电源电压有效值不变, 但频率 $f = 500 \text{ Hz}$, 求电路的功率 P , 此时电路呈何性质?



37. 在图示电路中, 已知: $u = 200\sqrt{2} \sin 314t \text{ V}, R = 25 \Omega, X_L = 50 \Omega, X_C = 20 \Omega$ 。(1) 求电流及功率因数 λ ; (2) 若电源电压 u 的有效值不变, 只调节其频率使电路谐振, 其它参数均不变, 求谐振时电路中的电流 I_0 及电源的频率 f_0 。

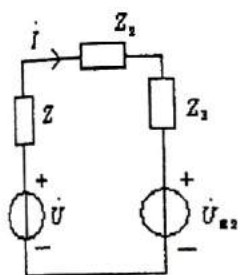


38. 某厂变电所经配电线向一车间供电, 若该车间一相等效负载的电阻 $R_2 = 10 \Omega$, 电抗 $X_2 = 10.2 \Omega$, 配电线的 $R_1 = 0.5 \Omega, X_1 = 1 \Omega$ 。(1) 欲保证车间电压 $U_2 = 220 \text{ V}$, 问电源电压 U_1 等于多少? 线路上的电压 U_L 为多少? (2) 求负载有功功率 P_2 及线路功率损失 P_L 。

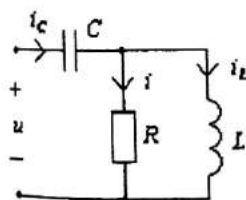


39. 已知 R, L 串联电路的有功功率 $P=8.8\text{kW}$, 无功功率 $Q=6.6\text{kvar}$, 电流 $i=70.7\sin(314t+30^\circ)\text{A}$ 。求: (1) 电源电压 u ; (2) 电路的电阻 R , 感抗 X_L 及功率因数 λ 。

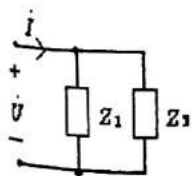
40. 在图示电路中, $Z_1=1-j\Omega$, $Z_2=2+j3\Omega$, $Z_3=3+j6\Omega$, $\dot{U}_{s1}=100\angle 60^\circ\text{V}$, $\dot{U}_{s2}=100\angle 0^\circ\text{V}$ 。求该电路的电流 \dot{I} , 有功功率 P , 无功功率 Q , 视在功率 S 及功率因数 λ 。



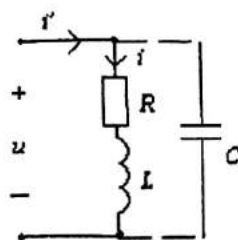
41. 图示为一正弦电路, 已知电源频率为 50Hz , $R=100\Omega$, 电流有效值 $I_C=2\text{A}$, $I_L=1.41\text{A}$, 若电路的总功率因数为 1。求 L 和 C 。



42. 图示为两复阻抗并联交流电路, 已知 $Z_1=2+j3\Omega$, $Z_2=3+j6\Omega$, Z_2 支路的视在功率 $S_2=1490\text{VA}$ 。求 Z_1 支路的有功功率 P_1 。

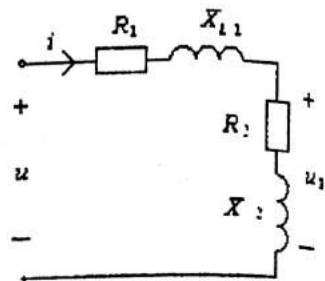


43. 在右图示电路中, 已知 $u=220\sqrt{2}\sin 314t\text{V}$, $P=10\text{kW}$, $\lambda=0.6$ 。求: (1) R, L, i ; (2) 欲使该电路的功率因数提高到 0.95, 应并联多大的电容 C ? (3) 求并联电容 C 后的总电流有效值 I' 。

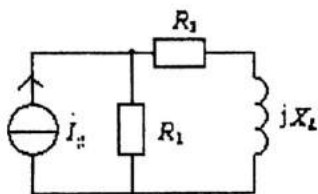


44. 在 R, L 串联电路中, 已知 $u = 100\sqrt{2} \sin 314t \text{ V}$, $i = 20\sqrt{2} \sin(314t - 53.1^\circ) \text{ A}$ 。求: (1) R, L 电路的有功功率 P , 功率因数 λ ; (2) 若 R, L 改为并联而 u 不变, 求总电流 i' , 有功功率 P' 及功率因数 λ' 。

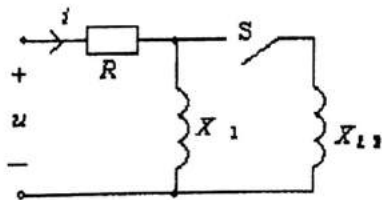
45. 在右图示正弦交流电路中, 电压有效值 $U = 150 \text{ V}$, $U_2 = 100 \text{ V}$, 电流有效值 $I = 10 \text{ A}$, 电路的有功功率 $P = 900 \text{ W}$, 电阻 $R_2 = 6 \Omega$ 。求电阻 R_1 , 感抗 X_{L1} 及 X_{L2} 。



46. 在图示电路中, $R_2 = 48 \Omega$, $X_L = 36 \Omega$, R_1, R_2 所消耗的有功功率 $P_1 = P_2 = 1.5 \text{ W}$ 。求 R_1 及电流源的电流有效值 I_S 。



47. 在图示电路中, $R = 12 \Omega$, $X_{L1} = 16 \Omega$, 电流 i 的有效值 $I = 15 \text{ A}$, 开关 S 闭合后总电流变为 $I = 20 \text{ A}$ 。求感抗 X_{L2} 。



48. 欲用额定容量 $S_N = 10 \text{ kVA}$, 电压 $u = 220\sqrt{2} \sin 314t \text{ V}$ 的正弦交流电源, 给 $P = 8 \text{ kW}$, $\lambda = 0.6$ 的感性负载供电。问: (1) 该电源供出的电流是否超过其额定电流? (2) 欲将功率因数提高到 0.95, 应并联多大的电容? (3) 并联电容后, 电源供出的电流是多少? 此时是否超过其额定电流?

4-1 单项选择题答案:

1. (c) 2. (a) 3. (b) 4. (c) 5. (a) 6. (c) 7. (c) 8. (c) 9. (a)
 10. (b) 11. (b) 12. (b) 13. (b) 14. (a) 15. (b) 16. (c) 17. (b) 18. (b) 19. (b)
 20. (a) 21. (c) 22. (b) 23. (b) 24. (b) 25. (b) 26. (a) 27. (b) 28. (c) 29. (c)
 30. (c) 31. (b) 32. (a) 33. (b) 34. (b) 35. (b) 36. (c) 37. (b) 38. (c) 39. (c)
 40. (a) 41. (b) 42. (c) 43. (a) 44. (c) 45. (a) 46. (a) 47. (c) 48. (b) 49. (a)
 50. (b) 51. (b) 52. (a) 54. (c) 55. (b) 56. (b) 59. (a)
 60. (a) 64. (a) 65. (b)

4-2 非客观题答案:

1. (1) $t=0$ 时, $u(0)=110\text{V}$, 即 $110=U_m\sin 30^\circ$, $U_m=220\text{V}$

$$u=220\sin(\omega t+30^\circ)\text{V} \quad \text{相量} \quad \dot{U}=\frac{220}{\sqrt{2}}\angle 30^\circ\text{V}=110\sqrt{2}\angle 30^\circ\text{V}$$

- (2) $t=0$ 时, $i(0)=-5\sqrt{2}\text{A}$, 即 $-5\sqrt{2}=\dot{I}_m\sin(-45^\circ)$ $I_m=10\text{A}$ $i=10\sin(\omega t-45^\circ)\text{A}$

$$\text{相量} \quad \dot{I}=\frac{10}{\sqrt{2}}\angle -45^\circ=5\sqrt{2}\angle -45^\circ\text{A}$$

2. (1) $u=141\cos(314t+60^\circ)=141\sin(314t+150^\circ)\text{V}$

u 与 i 相位差 $\varphi=150^\circ-(-120^\circ)=270^\circ$, 电流超前电压 $360^\circ-270^\circ=90^\circ$, 此元件为纯电容元件

$$(2) \text{复阻抗} \quad Z=\frac{141\angle 150^\circ}{7\angle -120^\circ}\approx 20\angle 270^\circ=20\angle -90^\circ=-j20\Omega$$

$$(3) W_{\frac{1}{2}}=\frac{1}{2}CU_{\frac{1}{2}}^2=\frac{1}{2}\times\frac{1}{X_C}\omega U_{\frac{1}{2}}^2=\frac{1}{2}\times 141^2\times\frac{1}{314\times 20}\approx 1.58\text{J}$$

$$3. (1) \tan \varphi=\frac{Q}{P}=0.73 \quad \varphi=36.25^\circ \lambda=\cos \varphi=\frac{P}{S}=0.81$$

$$(2) R=\frac{U^2}{P}=\frac{220^2}{7.5\times 10^3}=6.45\Omega \quad X_L=\frac{U^2}{Q}=\frac{220^2}{5.5\times 10^3}=8.8\Omega \quad L=\frac{X_L}{\omega}=\frac{8.8}{314}=28\text{mH}$$

$$4. \text{解: } S=\sqrt{P^2+Q^2}=\sqrt{8800^2+6600^2}=11000\text{VA}$$

$$I = \frac{S}{U} = \frac{11000}{220} = 50 \text{ A} \quad P = I^2 R \quad R = \frac{P}{I^2} = \frac{8800}{50^2} = 3.52 \Omega \quad Q = I^2 \omega L$$

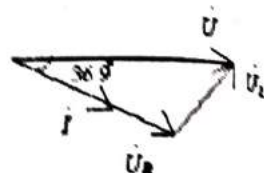
$$L = \frac{Q}{I^2 \omega} = \frac{6600}{50^2 \times 314} = 8.4 \times 10^{-3} \text{ H} = 8.4 \text{ mH} \quad \lambda = \cos \varphi = \frac{8800}{11000} = 0.8, \quad \varphi = 36.9^\circ$$

$$U_R = IR = 50 \times 3.52 = 176 \text{ V}$$

$$U_L = I \omega L = 50 \times 314 \times 0.0084 = 132 \text{ V}$$

$$i = 50\sqrt{2} \sin(314t - 36.9^\circ) \text{ A}$$

$$u_R = 176\sqrt{2} \sin(314t - 36.9^\circ) \text{ V} \quad u_L = 132\sqrt{2} \sin(314t + 53.1^\circ) \text{ V}$$



$$X_L = \omega L = 314 \times 0.382 = 120 \Omega$$

$$5. \quad X_C = \frac{1}{\omega C} = \frac{10^6}{314 \times 40} = 80 \Omega \quad |Z| = \sqrt{30^2 + (120 - 80)^2} = 50 \Omega \quad I = \frac{U}{|Z|} = \frac{250}{50} = 5 \text{ A}$$

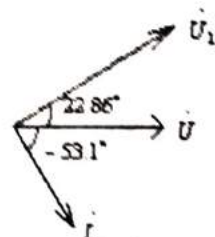
$$\tan \varphi = \frac{X}{R} = \frac{40}{30} \quad \varphi = 53.1^\circ \quad i = 5\sqrt{2} \sin(314t - 53.1^\circ) \text{ A}$$

$$\dot{U}_1 = \dot{I}(R + jX_L) = 5 \angle -53.1^\circ (30 + j120)$$

$$= 618.5 \angle 22.86^\circ \text{ V}$$

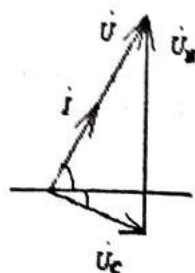
$$u_1 = 618.5\sqrt{2} \sin(314t + 22.86^\circ) \text{ V}$$

$$P = I^2 R = 5^2 \times 30 = 750 \text{ W} \quad \lambda = \cos 53.1^\circ = 0.6$$



$$6. \quad \dot{U}_R = \dot{U} - \dot{U}_C = 10 \angle 60^\circ - 5 \angle -30^\circ = 11.2 \angle 86.5^\circ \text{ V} \quad \dot{I} = \frac{\dot{U}_R}{-jX_C} = \frac{5 \angle -30^\circ}{10 \angle -90^\circ} = 0.5 \angle 60^\circ \text{ A}$$

$$Z_R = \frac{\dot{U}_R}{\dot{I}} = \frac{11.2 \angle 86.5^\circ}{0.5 \angle 60^\circ} = 22.4 \angle 26.5^\circ = 20 + j10 \Omega$$



$$P = I^2 R = 0.5^2 \times 20 = 5 \text{ W}$$

$$7. \quad (1) \quad Z = \frac{\dot{U}}{\dot{I}} = 5 - j8.66 \Omega \quad R = 5 \Omega \quad C = \frac{1}{1000 \times 8.66} = 115.5 \mu\text{F}$$

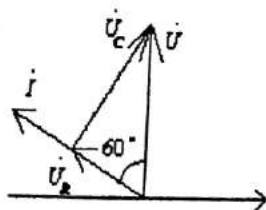
$$P = UI \cos \varphi = 250 \text{ W}$$

$$(2) u_R\left(\frac{\pi}{1000}\right) = 50 \cos\left(1000 \times \frac{\pi}{1000} + 60^\circ\right) = -25 \text{ V}$$

$$u_C\left(\frac{\pi}{1000}\right) = 86.6 \cos\left(1000 \times \frac{\pi}{1000} - \frac{\pi}{6}\right) = -75 \text{ V}$$

当 $t = \frac{\pi}{1000} \text{ s}$ 时, u_R , u_C 的实际方向与正方向相反

(3) 相量图



$$8. X_C = \frac{1}{\omega C} = 10 \Omega \quad \beta = \frac{U_{Cm}}{-jX_C} = 0.5 \angle 60^\circ \text{ A}; \quad P = UI \cos \phi = \frac{10}{\sqrt{2}} \times \frac{0.5}{\sqrt{2}} \cos(60^\circ - 60^\circ) = 2.5 \text{ W}$$

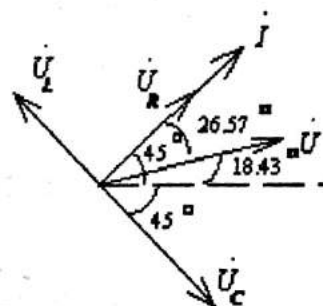
$$9. (1) u_R = i \times R = 4 \sin(600t + 45^\circ) \text{ V} \quad u_L = 6 \sin(600t - 45^\circ) \text{ V} \quad u_C = 4 \sin(600t + 135^\circ) \text{ V}$$

$$U_m = \sqrt{U_{Rm}^2 + (U_{Lm} - U_{Cm})^2} = \sqrt{4^2 + (4 - 6)^2} = 4.47 \text{ V}$$

$$\phi = \tan^{-1} \frac{(X_L - X_C)}{R} = \tan^{-1} \frac{(20 - 30)}{20} = -26.57^\circ$$

$$u = 4.47 \sin(600t + 18.43^\circ) \text{ V} \quad L = \frac{X_L}{\omega} = \frac{20}{600} = 33 \times 10^{-3} \text{ H} = 33 \text{ mH}$$

$$C = \frac{1}{\omega X_C} = \frac{1}{600 \times 30} = 55.6 \times 10^{-6} \text{ F} = 55.6 \mu\text{F}$$



$$10. |Z| = \frac{70.7}{1.5} = 47.13 \Omega \quad R = |Z| \cos 30^\circ = 47.13 \times \frac{\sqrt{3}}{2} = 40.82 \Omega$$

$$X = |Z| \sin 30^\circ = 47.13 \times \frac{1}{2} = 23.57 \Omega \quad X_C = \frac{1}{\omega C} = \frac{1}{100 \times 400 \times 10^{-6}} = 25 \Omega$$

$$\because X = X_L - X_C \therefore X_L = X + X_C = 23.57 + 25 = 48.57 \Omega$$

$$L = \frac{X_L}{\omega} = \frac{48.57}{100} = 486 \text{ mH}$$

$$11. (1) \dot{I} = \frac{\dot{U}_s}{Z_1 + Z_2} = \frac{225 \angle 53.1^\circ}{(3 + j4) + (6 + j8)} = 15 \angle 0^\circ$$

$$\dot{U}_1 = \dot{I} Z_1 = 15 \angle 0^\circ \times (3 + j4) = 75 \angle 53.1^\circ \text{ V}$$

$$\dot{U}_2 = \dot{I} Z_2 = 15 \angle 0^\circ \times (6 + j8) = 150 \angle 53.1^\circ \text{ V}$$

$$u_1 = 75\sqrt{2} \sin(\omega t + 53.1^\circ) \text{ V} \quad u_2 = 150\sqrt{2} \sin(\omega t + 53.1^\circ) \text{ V}$$

$$(2) \lambda = \frac{P}{S} = \cos \varphi = \cos 53.1^\circ = 0.6 \quad P = UI \lambda = 225 \times 15 \times 0.6 = 2025 \text{ W}$$

$$Q = UI \sin \varphi = 225 \times 15 \times 0.8 = 2700 \text{ Var} \quad \varphi \text{ 超前 } \beta, \text{ 该电路呈感性}$$

$$(1) Z = R + j(X_L - X_C) = 20 + j(20 - 30)$$

$$12. = 22.36 \angle -26.57^\circ \Omega$$

$$\dot{U}_Z = \dot{I}_Z Z = 0.2 \angle 45^\circ \times 22.36 \angle -26.57^\circ$$

$$= 4.47 \angle 18.4^\circ \text{ V}$$

$$u = 4.47 \sin(600t + 18.4^\circ) \text{ V}$$

$$(2) P = I^2 R = \left(\frac{0.2}{\sqrt{2}}\right)^2 \times 20 = 0.4 \text{ W} \quad Q = I^2 X = \left(\frac{0.2}{\sqrt{2}}\right)^2 \times (-10) = -0.2 \text{ Var}$$

$$S = UI = \frac{4.47}{\sqrt{2}} \times \frac{0.2}{\sqrt{2}} = 0.447 \text{ VA} \quad \lambda = \frac{P}{S} = \cos \varphi = \cos(-26.57^\circ) = 0.89$$

(3) 电路呈容性

$$13. I_1 = \sqrt{I^2 - I_2^2} = 4 \text{ A} \quad \text{设: } \dot{I}_1 = 4 \angle 0^\circ \text{ A} \quad \dot{U}_s = \dot{I}_1 R = 100 \angle 0^\circ \text{ V}$$

$$\dot{I}_s = 5 \angle \arctan \frac{3}{4} = 5 \angle 36.9^\circ \text{ A} \quad Z = \frac{\dot{U}_s}{\dot{I}_s} = 20 \angle -36.9^\circ \Omega$$

$$14. (1) Z_{LC} = \frac{-j^3 X_L X_C}{jX_L - jX_C} = -j3.64 \Omega \quad \dot{I}_1 = \dot{I}_s \frac{Z_{LC}}{R + Z_{LC}} = 5 \angle 0^\circ \text{ A}$$

$$\dot{U}_R = \dot{I}_1 R = 40 \angle 0^\circ \text{ V} \quad \dot{I}_2 = \frac{\dot{U}_R}{jX_L} = 1.8 \angle -90^\circ \text{ A} \quad \dot{I}_3 = \frac{\dot{U}_R}{-jX_C} = 12.7 \angle 90^\circ \text{ A}$$

$$(2) \lambda = \frac{P}{S} = \cos \varphi = \cos 65.4^\circ = 0.42$$

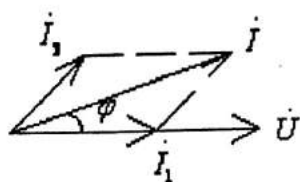
(3) φ 超前于 u_R (即电源电压 u), \therefore 电路呈容性

$$15. I_1 = \frac{P_1}{U} = \frac{100}{220} = 0.45 \text{ A} \quad I_2 = \frac{P_2}{U \lambda_2} = \frac{40}{220 \times 0.8} = 0.23 \text{ A}$$

$$\varphi = 36.9^\circ \quad \dot{I}_2 = 0.23 \angle 36.9^\circ \text{ A} \quad \dot{I} = 0.45 + 0.23 \angle 36.9^\circ = 0.45 + 0.18 + j0.14 = 0.65 \angle 12.5^\circ \text{ A}$$

$$i = 0.65\sqrt{2} \sin(314t + 12.5^\circ) \text{ A} \quad \lambda = \cos 12.5^\circ = 0.976$$

$$P = UI \cos \varphi = 220 \times 0.65 \cos 12.5^\circ = 139.61 \text{ W}$$

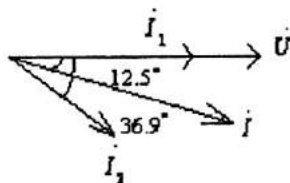
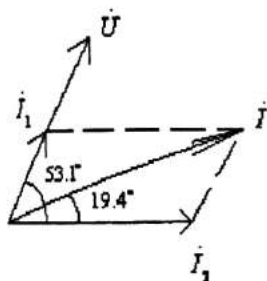


$$16. (1) \quad P_2 = I_2^2 R_2 \quad I_2 = \sqrt{\frac{P_2}{R_2}} = 0.5 \text{ A} \quad \text{设: } \dot{I}_2 = 0.5 \angle 0^\circ \text{ A}$$

$$\dot{U} = \dot{I}_2 (R_2 + j\omega L) = 25 \angle 53.1^\circ \text{ V} \quad R_1 = \frac{U^2}{P} = 83.33 \Omega \quad \dot{I}_1 = \frac{\dot{U}}{R_1} = 0.3 \angle 53.1^\circ \text{ A}$$

$$\dot{I} = \dot{I}_1 + \dot{I}_2 = 0.72 \angle 19.4^\circ \text{ A} \quad i = 0.72\sqrt{2} \sin(100t + 19.4^\circ) \text{ A}$$

(2) 相量图见左下图



$$17. \quad I_1 = \frac{P_1}{U} = \frac{100}{220} = 0.45 \text{ A} \quad I_2 = \frac{P}{U \lambda_2} = \frac{40}{220 \times 0.8} = 0.23 \text{ A} \quad \varphi_2 = 36.9^\circ$$

$$\dot{I} = \dot{I}_1 + \dot{I}_2 = 0.45 \angle 0^\circ + 0.23 \angle -36.9^\circ = 0.65 \angle -12.5^\circ \text{ A}$$

$$i = 0.65\sqrt{2} \sin(314t - 12.5^\circ) \text{ A} \quad \lambda = \cos 12.5^\circ = 0.98 \quad P = P_1 + P_2 = 100 + 40 = 140 \text{ W}$$

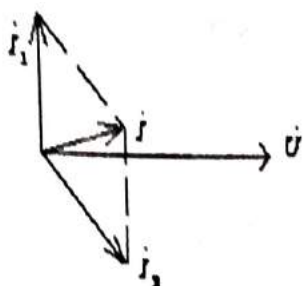
相量图见右上图

$$18. \quad Z_1 = -j \frac{1}{\omega C} = -j5 \Omega \quad Z_2 = R + j\omega L = (3 + j4) \Omega \quad \dot{I}_1 = \frac{\dot{U}}{Z_1} = 20 \angle 90^\circ \text{ A}$$

$$\dot{I}_2 = 20 \angle -53.1^\circ \text{ A} \quad \dot{I} = \dot{I}_1 + \dot{I}_2 = (12 + j4) \text{ A} \quad i_1 = 20\sqrt{2} \sin(1000t + 90^\circ) \text{ A}$$

$$i_2 = 20\sqrt{2} \sin(1000t - 53.1^\circ) \text{ A} \quad i = 12.65\sqrt{2} \sin(1000t + 18.4^\circ) \text{ A}$$

$$P = UI \lambda = 1.2 \text{ kW}$$



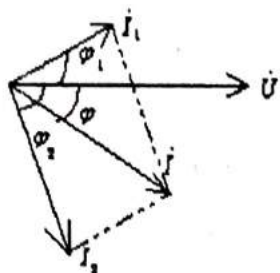
19. (1) $I_1 = \frac{P_1}{U \lambda_1} = \frac{10000}{1000 \times 0.8} = 12.5 \text{ A} \quad \varphi_1 = 36.9^\circ$

$I_2 = \frac{P_2}{U \lambda_2} = \frac{15000}{1000 \times 0.6} = 25 \text{ A} \quad \varphi_2 = 53.1^\circ \quad \dot{P} = \dot{P}_1 + \dot{P}_2 = 28 \angle -26.6^\circ \text{ A}$

$i_1 = 12.5\sqrt{2} \sin(\omega t + 36.9^\circ) \text{ A} \quad i_2 = 25\sqrt{2} \sin(\omega t - 53.1^\circ) \text{ A}$

$i = 28\sqrt{2} \sin(\omega t - 26.6^\circ) \text{ A}$

(2) 全电路呈感性



(3) 相量图:

20. (1) $Z = jX_{L1} + \frac{(R - jX_C)jX_{L2}}{(R - jX_C) + jX_{L2}} = 2.83 \angle 45^\circ \Omega$

$\dot{U}_m = \dot{I}_m Z = 2.83 \angle 90^\circ \text{ V} \quad u = 2.83 \sin(3t + 90^\circ) \text{ V}$

(2) $P = UI \lambda = 1 \text{ W}$ (3) u 超前 i 45° , 电路呈感性

21. $Z = R_1 + j\omega L + \frac{-jR_2/\omega C}{R_2 - j/\omega C} = 1.59 \angle 18.4^\circ \Omega$

$\dot{I} = \frac{\dot{U}}{Z} = 200 \angle -18.4^\circ \text{ A} \quad i = 200\sqrt{2} \sin(10000t - 18.4^\circ) \text{ A}$

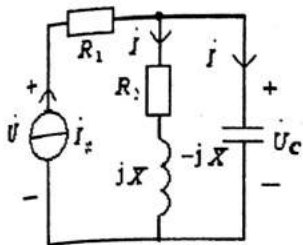
$\lambda = \cos 18.4^\circ = 0.95, \quad P = UI \lambda = 60.42 \text{ kW}$

22. $\dot{I}_2 = \dot{I} \frac{R_2 + jX_L}{(R_2 + jX_L) - jX_C} = 50 \angle 83^\circ \text{ A}$

$$\dot{I}_1 = \frac{\dot{U}_1}{(R_2 + jX_L) - jX_C} = 40 \angle -60^\circ \text{ A} \quad \dot{U} = \dot{I}_1 R_1 + \dot{I}_1 (R_2 + jX_L) = 332.8 \angle 8.7^\circ \text{ V}$$

$$\lambda = \cos(8.7^\circ - 30^\circ) = 0.93 \quad P = UI\lambda = 9.3 \text{ kW}$$

23. 电容两端电压 \dot{U}_C 及通过的电流 \dot{I}_C 正方向如图中所设



$$\dot{U}_C = \dot{I}_C (R_2 + jX_L) = 200 \angle -6.9^\circ \text{ V} \quad \dot{I}_C = \frac{\dot{U}_C}{-jX_C} = 50 \angle 83.1^\circ \text{ A}$$

$$\dot{I}_S = \dot{I}_1 + \dot{I}_C = 30 \angle 30^\circ \text{ A} \quad \dot{U} = \dot{I}_S R_1 + \dot{U}_C = 332.5 \angle 8.8^\circ \text{ V}$$

$$P = I_S^2 R_1 + I^2 R_2 = 9.3 \text{ kW}$$

$$24. \quad \dot{I}_1 = 10 \angle 0^\circ \text{ A} \quad \dot{I}_2 = 10 \angle 90^\circ \text{ A}; \quad \dot{I} = \dot{I}_1 + \dot{I}_2 = 10\sqrt{2} \angle 45^\circ \text{ A}$$

$$\dot{U}_2 = \dot{U} - \dot{U}_1 = 86.6\sqrt{2} \angle 135^\circ \text{ V}; \quad X_L = \frac{U_L}{I} = 8.66 \Omega; \quad \lambda = \cos(120^\circ - 45^\circ) = 0.26$$

$$25. (1) \text{ 设 } \dot{I}_1 = 9 \angle 0^\circ \text{ A} \quad \text{则 } \dot{I}_2 = 12 \angle -90^\circ \text{ A}; \quad \dot{I} = \dot{I}_1 + \dot{I}_2 = 15 \angle -53.1^\circ \text{ A}$$

$$\dot{U} = \dot{I}_1 R_1 + \dot{I} (R + jX_L) = 714.8 \angle 9.66^\circ \text{ V} \quad U = 714.8 \text{ V}$$

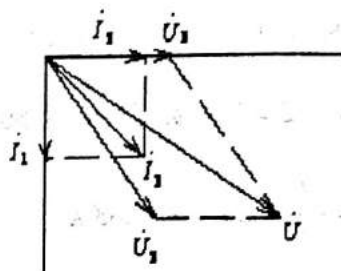
$$(2) \quad \lambda = \cos(9.66^\circ + 53.1^\circ) = 0.46 \quad P = UI\lambda = 4.93 \text{ kW}$$

$$26. \quad Z_1 = \frac{\dot{U}_2}{\dot{I}_1} = 8 + j6 \Omega \quad Z_2 = \frac{\dot{U}_2}{\dot{I}_2} = 6 - j8 \Omega$$

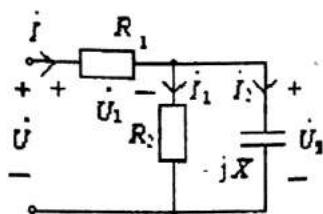
$$\dot{I}_3 = \dot{I}_1 + \dot{I}_2 = 40 - j40 \text{ A}$$

$$\dot{U}_3 = \dot{I}_3 Z_3 = 240 \angle 0^\circ \text{ V} \quad \dot{U} = \dot{U}_2 + \dot{U}_3 = 576.9 \angle -33.7^\circ \text{ V}$$

$$P_3 = I_3^2 \times R_3 = 9.6 \text{ kW} \quad \lambda_3 = \cos 45^\circ = 0.707$$



27. (1) 电路的相量模型如图示

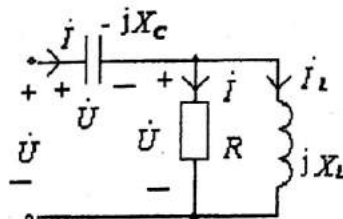
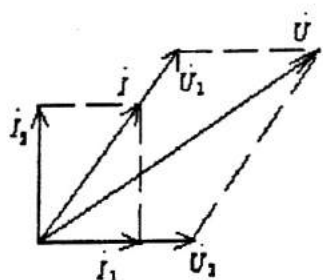


设 $\dot{U}_2 = 17.3 \angle 0^\circ \text{ V}$ 则 $\dot{I}_2 = \frac{\dot{U}_2}{-jX_c} = 0.173 \angle 90^\circ \text{ A}$ $\dot{I}_1 = \frac{\dot{U}_2}{R_2} = 0.1 \angle 0^\circ \text{ A}$

$\dot{I} = \dot{I}_1 + \dot{I}_2 = 0.2 \angle 60^\circ \text{ A}$ $\dot{U}_1 = \dot{I}_1 R_1 = 17.3 \angle 60^\circ \text{ V}$ $\dot{U} = \dot{U}_1 + \dot{U}_2 = 30 \angle 30^\circ \text{ V}$

$u = 30\sqrt{2} \sin(\omega t + 30^\circ) \text{ V}$ $P = UI \cos \varphi = 5.19 \text{ W}$

(2) 相量图:



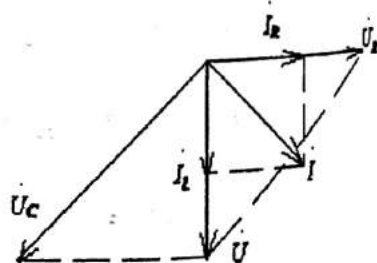
28. 各支路电流和各部分电压相量正方向如右上图中所标示:

$U_R = \sqrt{R P} = 1 \text{ V}$ 设 $\dot{U}_R = 1 \angle 0^\circ \text{ V}$ 则

$\dot{I} = \dot{I}_R + \dot{I}_L = 1 \angle 0^\circ + 1 \angle -90^\circ = \sqrt{2} \angle -45^\circ \text{ A}$

$\dot{U} = \dot{I}(-jX_c) + \dot{U}_R = \sqrt{2} \angle -135^\circ + 1 \angle 0^\circ = 1 \angle -90^\circ \text{ V}$

$\lambda = \cos \varphi = \cos(-90^\circ - (-45^\circ)) = 0.707$



相量图(根据所设参量而确定, 答案不唯一)

29. $Z = 25 + j20 // (10 - j30) = 60.38 \angle 41.63^\circ \Omega$

$\dot{I} = \frac{\dot{U}}{Z} = 3.97 \angle -41.63^\circ \text{ A}$ $P = UI \cos \varphi = 240 \times 3.97 \times \cos 41.63^\circ = 712.17 \text{ W}$

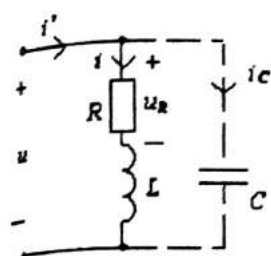
30. (1) $X_L = \omega L = 80 \Omega$ $\dot{U} = \dot{I}(R + jX_L) = 282 \angle 53.1^\circ \text{ V}$

并联电容 C 后 $\dot{I}_C = \frac{\dot{U}}{-jX_C} = j282 \angle 53.1^\circ \times 314 \times 11.3 \times 10^{-6} = 1 \angle 143.1^\circ \text{ A}$

$$I = I_R + I_C = 2.82 \angle 0^\circ + 1 \angle 143.1^\circ = 2.11 \angle 16.5^\circ \text{ A} \quad \Delta I = 2.82 - 2.11 = 0.71 \text{ A}$$

总电流比原电路降低 0.71 A (2) $\lambda' = \cos(53.1^\circ - 16.5^\circ) = 0.8$

31. (1) 电路如图:



$$\lambda = \cos \varphi = \frac{U_R}{U} = \frac{110}{220} = 0.5$$

$$(2) \cos \varphi = 0.5 \quad \tan \varphi = 1.73 \quad \lambda' = \cos \varphi' = 0.85 \quad \tan \varphi' = 0.62$$

$$C = \frac{P}{\omega U^2} (\tan \varphi - \tan \varphi') = \frac{40}{314 \times 220^2} (1.73 - 0.62) = 2.93 \times 10^{-6} \text{ F} = 2.93 \mu\text{F}$$

$$32. \quad R = \frac{U}{I} = \frac{100}{1} = 100 \Omega \quad X_L = X_C = \frac{U_C}{I} = \frac{180}{1} = 180 \Omega \quad L = \frac{X_L}{\omega} = 5.73 \times 10^{-1} \text{ H}$$

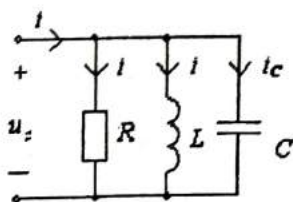
$$C = \frac{1}{\omega X_C} = 17.6 \mu\text{F}$$

33. 电路如图所示:

$$(1) f_0 = \frac{1}{2\pi\sqrt{LC}} = 500 \text{ Hz}$$

$$(2) \text{电路谐振时, } X_L = 2\pi f_0 L = 100 \Omega$$

$$I_C = I_L = \frac{U_S}{X_L} = 0.1 \text{ A} \quad I = I_R = \frac{U_S}{R} = 0.01 \text{ A}$$



$$34. (1) U = U_R \quad R = \frac{U}{I} = 100 \Omega \quad X_C = \frac{U_C}{I} = 180 \Omega \quad C = \frac{1}{\omega X_C} = 17.7 \mu\text{F}$$

$$X_L = X_C \quad L = \frac{X_L}{\omega} = 0.573 \text{ H}$$

$$(2) f = 100 \text{ Hz 时: } X_L = 360 \Omega \quad X_C = 90 \Omega \quad Z = R + j(X_L - X_C) = 287.9 \angle 69.7^\circ \Omega$$

$$I = \frac{U}{|Z|} = 0.35 \text{ A}$$

$$i = 0.35\sqrt{2} \sin(628t - 69.7^\circ) \text{ A} \quad P = UI \cos \varphi = 12.14 \text{ W}$$

此时电路呈感性

$$35. \quad (1) \quad L = \frac{1}{(2\pi f_0)^2 C} = 2.54 \times 10^{-3} \text{ H} = 2.54 \text{ mH}$$

$$(2) \text{ 当 } f_1 = 500 \text{ Hz 时, } Z_1 = 50 + j(2\pi f_1 L - \frac{1}{2\pi f_1 C}) = 50 + j(7.96 - 31.85) = 50 - j23.89 \Omega$$

电路呈容性:

$$\text{当 } f_2 = 1500 \text{ Hz 时, } Z_2 = 50 + j(7.96 \times 3 - \frac{31.85}{3}) = 50 + j13.28 \Omega, \text{ 电路呈感性}$$

$$36. \quad (1) \text{ 谐振时 } I_1 = I_0 = \frac{U}{R} \quad U = RI_0 = 250 \text{ V} \quad L = \frac{1}{(2\pi f_0)^2} = 0.0127 \text{ H}$$

$$I_2 = \frac{U}{j\omega L} = 3.13 \angle -90^\circ \text{ A} \quad I_3 = -I_2 = 3.13 \angle 90^\circ \text{ A}$$

$$i_1 = 0.1\sqrt{2} \sin(6280t + 0^\circ) \text{ A} \quad i_2 = 3.13\sqrt{2} \sin(6280t - 90^\circ) \text{ A}$$

$$i_3 = 3.13\sqrt{2} \sin(6280t + 90^\circ) \text{ A}$$

$$(2) \quad f = 500 \text{ Hz 时, } X_C > X_L \quad I_L > I_C, \text{ 电路呈感性, } P = I_1^2 R = 25 \text{ W}$$

$$37. \quad (1) \quad I_R = \frac{U}{R} = 8 \angle 0^\circ \text{ A} \quad I_L = \frac{U}{jX_L} = 4 \angle -90^\circ \text{ A} \quad I_C = \frac{U}{-jX_C} = 10 \angle 90^\circ \text{ A}$$

$$I = I_R + I_L + I_C = 10 \angle 36.9^\circ \text{ A} \quad i = 10\sqrt{2} \sin(314t + 36.9^\circ) \text{ A} \quad \lambda = \cos \varphi = 0.6$$

$$(2) \quad I_0 = \frac{U}{R} = 8 \text{ A} \quad L = \frac{X_L}{\omega} = 0.159 \text{ H} \quad C = \frac{1}{\omega X_C} = 159 \times 10^{-6} \text{ F} = 159 \mu\text{F}$$

$$f_0 = \frac{1}{2\pi\sqrt{LC}} = 31.7 \text{ Hz}$$

$$38. \quad (1) \text{ 设 } U_2 = 220 \angle 0^\circ \text{ V, } I_2 = \frac{U_2}{R_2 + jX_2} = \frac{220 \angle 0^\circ}{10 + j10.2} = 15.4 \angle -45.6^\circ \text{ A}$$

$$U_1 = I_1(R_1 + jX_1) = 17.2 \angle 17.8^\circ \text{ V} \quad U = U_1 + U_2 = 236 \angle 1.27^\circ \text{ V} \quad U = 236 \text{ V} \quad U_1 = 17.2 \text{ V}$$

$$(2) P_2 = I^2 R_2 = 2.37 \times 10^3 \text{ W} = 2.37 \text{ kW} \quad P_1 = I^2 R_1 = 118.6 \text{ W}$$

$$39. (1) S = \sqrt{P^2 + Q^2} = 11 \times 10^3 \text{ VA} = 11 \text{ kVA} \quad U = \frac{S}{I} = 220 \text{ V} \quad \lambda = \frac{P}{S} = 0.8$$

$$\varphi = 36.9^\circ \quad u = 220\sqrt{2} \sin(314t + 66.9^\circ) \text{ V}$$

$$(2) R = \frac{P}{I^2} = 3.52 \Omega \quad X_L = \frac{Q}{I^2} = 2.64 \Omega \quad (3) \lambda = 0.8$$

$$40. Z = Z_1 + Z_2 + Z_3 = 6 + j8 = 10 \angle 53.1^\circ \Omega \quad \theta = \frac{\theta_{S1} - \theta_{S2}}{Z} = 10 \angle 66.9^\circ \text{ A}$$

$$P = I^2 R = 10^2 \times 6 = 600 \text{ W} \quad Q = I^2 X = 10^2 \times 8 = 800 \text{ Var}$$

$$S = \sqrt{P^2 + Q^2} = 1000 \text{ VA} \quad \lambda = \cos(120^\circ - 66.9^\circ) = 0.6$$

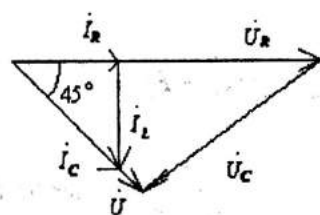
41. 设 $\dot{U}_R = U_R \angle 0^\circ \text{ V}$ 画出 \dot{I}_R , \dot{I}_L , \dot{I}_C 及 \dot{U} , \dot{U}_C , \dot{U}_R 的相量图。

由相量图可得: $I_R = \sqrt{I_C^2 - I_L^2} = 1.41 \text{ A} \quad U_R = I_R R = 141 \text{ V}$

$$\omega L = \frac{U_R}{I_L} = 100 \Omega \quad L = 318 \text{ mH}$$

$$U_C = U = U_R \cos(-45^\circ) = 100 \text{ V}$$

$$X_C = \frac{U_C}{I_C} = 50 \Omega \quad C = \frac{1}{\omega X_C} = 63.7 \mu\text{F}$$



$$42. S_2 = \frac{U^2}{\sqrt{3^2 + 6^2}} = \frac{U^2}{6.7} \quad S_1 = \frac{U^2}{\sqrt{2^2 + 3^2}} = \frac{U^2}{3.6} \quad \frac{S_1}{S_2} = 1.86$$

$$\text{即 } S_1 = 1.86 S_2 = 2.77 \times 10^3 \text{ VA} = 2.77 \text{ kVA}$$

$$P_1 = S_1 \cos \varphi_1 = 2.77 \cos(\arctan \frac{3}{2}) = 1.54 \text{ kW}$$

$$43. (1) I = \frac{P}{U \lambda} = 75.76 \text{ A} \quad R = \frac{P}{I^2} = 1.74 \Omega$$

$$|Z| = \frac{U}{I} = 2.9 \Omega \quad X = \sqrt{Z^2 - R^2} = 2.32 \Omega \quad L = \frac{X}{\omega} = 7.4 \text{ mH} \quad \varphi = \arctan \frac{X}{R} = 53.1^\circ$$

$$i = 75.76\sqrt{2} \sin(314t - 53.1^\circ) \text{ A}$$

$$(2) C = \frac{P}{\omega U^2} (\tan \varphi - \tan \varphi') = 658 \mu\text{F} \quad (3) I' = \frac{P}{U \lambda'}$$

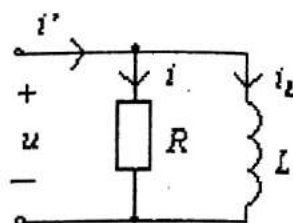
$$44. (1) |Z| = \frac{U}{I} = \frac{100}{20} = 5 \Omega \quad \varphi = 53.1^\circ \quad R = |Z| \cos \varphi = 3 \Omega$$

$$X_L = |Z| \sin \varphi = 4 \Omega \quad L = \frac{X_L}{\omega} = 12.7 \text{ mH} \quad P = I^2 R = 1200 \text{ W} \quad \lambda = \cos 53.1^\circ = 0.6$$

$$(2) \dot{I} = \dot{I}_2 + \dot{I}_1 = \frac{100}{3} + \frac{100}{j4} = 41.67 \angle -36.9^\circ \text{ A}$$

$$\lambda' = \cos 36.9^\circ = 0.8$$

$$i' = 41.67 \sqrt{2} \sin(314t - 36.9^\circ) \text{ A}$$



$$P' = \frac{U^2}{R} = \frac{100^2}{3} = 3.33 \times 10^3 \text{ W} = 3.33 \text{ kW}$$

$$45. P = I^2 (R_1 + R_2) \quad R_1 = \frac{P}{I^2} - R_2 = \frac{900}{10^2} - 6 = 3 \Omega \quad |Z_2| = \frac{U_2}{I} = \frac{100}{10} = 10 \Omega$$

$$\therefore X_{L2} = \sqrt{|Z_2|^2 - R_2^2} = \sqrt{100 - 36} = 8 \Omega \quad P = UI \lambda \quad \lambda = \frac{900}{150 \times 10} = 0.6 \text{ 感性}$$

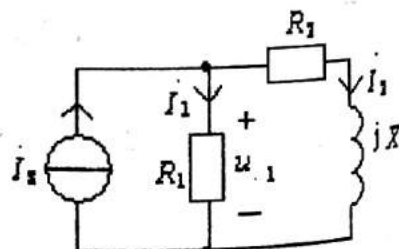
$$\varphi = 53.1^\circ \quad \frac{X_{L1} + X_{L2}}{R_1 + R_2} = \tan 53.1^\circ = 1.33 \quad X_{L1} = 1.33 \times (3 + 6) - 8 = 3.97 \Omega$$

46. 电路相量模型及各支路电流方向如下图:

$$I_2 = \sqrt{\frac{P_2}{R_2}} = 0.177 \text{ A}$$

$$U_{R1} = I_2 \sqrt{R_2^2 + X_L^2} = 10.6 \text{ V}$$

$$R_1 = \frac{U_{R1}^2}{P_1} = 75 \Omega$$



$$\text{设 } \dot{U}_{R1} = 10.6 \angle 0^\circ \text{ V, 则 } \dot{I}_1 = \frac{\dot{U}_{R1}}{R_1} = 0.142 \angle 0^\circ \text{ A} \quad \varphi_2 = \arctan \frac{X_L}{R_2} = 36.9^\circ$$

$$\dot{I}_2 = 0.177 \angle -36.9^\circ \text{ A} \quad \dot{I}_3 = \dot{I}_1 + \dot{I}_2 = 0.303 \angle -20.5^\circ \text{ A} \quad I_3 = 0.303 \text{ A}$$

$$47. |Z_1| = \sqrt{R^2 + X_{L1}^2} = 20 \Omega \quad U = I |Z_1| = 300 \text{ V}$$

$$|Z_2| = \frac{U}{I} = 15 \Omega \quad X' = \sqrt{|Z_2|^2 - R^2} = 9 \Omega \quad X' = \frac{X_{L1} X_{L2}}{X_{L1} + X_{L2}} \quad \text{开关闭合后:}$$

$$X_D = 20.6 \Omega$$

48. (1) 电源供出电流 $I = \frac{P}{U \lambda} = \frac{8 \times 10^3}{220 \times 0.6} = 60.6 \text{ A}$, $I_N = \frac{10 \times 10^3}{220} = 45.45 \text{ A}$

供出的电流超过其额定电流

(2) 若 $\lambda' = 0.95$ $\tan \varphi' = 0.33$, 根据已知条件 $\tan \varphi = 1.33$

$$C = \frac{P}{\omega U^2} (\tan \varphi - \tan \varphi') = \frac{8 \times 10^3}{314 \times 220^2} (1.33 - 0.33) = 526 \mu\text{F}$$

(3) 并联电容后电源供出的电流

$$I' = \frac{P}{U \lambda'} = \frac{8 \times 10^3}{220 \times 0.95} = 38.28 \text{ A} , \quad I' < I_N = 45.45 \text{ A}$$