#### 6.3: Classification

\$ echo "Data Science Institute"

#### What is Classification?

Classification involves predicating a qualitative response by a assigning it to a category. The methods that are used to classify observations are called **classifiers** and most of them work by following two steps:

- Compute the probability that an observation belongs to a category.
- Classify the observation based on some probability threshold (i.e. if the probability that an observation belongs to some category is greater than 0.5 then assign the observation to that category)

#### **Breakout Room**

What are some classification methods?

# Why use Classification?

We need to predict a qualitiative response.

#### Example

On the basis of DNA sequence data for a number of patients with and without a given disease, a biologist would like to figure out which DNA mutations are deleterious (disease-causing) and which are not.

Let's categorize this as a class!

#### **Breakout Room**

A person is donating a blood test. How would you qualify this?

Suppose we are trying to diagnose a patient with either a stroke, drug overdose, or epileptic seizure based on their symptoms. We can code this response as follows

$$Y = egin{cases} 1 & ext{if stroke;} \ 2 & ext{if drug overdose;} \ 3 & ext{if epileptic seizure.} \end{cases}$$

At this point we could use linear regression to predict Y based on a set of predictors. However there are several problems with this coding. One of them is we cannot use linear regression.

## Breakout Room: Why can't we use linear regression?

$$Y = egin{cases} 1 & ext{if stroke;} \ 2 & ext{if drug overdose;} \ 3 & ext{if epileptic seizure.} \end{cases}$$

#### Other problems:

- Implies an ordering of the outcomes.
- The difference between epileptic seizure and stroke versus stroke and drug overdose is assumed to be the same.

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A different ordering would give completely different results for the linear regression. 

There is no convenient way to code a qualitative response with more than two levels so that linear regression can be used.

The 0/1 coding for a binary qualitative response variable does not suffer the same problems. However the probabilities we obtain will be difficult to interpret

- negative probabilities
- probabilities above 1

So, linear regression only able to give **crude estimates of the probabilities for a binary response.** 

In summary, we don't use linear regression for classification since:

- It does not work for a qualitative response variable with more than 2 classes.
- With 2 classes, the probability estimates are not meaningful.

# K-Nearest Neighbours

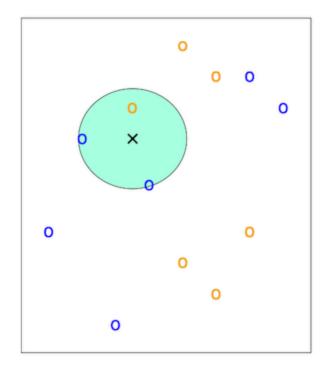
The K-nearest neighbors (KNN) classifier works very differently than any of the previous classification methods. For a test observation  $x_0$ , it identifies K training data points that are closest to  $x_0$  (represented by  $\mathcal{N}_0$ ) and estimates the conditional probability for class j as

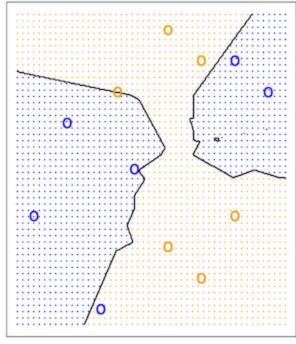
$$\Pr\left(Y=j\mid X=x_0
ight)=rac{1}{K}\sum_{i\in\mathcal{N}_0}I\left(y_i=j
ight)$$

where  $I(y_i=j)$  if an **indicator variable** that equals 1 is  $y_i=j$  and 0 otherwise. The KNN classifier classifies the test observation  $x_0$  to the class for which the above probability is the largest.

# K-Nearest Neighbours

These figures illustrate the KNN approach with K=3. To the left we see the 3 closest points to x are 1 orange and 2 blue so this observation will be classified as blue. The right figure shows the decision boundaries where an observation will be classified as blue or orange.





#### **Exercise: K-Nearest Neighbours**

Open the Classification Exercises Jupyter Notebook file.

- Go over the "K-Nearest Neighbours" section together as a class.
- 5 minutes for students to complete the questions from "K-Nearest Neighbours".
- Questions should be completed at home if time does not allow.

#### References

Chapter 4 and section 2.2.3 of the ISLP book:

James, Gareth, et al. "Classification." An Introduction to Statistical Learning: with Applications in Python, Springer, 2023.