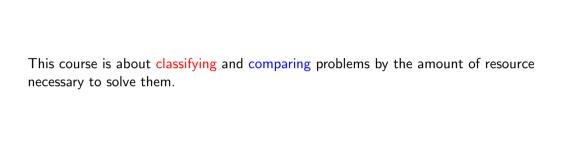


Let's take a look at some familiar problems.

- ► Diophantine Problem
- ► Matching Problem
- Vertex Cover Problem
- ► Graph Isomorphism Problem

We learnt from Computability Course and Algorithm Course that

- ► Diophantine is undecidable,
- ► Matching is in **P**,
- ► Vertex Cover is **NP**-complete, and
- ► Graph Isomorphism is yet to be classified.



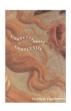
We shall get to know some of the main techniques in theoretical investigation.

- Recursion Theoretical Method
- Combinatorial Method
- Algebraic Method
- Probabilistic Method
- •

We shall be exposed to many great ideas in Computer Science.

Blum's Speedup Theorem, Borodin-Trakhtenbrot Gap Theorem, BPP, Hierarchy Theorem, Savitch Theorem, Stockmeyer-Meyer Theorem, NC, Karp Theorem, Cook-Levin Theorem, PH C PSPACE, Ladner Theorem, Baker-Gill-Solovay Theorem, Immerman-Szelepcsényi Theorem, Dist NP, Circuit Complexity, Chandra-Kozen-Stockmeyer Theorem, PCP Theorem. P-Completeness, Aleliunas-Karp-Lipton-Lovász-Rackoff Theorem, PP, Valiant Theorem, #P, Valiant-Vazirani Theorem, Toda Theorem, Impagliazzo-Levin Theorem, Levin Theory, Goldbach-Levin Theorem, NP-Completeness, Zero Knowledge, Yao's Unpredictability Theorem. Lund-Karloff-Fortnow-Nisan Theorem, Yao's Max-Min Theorem, Derandomization, Barrier Results, Goldbach-Goldwasser-Micali Theorem, Pseudorandomness, One-Way Function, Nisan-Wigderson Generator, Hartmanis Conjecture, Hardness Amplification, Exponential Conjecture. Hartmanis-Stearns-Hennie Theorem. IP = PSPACE. Hierarchy Theorem. Reigold Theorem, Sudan's List Decoding, Goldwasser-Sipser Theorem, Randomness Extractor, Natural Proof. Adleman Theorem. Babai's AM. Log-Rank Conjecture. Circuit Lower Bound. QIP = PSPACE...

- 1. Christos Papadimitriou. Computational Complexity. 1994.
- 2. Ingo Wegener. Complexity Theory, exploring the limits of efficient algorithms. 2005.
- 3. Oded Goldreich. Computational Complexity, a conceptual perspective. 2008.
- 4. Sanjeev Arora, Boaz Barak. Computational Complexity, a modern approach. 2009.









Your final score of the course:

- ▶ Performance in class (20)
- ► Test (20 + 15 + 15 + 15 + 15 = 80)

Test One

Design a universal Turing Machine ${\mathbb U}$ that satisfies the following:

▶ If \mathbb{M}_{α} runs in O(T(n)) time, then $\mathbb{U}(\alpha, _)$ runs in $O(T(n) \log T(n))$ time.

You need to write down the complete (executable) program of $\mathbb U$ and explain how it works.

Test Two

Prove Ladner Theorem.

Test Three

Let L be decided by a P-time NDTM \mathbb{N} . Construct a Cook-Levin reduction from L to SAT that is implicitly logspace computable.

Test Four

Prove Immerman-Szelepcsényi Theorem.

Test Five

- 1. Prove that reachability problem is in NC^2 .
- 2. Prove that logspace reduction is efficient parallel.
- 3. Suppose *L* is **P**-complete. Prove that $L \in NC$ iff **P** = NC.