Lecture 2 Language Models

Lê Anh Cường

Outline

- 1. Definition of Language Model (LM)
- 2. Applications of Language Model
- 3. N-gram based Language Models
- 4. Model Evaluation
- 5. Zero problem and Smoothing Techniques
- 6. Neural based Language Models: an Introduction

Definition

• A language model aims to determines the ability or likelihood of a sentence (or a sequence of words) belong to a given language.

Goal: compute the probability of a sentence or sequence of words:

$$P(W) = P(w_1, w_2, w_3, w_4, w_5...w_n)$$

 $P('bo', 'vang', 'gam', 'co'), P('bo', 'nang', 'gam', 'co')$

LM's Applications

- Speech Recognition
- Optical Character Recognition (OCR)
- Machine Translation
- Spelling

•

$$\underset{W}{\operatorname{arg\,max}} P(W \mid A) = \underset{W}{\operatorname{arg\,max}} \frac{P(A \mid W)P(W)}{P(A)}$$

Language Model ~ Word Prediction Model

Chain rule

$$P(x_1,x_2,x_3,...,x_n) = P(x_1)P(x_2|x_1)P(x_3|x_1,x_2)...P(x_n|x_1,...,x_{n-1})$$

- P("its water is so transparent") =
- P(its) × P(water|its) × P(is|its water)
- Y P(so | its water is)
 Y P(transparent | its water is so)

Word Prediction

$$P(w_1 w_2 ... w_n) = \prod_{i} P(w_i | w_1 w_2 ... w_{i-1})$$

N-gram based Probability Estimation

$$P(w_1 w_2 ... w_n) = \prod_{i} P(w_i | w_1 w_2 ... w_{i-1})$$

P(the lits water is so transparent that) =

Count(its water is so transparent that the)

Count(its water is so transparent that)

Markov Assumption



•Simplifying assumption:

 $P(\text{the }|\text{its water is so transparent that}) \approx P(\text{the }|\text{that})$

Or maybe

 $P(\text{the }|\text{its water is so transparent that}) \approx P(\text{the }|\text{transparent that})$

Markov Assumption

$$P(w_1 w_2 \dots w_n) \approx \prod_i P(w_i | w_{i-k} \dots w_{i-1})$$

•In other words, we approximate each component in the product

$$P(w_i | w_1 w_2 ... w_{i-1}) \approx P(w_i | w_{i-k} ... w_{i-1})$$

Bigram (2-gram) based Model

The probability of a word depending the word standing right before it.

$$P(w_i | w_1 w_2 ... w_{i-1}) \approx P(w_i | w_{i-1})$$

texaco, rose, one, in, this, issue, is, pursuing, growth, in, a, boiler, house, said, mr., gurria, mexico, 's, motion, control, proposal, without, permission, from, five, hundred, fifty, five, yen

outside, new, car, parking, lot, of, the, agreement, reached

this, would, be, a, record, november

Bigram Probabilities

Maximum Likelihood Estimate

$$P(w_i \mid w_{i-1}) = \frac{count(w_{i-1}, w_i)}{count(w_{i-1})}$$

$$P(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$$

Example

$$P(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})} \quad \begin{array}{l} ~~1 \text{ am Sam }~~ \\ ~~Sam I \text{ am }~~ \\ ~~I \text{ do not like green eggs and ham }~~ \\ \end{array}$$

$$P({
m I}|{
m <} {
m >}) = {2\over 3} = .67$$
 $P({
m Sam}|{
m <} {
m >}) = {1\over 3} = .33$ $P({
m am}|{
m I}) = {2\over 3} = .67$ $P({
m <} {
m /s} {
m >} |{
m Sam}) = {1\over 2} = 0.5$ $P({
m Sam}|{
m am}) = {1\over 2} = .5$ $P({
m do}|{
m I}) = {1\over 3} = .33$

Unigram (1-gram) based Model

$$P(w_1 w_2 \dots w_n) \approx \prod_i P(w_i)$$

Xác suất của một từ không phụ thuộc vào từ phía trước

fifth, an, of, futures, the, an, incorporated, a, a, the, inflation, most, dollars, quarter, in, is, mass

thrift, did, eighty, said, hard, 'm, july, bullish

that, or, limited, the

Statistics on the Berkeley Restaurant Project sentences

Out of 9222 sentences

- can you tell me about any good cantonese restaurants close by
- mid priced thai food is what i'm looking for
- tell me about chez panisse
- can you give me a listing of the kinds of food that are available
- i'm looking for a good place to eat breakfast
- when is caffe venezia open during the day
- •

Bigram counts

	i	want	to	eat	chinese	food	lunch	spend
i	5	827	0	9	0	0	0	2
want	2	0	608	1	6	6	5	1
to	2	0	4	686	2	0	6	211
eat	0	0	2	0	16	2	42	0
chinese	1	0	0	0	0	82	1	0
food	15	0	15	0	1	4	0	0
lunch	2	0	0	0	0	1	0	0
spend	1	0	1	0	0	0	0	0

Bigram Probabilities

•Normalize by unigrams:

•Result:

i	want	to	eat	chinese	food	lunch	spend
2533	927	2417	746	158	1093	341	278

	i	want	to	eat	chinese	food	lunch	spend
i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011
to	0.00083	0	0.0017	0.28	0.00083	0	0.0025	0.087
eat	0	0	0.0027	0	0.021	0.0027	0.056	0
chinese	0.0063	0	0	0	0	0.52	0.0063	0
food	0.014	0	0.014	0	0.00092	0.0037	0	0
lunch	0.0059	0	0	0	0	0.0029	0	0
spend	0.0036	0	0.0036	0	0	0	0	0

Kinds of Knowledge

- P(english|want) = .0011
- P(chinese|want) = .0065
- P(to|want) = .66
- P(eat | to) = .28
- P(food | to) = 0
- P(want | spend) = 0
- P(i | <s>) = .25

- World knowledge
- Syntax

Discourse

Exercise

A corpus includes the following sentences:

```
<s> cô ấy dạy môn tin học </s>
```

<s> anh dạy môn toán </s>

<s> cô ấy học toán anh ấy dạy </s>

<s> môn toán môn tin đều hay </s>

<s> anh ấy dạy môn toán hay môn tin </s>

Building language models based on unigram and bigram?

Language Modeling

Evaluation and Perplexity

Extrinsic Evaluation

- Based on the evaluation of Language Models' applications:
 - For example: speech recognition, spelling, machine translation

Intrinsic Evaluation

- Using a Test dataset including sentences in the language.
- Using the measurment Perplexity

Perplexity

The best language model is one that best predicts an unseen test set

Gives the highest P(sentence)

Perplexity is the inverse probability of the test set, normalized by the number of words

$$PP(W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i|w_{i-1})}}$$

$$PP(W) = P(w_1 w_2 ... w_N)^{-\frac{1}{N}}$$

$$= \sqrt[N]{\frac{1}{P(w_1 w_2 ... w_N)}}$$

$$PP(W) = \sqrt[N]{\prod_{i=1}^{N} \frac{1}{P(w_i | w_1 ... w_{i-1})}}$$

Minimizing perplexity is the same as maximizing probability

Perplexity as branching factor

- Let's suppose a sentence consisting of random digits
- •What is the perplexity of this sentence according to a model that assign P=1/10 to each digit?

$$PP(W) = P(w_1 w_2 ... w_N)^{-\frac{1}{N}}$$

$$= (\frac{1}{10}^{N})^{-\frac{1}{N}}$$

$$= \frac{1}{10}^{-1}$$

$$= 10$$

Lower perplexity = better model

•Training 38 million words, test 1.5 million words, WSJ

Perplexity	962	170	109

Lower perplexity = better model

•Training 38 million words, test 1.5 million words, WSJ

	Unigram	Bigram	Trigram
Perplexity	962	170	109

The Shannon Visualization Method

Approximating Shakespeare

Unigram

To him swallowed confess hear both. Which. Of save on trail for are ay device and rote life have

Every enter now severally so, let

Hill he late speaks; or! a more to leg less first you enter

Are where exeunt and sighs have rise excellency took of.. Sleep knave we. near; vile like

Bigram

What means, sir. I confess she? then all sorts, he is trim, captain.

Why dost stand forth thy canopy, forsooth; he is this palpable hit the King Henry. Live king. Follow.

What we, hath got so she that I rest and sent to scold and nature bankrupt, nor the first gentleman?

Trigram

Sweet prince, Falstaff shall die. Harry of Monmouth's grave.

This shall forbid it should be branded, if renown made it empty.

Indeed the duke; and had a very good friend.

Fly, and will rid me these news of price. Therefore the sadness of parting, as they say, 'tis done.

Quadrigram

King Henry. What! I will go seek the traitor Gloucester. Exeunt some of the watch. A great banquet serv'd in;

Will you not tell me who I am?

It cannot be but so.

Indeed the short and the long. Marry, 'tis a noble Lepidus.

The wall street journal is not shakespeare (no offense)

Unigram

Months the my and issue of year foreign new exchange's september were recession exchange new endorsed a acquire to six executives

Bigram

Last December through the way to preserve the Hudson corporation N. B. E. C. Taylor would seem to complete the major central planners one point five percent of U. S. E. has already old M. X. corporation of living on information such as more frequently fishing to keep her

Trigram

They also point to ninety nine point six billion dollars from two hundred four oh six three percent of the rates of interest stores as Mexico and Brazil on market conditions

Which value for N?

How large *n*?

- Nothing is enough (theoretically)
- But anyway: as much as possible (→ close to "perfect" model)
- Empirically: 3
 - parameter estimation? (reliability, data availability, storage, space, ...)
 - 4 is too much: $|V|=60k \rightarrow 1.296 \times 1019$ parameters
 - but: 6-7 would be (almost) ideal (having enough data): in fact, one can recover original from 7-grams!

Shakespeare as corpus

- •N=884,647 tokens, V=29,066
- •Shakespeare produced 300,000 bigram types out of V^2 = 844 million possible bigrams.
 - •So 99.96% of the possible bigrams were never seen (have zero entries in the table)
- •Quadrigrams worse: What's coming out looks like Shakespeare because it *is* Shakespeare

Language Modeling

Zeros problem and Smoothing: Add-one (Laplace) smoothing

Zeros

- •Training set:
- ... denied the allegations
- ... denied the reports
- ... denied the claims
- ... denied the request

P("offer" | denied the) = 0

Test set

... denied the offer

... denied the loan

mean that we will assign 0 probability to the sentence

The intuition of smoothing (from Dan Klein)

•When we have sparse statistics:

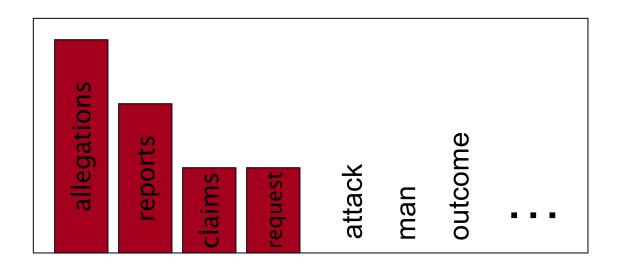
P(w | denied the)

3 allegations

2 reports

1 claims

1 request



Steal probability mass to generalize better

P(w | denied the)

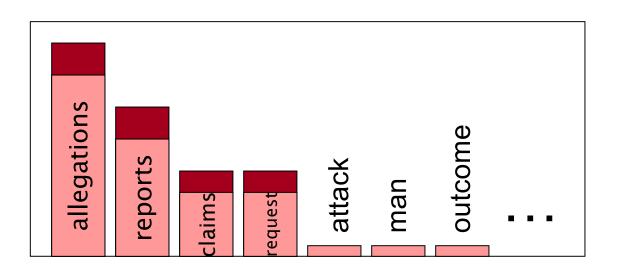
2.5 allegations

1.5 reports

0.5 claims

0.5 request

2 other



Add-one estimation

- Also called Laplace smoothing
- Pretend we saw each word one more time than we did
- •Just add one to all the counts!
- •MLE estimate:
- •Add-1 estimate:

$$P_{MLE}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i)}{c(w_{i-1})}$$

$$P_{Add-1}(w_i \mid w_{i-1}) = \frac{c(w_{i-1}, w_i) + 1}{c(w_{i-1}) + V}$$

Add-one estimation

$$\hat{P}(w_i \mid c) = \frac{count(w_i, c) + 1}{\sum_{w \in V} (count(w, c)) + 1}$$

$$= \frac{count(w_i, c) + 1}{\left(\sum_{w \in V} count(w, c)\right) + |V|}$$

Berkeley Restaurant Corpus: Laplace smoothed bigram counts

	i	want	to	eat	chinese	food	lunch	spend
i	6	828	1	10	1	1	1	3
want	3	1	609	2	7	7	6	2
to	3	1	5	687	3	1	7	212
eat	1	1	3	1	17	3	43	1
chinese	2	1	1	1	1	83	2	1
food	16	1	16	1	2	5	1	1
lunch	3	1	1	1	1	2	1	1
spend	2	1	2	1	1	1	1	1

Laplace-smoothed bigrams

$$P^*(w_n|w_{n-1}) = \frac{C(w_{n-1}w_n) + 1}{C(w_{n-1}) + V}$$

	i	want	to	eat	chinese	food	lunch	spend
i	0.0015	0.21	0.00025	0.0025	0.00025	0.00025	0.00025	0.00075
want	0.0013	0.00042	0.26	0.00084	0.0029	0.0029	0.0025	0.00084
to	0.00078	0.00026	0.0013	0.18	0.00078	0.00026	0.0018	0.055
eat	0.00046	0.00046	0.0014	0.00046	0.0078	0.0014	0.02	0.00046
chinese	0.0012	0.00062	0.00062	0.00062	0.00062	0.052	0.0012	0.00062
food	0.0063	0.00039	0.0063	0.00039	0.00079	0.002	0.00039	0.00039
lunch	0.0017	0.00056	0.00056	0.00056	0.00056	0.0011	0.00056	0.00056
spend	0.0012	0.00058	0.0012	0.00058	0.00058	0.00058	0.00058	0.00058

Compare with the original probabilies

	i	want	to	eat	chinese	food	lunch	spend
i	0.002	0.33	0	0.0036	0	0	0	0.00079
want	0.0022	0	0.66	0.0011	0.0065	0.0065	0.0054	0.0011
to	0.00083	0	0.0017	0.28	0.00083	0	0.0025	0.087
eat	0	0	0.0027	0	0.021	0.0027	0.056	0
chinese	0.0063	0	0	0	0	0.52	0.0063	0
food	0.014	0	0.014	0	0.00092	0.0037	0	0
lunch	0.0059	0	0	0	0	0.0029	0	0
spend	0.0036	0	0.0036	0	0	0	0	0

	i	want	to	eat	chinese	food	lunch	spend
i	0.0015	0.21	0.00025	0.0025	0.00025	0.00025	0.00025	0.00075
want	0.0013	0.00042	0.26	0.00084	0.0029	0.0029	0.0025	0.00084
to	0.00078	0.00026	0.0013	0.18	0.00078	0.00026	0.0018	0.055
eat	0.00046	0.00046	0.0014	0.00046	0.0078	0.0014	0.02	0.00046
chinese	0.0012	0.00062	0.00062	0.00062	0.00062	0.052	0.0012	0.00062
food	0.0063	0.00039	0.0063	0.00039	0.00079	0.002	0.00039	0.00039
lunch	0.0017	0.00056	0.00056	0.00056	0.00056	0.0011	0.00056	0.00056
spend	0.0012	0.00058	0.0012	0.00058	0.00058	0.00058	0.00058	0.00058

Laplace Smoothing

$$\hat{P}(w_i \mid c) = \frac{count(w_i, c) + 1}{\sum_{w \in V} (count(w, c)) + 1}$$

$$= \frac{count(w_i, c) + 1}{\left(\sum_{w \in V} count(w, c)\right) + |V|}$$

Language Modeling

Interpolation, Backoff, and Web-Scale LMs

Backoff and Interpolation

- •Sometimes it helps to use less context
 - •Condition on less context for contexts you haven't learned much about

•Backoff:

- use trigram if you have good evidence,
- •otherwise bigram, otherwise unigram

•Interpolation:

•mix unigram, bigram, trigram

Linear Interpolation

Simple interpolation

$$\hat{P}(w_n|w_{n-1}w_{n-2}) = \lambda_1 P(w_n|w_{n-1}w_{n-2})
+ \lambda_2 P(w_n|w_{n-1})
+ \lambda_3 P(w_n)$$

 $\sum_{i} \lambda_{i} = 1$

Lambdas conditional on context:

$$\hat{P}(w_n|w_{n-2}w_{n-1}) = \lambda_1(w_{n-2}^{n-1})P(w_n|w_{n-2}w_{n-1})
+ \lambda_2(w_{n-2}^{n-1})P(w_n|w_{n-1})
+ \lambda_3(w_{n-2}^{n-1})P(w_n)$$

How to set the lambdas?

Training Data

Held-Out Data Test Data

- Use a held-out corpus
- •Choose λs to maximize the probability of held-out data:
 - •Fix the N-gram probabilities (on the training data)
 - •Then search for λs that give largest probability to held-out set:

$$\log P(w_1...w_n | M(\lambda_1...\lambda_k)) = \sum_{i} \log P_{M(\lambda_1...\lambda_k)}(w_i | w_{i-1})$$

Unknown words: Open versus closed vocabulary tasks

- •If we know all the words in advanced
 - Vocabulary V is fixed
 - Closed vocabulary task
- •Often we don't know this
 - •Out Of Vocabulary = OOV words
 - Open vocabulary task
- •Instead: create an unknown word token <UNK>
 - Training of <UNK> probabilities
 - Create a fixed lexicon L of size V
 - •At text normalization phase, any training word not in L changed to <UNK>
 - Now we train its probabilities like a normal word
 - At decoding time
 - •If text input: Use UNK probabilities for any word not in training

Huge web-scale n-grams

- •How to deal with, e.g., Google N-gram corpus
- Pruning
 - Only store N-grams with count > threshold.
 - Remove singletons of higher-order n-grams
 - Entropy-based pruning
- Efficiency
 - •Efficient data structures like tries
 - •Bloom filters: approximate language models
 - Store words as indexes, not strings
 - •Use Huffman coding to fit large numbers of words into two bytes
 - Quantize probabilities (4-8 bits instead of 8-byte float)

Smoothing for Web-scale N-grams

- •"Stupid backoff" (Brants et al. 2007)
- No discounting, just use relative frequencies

$$S(w_{i} \mid w_{i-k+1}^{i-1}) = \begin{cases} \frac{\text{count}(w_{i-k+1}^{i})}{\text{count}(w_{i-k+1}^{i-1})} & \text{if } \text{count}(w_{i-k+1}^{i}) > 0 \\ 0.4S(w_{i} \mid w_{i-k+2}^{i-1}) & \text{otherwise} \end{cases}$$

$$S(w_i) = \frac{\text{count}(w_i)}{N}$$

Advanced smoothing algorithms

- Intuition used by many smoothing algorithms
 - Good-Turing
 - Kneser-Ney
 - Witten-Bell
- Use the count of things we've seen once
 - •to help estimate the count of things we've never seen

Notation: N_c = Frequency of frequency c

- $\bullet N_c$ = the count of things we've seen c times
- •Sam I am I am Sam I do not eat

```
I 3
sam 2
am 2
do 1
not 1
eat 1
```

$$N_1 = 3$$

$$N_2 = 2$$

$$N_3 = 1$$

Good-Turing smoothing intuition

- •You are fishing (a scenario from Josh Goodman), and caught:
 - •10 carp, 3 perch, 2 whitefish, 1 trout, 1 salmon, 1 eel = 18 fish
- •How likely is it that next species is trout?
 - •1/18
- How likely is it that next species is new (i.e. catfish or bass)
 - Let's use our estimate of things-we-saw-once to estimate the new things.
 - •3/18 (because $N_1=3$)
- •Assuming so, how likely is it that next species is trout?
 - •Must be less than 1/18
 - •How to estimate?

Good Turing calculations

$$P_{GT}^*$$
 (things with zero frequency) = $\frac{N_1}{N}$

- •Unseen (bass or catfish)

 - •MLE p = 0/18 = 0
 - $\bullet P^*_{GT}$ (unseen) = $N_1/N = 3/18$

$$c^* = \frac{(c+1)N_{c+1}}{N_c}$$

- Seen once (trout)
 - $\cdot c = 1$
 - •MLE p = 1/18

•C*(trout) = 2 * N2/N1
= 2 * 1/3
=
$$2/3$$

$$\bullet P^*_{GT}(trout) = 2/3 / 18 = 1/27$$

Resulting Good-Turing numbers

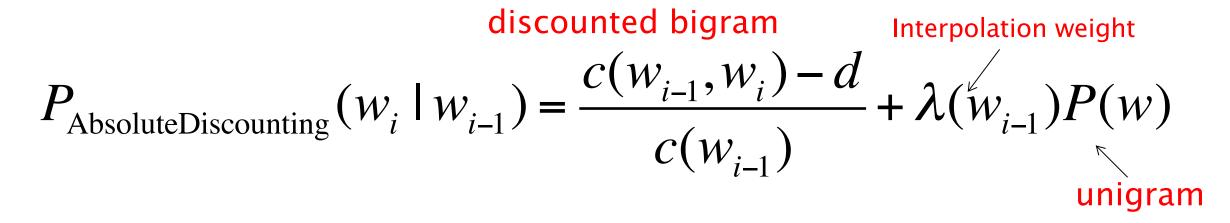
- •Numbers from Church and Gale (1991)
- •22 million words of AP Newswire

$$c^* = \frac{(c+1)N_{c+1}}{N_c}$$

Count	Good Turing c*
С	
0	.0000270
1	0.446
2	1.26
3	2.24
4	3.24
5	4.22
6	5.19
7	6.21
8	7.24
9	8.25

Absolute Discounting Interpolation

•Save ourselves some time and just subtract 0.75 (or some d)!



- •(Maybe keeping a couple extra values of d for counts 1 and 2)
- •But should we really just use the regular unigram P(w)?

Kneser-Ney Smoothing I

- Better estimate for probabilities of lower-order unigrams!
 - •Shannon game: I can't see without my reading______?
 - "Francisco" is more common than "glasses"
 - •... but "Francisco" always follows "San"
- •The unigram is useful exactly when we haven't seen this bigram!
- •Instead of P(w): "How likely is w"
- •P_{continuation}(w): "How likely is w to appear as a novel continuation?
 - •For each word, count the number of bigram types it completes
 - •Every bigram type was a novel continuation the first time it was seen

$$P_{CONTINUATION}(w) \propto |\{w_{i-1} : c(w_{i-1}, w) > 0\}|$$

glasses

Francisco

Kneser-Ney Smoothing II

•How many times does w appear as a novel continuation:

$$P_{CONTINUATION}(w) \propto \left| \{ w_{i-1} : c(w_{i-1}, w) > 0 \} \right|$$

Normalized by the total number of word bigram types

$$\left| \{ (w_{j-1}, w_j) : c(w_{j-1}, w_j) > 0 \} \right|$$

$$P_{CONTINUATION}(w) = \frac{\left| \left\{ w_{i-1} : c(w_{i-1}, w) > 0 \right\} \right|}{\left| \left\{ (w_{j-1}, w_j) : c(w_{j-1}, w_j) > 0 \right\} \right|}$$

Kneser-Ney Smoothing III

•Alternative metaphor: The number of # of word types seen to precede w

$$|\{w_{i-1}: c(w_{i-1}, w) > 0\}|$$

•normalized by the # of words preceding all words:

$$P_{CONTINUATION}(w) = \frac{\left| \left\{ w_{i-1} : c(w_{i-1}, w) > 0 \right\} \right|}{\sum_{w'} \left| \left\{ w'_{i-1} : c(w'_{i-1}, w') > 0 \right\} \right|}$$

•A frequent word (Francisco) occurring in only one context (San) will have a low continuation probability

Kneser-Ney Smoothing IV

$$P_{KN}(w_i \mid w_{i-1}) = \frac{\max(c(w_{i-1}, w_i) - d, 0)}{c(w_{i-1})} + \lambda(w_{i-1})P_{CONTINUATION}(w_i)$$

λ is a normalizing constant; the probability mass we've discounted

$$\lambda(w_{i-1}) = \frac{d}{c(w_{i-1})} |\{w : c(w_{i-1}, w) > 0\}|$$

the normalized discount

The number of word types that can follow w_{i-1}

- = # of word types we discounted
- = # of times we applied normalized discount

Kneser-Ney Smoothing: Recursive formulation

$$P_{KN}(w_i \mid w_{i-n+1}^{i-1}) = \frac{\max(c_{KN}(w_{i-n+1}^i) - d, 0)}{c_{KN}(w_{i-n+1}^{i-1})} + \lambda(w_{i-n+1}^{i-1})P_{KN}(w_i \mid w_{i-n+2}^{i-1})$$

$$c_{KN}(\bullet) = \begin{cases} count(\bullet) & \text{for the highest order} \\ continuationcount}(\bullet) & \text{for lower order} \end{cases}$$

Continuation count = Number of unique single word contexts for •

Language Modeling

Neural Language Model

Limitation of N-gram based Language Models

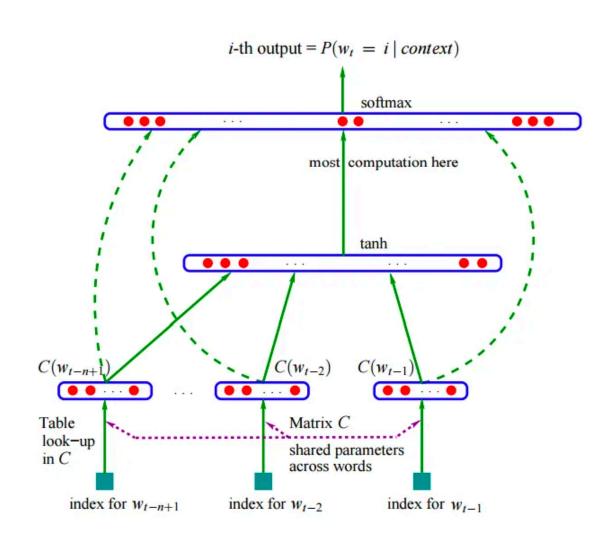
- Sparse data causes zero
- Can not use a large N.
 - Therefore it can not model the long relationship:

"Hùng sống ở Pháp hồi nhỏ nên anh ấy có thể nói tiếng ... khá thạo" "The girl that I met in the train was ..."

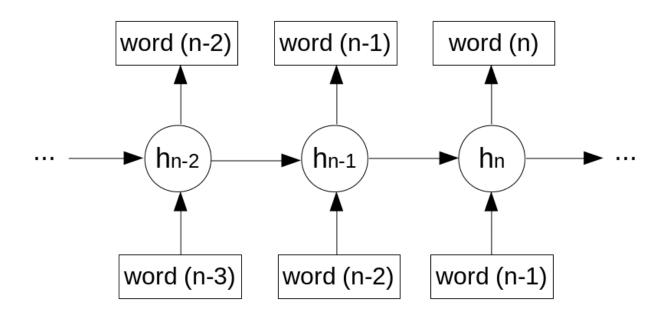
Neural Network Language Models

- Neural network language model NNLM (Bengio, 2003)
- Recurrent NNLM (Mikolov, 2010)
- Các mô hình mới: Transformer model (2018)

Neural network language model



Recurrent Neural Network Language Model



Language Model

- Word prediction
- Classification problem -> probability distribution on the vocabulary

Some Experiments

Language Model	$H(H_c)$	PPL	WER
KN5	-	248.0	12.8
RNN	200 (-)	226.2	12.0
RNN-BOW	190 (10)	218.8	11.7
RNN+KN5	200 (-)	191.6	11.8
RNN-BOW+KN5	190 (10)	183.0	11.3

RNN-BOW LM to combine short term (RNN) and long term (BOW) information (Haidar & Kurimo, 2016)

Summary

- The importance of Lânguge Models
- Language Models based on N-gram
- Model Evaluation
- Zero Problem and Smoothing Techniques
- Neural Network based Language Models