

Confidence Interval for VaR estimates

- Assuming Normal Returns

- $SE(\hat{\mu}) = \sigma \sqrt{\frac{1}{T}}$

- $SE(\hat{\sigma}) = \sigma \sqrt{\frac{1}{2T}} \quad (T \text{ large})$

- $\frac{(T-1)\hat{\sigma}^2}{\sigma^2} \sim \chi^2(T-1) \xrightarrow{T \text{ large}} \hat{\sigma}^2 \sim N\left(\sigma^2, \sigma^4 \frac{2}{T-1}\right)$

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- Under Non-Normality, use bootstrapping
 1. Resample from the simulated data using their empirical distribution; or run the simulation several times.
 - Resampling from the simulated data using their empirical distribution can be done in RSP.
 2. In each new sample (either from resampling or simulation), calculate VaR.
 3. Repeat steps 1 and 2 many times to get several VaR estimates; use these estimates to get the expected VaR and its confidence level.