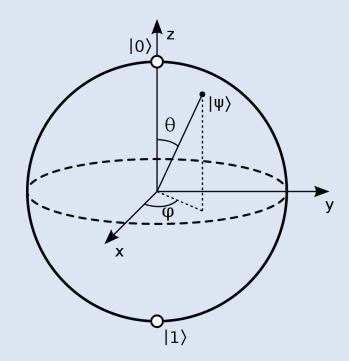
Basics

• Single Qubit:
$$|\psi\rangle = \cos\frac{\theta}{2}|0\rangle + e^{i\phi}\sin\frac{\theta}{2}|1\rangle$$

- Bit and Phase information
 - Measurement:
 - formally: projection onto a basis
 - Change
 - Bit-Flip $X(a|0\rangle + b|1\rangle) = b|0\rangle + a|1\rangle$
 - Phase-Flip $Z(a|0\rangle + b|1\rangle) = a|0\rangle b|1\rangle$



Bases

• Computational Basis $= (|0\rangle \equiv \begin{pmatrix} 1 \\ 0 \end{pmatrix}, |1\rangle \equiv \begin{pmatrix} 0 \\ 1 \end{pmatrix})$

$$Z|0\rangle = |0\rangle$$
 , $Z|1\rangle = -|1\rangle$

$$X\ket{0}=\ket{1}$$
 , $X\ket{1}=\ket{0}$

• Hadamard Basis $=\left(|+\rangle\equiv\frac{|0\rangle+|1\rangle}{\sqrt{2}},|-\rangle\equiv\frac{|0\rangle-|1\rangle}{\sqrt{2}}\right)$

$$X \mid + \rangle = \mid + \rangle$$
, $X \mid - \rangle = - \mid - \rangle$

$$Z|+\rangle = |-\rangle$$
, $Z|-\rangle = |+\rangle$

Conversion

$$H|0\rangle = |+\rangle$$
 , $H|1\rangle = |-\rangle$, $H^2 = 1$

Basics

• Bloch Sphere:

$$\rho = |\psi\rangle \langle \psi|$$

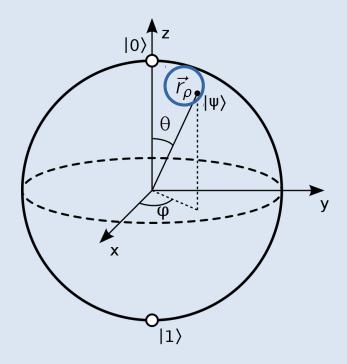
$$= \frac{1}{2}(\mathbb{1} + X\cos\phi\sin\theta + Y\sin\phi\sin\theta + Z\cos\theta)$$

$$= \frac{1}{2}(\mathbb{1} + \vec{r}_{\rho} \cdot \vec{\sigma})$$

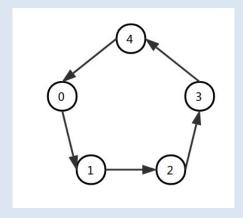
• Rotations:

$$R_{\hat{n}}(\alpha) = \exp\left(-i\frac{\alpha}{2}\hat{n}\cdot\vec{\sigma}\right)$$

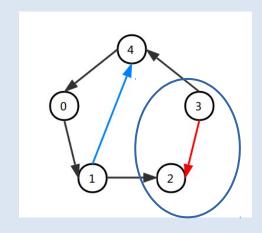
 $R_{\hat{x}}(\pi) = X$, $R_{\hat{z}}(\pi) = Z$ $(R_{\hat{y}}(\pi) = Y)$



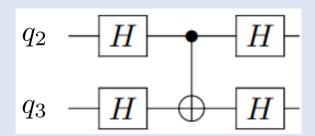
Suppose a device has this layout:



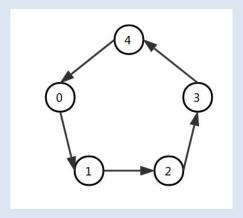
But we want to do this:



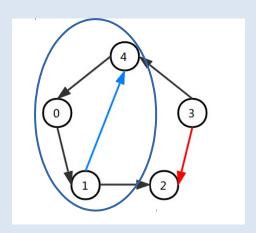
Wrong direction! Circumvent it with



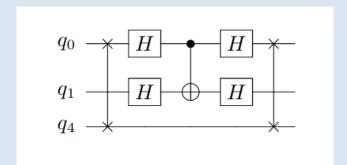
Suppose a device has this layout:



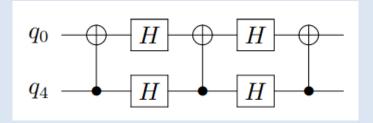
But we want to do this:



No direct connection available! Circumvent it with e.g.



SWAP, CNOT, SWAP



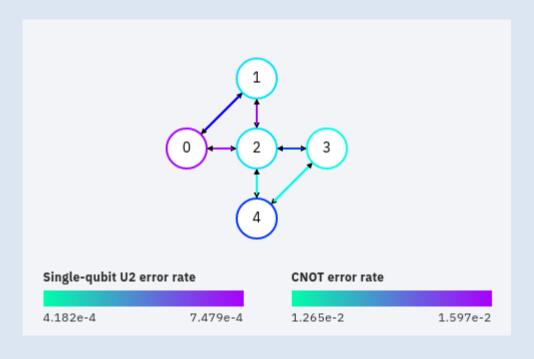
SWAP(q0, q4)

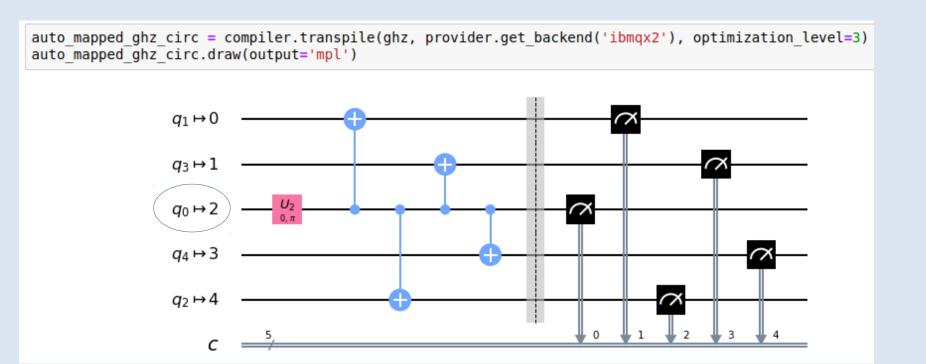
- → Minimize the cost for given quantum algorithm on a given hardware layout
- Software: Compilation/Transpilation
- Hardware: optimized layout for specific algorithms

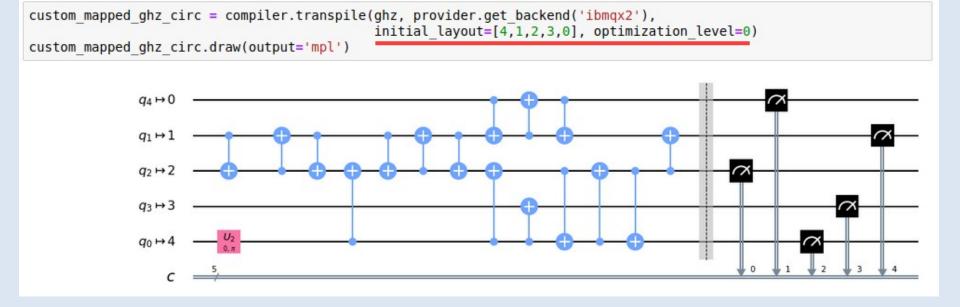
Example:

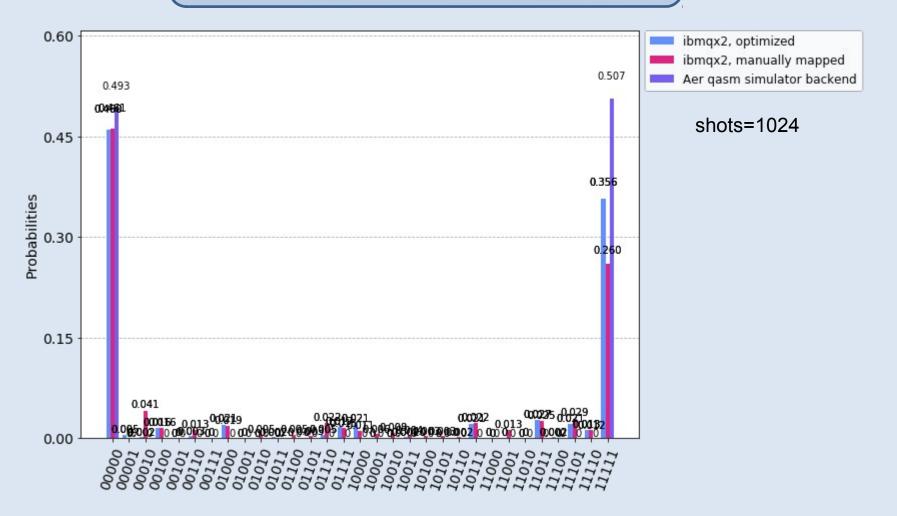
- Device:ibmqx2 (Yorktown)
- Algorithm:GHZ state preparation

$$|00000\rangle \rightarrow \frac{1}{\sqrt{2}} (|00000\rangle + |11111\rangle)$$









→ in this case: optimized circuit performed better