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Model Solution

bvd top robe

```
1 Contest
2 Mathematics
3 Data structures
4 Graph
5 Flows and Matching
6 Strings
Contest (1)
template.cpp
#include <bits/stdc++.h>
using namespace std;
#define rep(i, a, b) for(int i = a; i < (b); ++i)
#define trav(a, x) for(auto& a : x)
#define all(x) begin(x), end(x)
#define sz(x) (int)(x).size()
typedef long long 11;
typedef pair<int, int> pii;
typedef vector<int> vi;
int main() {
 cin.sync_with_stdio(0); cin.tie(0);
  cin.exceptions(cin.failbit);
.bashrc
alias c='q++ -Wall -Wconversion -Wfatal-errors -q -std=c++14 \
 -fsanitize=undefined,address'
xmodmap -e 'clear lock' -e 'keycode 66=less greater' \#caps = \diamondsuit
.vimrc
set cin aw ai is ts=4 sw=4 tm=50 nu noeb bg=dark ru cul
sy on | im jk <esc> | im kj <esc> | no;:
" Select region and then type : Hash to hash your selection.
" Useful for verifying that there aren't mistypes.
ca Hash w !cpp -dD -P -fpreprocessed \| tr -d '[:space:]' \
\| md5sum \| cut -c-6
hash.sh
# Hashes a file, ignoring all whitespace and comments. Use for
                                                                bool p[M];
# verifying that code was correctly typed.
cpp -dD -P -fpreprocessed | tr -d '[:space:]' | md5sum |cut -c-6
troubleshoot.txt
                                                        52 lines
Write a few simple test cases, if sample is not enough.
Are time limits close? If so, generate max cases.
Is the memory usage fine?
Could anything overflow?
Make sure to submit the right file.
```

Print your solution! Print debug output, as well.

```
Are you clearing all datastructures between test cases?
Can your algorithm handle the whole range of input?
Read the full problem statement again.
Do you handle all corner cases correctly?
Have you understood the problem correctly?
Any uninitialized variables?
Any overflows?
Confusing N and M, i and j, etc.?
Are you sure your algorithm works?
What special cases have you not thought of?
Are you sure the STL functions you use work as you think?
Add some assertions, maybe resubmit.
Create some testcases to run your algorithm on.
Go through the algorithm for a simple case.
Go through this list again.
Explain your algorithm to a team mate.
Ask the team mate to look at your code.
Go for a small walk, e.g. to the toilet.
Is your output format correct? (including whitespace)
Rewrite your solution from the start or let a team mate do it.
Runtime error:
Have you tested all corner cases locally?
Any uninitialized variables?
Are you reading or writing outside the range of any vector?
Any assertions that might fail?
Any possible division by 0? (mod 0 for example)
Any possible infinite recursion?
Invalidated pointers or iterators?
Are you using too much memory?
Debug with resubmits (e.g. remapped signals, see Various).
Time limit exceeded:
Do you have any possible infinite loops?
What is the complexity of your algorithm?
Are you copying a lot of unnecessary data? (References)
How big is the input and output? (consider scanf)
Avoid vector, map. (use arrays/unordered_map)
What do your team mates think about your algorithm?
Memory limit exceeded:
What is the max amount of memory your algorithm should need?
Are you clearing all datastructures between test cases?
Mathematics (2)
Mobius Sieve.cpp
<br/>
<br/>
dits/stdc++.h>
                                                     74cf4c, 30 lines
using namespace std;
typedef long long 11;
const int M = 100050;
int mu[M], pm[M], phi[M], pms;
void get_mobius_and_sieve() {
    mu[1] = 1;
    phi[1] = 1;
    fill(p, p + M, true);
    pms = 0:
    for(int i = 2; i < M; i++) {</pre>
        if(p[i]){
            pm[pms++] = i;
            mu[i] = -1;
            phi[i] = i - 1;
```

for(int j = 0; j < pms && i * pm[j] < M; j++) {</pre>

```
p[i * pm[j]] = false;
            if(i % pm[j] == 0){
                mu[i * pm[j]] = 0;
                phi[i * pm[j]] = phi[i] * pm[j];
                break;
            mu[i * pm[j]] = -mu[i];
            phi[i * pm[j]] = phi[i] * (pm[j] - 1);
NTT.cpp
<br/>
<br/>
dits/stdc++.h>
                                                      0964fe, 68 lines
using namespace std;
// 469762049
                 26
                 23
// 998244353
                      3
// 1004535809
                 21 3
// 2281701377
                 27
typedef long long 11;
typedef pair<int, int> P;
const int N = (1 << 16) + 50, mod = 998244353, g = 3;
int rev[N], w[2][N];
int pow(int x, int k){
    int c = 1;
    for(; k; k >>= 1, x = int(x * 1LL * x % mod)) if(k & 1) c =
          int(c * 1LL * x % mod);
    return c;
void init(int len){
    for(int i = 0; i < len; i++) {</pre>
        int y = 0, x = i;
        for(int k = 1; k < len; k *= 2, x >>= 1) (y <<= 1) |= (
            x & 1);
        rev[i] = y;
    w[0][0] = w[1][0] = 1;
    int mp = pow(g, (mod-1)/len), ni = pow(mp, mod - 2);
    for(int i = 1; i < len; i++) {</pre>
        w[0][i] = int(w[0][i-1] * 1LL * mp % mod);
        w[1][i] = int(w[1][i-1] * 1LL * ni % mod);
void NTT(vector<int> &y, int on, int len) {
    y.resize(len, 0);
    for(int i = 0; i < len; i++) if(i > rev[i]) {int tmp = y[i];
          y[i] = y[rev[i]], y[rev[i]] = tmp;}
    for(int h = 2; h <= len; h <<= 1) {</pre>
        int wi = len / h;
        for (int j = 0; j < len; j += h) {</pre>
            int 1 = 0;
            for (int k = j; k < j + h / 2; k++) {
                int u = y[k];
                int t = int(1LL * w[on==-1][1] * y[k + h / 2] %
                y[k] = (u + t) % mod;
                y[k + h / 2] = ((u - t) % mod + mod) % mod;
                1 += wi;
```

7ca530, 64 lines

```
if (on == -1) {
        int ni = pow(len, mod-2);
        for(int i = 0; i < len; i++) y[i] = int(1LL * y[i] * ni</pre>
vector<int> mult_poly(vector<int> a, vector<int> b) {
    int len = 1;
    while(len < a.size() + b.size() + 1) len *= 2;
   init(len);
   NTT(a, 1, len);
   NTT(b, 1, len);
    for (int i = 0; i < len; i++) a[i] = (int) (1LL * a[i] * b[i]
         % mod);
    NTT(a, -1, len);
    while(!a.empty() && a.back() == 0) a.pop_back();
    return a;
FFT.cpp
                                                     eb68a8, 65 lines
const double PI = acos(-1.0);
```

```
struct Complex{
    double x, y;
    Complex (double x = 0.0, double y = 0.0) {
        x = _x, y = _y;
    Complex operator - (const Complex &b) const{
        return Complex(x - b.x, y - b.y);
    Complex operator + (const Complex &b) const{
        return Complex(x + b.x, y + b.y);
    Complex operator * (const Complex &b) const{
        return Complex (x * b.x - y * b.y, x * b.y + y * b.x);
};
void change(Complex y[], int len){
    int i, j, k;
    for(i = 1, j = len/2; i < len - 1; i++) {</pre>
        if(i < j){Complex tmp = y[i]; y[i] = y[j], y[j] = tmp;}</pre>
        k = len / 2;
        while (j >= k) {
            j = j - k;
            k = k / 2;
        if(j < k) j += k;
void fft(Complex y[], int len, int on){
    change(y, len);
    for(int h = 2; h <= len; h <<= 1){</pre>
        Complex wn(cos(-on*2*PI/h), sin(-on*2*PI/h));
        for(int j = 0; j < len; j += h) {</pre>
            Complex w(1,0);
            for (int k = j; k < j + h/2; k++) {
                Complex u = y[k];
                Complex t = w * y[k + h/2];
                y[k] = u + t;
                y[k + h/2] = u - t;
                w = w * wn;
```

```
if(on == -1){
        for(int i = 0; i < len; i++) {</pre>
            y[i].x /= len;
const int N = 200050;
Complex x1[N], x2[N];
int main() {
    for(int i = 0; i < len1; i++) x1[i] = Complex(1, 0);</pre>
    for(int i = 0; i < len2; i++) x2[i] = Complex(1, 0);</pre>
    fft(x1, len, 1);
    fft(x2, len, 1);
    for(int i = 0; i < len; i++) x1[i] = x1[i] * x2[i];</pre>
    fft(x1, len, -1);
FWT.cpp
                                                       df14b<u>9, 51 lines</u>
<br/>
<br/>
dits/stdc++.h>
using namespace std;
typedef long long 11;
const int N = (int) 1e6 + (int) 1e5, mod = (int) 1e9 + 7, inv2 = (
    int)5e8 + 4, M = (int)1e5 + 50, INF = (int)1e9;
int add(int a, int b) {
    a = (a + b) % mod;
    if(a < 0) a += mod;
    return a:
int mul(int a, int b) {
    return (int) (1LL * a * b % mod);
int p[N];
int n, m;
string str[20];
int freq[N], cnt[N], res[N];
struct FWT {
    // Please set N!!!
    int N:
    // Sum over Subsets
    void FWTor(int *a, int opt) {
        for(int mid = 1; mid < N; mid <<= 1)</pre>
            for (int R = mid \ll 1, j = 0; j \ll N; j += R)
                 for (int k = 0; k < mid; k++)
                     if(opt == 1) a[j + k + mid] = add(a[j + k],
                           a[j + k + mid]);
                     else a[j + k + mid] = add(a[j + k + mid], -
                          a[j + k]);
    // Sum over supersets
    void FWTand(int *a, int opt) {
        for(int mid = 1; mid < N; mid <<= 1)</pre>
            for (int R = mid \ll 1, j = 0; j \ll N; j += R)
                 for(int k = 0; k < mid; k++)
                     if(opt == 1) a[j + k] = add(a[j + k], a[j +
                           k + mid]);
                     else a[j + k] = add(a[j + k], -a[j + k +
                          mid]);
    void FWTxor(int *a, int opt) {
```

```
for(int mid = 1; mid < N; mid <<= 1)
    for(int R = mid << 1, j = 0; j < N; j += R)
    for(int k = 0; k < mid; k++) {
        int x = a[j + k], y = a[j + k + mid];
        if(opt == 1) a[j + k] = add(x, y), a[j + k + mid] = add(x, -y);
        else a[j + k] = mul(add(x, y), inv2), a[j + k + mid] = mul(add(x, -y), inv2);
    }
}
fwt;</pre>
```

fast exponentiation and factorial inverse.cpp

```
<br/>
<br/>
dits/stdc++.h>
                                                       01518e, 33 lines
using namespace std;
typedef long long 11;
const int N = 105;
const 11 mod = 998244353;
int n, num[N];
11 fac[N], facinv[N];
11 inv[N];
ll fp(ll x, ll k){
    if(k == 0) return 1;
    11 hf = fp(x, k/2);
    return k % 2 ? hf * hf % mod * x % mod: hf * hf % mod;
11 comb(int n, int k){
    return fac[n] * facinv[k] % mod * facinv[n - k] % mod;
void init fac() {
 inv[1] = 1;
  for(int i = 2; i < N; i++) inv[i] = (mod - (mod / i) * inv[</pre>
      mod % i] % mod) % mod;
    fac[0] = 1;
    for(int i = 1; i <= N-1; i++) fac[i] = fac[i-1] * i % mod;</pre>
    facinv[N-1] = fp(fac[N-1], mod - 2);
    for(int i = N-1 - 1; i >= 0; i--) facinv[i] = facinv[i+1] *
          (i+1) % mod;
int main(){
  init_fac();
```

for(int i = 2; i < N; i++) inv[i] = (mod - (mod / i) * inv[</pre>

Gaussian Elimination.cpp

dits/stdc++.h>

int mod;

int n, m;

ll inv[N];

int num[N][N];

void calc_inv() {

inv[1] = 1;

mod % il % mod) % mod;

using namespace std;

typedef long long 11;

const int N = 100 + 2;

```
struct matrix {
    static const int maxn = 405;
    int n, m;
   11 mat[maxn][maxn];
   11 x[maxn];
   ll res[maxn];
    matrix() { memset(mat, 0, sizeof(mat)); }
   bool gauss() {
        for (int i = 0; i < n; i++) {</pre>
            int sid = -1;
            for (int j = i; j < n; j++)
                if (mat[j][i] > 0) {
                    sid = i;
                     break;
            if (sid == -1) continue;
            if (sid != i) {
                for (int j = 0; j < n; j++) {
                    swap (mat[sid][j], mat[i][j]);
                swap(res[sid], res[i]);
            for (int j = i + 1; j < n; j++) {
                11 ratio = mat[j][i] * inv[mat[i][i]] % mod;
                for (int k = 0; k < n; k++) {
                    mat[j][k] -= mat[i][k] * ratio % mod;
                    mat[i][k] += mod;
                    if (mat[j][k] >= mod) mat[j][k] -= mod;
                res[j] -= res[i] * ratio % mod;
                res[i] += mod;
                if(res[j] >= mod) res[j] -= mod;
        for(int i = m - 1; i >= 0; i--) {
            11 \text{ sum} = \text{res[i]};
            for(int j = i + 1; j < m; j++) {</pre>
                sum -= x[j] * mat[i][j] % mod;
                sum %= mod;
            sum = (sum + mod) % mod;
            x[i] = sum * inv[mat[i][i]] % mod;
            if (mat[i][i] == 0 && sum != 0) return false;
        return true;
} mat;
Euclid-like.cpp
Description: Calculate Sigma 0 to n, floor((a*i+b)/c) in O(log n)
<br/>dits/stdc++.h>
                                                      f64150, 11 lines
using namespace std;
typedef long long 11;
ll fd(ll a, ll b, ll c, ll n) {
   if (a == 0) return ((b / c) * (n + 1));
   if (a >= c || b >= c) return fd(a % c, b % c, c, n) + (a /
        c) * n * (n + 1) / 2 + (b / c) * (n + 1);
    11 m = (a * n + b) / c;
   11 v = fd(c, c - b - 1, a, m - 1);
    return n * m - v;
```

```
XOR Basis.cpp
<br/>bits/stdc++.h>
                                                        a667cf, 24 lines
using namespace std;
const int N = (int) 2e5 + 50, B = 31;
int n:
int a[N];
struct Basis {
    int sz = 0;
    int bas[B];
    bool add(int x) {
        if(x == 0) return false;
        for(int i = 0; i < sz; i++) {</pre>
            if((x ^ bas[i]) < x) x ^= bas[i];
            if(x == 0) return false;
        bas[sz++] = x;
        for(int i = sz - 2; i >= 0; i--) {
            if(bas[i] < bas[i+1]) swap(bas[i], bas[i+1]);</pre>
        return true;
}basis:
BabyStepGiantStep.cpp
                                                       27d863, 31 lines
//Given q^x=y \pmod{p}, find x in O(\log(p)*sqrt(p))
struct BSGS {
    const static int p = 998244353;
    const static int g = 3;
    int m:
    map<int, int> mp;
    vector<int> V;
    void pre() {
        m = (int) ceil(sqrt(p + 0.0) + 1);
        int cq = 1, revqm = 1;
        int invm = (int) (fp(fp(g, m), p - 2));
        for(int i = 0; i < m; i++) {</pre>
            mp[cq] = i;
            V.push_back(revgm);
            cg = (int)(1LL * cg * g % p);
            revgm = (int)(1LL * revgm * invm % p);
    int find(int y) {
        for(int i = 0; i < m; i++) {</pre>
             int cur = (int)(1LL * V[i] * y % p);
            if (mp.count(cur)) {
                 return i * m + mp[cur];
        return -1;
};
Matrix.cpp
<br/>
<br/>
dits/stdc++.h>
                                                       785505, 48 lines
using namespace std;
const int D = (int)101, mod = (int)1e9 + 7;
typedef long long 11;
```

```
struct matrix
    int size:
    11 a[D][D];
    void init(int _size = -1){
        if(_size != -1) size = _size;
        memset(a, 0, sizeof(a));
    matrix(int _size = -1){
         (*this).init( size);
    void set_identity(){
        for(int i = 0; i < size; i++) {</pre>
             for (int j = 0; j < size; j++) a[i][j] = (11)(i == j
                 );
    matrix operator * (const matrix &B) const
        matrix C = matrix(size);
        for(int i = 0; i < size; i++)</pre>
             for(int j = 0; j < size; j++) {</pre>
                 for(int k = 0; k < size; k++)
                     C.a[i][j] += a[i][k] * B.a[k][j] % mod;
                 C.a[i][i] %= mod;
        return C:
    matrix operator ^ (const 11 &p) const
        matrix A = (*this), res = matrix(A.size);
        res.set identity();
        11 t = p;
        while(t > 0)
            if(t % 2) res = res * A;
            A = A * A:
            t /= 2;
        return res;
};
Extended GCD.cpp
Description: want to solve ax + by = gcd(a,b); be careful that gcd(a,b)
can be negative.
<br/>
<br/>
dits/stdc++.h>
                                                       e4650e, 25 lines
using namespace std;
typedef long long 11;
ll al, bl, a2, b2, L, R;
ll extgcd(ll a, ll b, ll &x, ll &y) {
    11 d = a;
    if(b != 0) {
        d = extgcd(b, a % b, y, x);
        y = (a / b) * x;
    else {
        x = 1; y = 0;
    return d;
ll mod(ll a, ll b) {
```

```
return (a % b + b) % b;
ll dvd(ll a, ll b) {
    return (a - mod(a, b)) / b;
Big Integer.cpp
<iostream>, <string>, <cstdio>, <queue>, <cstring>
                                                      db68dc, 79 lines
struct BigInt
    const static int mod = 10000;
    const static int DLEN = 4;
   int a[50],len;
   BigInt()
       memset(a,0,sizeof(a));
       len = 1;
   BigInt(int v)
       memset(a,0,sizeof(a));
       len = 0;
            a[len++] = v%mod;
            v /= mod;
        }while(v);
    BigInt(const char s[])
        memset(a,0,sizeof(a));
        int L = strlen(s);
        len = L/DLEN;
        if (L%DLEN) len++;
        int index = 0;
        for (int i = L-1; i >= 0; i -= DLEN)
            int t = 0;
            int k = i - DLEN + 1;
            if(k < 0)k = 0;
            for(int j = k; j <= i; j++)
                t = t * 10 + s[j] - '0';
            a[index++] = t;
    BigInt operator +(const BigInt &b)const
        BigInt res:
       res.len = max(len,b.len);
        for(int i = 0;i <= res.len;i++)</pre>
           res.a[i] = 0;
        for(int i = 0; i < res.len; i++)</pre>
            res.a[i] += ((i < len)?a[i]:0)+((i < b.len)?b.a[i]
                 1:0);
            res.a[i+1] += res.a[i]/mod;
            res.a[i] %= mod;
        if(res.a[res.len] > 0)res.len++;
       return res:
    BigInt operator *(const BigInt &b)const
        BigInt res;
        for(int i = 0; i < len;i++)</pre>
            int up = 0;
```

Data structures (3)

if (x < 0 || y < 0) **return** 0;

1D BIT.cpp

```
e3a683, 14 lines
//BIT is 0-indexed!!!
int n:
int bit[N];
void add(int x, int val) {
    for(int i = x; i < n; i |= i + 1) bit[i] += val;</pre>
ll get(int x) {
    11 \text{ res} = 0;
    for(int i = x; i >= 0; i = (i & (i + 1)) - 1) res += bit[i
    return res;
Compressed 2D BIT.cpp
                                                       a56764, 29 lines
vector<int> vals[N], f[N];
void addupd(int x, int y) {
    for (int i = x; i < N; i |= i + 1) vals[i].push_back(y);</pre>
void addget(int x, int y) {
    if (x < 0 || y < 0) return;</pre>
    for (int i = x; i >= 0; i = (i & (i + 1)) - 1) vals[i].
         push back (v);
void upd(int x, int y, int v) {
    for (int i = x; i < N; i = i + 1) {
        for (int j = lower_bound(vals[i].begin(), vals[i].end()
             , y) - vals[i].begin();
             j < (int) f[i].size(); j |= j + 1) {</pre>
             f[i][j] += v;
int get(int x, int y) {
```

```
struct Line {
 mutable 11 k, m, p;
 bool operator<(const Line& o) const { return k < o.k; }</pre>
 bool operator<(l1 x) const { return p < x; }</pre>
struct LineContainer : multiset<Line, less<>>> {
 // (for doubles, use inf = 1/.0, div(a,b) = a/b)
  const ll inf = LLONG MAX;
  ll div(ll a, ll b) { // floored division
    return a / b - ((a ^ b) < 0 && a % b); }
 bool isect(iterator x, iterator y) {
   if (y == end()) { x->p = inf; return false; }
   if (x->k == y->k) x->p = x->m > y->m ? inf : -inf;
    else x->p = div(y->m - x->m, x->k - y->k);
    return x->p >= y->p;
 void add(ll k, ll m) {
    auto z = insert(\{k, m, 0\}), y = z++, x = y;
    while (isect(y, z)) z = erase(z);
    if (x != begin() && isect(--x, y)) isect(x, y = erase(y));
    while ((y = x) != begin() && (--x)->p >= y->p)
     isect(x, erase(y));
 ll query(ll x) {
   assert(!empty());
    auto 1 = *lower_bound(x);
    return 1.k * x + 1.m;
};
```

Convex Hull Trick (Static).cpp

Description: Maintaining upper convex hull, querying the maximum. Need to put in lines in strictly increasing order of slope.

return LHS + RHS;

```
Medium Divide Tree.cpp
    // k needs to be strictly increasing!
    void add(ll k, ll m) {
        while(que.size() > 1) {
            int ls = que.size() - 1;
            if (leg(que[ls].inter(Line(k, m)), que[ls-1].inter(
                 que[ls]))) que.pop_back();
            else break;
        que.push back({k, m});
    // Arbitrary x.
    ll query bin(ll x) {
        int l = 0, r = que.size() - 1;
        while (1 < r)
            int mi = (1 + r) / 2;
            if(que[mi].k * x + que[mi].m < que[mi+1].k * x +
                 que[mi+1].m) l = mi + 1;
            else r = mi:
        return que[1].k * x + que[1].m;
    // If querying increasing x.
    11 query(ll x) {
        while(que.size() > 1) {
            if(que[0].k * x + que[0].m < que[1].k * x + que[1].
                 m) que.pop_front();
            else break;
        return que[0].k * x + que[0].m;
} hull;
Interval Tree.cpp
                                                     c569c2, 27 lines
int dat[LOGN][N];
void build(int dep, int 1, int r){
    if(l == r) {dat[dep][l] = num[l]; return ;}
    int mid = (1 + r) / 2;
   build (dep + 1, 1, mid);
   build(dep + 1, mid + 1, r);
    int j = mid + 1, cur = 1;
    for(int i = 1; i <= mid; i++) {</pre>
        while(j <= r && dat[dep+1][j] < dat[dep+1][i]){</pre>
            dat[dep][cur++] = dat[dep+1][j++];
        dat[dep][cur++] = dat[dep+1][i];
    while(j <= r) dat[dep][cur++] = dat[dep+1][j++];</pre>
int query(int ql, int qr, int dep, int l, int r, int val){
    if(r < ql || l > qr) return 0;
    if(gl <= l && r <= gr) {
        return int(upper_bound(dat[dep] + 1, dat[dep] + r + 1,
             val) - (dat[dep] + 1));
    int mid = (1 + r) / 2;
    int LHS = query(ql, qr, dep + 1, 1, mid, val);
    int RHS = query(ql, qr, dep + 1, mid + 1, r, val);
```

```
Description: I unofficially named it medium divide tree. HDU 2665 / POJ
2104 O(logn) query for kth number in certain interval
<iostream>, <cstdio>, <algorithm>
                                                      a307e1, 64 lines
using namespace std;
const int N = (int) 1e5 + 500, LOGN = 20;
int n,q;
int num[N], sorted[N];
int tree[LOGN][N], toleft[LOGN][N];
void build(int dep, int 1, int r){
    if(1 == r) return ;
    int mid = (1 + r) / 2;
    int same = mid - 1 + 1;
    for(int i = 1; i <= r; i++) if(tree[dep][i] < sorted[mid])</pre>
    int lpos = 1, rpos = mid + 1;
    for(int i = 1; i <= r; i++) {</pre>
        if(tree[dep][i] < sorted[mid]){</pre>
            tree[dep+1][lpos++] = tree[dep][i];
        else if(tree[dep][i] == sorted[mid] && same > 0){
            tree[dep+1][lpos++] = tree[dep][i]; same--;
        else tree[dep+1][rpos++] = tree[dep][i];
        toleft[dep][i] = toleft[dep][l-1] + lpos - 1;
    build(dep + 1, 1, mid);
    build(dep + 1, mid + 1, r);
void init(){
    for(int i = 1; i <= n; i++) sorted[i] = tree[0][i] = num[i</pre>
    sort(sorted + 1, sorted + n + 1);
    build(0, 1, n);
int query(int dep, int 1, int r, int q1, int qr, int k){
    if(ql == qr) return tree[dep][ql];
    int mid = (1 + r) / 2;
    int cnt = toleft[dep][qr] - toleft[dep][ql - 1];
    if(cnt >= k){
        int newl = 1 + toleft[dep][ql-1] - toleft[dep][l-1];
        int newr = newl + cnt - 1;
        return query(dep + 1, 1, mid, newl, newr, k);
    else{
        int newr = qr + toleft[dep][r] - toleft[dep][qr];
        int newl = newr - (qr - ql - cnt);
        return query(dep + 1, mid + 1, r, newl, newr, k - cnt);
int main(){
    int T;
    scanf("%d", &T);
    while (T--) {
        scanf("%d%d", &n, &q);
        for(int i = 1; i <= n; i++) scanf("%d", &num[i]);</pre>
        init();
        while(q--){
            int a, b, k;
            scanf("%d%d%d", &a, &b, &k);
            printf("%d\n", query(0, 1, n, a, b, k));
```

```
Monotonous Deque.cpp
<br/>
<br/>
dits/stdc++.h>
                                                      e8856b, 29 lines
using namespace std;
typedef pair<int, int> P;
typedef long long 11;
const int N = 3005, INF = (int)1e9 + 50;
int n, m, a, b;
11 q0, x, y, z;
int num[N][N];
11 mn[N];
// Monotonous Interval Min Queries
struct MonOueue {
    deque<P> que;
    void clear()
        que.clear();
    void add(P p) {
        while(!que.empty() && que.back().first >= p.first) que.
             pop_back();
        que.push_back(p);
    int get(int 1, int r) {
        while(!que.empty() && (que.front().second < 1 || que.</pre>
             front().second > r)) que.pop_front();
        return que.empty() ? -INF : que.front().first;
} mque[N], cque;
Persistent Segment Tree, point update.cpp
<iostream>, <cstdio>, <vector>, <algorithm>, <assert.h>
                                                      a04195, 51 lines
using namespace std;
const int N = (int)1e5 + 50;
typedef pair<int, int> P;
//Need to initialize before every test case!
int ncnt = 1:
struct node {
    int ls, rs, sum;
ns[N * 301;
int newnode(int val){
    ns[ncnt].ls = ns[ncnt].rs = 0;
    ns[ncnt].sum = val;
    return ncnt++;
int newnode(int ls, int rs){
    ns[ncnt].ls = ls;
    ns[ncnt].rs = rs;
    ns[ncnt].sum = (ls ? ns[ls].sum : 0) + (rs ? ns[rs].sum :
         0);
    return ncnt++;
int n, q;
int num[N];
```

int x[N], zeros[N];

```
int vs[N];
int build(int a[], int t1 = 0, int tr = n-1){
    if(tl == tr) return newnode(a[tl]);
    int mid = (tl + tr) / 2;
    return newnode(build(a, tl, mid), build(a, mid + 1, tr));
int qet_sum(int v, int 1, int r, int t1 = 0, int tr = n-1){
    if(tr < 1 || t1 > r) return 0;
    if(1 <= t1 && tr <= r) return ns[v].sum;</pre>
    int tm = (tl + tr) / 2;
    return get_sum(ns[v].ls, l, r, tl, tm)
           + get_sum(ns[v].rs, 1, r, tm + 1, tr);
int update(int v, int pos, int t1 = 0, int tr = n-1){
    if(tl == tr) return newnode(ns[v].sum + 1);
    int tm = (t1 + tr) / 2;
    if(pos <= tm) return newnode(update(ns[v].ls, pos, tl, tm),</pre>
         ns[v].rs);
    else return newnode(ns[v].ls, update(ns[v].rs, pos, tm+1,
Persistent Segment Tree, range update.cpp
```

```
0a9451, 77 lines
<iostream>, <cstdio>, <vector>, <algorithm>, <assert.h>
using namespace std;
const int N = (int)1e5 + 50;
typedef pair<int, int> P;
typedef long long 11;
//Need to initialize before every test case!
int nent = 1:
struct node(
    int ls, rs, lazy;
    11 sum:
\} ns[N * 100];
int newnode(int val){
    ns[ncnt].ls = ns[ncnt].rs = 0;
   ns[ncnt].sum = val;
   ns[ncnt].lazy = 0;
    return ncnt++;
int newnode(int ls, int rs){
   ns[ncnt].ls = ls;
    ns[ncnt].rs = rs;
   ns[ncnt].sum = (ls ? ns[ls].sum : 0) + (rs ? ns[rs].sum :
    ns[ncnt].lazy = 0;
    return ncnt++;
int n, q;
int num[N];
int vs[N];
int tim = 0;
int newlazynode(int v, int val, int l, int r){
    ns[ncnt].ls = ns[v].ls;
    ns[ncnt].rs = ns[v].rs;
    ns[ncnt].lazy = ns[v].lazy + val;
```

```
ns[ncnt].sum = ns[v].sum + (r - 1 + 1) * val;
    return ncnt++;
void push_down(int v, int tl, int tr){
    if(ns[v].lazv){
        if(tl != tr) {
            int mid = (tl + tr) / 2;
            ns[v].ls = newlazynode(ns[v].ls, ns[v].lazy, tl,
            ns[v].rs = newlazynode(ns[v].rs, ns[v].lazy, mid +
        ns[v].lazy = 0;
int build(int a[], int t1 = 0, int tr = n-1){
    if(tl == tr) return newnode(a[tl]);
    int mid = (tl + tr) / 2;
    return newnode(build(a, tl, mid), build(a, mid + 1, tr));
11 get_sum(int v, int 1, int r, int t1 = 0, int tr = n-1) {
    if(tr < 1 || t1 > r) return 0;
    if(1 <= t1 && tr <= r) return ns[v].sum;</pre>
    push down(v, tl, tr);
    int tm = (t1 + tr) / 2;
    return get_sum(ns[v].ls, l, r, tl, tm)
           + get_sum(ns[v].rs, 1, r, tm + 1, tr);
int update(int v, int 1, int r, int val, int tl = 0, int tr = n
    if(tr < 1 || t1 > r) return v;
    if(1 <= t1 && tr <= r) return newlazynode(v, val, tl, tr);</pre>
    push_down(v, tl, tr);
    int tm = (tl + tr) / 2;
    return newnode(update(ns[v].ls, l, r, val, tl, tm), update(
         ns[v].rs, l, r, val, tm+1, tr));
segment tree, point update.cpp
<bits/stdc++.h>
                                                     05495a, 61 lines
using namespace std;
#define lson(x) 2*x+1
#define rson(x) 2*x+2
typedef long long 11;
typedef pair<int, int> P;
const int N = (int) 2e5 + 500, mod = (int) 1e9 + 7;
P p[N];
int rs[N];
struct node {
    int mn;
    int cnt;
    void merge(node &LHS, node &RHS) {
        mn = min(LHS.mn, RHS.mn);
        cnt = (LHS.mn == mn ? LHS.cnt : 0) + (RHS.mn == mn ?
             RHS.cnt : 0);
        cnt %= mod;
```

```
struct Tree {
    node dat[N * 4];
    void init_dat(int 1, int r, int x){
        if(1 == r) {dat[x].mn = p[1].first; dat[x].cnt = 1;
             return ;}
        int mid = (1 + r) / 2;
        init_dat(1, mid, lson(x));
        init_dat(mid+1, r, rson(x));
        dat[x].merge(dat[lson(x)], dat[rson(x)]);
    void update(int pos, int x, int 1, int r, int val, int cnt)
        int mid = (1 + r) / 2;
        if(1 == r) {
            dat[x].mn = val;
            dat[x].cnt = cnt;
            return ;
        if(pos <= mid) update(pos, lson(x), l, mid, val, cnt);</pre>
        else update(pos, rson(x), mid+1, r, val, cnt);
        dat[x].merge(dat[lson(x)], dat[rson(x)]);
    node query(int a, int b, int x, int 1, int r){
        if(r < a | | b < 1) return {mod + 5, 0};</pre>
        int mid = (1 + r) / 2;
        if(a <= 1 && r <= b) return dat[x];</pre>
        node res:
        node LHS = query(a, b, lson(x), l, mid);
        node RHS = query(a, b, rson(x), mid+1, r);
        res.merge(LHS, RHS);
        return res;
} tree;
segment tree, range update.cpp
<br/>
<br/>
dits/stdc++.h>
                                                      826cd9, 103 lines
#define ls(x) x * 2 + 1
#define rs(x) \times * 2 + 2
using namespace std;
typedef long long 11;
const int N = (int) 1e6 + 50;
int INF = (int) 1e9 + 50;
int n, m, q;
int a[N], b[N];
int num[N];
struct node {
    int mn, add;
    void add_val(int x) {
        mn += x;
        add += x;
    void merge(node &ls, node &rs) {
        mn = min(ls.mn, rs.mn);
```

Sparse Table Biconnected Component (Vertex)

if (dat[rs(x)].mn < 0) return find(rs(x), mid + 1, r);</pre>

```
struct Tree {
   node dat[4 * N];
    void push_down(int x, int 1, int r) {
       if(dat[x].add) {
           if(1 < r) {
               dat[ls(x)].add_val(dat[x].add);
                dat[rs(x)].add val(dat[x].add);
            dat[x].add = 0;
    void init(int x = 0, int l = 0, int r = n-1) {
       if(1 == r) {
           dat[x].mn = num[1];
            dat[x].add = 0;
            return ;
        int mid = (1 + r) / 2;
       init(ls(x), l, mid);
       init(rs(x), mid + 1, r);
       dat[x].add = 0;
        dat[x].merge(dat[ls(x)], dat[rs(x)]);
   node query (int a, int b, int x = 0, int 1 = 0, int r = N-1)
        int mid = (1 + r) / 2;
       if(r < a | | 1 > b) return {INF, 0};
       push down(x, l, r);
       if(1 >= a && r <= b) return dat[x];</pre>
       node LHS = query(a, b, ls(x), l, mid);
       node RHS = query(a, b, rs(x), mid+1, r);
       node res;
        res.merge(LHS, RHS);
        return res;
    void update(int a, int b, int x, int l, int r, int delta) {
       int mid = (1 + r) / 2;
       if(r < a \mid \mid 1 > b) return ;
       push_down(x, 1, r);
        if(1 >= a && r <= b) {
           dat[x].add_val(delta);
            return ;
        update(a, b, ls(x), l, mid, delta);
       update(a, b, rs(x), mid+1, r, delta);
        dat[x].merge(dat[ls(x)], dat[rs(x)]);
    void update(int a, int b, int delta) {
       update(a, b, 0, 0, N - 1, delta);
   int find(int x, int 1, int r) {
       if(l == r) return l;
       int mid = (1 + r) / 2;
       push_down(x, 1, r);
```

```
else return find(ls(x), l, mid);
    int find() {
        if(dat[0].mn >= 0) return -1;
        else return find(0, 0, N-1);
} tree;
Sparse Table.cpp
<br/>
<br/>
dits/stdc++.h>
                                                       7c6adf, 90 lines
using namespace std;
typedef long long 11;
const int N = (int)3e5 + 50, LOGN = 19;
struct SA {
    // ht[i] = lcp(suffix[sa[i]], suffix[sa[i-1]])
    int rk[N], sa[N], ht[N];
    int st[LOGN + 1][N], mm[N];
    void build(string str) {
        n = str.length();
        str = " " + str;
        static int set[N], a[N];
        for(int i = 1; i <= n; i++) set[i] = str[i];</pre>
        sort(set + 1, set + n + 1);
        int *end = unique(set + 1, set + n + 1);
        for (int i = 1; i \le n; i++) a[i] = (int) (lower bound)
             set + 1, end, str[i]) - set);
        static int fir[N], sec[N], tmp[N], buc[N];
        fill (buc, buc + n + 1, 0);
        for(int i = 1; i <= n; i++) buc[a[i]]++;</pre>
        for(int i = 1; i <= n; i++) buc[i] += buc[i-1];</pre>
        for(int i = 1; i <= n; i++) rk[i] = buc[a[i]-1] + 1;</pre>
        for (int t = 1; t \le n; t \ne 2) {
            for(int i = 1; i <= n; i++) fir[i] = rk[i];</pre>
            for(int i = 1; i \le n; i++) sec[i] = i + t > n ? 0
                 : rk[i + t];
            fill (buc, buc + n + 1, 0);
            for(int i = 1; i <= n; i++) buc[sec[i]]++;</pre>
            for(int i = 1; i <= n; i++) buc[i] += buc[i - 1];</pre>
            for(int i = 1; i <= n; i++) tmp[n - (--buc[sec[i]])</pre>
                 ] = i;
            fill(buc, buc + n + 1, 0);
            for (int i = 1; i <= n; i++) buc[fir[i]]++;</pre>
            for(int i = 1; i <= n; i++) buc[i] += buc[i - 1];</pre>
            for(int j = 1, i; j <= n; j++) i = tmp[j], sa[buc[</pre>
                 fir[i]]--] = i;
            bool unique = true;
            for (int j = 1, i, last = 0; j \le n; j++)
                i = sa[j];
                if (!last) rk[i] = 1;
                else if (fir[i] == fir[last] && sec[i] == sec[
                      last]) rk[i] = rk[last], unique = false;
                 else rk[i] = rk[last] + 1;
                last = i;
```

```
if (unique) break;
        for (int i = 1, k = 0; i \le n; i++) {
            if (rk[i] == 1) k = 0;
            else (
                 if (k > 0) k--;
                 int j = sa[rk[i]-1];
                 while(i + k <= n && j + k <= n && a[i + k] == a
                      [j + k]) k++;
            ht[rk[i]] = k;
        for(int i = 1; i <= n; i++) mm[i] = (i & (i-1)) == 0 ?</pre>
             mm[i-1] + 1 : mm[i-1];
        for(int i = 0; i <= n; i++) {</pre>
             st[0][i] = ht[i];
        for(int lg = 1; lg < LOGN; lg++) {</pre>
             for(int j = 0; j + (1 << lg) - 1 <= n; j++) {</pre>
                 st[lg][j] = min(st[lg-1][j], st[lg-1][j+(1<<(lg-1)[j+1][j+1])
                      -1))]);
    int rmg(int 1, int r){
        int k = mm[r - 1 + 1];
        return min(st[k][l], st[k][r-(1<<k)+l]);
    int lcp(int 1, int r) {
        if(1 == r) return -1;
        int li = rk[1], ri = rk[r];
        if(li > ri) swap(li, ri);
        return rmq(li, ri);
} sa;
```

Graph (4)

Biconnected Component (Vertex).cpp

```
<iostream>, <vector>, <set>, <stack>
                                                      5b4cdd, 78 lines
using namespace std;
typedef pair<int, int> P;
const int N = (int) 1e4 + 50, M = (int) 1e5 + 50;
struct edge {
    int to, id;
int n, m;
vector<edge> G[N];
P p[M];
int low[N], pre[N];
int ccnt = 0;
vector<int> bcc[N];
int cut[N];
stack<int> S;
int cnt = 0;
```

Centroid Decomposition Diameter of the tree

```
void init(int n) {
    for(int i = 0; i < n; i++) G[i].clear();</pre>
    for(int i = 0; i < n; i++) bcc[i].clear();</pre>
    ccnt = cnt = 0;
    fill(cut, cut + n, 0);
    fill(pre, pre + n, 0);
    fill(low, low + n, 0);
    while(!S.empty()) S.pop();
void dfs(int v, int par) {
    low[v] = pre[v] = ++cnt;
    int childent = 0;
    for(int j = 0; j < G[v].size(); j++) {</pre>
        edge e = G[v][j];
        if(e.to == par) continue;
        if(!pre[e.to]) {
            S.push (e.id);
            childcnt++;
            dfs(e.to, v);
            low[v] = min(low[v], low[e.to]);
            if(low[e.to] >= pre[v]) {
                cut[v] = true;
                int cur:
                 do {
                     cur = S.top();
                    S.pop();
                    bcc[ccnt].push_back(cur);
                } while(cur != e.id);
                ccnt++;
        else if(pre[e.to] < pre[v]){</pre>
            S.push(e.id);
            low[v] = min(low[v], pre[e.to]);
    if(childcnt < 2 && par == -1) cut[v] = false;</pre>
int main() {
    cin >> n >> m;
    init(n);
    for(int i = 0; i < m; i++) {</pre>
        int a, b; cin >> a >> b; a--, b--;
        p[i].first = a, p[i].second = b;
        G[a].push_back({b, i});
        G[b].push_back({a, i});
    for(int i = 0; i < n; i++) {</pre>
        if(!pre[i]) {
            dfs(i, -1);
```

Centroid Decomposition.cpp

```
const int LOG_N = 17;
int root = 0;
int n, m, a, b;
set<int> G[N];
int parent[LOG_N][N];
int depth[N], par[N], sub[N], dis[N];
void dfs(int v, int p, int d) {
    parent[0][v] = p;
    depth[v] = d;
    for(int nxt : G[v]){
        if(nxt != p) dfs(nxt, v, d+1);
void init(int V) {
    dfs(root, -1, 0);
    for (int k = 0; k+1 < LOG N; k++) {
        for (int v = 0; v < V; v++) {
             if (parent \lceil k \rceil \lceil v \rceil < 0) parent \lceil k+1 \rceil \lceil v \rceil = -1;
             else parent[k+1][v] = parent[k][parent[k][v]];
    }
int lca(int u, int v){
    if (depth[u] > depth[v]) {int tmp = u; u = v; v = tmp;}
    for(int k = 0; k < LOG_N; k++) {</pre>
        if((depth[v] - depth[u]) >> k & 1){
             v = parent[k][v];
    if(u == v) return u;
    for(int k = LOG_N - 1; k >= 0; k--) {
        if(parent[k][u] != parent[k][v]){
            u = parent[k][u];
            v = parent[k][v];
    return parent[0][u];
int min dis(int u, int v){
    int ca = lca(u, v);
    return depth[u] + depth[v] - 2 * depth[ca];
int dfs1(int v, int p) {
    sub[v] = 1;
    for(int nxt : G[v])
        if(nxt != p)
            sub[v] += dfsl(nxt, v);
    return sub[v];
int dfs2(int v, int p, int nn){
    for(int nxt : G[v]){
        if(nxt != p && sub[nxt] > nn/2) return dfs2(nxt, v, nn)
    return v;
void decompose(int v, int p) {
    dfs1(v, -1);
    int centroid = dfs2(v, -1, sub[v]);
    par[centroid] = p;
```

```
for(int nxt : G[centroid]) {
        G[nxt].erase(centroid);
        decompose (nxt, centroid);
    G[centroid].clear();
void update(int v) {
    int cur = v;
    while(1){
        dis[cur] = min(dis[cur], min_dis(v, cur));
        if(par[cur] == -1) break;
        cur = par[cur];
int query(int v) {
    int res = (int)1e9;
    int cur = v;
    while(1){
        res = min(dis[cur] + min_dis(v, cur), res);
        if(par[cur] == -1) break;
        cur = par[cur];
    return res;
int main(){
    init(n);
    decompose(0, -1);
    update(0);
Diameter of the tree.cpp
<br/>dits/stdc++.h>
                                                     14c68b, 46 lines
using namespace std;
const int N = 123456 + 50;
const int INF = (int)1e9;
typedef pair<int, int> P;
int n. m:
set<int> G[N];
int dis[N];
P bfs(int v) {
    fill(dis, dis + n, INF);
    queue<int> que;
    dis[v] = 0;
    que.push(v);
    while(!que.empty()) {
        int u = que.front(); que.pop();
        for(int nxt : G[u]) {
            if(dis[nxt] > dis[u] + 1) {
                dis[nxt] = dis[u] + 1;
                que.push(nxt);
    int res = -1, u = -1;
    for(int i = 0; i < n; i++) {</pre>
        if(dis[i] != INF) {
            if(dis[i] > res){
                res = dis[i];
                u = i;
            else if(dis[i] == res) {
                if(i < u) u = i;
```

```
return {res, u};
int get_diameter() {
    int u = -1;
    for(int i = 0; i < n; i++) if(in[i]) {u = i; break;}</pre>
    P p = bfs(u);
    P p2 = bfs(p.second);
    return p2.first;
Dijkstra.cpp
<br/>dits/stdc++.h>
                                                      87862d, 39 lines
using namespace std;
typedef long long 11;
typedef pair<11, int> P;
const int N = (int)1e5 + 500;
const 11 INF = (11)1e18;
struct edge{
    int to, cost;
    edge(int _to, int _cost){
       to = _to, cost = _cost;
};
int n,m,k,a,b,y;
vector<edge> G[N];
ll dis[N];
void dijkstra() {
    fill(dis, dis+N, INF);
    dis[0] = 0;
    priority_queue<P, vector<P>, greater<P> > pque;
    pque.push({0, 0});
    while(!pque.empty()){
        P p = pque.top(); pque.pop();
        int i = p.second;
        11 dist = p.first;
        if(dist > dis[i]) continue;
        for(edge e : G[i]){
            if(e.cost + dis[i] < dis[e.to]){</pre>
                dis[e.to] = e.cost + dis[i];
                pque.push({dis[e.to], e.to});
Dominator Tree.cpp
```

Description: Dominator tree in $O(M \log(N)/\log(2+M/N))$ time, O(M+N) space Algorithm by T.Lengauer and R.E.Tarjan This is essentially the directed version of articulation points

<bits/stdc++.h> d944ba, 108 lines

```
using namespace std;

typedef long long 11;
const int N = (int)1e5 + 50;
struct Dominator{
```

```
struct min_DSU{
   vector<int> par, val;
    vector<int> const&semi;
    min_DSU(int N, vector<int> const&semi):par(N, -1),val(N
        ), semi(semi){
        iota(val.begin(), val.end(), 0);
    void comp(int x) {
        if(par[par[x]]!=-1){
            comp(par[x]);
            if(semi[val[par[x]]]<semi[val[x]])</pre>
                val[x] = val[par[x]];
            par[x]=par[par[x]];
    int f(int x) {
        if (par[x]==-1) return x;
        comp(x);
        return val[x];
    void link(int x, int p){
        par[x] = p;
};
int N:
vector<vector<int> > G, rG;
vector<int> idom, order;
Dominator(int _N):N(_N), G(N), rG(N) { }
void add_edge(int a, int b) {
    G[a].emplace_back(b);
    rG[b].emplace_back(a);
vector<int> calc_dominators(int S) {
    idom.assign(N, -1);
    vector<int> par(N, -1), semi(N, -1);
   vector<vector<int> > bu(N);
   stack<int> s;
   s.emplace(S);
    while(!s.empty()){
        int a=s.top();s.pop();
        if(semi[a] ==-1) {
            semi[a] = order.size();
            order.emplace_back(a);
            for(int i=0; i<(int)G[a].size();++i){</pre>
                if (semi[G[a][i]]==-1) {
                    par[G[a][i]]=a;
                    s.push(G[a][i]);
    min_DSU uni(N, semi);
    for(int i=(int)order.size()-1;i>0;--i){
        int w=order[i];
        for(int f:rG[w]){
            int oval = semi[uni.f(f)];
            if(oval>=0 && semi[w]>oval) semi[w] = oval;
        bu[order[semi[w]]].push_back(w);
        uni.link(w, par[w]);
        while(!bu[par[w]].empty()){
            int v = bu[par[w]].back(); bu[par[w]].pop_back
                 ();
            int u=uni.f(v);
            idom[v] = semi[u] < semi[v] ? u : par[w];</pre>
    for(int i=1;i<(int)order.size();++i){</pre>
        int w=order[i];
```

```
if(idom[w] != order[semi[w]])
                idom[w] = idom[idom[w]];
        idom[S]=-1;
        return idom;
};
int n, m;
vector<int> par;
int sz[N];
int main() {
    ios::sync_with_stdio(false);
    cin.tie(NULL);
    cin >> n >> m;
    Dominator D(n);
    for(int i = 0; i < m; i++) {</pre>
        int a, b;
        cin >> a >> b; a--, b--;
        D.add_edge(a, b);
    // Calc the immediate dominators for each node.
    par = D.calc_dominators(0);
    // D. order stores the topological order the the dominator
         tree. 0 is the root.
    // Only reachable nodes from the source will appear here.
    for(int i = 0; i < n; i++) sz[i] = 1;
    for(int i = (int)D.order.size() - 1; i > 0; i--) {
        int e = D.order[i];
        sz[par[e]] += sz[e];
Edge Connected Component.cpp
<iostream>, <vector>, <set>, <stack>
                                                     014e74, 39 lines
using namespace std;
const int N = (int) 3e5 + 50;
struct edge {
    int to, id;
};
int n, m;
vector<edge> G[N];
set<int> nG[N];
int low[N], pre[N];
int ccnt = 0;
int cmp[N];
stack<int> S;
int cnt = 0;
void dfs(int v, int id) {
    pre[v] = low[v] = ++cnt;
    S.push(v);
    for(int j = 0; j < G[v].size(); j++) {</pre>
        edge e = G[v][j];
        if(e.id == id) continue;
        if(pre[e.to] == 0) {
            dfs(e.to, e.id);
            low[v] = min(low[v], low[e.to]);
        else low[v] = min(low[v], pre[e.to]);
```

if(pre[v] == low[v]) {

```
int cur;
        do {
            cur = S.top(); S.pop();
            cmp[cur] = ccnt;
       } while(cur != v);
        ccnt++;
Heavy-Light Decomposition.cpp
                                                     ca9278, 59 lines
using namespace std;
const int N = 100050;
int n,m,q;
vector<int> G[N];
int chainNo, chainHead[N], chainInd[N], totPos[N], totsize,
    veridx[N];
int subsize[N], par[N];
void dfs(int v, int p, int d){
   par[v] = parent[0][v] = p;
    subsize[v] = 1;
    for(int &nxt : G[v]) {
        if(nxt == p) continue;
       dfs(nxt, v, d+1);
       subsize[v] += subsize[nxt];
       if(subsize[nxt] > subsize[G[v][0]])
            swap(nxt, G[v][0]);
void hld(int v, int p) {
    if (chainHead[chainNo] == -1) chainHead[chainNo] = v;
    chainInd[v] = chainNo;
    in[v] = totPos[v] = totsize;
    veridx[totsize++] = v;
// v_{-}cost[totsize ++] = cost;
    for(auto nxt : G[v]) {
       if(nxt == p) continue;
       if (nxt != G[v][0]) chainNo ++;
       hld(nxt, v);
    out[v] = totsize;
void init hld(int V) {
    chainNo = totsize = 0;
    fill(chainHead, chainHead + n, -1);
   dfs(0, -1, 0);
   hld(0, -1);
    fill(sum, sum + 4 * n, 0);
    fill(add, add + 4 * n, 0);
int query(int pos, int x, int 1, int r) {
    // Segment Tree Query
void update(int a, int b, int x, int 1, int r, int val) {
    // Segment Tree Update
void update_to_root(int v, int val) {
    while(chainInd[v] != chainInd[0]) {
```

```
update(totPos[chainHead[chainInd[v]]], totPos[v], 0, 0,
              n-1, val);
        v = par[chainHead[chainInd[v]]];
    update(totPos[0], totPos[v], 0, 0, n-1, val);
LCA.cpp
<br/>
<br/>
dits/stdc++.h>
                                                      761d7e, 54 lines
using namespace std;
typedef long long 11;
typedef pair<int, int> P;
const int N = 100050, INF = (int)1e9;
const int LOG_N = 17;
int root = 0;
int n,m,a,b;
vector<int> G[N];
int parent[LOG N][N];
int depth[N], par[N];
void dfs(int v, int p, int d) {
   parent[0][v] = p;
    depth[v] = d;
    for(int nxt : G[v]){
        if (nxt != p) dfs (nxt, v, d+1);
void init(int V) {
   dfs(root, -1, 0);
    for (int k = 0; k+1 < LOG_N; k++) {
        for(int v = 0; v < V; v++) {</pre>
            if (parent[k][v] < 0) parent[k+1][v] = -1;
            else parent[k+1][v] = parent[k][parent[k][v]];
    }
int lca(int u, int v){
    if(depth[u] > depth[v]){int tmp = u; u = v; v = tmp;}
    for(int k = 0; k < LOG_N; k++) {</pre>
        if((depth[v] - depth[u]) >> k & 1){
            v = parent[k][v];
    if(u == v) return u;
    for (int k = LOG_N - 1; k >= 0; k--) {
        if(parent[k][u] != parent[k][v]){
            u = parent[k][u];
            v = parent[k][v];
    return parent[0][u];
int min_dis(int u, int v){
    int ca = lca(u, v);
    return depth[u] + depth[v] - 2 * depth[ca];
Strongly Connected Component.cpp
                                                      c86624, 46 lines
using namespace std;
```

```
const int N = (int)2e5 + 500, INF = (int)1e9;
typedef pair<int, int> P;
typedef long long 11;
int n, m;
vector<int> G[N], rG[N], vs;
bool used[N];
int cmp[N];
void add_edge(int from, int to) {
    G[from].push_back(to);
    rG[to].push_back(from);
void dfs(int v) {
    used[v] = true;
    for(int nxt : G[v]){
        if(!used[nxt]) dfs(nxt);
    vs.push_back(v);
void rdfs(int v, int k){
    used[v] = true;
    cmp[v] = k;
    for(int nxt : rG[v]) {
        if(!used[nxt]) rdfs(nxt, k);
int scc(){
    memset (used, 0, sizeof(used));
    vs.clear();
    for (int v = 0; v < n; v++) {
        if(!used[v]) dfs(v);
    memset(used, 0, sizeof(used));
    int k = 0;
    reverse(vs.begin(), vs.end());
    for(int v : vs) {
        if(!used[v]) rdfs(v, k++);
    return k;
```

Flows and Matching (5)

```
Dinic.cpp
```

<bits/stdc++.h> ec1c8c, 72 lines

```
using namespace std;
const int N = 100050;
const int INF = (int)1e9;

struct edge{
   int to, cap, rev;
   edge(int _to, int _cap, int _rev){
      to = _to, cap = _cap, rev = _rev;
   }
};

// Finding max flow in O(V^2 * E)
struct Dinic {
   vector<edge> G[N];
   int level[N], iter[N];
```

```
void add_edge(int from, int to, int cap){
        G[from].push_back(edge(to, cap, G[to].size()));
        G[to].push_back(edge(from, 0, G[from].size() - 1));
    void bfs(int s){
        memset(level, -1, sizeof(level));
        queue<int> que;
        level[s] = 0;
        que.push(s);
        while(!que.empty()){
            int v = que.front(); que.pop();
            for(int i = 0; i < G[v].size(); i++){</pre>
                 edge &e = G[v][i];
                 if(e.cap > 0 && level[e.to] < 0){</pre>
                     level[e.to] = level[v] + 1;
                     que.push(e.to);
    int dfs(int v, int t, int f){
        if(v == t) return f;
        for(int &i = iter[v]; i < G[v].size(); i++) {</pre>
            edge \&e = G[v][i]:
            if(e.cap > 0 && level[v] < level[e.to]) {</pre>
                int d = dfs(e.to, t, min(e.cap, f));
                if(d > 0){
                     e.cap -= d;
                     G[e.to][e.rev].cap += d;
                     return d;
        return 0:
    int max_flow(int s, int t) {
        int flow = 0;
        for(;;){
            bfs(s);
            if(level[t] < 0) return flow;</pre>
            memset(iter, 0, sizeof(iter));
            while ((f = dfs(s, t, INF)) > 0)
                flow += f;
} dinic;
Ford-Fulkerson.cpp
<cstdio>, <iostream>, <vector>
                                                      2e195b, 47 lines
using namespace std;
const int N = 3100, INF = (int)1e9;
struct edge{
    int to, cap, rev;
    edge(int _to, int _cap, int _rev){
        to = _to, cap = _cap, rev = _rev;
};
int n, m;
vector<edge> G[N];
```

```
bool used[N];
void add_edge(int from, int to, int cap){
    G[from].push_back(edge(to, cap, G[to].size()));
    G[to].push_back(edge(from, 0, G[from].size() - 1));
int dfs(int v, int t, int f) {
    if(v == t) return f;
    used[v] = true;
    for(int i = 0; i < G[v].size(); i++){</pre>
        edge &e = G[v][i];
        if(!used[e.to] && e.cap > 0){
            int d = dfs(e.to, t, min(e.cap, f));
            if(d > 0){
                e.cap -= d;
                G[e.to][e.rev].cap += d;
                return d;
    return 0;
int max_flow(int s, int t) {
    int f = 0:
    for(;;){
        fill (used, used + N, false);
        int d = dfs(s, t, INF);
        if(d == 0) return f;
        f += d;
KM (Maximum Weight Matching).cpp
<br/>bits/stdc++.h>
                                                      47d906, 48 lines
using namespace std;
const int MAXN = 2010;
const int oo = 1000000007;
int dist[MAXN][MAXN];
// Finding the minimum weight prefect matching (of size n) in O
     (N^3)
// The dist matrix is 1-indexed.
int hungarian(int n, int m) {
  vector<int> u(n + 1), v(m + 1), p(m + 1), way(m + 1);
 for(int i = 1; i <= n; i++) {</pre>
   p[0] = i;
    int j0 = 0;
    vector<int> minv(m + 1, oo);
    vector<char> used(m + 1, false);
      used[j0] = true;
      int i0 = p[j0], delta = oo, j1;
      for(int j = 1; j <= m; j++) {</pre>
        if(!used[j]){
          int cur = dist[i0][j] - u[i0] - v[j];
          if(cur < minv[j]){</pre>
            minv[j] = cur;
            way[j] = j0;
          if(minv[j] < delta){</pre>
            delta = minv[j];
            j1 = j;
```

```
v[j] -= delta;
        } else {
          minv[j] -= delta;
      j0 = j1;
    } while (p[j0] != 0);
      int j1 = way[j0];
      p[j0] = p[j1];
      j0 = j1;
    } while(j0);
 return -v[0];
Minimum Cost Flow using Dijkstra.cpp
<iostream>, <cstdio>, <vector>, <queue>
                                                     dfc98e, 61 lines
using namespace std;
const int N = 55, MAX_V = 105, INF = (int)1e9;
typedef pair<int, int> P;
struct edge{int to, cap, cost, rev;};
// Finding Min Cost Max Flow in min(O(F * E * log(V), O(F * V *
      V)):
struct MincostFlow {
    int V; //Please set V!!!!
    vector<edge> G[MAX V];
    int h[MAX V];
    int dist[MAX_V];
    int prevv[MAX_V], preve[MAX_V];
    void add_edge(int from, int to, int cap, int cost){
        G[from].push_back((edge){to, cap, cost, (int)G[to].size
        G[to].push_back((edge) {from, 0, -cost, (int)G[from].
             size() - 1);
    int min_cost_flow(int s, int t, int f) {
        int res = 0;
        fill(h, h + V, 0);
        while(f > 0) {
            priority_queue<P, vector<P>, greater<P> > que;
            fill(dist, dist + V, INF);
            dist[s] = 0;
            que.push(P(0, s));
            while(!que.empty()){
                P p = que.top(); que.pop();
                int v = p.second;
                if(dist[v] < p.first) continue;</pre>
                for(int i = 0; i < G[v].size(); i++){</pre>
                    edge &e = G[v][i];
                    if(e.cap > 0 && dist[e.to] > dist[v] + e.
                         cost + h[v] - h[e.to]){
                        dist[e.to] = dist[v] + e.cost + h[v] -
                             h[e.to];
                        prevv[e.to] = v;
                        preve[e.to] = i;
                        que.push(P(dist[e.to], e.to));
```

for(**int** j = 0; j <= m; j++) {

u[p[j]] += delta;

if(used[j]){

```
if(dist[t] == INF) return -1;
            for(int v = 0; v < V; v++) h[v] += dist[v];
            int d = f;
            for(int v = t; v != s; v = prevv[v]){
                d = min(d, G[prevv[v]][preve[v]].cap);
            f -= d;
            res += d * h[t];
            for(int v = t; v != s; v = prevv[v]) {
                edge &e = G[prevv[v]][preve[v]];
                e.cap -= d;
                G[v][e.rev].cap += d;
        return res;
} mf;
```

Strings (6)

Aho-Corasick Algorithm.cpp

Description: Init, and insert strings, and then build.

dits/stdc++.h> 263a36, 66 lines

```
using namespace std;
const int M = (int)5e5 + 500;
struct Trie{
    static const int B = 26;
    int next[M][B], fail[M], end[M];
    int root, L:
    int newnode(){
        for(int i = 0; i < B; i++) next[L][i] = -1;</pre>
        end[L++] = 0;
        return L - 1;
    // Please do initalize it !!!
    void init() {
       L = 0;
        root = newnode();
    void insert(const string &buf) {
        int len = buf.length();
       int now = root;
        for(int i = 0; i < len; i++) {</pre>
            if (next [now] [buf[i]-'a'] == -1) next [now] [buf[i]-'a
                 '] = newnode();
            now = next[now][buf[i]-'a'];
        end[now] ++;
    void build() {
        queue<int> Q;
        fail[root] = root;
        for(int i = 0; i < B; i++) {</pre>
            if(next[root][i] == -1) next[root][i] = root;
                fail[next[root][i]] = root;
                O.push(next[root][i]);
        while(!Q.empty()){
            int now = Q.front();
            Q.pop();
```

```
for(int i = 0; i < B; i++) {</pre>
                if (next[now][i] == -1) next[now][i] = next[fail
                      [now]][i];
                 else
                     fail[next[now][i]] = next[fail[now]][i];
                     Q.push(next[now][i]);
    int query(const string &buf) {
        int len = buf.length();
        int now = root;
        int res = 0;
        for(int i = 0; i < len; i++){</pre>
            now = next[now][buf[i]-'a'];
            int temp = now;
            while(temp != root){
                res += end[temp];
                end[temp] = 0;
                temp = fail[temp];
        return res;
} Aho;
KMP.cpp
<bits/stdc++.h>
                                                       3a7af0, 28 lines
using namespace std;
const int N = (int)1e6 + 500, M = (int)1e4 + 500;
string s, t;
int f[M];
void getnext(){
    int m = t.length();
    f[0] = 0; f[1] = 0;
    for(int i = 1; i < m; i++) {</pre>
        int j = f[i];
        while(j && t[i] != t[j]) j = f[j];
        f[i+1] = t[i] == t[j] ? j + 1 : 0;
    }
int find(){
    int n = s.length(), m = t.length();
    int res = 0;
    int j = 0;
    for(int i = 0; i < n; i++) {
        while(j \& \& t[j] != s[i]) j = f[j];
        if(t[j] == s[i]) j++;
        if(j == m) res ++, j = f[j];
    return res;
Manacher.cpp
<iostream>, <cstdio>, <algorithm>, <cstring>
                                                       2065b8, 50 lines
struct Manacher {
    string s, sn;
    int p[2*N];
    int Init()
```

int len = s.length();

```
sn = "$#";
        int j = 2;
        for (int i = 0; i < len; i++)
            sn.push_back(s[i]);
            sn.push_back('#');
        sn.push back(' \setminus 0');
        return sn.length();
    int run()
        int len = Init();
        int max len = -1;
        int id = 0;
        int mx = 0;
        for (int i = 1; i < len; i++)</pre>
            if (i < mx)
                p[i] = min(p[2 * id - i], mx - i);
            else
                p[i] = 1;
            while (sn[i - p[i]] == sn[i + p[i]])
                p[i]++;
            if (mx < i + p[i])
                id = i:
                mx = i + p[i];
            max_len = max(max_len, p[i] - 1);
        return max_len;
} mnc;
```

Polynomial Hashing.cpp

```
<br/>
<br/>
dits/stdc++.h>
                                                       3a4d96, 64 lines
using namespace std;
typedef long long 11;
typedef pair<int, int> P;
const int mods[4] = {(int)1e9 + 7, (int)1e9 + 9, (int)1e9 + 21,}
      (int)1e9 + 33};
const int N = (int)2e5 + 50;
string s, t;
int p = 37;
11 pw[4][N];
struct hs {
    11 val[4];
    hs() { fill(val, val + 4, 0); }
    hs(ll a, ll b, ll c, ll d) {
        val[0] = a, val[1] = b, val[2] = c, val[3] = d;
```

bool operator<(const hs &other) const {</pre>

SAM Suffix Array Z-algorithm

```
for (int i = 0; i < 4; i++) if (val[i] != other.val[i])</pre>
              return val[i] < other.val[i];</pre>
        return false;
    bool operator==(const hs &other) const {
        for (int i = 0; i < 4; i++) if (val[i] != other.val[i])</pre>
              return false;
        return true;
    hs operator + (const hs &other) const{
        for(int i = 0; i < 4; i++) res.val[i] = ( val[i] +</pre>
             other.val[i]) % mods[i];
        return res;
    hs operator - (const hs &other) const {
        hs res;
        for(int i = 0; i < 4; i++) res.val[i] = (val[i] - other</pre>
             .val[i] + mods[i]) % mods[i];
        return res;
    hs operator ^ (const int pwi) const {
        hs res:
        for(int i = 0; i < 4; i++) {</pre>
             res.val[i] = (val[i] * pw[i][pwi]) % mods[i];
        return res:
    void add(int x, int pwi){
        for(int i = 0; i < 4; i++) {
             val[i] = (val[i] + x * pw[i][pwi]) % mods[i];
            if(val[i] < 0) val[i] += mods[i];</pre>
};
void init() {
    for(int t = 0; t < 4; t++) {
        pw[t][0] = 1;
        for(int i = 1; i < N; i++) pw[t][i] = pw[t][i-1] * p %</pre>
             mods[t]:
                                                        b6e7ac, 60 lines
<br/>
<br/>bits/stdc++.h>
    int len, link;
```

SAM.cpp

```
using namespace std;
const int N = (int) 1e5 + 50, B = 256;
struct state {
    int next[B];
};
struct SAM {
    const static int MAXLEN = (int)1005;
    state st[MAXLEN * 2];
    int sz, last;
    void sam init() {
       st[0].len = 0;
        st[0].link = -1;
```

```
memset(st[0].next, -1, sizeof(st[0].next));
        sz = 1;
        last = 0;
    void sam extend(int c) {
        int cur = sz++;
        st[cur].len = st[last].len + 1;
        memset(st[cur].next, -1, sizeof(st[cur].next));
        int p = last;
        while (p != -1 && st[p].next[c] == -1) {
            st[p].next[c] = cur;
            p = st[p].link;
        if (p == -1) {
            st[cur].link = 0;
            int q = st[p].next[c];
            if(st[p].len + 1 == st[q].len) {
                st[cur].link = q;
            } else {
                int clone = sz++;
                st[clone].len = st[p].len + 1;
                memcpy(st[clone].next, st[q].next, sizeof(st[q
                     l.next));
                st[clone].link = st[q].link;
                while(p != -1 && st[p].next[c] == q) {
                    st[p].next[c] = clone;
                    p = st[p].link;
                st[q].link = st[cur].link = clone;
        last = cur;
    int calc() {
        int res = 0;
        for(int v = 0; v < sz; v++) {</pre>
            if(st[v].link != -1) res += st[v].len - st[st[v].
                 linkl.len:
        return res;
} sam;
Suffix Array.cpp
<br/>
<br/>
dits/stdc++.h>
                                                      24a7e4, 68 lines
using namespace std;
typedef long long 11;
const int N = (int) 1e5 + 50;
int n;
struct SA {
    int n:
    // ht[i] = lcp(suffix[sa[i]], suffix[sa[i-1]])
    int rk[N], sa[N], ht[N];
    void build(string str) {
```

n = str.length(); str = " " + str;

static int set[N], a[N];

sort(set + 1, set + n + 1);

for(int i = 1; i <= n; i++) set[i] = str[i];</pre>

int *end = unique(set + 1, set + n + 1);

```
set + 1, end, str[i]) - set);
        static int fir[N], sec[N], tmp[N], buc[N];
        fill(buc, buc + n + 1, 0);
        for(int i = 1; i <= n; i++) buc[a[i]]++;</pre>
        for(int i = 1; i <= n; i++) buc[i] += buc[i-1];</pre>
        for(int i = 1; i <= n; i++) rk[i] = buc[a[i]-1] + 1;</pre>
        for(int t = 1; t \le n; t *= 2) {
            for(int i = 1; i <= n; i++) fir[i] = rk[i];</pre>
            for(int i = 1; i \le n; i++) sec[i] = i + t > n ? 0
                 : rk[i + t];
            fill (buc, buc + n + 1, 0);
            for(int i = 1; i <= n; i++) buc[sec[i]]++;</pre>
            for(int i = 1; i <= n; i++) buc[i] += buc[i - 1];</pre>
            for(int i = 1; i <= n; i++) tmp[n - (--buc[sec[i]])</pre>
                 ] = i;
            fill (buc, buc + n + 1, 0);
            for(int i = 1; i <= n; i++) buc[fir[i]]++;</pre>
            for(int i = 1; i <= n; i++) buc[i] += buc[i - 1];</pre>
            for(int j = 1, i; j <= n; j++) i = tmp[j], sa[buc[</pre>
                 fir[i]]--1 = i;
            bool unique = true;
            for (int j = 1, i, last = 0; j \le n; j++)
                i = sa[i];
                if (!last) rk[i] = 1;
                 else if (fir[i] == fir[last] && sec[i] == sec[
                     last]) rk[i] = rk[last], unique = false;
                 else rk[i] = rk[last] + 1;
                last = i;
            if (unique) break;
        for(int i = 1, k = 0; i <= n; i++) {</pre>
            if(rk[i] == 1) k = 0;
            else {
                if (k > 0) k--;
                int j = sa[rk[i]-1];
                while(i + k <= n && j + k <= n && a[i + k] == a
                     [j + k]) k++;
            ht[rk[i]] = k;
} sa;
Z-algorithm.cpp
<bits/stdc++.h>
                                                       06f29b, 27 lines
```

for(int i = 1; i <= n; i++) a[i] = (int)(lower_bound(</pre>

```
using namespace std;
const int MAXN = (int) 1e6 + 500;
string s;
int z[MAXN], cnt[MAXN];
// Examples:
// str = "aabaacd"
// z// = \{x, 1, 0, 2, 1, 0, 0\}
```

// str = "abababab"

KTH

14

```
// z[] = {x, 0, 6, 0, 4, 0, 2, 0}

void getZarr(string str)
{
    memset(z, 0, sizeof(z));
    int n = str.length();
    for(int i = 1, 1 = 0, r = 0; i < n; ++i) {
        if(i <= r)
            z[i] = min(r - i + 1, z[i - 1]);
        while(i + z[i] < n && str[z[i]] == str[i + z[i]])
            ++z[i];
    if(i + z[i] - 1 > r)
        l = i, r = i + z[i] - 1;
}
```

Techniques (A)

techniques.txt

Combinatorics

159 lines

Recursion Divide and conquer Finding interesting points in N log N Algorithm analysis Master theorem Amortized time complexity Greedy algorithm Scheduling Max contiquous subvector sum Invariants Huffman encoding Graph theory Dynamic graphs (extra book-keeping) Breadth first search Depth first search * Normal trees / DFS trees Dijkstra's algorithm MST: Prim's algorithm Bellman-Ford Konig's theorem and vertex cover Min-cost max flow Lovasz toggle Matrix tree theorem Maximal matching, general graphs Hopcroft-Karp Hall's marriage theorem Graphical sequences Floyd-Warshall Euler cycles Flow networks * Augmenting paths * Edmonds-Karp Bipartite matching Min. path cover Topological sorting Strongly connected components Cut vertices, cut-edges and biconnected components Edge coloring * Trees Vertex coloring * Bipartite graphs (=> trees) * 3^n (special case of set cover) Diameter and centroid K'th shortest path Shortest cycle Dynamic programming Knapsack Coin change Longest common subsequence Longest increasing subsequence Number of paths in a dag Shortest path in a dag Dynprog over intervals Dynprog over subsets Dynprog over probabilities Dynprog over trees 3^n set cover Divide and conquer Knuth optimization Convex hull optimizations RMQ (sparse table a.k.a 2^k-jumps) Bitonic cycle Log partitioning (loop over most restricted)

Computation of binomial coefficients Pigeon-hole principle Inclusion/exclusion Catalan number Pick's theorem Number theory Integer parts Divisibility Euclidean algorithm Modular arithmetic * Modular multiplication * Modular inverses * Modular exponentiation by squaring Chinese remainder theorem Fermat's little theorem Euler's theorem Phi function Frobenius number Quadratic reciprocity Pollard-Rho Miller-Rabin Hensel lifting Vieta root jumping Game theory Combinatorial games Game trees Mini-max Nim Games on graphs Games on graphs with loops Grundy numbers Bipartite games without repetition General games without repetition Alpha-beta pruning Probability theory Optimization Binary search Ternary search Unimodality and convex functions Binary search on derivative Numerical methods Numeric integration Newton's method Root-finding with binary/ternary search Golden section search Matrices Gaussian elimination Exponentiation by squaring Sorting Radix sort Geometry Coordinates and vectors * Cross product * Scalar product Convex hull Polygon cut Closest pair Coordinate-compression Ouadtrees KD-trees All segment-segment intersection Discretization (convert to events and sweep) Angle sweeping Line sweeping Discrete second derivatives Strings Longest common substring Palindrome subsequences

Knuth-Morris-Pratt Tries Rolling polynomial hashes Suffix array Suffix tree Aho-Corasick Manacher's algorithm Letter position lists Combinatorial search Meet in the middle Brute-force with pruning Best-first (A*) Bidirectional search Iterative deepening DFS / A* Data structures LCA (2^k-jumps in trees in general) Pull/push-technique on trees Heavy-light decomposition Centroid decomposition Lazy propagation Self-balancing trees Convex hull trick (wcipeg.com/wiki/Convex hull trick) Monotone queues / monotone stacks / sliding queues Sliding queue using 2 stacks Persistent segment tree

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