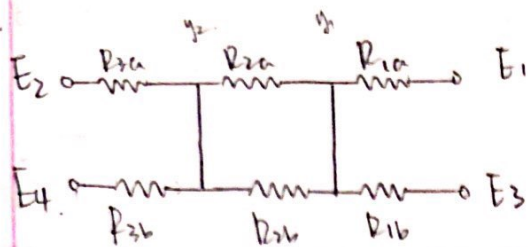


1b)

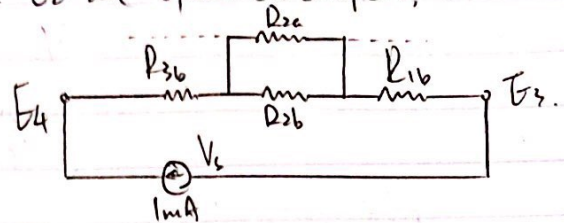


Given that  $R_{total} = l \frac{H}{W \cdot T} = 8 \text{ k}\Omega$ ,  $y_1 = 3 \text{ cm}$ ,  $y_2 = 7 \text{ cm}$ ,  $H = 12 \text{ cm}$   
 with  $R_{total} = 8 \text{ k}\Omega$ ,  
 so  $R_{1a} = R_{1b} = R_{total} \cdot \frac{y_1}{H} = 2 \text{ k}\Omega$ .

$$R_{2a} = R_{2b} = R_{total} \cdot \frac{y_2 - y_1}{H} = 2.667 \text{ k}\Omega$$

$$R_{3a} = R_{3b} = R_{total} \cdot \frac{H - y_2}{H} = 3.333 \text{ k}\Omega$$

(c) Using the given conditions, since  $E_1$  and  $E_2$  are open-circuited, so no current flow through resistors  $R_{2a}$  and  $R_{1a}$ , which means that the circuit diagram is equivalent to:



We can calculate using methods that the resistance between  $E_4$  and  $E_3$  is:

$$R_{eq} = R_{3b} + \frac{1}{\frac{1}{R_{2a}} + \frac{1}{R_{2b}}} + R_{1b} = R_{total} \cdot \frac{H - y_2}{H} + \frac{1}{2} \cdot R_{total} \cdot \frac{y_2 - y_1}{H} + R_{total} \cdot \frac{y_1}{H}$$

with  $y_1 = 3 \text{ cm}$ ,  $y_2 = 7 \text{ cm}$ ,  $H = 12 \text{ cm}$ , so  $= R_{total} \cdot \frac{H - y_2/2 + y_1/2}{H} = \frac{20}{3} \text{ k}\Omega = 6.667 \text{ k}\Omega$

Thus,  $V_s = I_s \cdot R_{eq} = 1 \text{ mA} \cdot 6.667 \text{ k}\Omega = 6.667 \text{ V}$ .

which means that  $V_{E_4 - E_3} = V_s = \boxed{6.667 \text{ V}}$

(d) Using what we've deduced in the steps of part (c), we have that:

$$R_{eq} = R_{total} \cdot \frac{H - y_2/2 + y_1/2}{H}$$

So,  $V_{E_4 - E_3} = V_s = I_s \cdot R_{eq} = 1 \text{ mA} \cdot 8 \text{ k}\Omega \cdot \frac{H - y_2/2 + y_1/2}{H} = 8 \text{ V} \cdot \left(1 - \frac{y_2}{24} + \frac{y_1}{24}\right)$

So,  $\boxed{V_{E_4 - E_3} = \left(8 - \frac{1}{3}y_2 + \frac{1}{3}y_1\right) \text{ V}}$

(e) Using similar logic from part (c) and (d), so we can drive  $E_2, E_4$  with a  $1 \text{ mA}$  current source and measure  $V_{E_4 - E_2} = I_s \cdot R_{eq_{2,4}}$  where

$$R_{eq_{2,4}} = R_{3a} + \frac{1}{\frac{1}{R_{2a}} + \frac{1}{R_{3b}}} + R_{3b} = R_{total} \cdot \left(\frac{H - y_2}{H} + \frac{1}{2} \cdot \frac{y_2 - y_1}{H} + \frac{H - y_2}{H}\right)$$

$$= 8 \text{ k}\Omega \cdot \frac{2H - \frac{3}{2}y_2 - \frac{1}{2}y_1}{H}$$

So,  $V_{E_4 - E_2} = 1 \text{ mA} \cdot 8 \text{ k}\Omega \cdot \left(2 - \frac{3}{24}y_2 - \frac{1}{24}y_1\right) = \left(16 - y_2 - \frac{1}{3}y_1\right) \text{ V}$

Similarly,  $R_{eq1,3} = R_{1a} + \frac{1}{\frac{1}{R_{2a}} + \frac{1}{R_{2b}}} + R_{1b} = R_{total} \cdot \left( \frac{y_1}{H} + \frac{1}{2} \cdot \frac{y_2 - y_1}{H} + \frac{y_1}{H} \right)$

$$= 8k\Omega \cdot \left( \frac{y_1 + \frac{1}{2}y_2 - \frac{1}{2}y_1 + y_1}{H} \right) \text{ where } H = 12 \text{ cm}$$

$$= 8k\Omega \cdot \left( \frac{1}{8}y_1 + \frac{1}{24}y_2 \right)$$

And, providing/driving  $E_1, E_3$  with a 1mA current source gives:

$$V_{E_1 - E_3} = I_s \cdot R_{eq1,3} = 1mA \cdot 8k\Omega \left( \frac{1}{8}y_1 + \frac{1}{24}y_2 \right)$$

$$\text{So } V_{E_1 - E_3} = \left( y_1 + \frac{1}{3}y_2 \right) V$$

Thus, we have two (plus one) equations:

$$V_{E_4 - E_2} = \left( 16 - \frac{1}{3}y_1 - y_2 \right) V$$

$$V_{E_1 - E_3} = \left( y_1 + \frac{1}{3}y_2 \right) V$$

$$[\text{from (1)}] \quad V_{E_4 - E_3} = \left( 8 + \frac{1}{3}y_1 - \frac{1}{3}y_2 \right) V$$