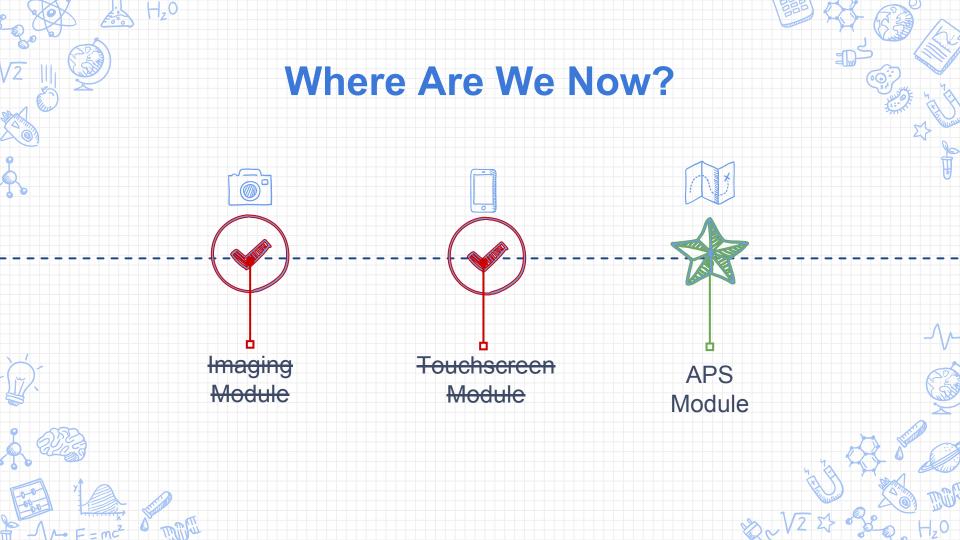
# EE16A Lab: Acoustic Positioning System 1



#### **Announcements**

- All software; no hardware involved
  - That means you can finish at home!
    - Just APS 1 though, come in for APS2
- No lab on Thanksgiving week, check Piazza for more detail

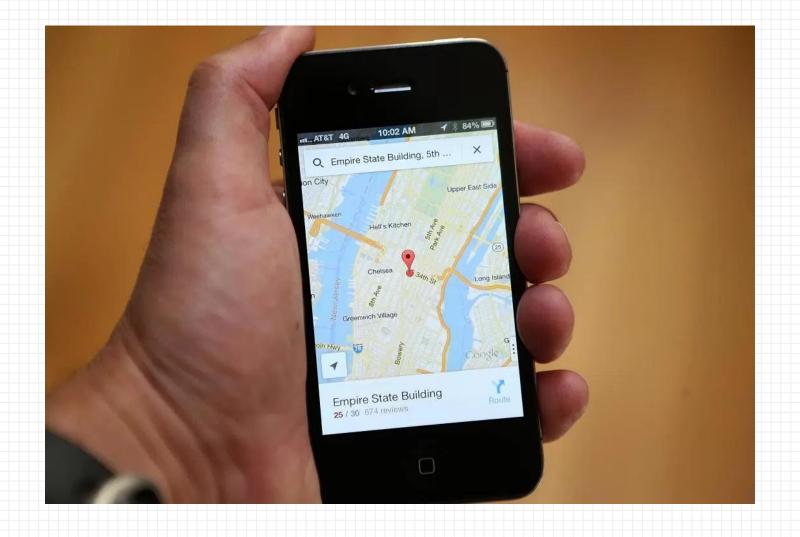




# Today's Lab: Acoustic Positioning System

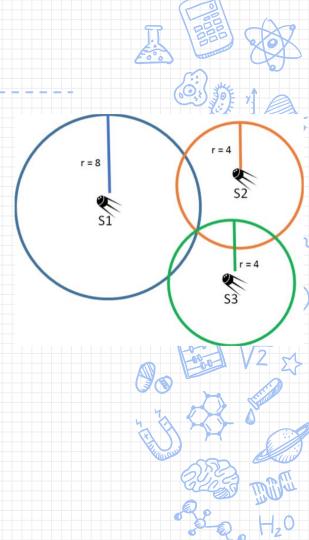
- Global Positioning System (GPS)
  - Basically the same thing
  - Uses radio waves instead of sound waves
- Understand mathematical tools used for sifting and detecting signals
  - Think about cross correlation!

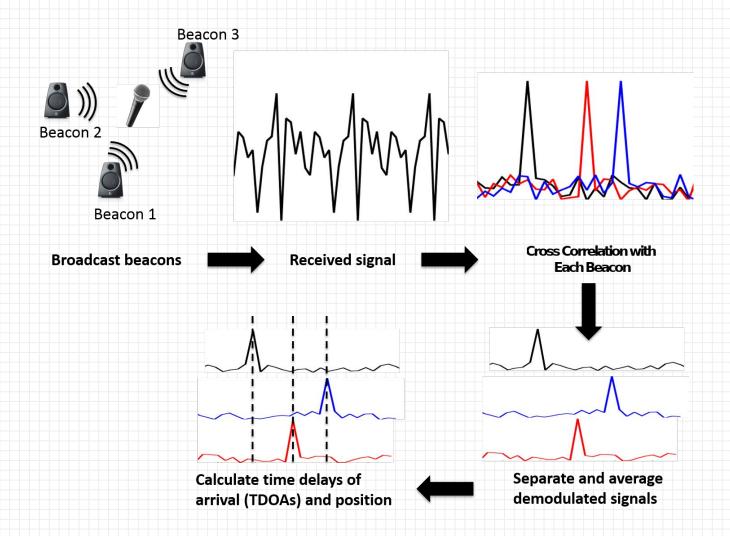




#### GPS?

- Satellites send signals at known times (beacons are synchronized)
  - But we aren't synchronized to the beacons
- Receiver (das us) gets these signals
- From time-delay of a beacon signal,
   receiver calculates distance to the beacon
- From distances to satellites, position is determined by lateration
- How many beacons do you need to determine your location in 2D?





## Time of Flight

- Receiver gets signals from multiple satellites at the same time
  - Each is a known beacon/waveform
  - Periodic
  - We also know where the satellites are
- The receiver then determines when each beacon is received, with reference to when other beacons are received
  - Harder than it seems! Why?



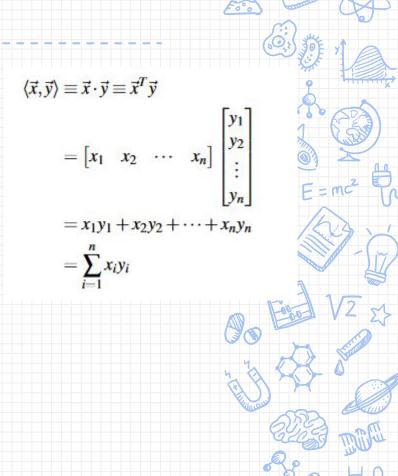
#### **Problem**

- Our antenna receives all the signals at once
  - We have to separate out the useful information
- We have no clue when the satellites sent their signals
  - Signals repeat every 230ms
  - Because of this we can't use the start of the recording as a reference
- Even if we can separate the info, we can't just wait until we receive something, because we don't know when it was sent
  - This week we will cheat a little bit, next time we'll see how to really handle it



# Recall: Inner (Dot) Product

- A mathematical operation for vectors
- One way to think about it is that it computes how similar two vectors are



## Recall: Inner (Dot) Product

- A mathematical operation for vectors
- One way to think about it is that it computes how similar two vectors are

 Given this expression, and assuming ||x|| = ||y|| = 1, when is this expression maximum?

$$\langle \vec{x}, \vec{y} \rangle = ||x|| \, ||y|| \cos \theta$$

An alternate form of the dot product

The value is maximized when theta = 0
This is when the vectors point in the **SAME DIRECTION**, which is to say, the vectors are the **SAME SIGNAL** 

Thus the bigger the dot product, the more "similar" the two vectors are

## **Tool: Cross-correlation**

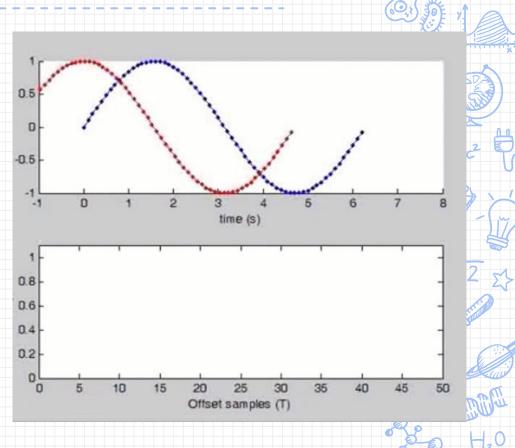
$$corr(f,g)[n] = \sum_{k} f[k]g[k-n]$$

- Mathematical tool for finding similarities between signals
- Idea: Take g and slide over f, compute dot product, slide again
  - Gets plotted with the <u>shift amount</u>
- From the previous slide, <u>peak</u> of cross-correlation tells us which shift amount makes g "most similar" to f



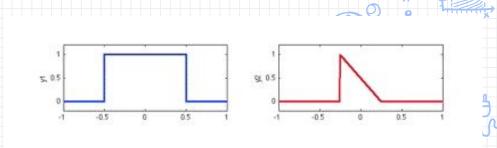
#### **Tool: Cross-correlation**

- "Sliding Dot Product"?
- Helps us find a specific signal midst a mix of many signals
  - Dot product computes similarity
  - Sliding dot product tells us how similar two signals are for a given shift amount (see gif)
- Use it to decode ambiguous texts from your crush
- At how many offset samples is the signal most similar?



#### **How Will We Use It?**

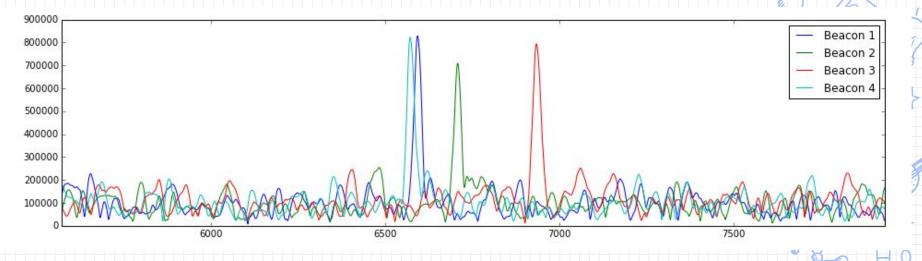
- Cross correlating should tell us where our beacons arrived in our signal
- From there we can try to find a way to compute the time delays
  - Then we can find the distances!





## **Solution Attempt**

- Let's cross-correlate each of the known beacon signals with what we recorded and plot the result
  - What do you expect to see?

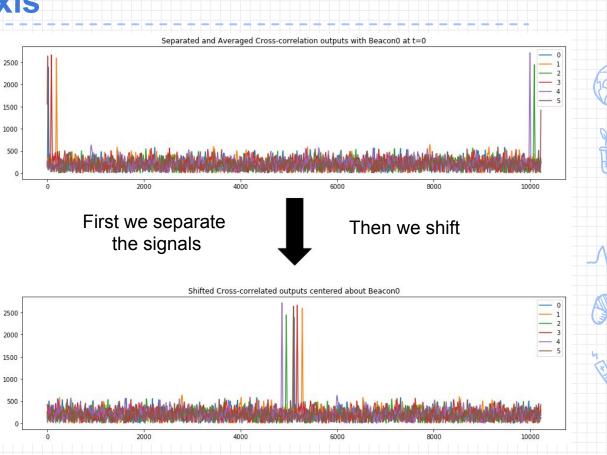


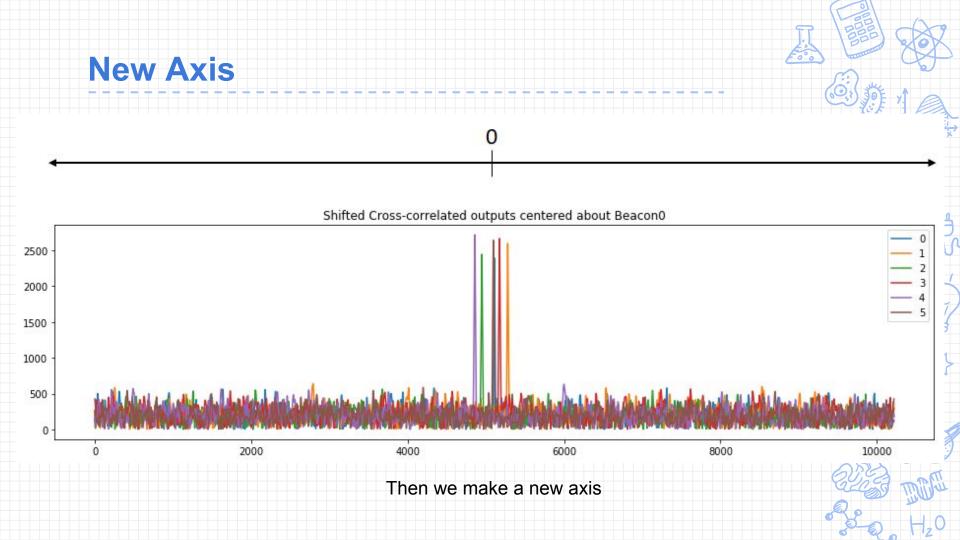
## Ok, What Now?

- Great! We can clearly see where each signal is in our received waveform
- Unfortunately we're still not quite there... This doesn't tell us much
- Idea: we don't know when the beacons arrived, but based off of the offsets we know how much longer it took for beacon 1 to arrive RELATIVE to beacon 0!
- Let's shift our axis so beacon 0 is at 0
  - We could pick any beacon to be the center. 0 is arbitrary



## **New Axis**





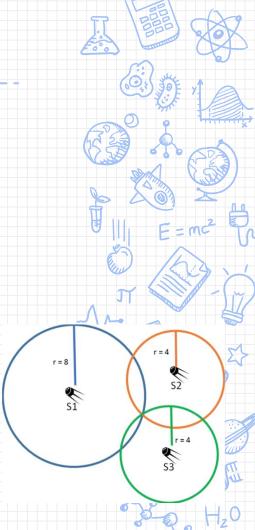
# **New Axis** Relative location of beacon 1 Shifted Cross-correlated outputs centered about Beacon0

### **Shifted Beacons**

- We know the rate at which we recorded samples, and we know how many samples each beacon is from beacon 0
- Since sampling frequency is samples/second, then  $\frac{\text{samples}}{f_s} = \frac{\text{samples}}{\frac{\text{samples}}{\text{samples}}} = \text{seconds}$
- We know how long relative to beacon 0 it took for every other beacon to arrive

second

- We know where the satellites are, so we can use the distances to find our location!
  - Or can we..?



# **And Finally, Computing Distances??**

- distance = rate x time
  - For beacons 1 through N, we know the time it took to travel
  - We know how fast various types of waves travel in air (AKA rate)
  - We can directly compute distance!
    - RELATIVE to beacon 0, not what we want
    - Oh, I guess we haven't quite solved it yet



# Actually wait, one more problem

- We know how long it took for beacon 1 to arrive AFTER beacon 0.
- If we magically knew beacon 0 arrived 4s into our recording, and beacon 1 arrived 3s after that, how long did it take for beacon 1 to arrive?
  - Knowing the time beacon 0 arrived (t0) we can fully compute our distance
  - But in general, we don't know when beacon 0
    arrived. You'll be given it for today, though.

#### **Notes + Next Lab:**

- If we knew distance / time of flight for beacon 0, finding location is easy
  - Today this value will be given to you for testing purposes
  - Find out how to deal with this in APS2!
- It's a long lab, don't feel pressured to finish it here.
  - Go home and get help from friends/TAs
- Note: Sliders in the notebook may not work; not so important so you can move on

