Instructions for MA2

This document contains the material for the second module (M2) in the course Computer Programming II. Concepts covered are parsing with "recursive descent", exceptions, function objects.

> In this module, you will write a calculator which reads and calculates arithmetic expressions. You will get a very simple version to start with, on which several features should be built. The description of this mandatory assignment can be found in the yellow frames below.

The following files are associated with the module:

1. `MA2.py` An embryo of the program that you are going to write and upload in the end.
2. `MA2tokenizer` A help class that you have to use.
3. `MA2init.txt` A file with test data that is read automatically when the program starts. You can provide it with more test cases for the features that you implement.
4. `MA2_test.py`: Unit-tests. Run this program when you think that you have completed all tasks!
5. `MA2micro.py` A small calculator that executes simple operations.

Follow the instruction below when preparing your solutions for presenting:

1. You may `not` use packages other than those already imported
2. You must use all functions that are specified in this document and they must be defined with exactly the same name and parameters.
3. Implement and test one feature at a time!
4. You can run the file with unit tests when you think you are done. If you want to run the unit test before every function is in use, enter the tests gradually.
5. Before you present your solution
   - Check that the complete unit test works!
   - Remember that functions should be implemented using a dictionary with function names and function *function objects*. Adding a new function should only require updating that dictionary (and writing the function if it doesn't exist).
   - Make sure that you understand how exception handling works!
6. When your solution is approved by a teacher or assistant:
   (a) Fill in the name, email and assistants / teachers who reviewed the assignment.
   (b) Upload the file `MA2.py` in Studium under MA2.

Note that you should upload only **one** file and it should be a `.py` file that is directly executable in Python! We do not accept other formats (word, pdf files, Jupyter notebook, ...) and no submissions via email.

Note: You may collaborate with other students, but you must write and be able to explain your own code. You may not copy code, neither from other students nor from the Internet except from the places explicitly pointed out in this lesson. Changing variable names and similar modifications does not count as writing your own code. Since these assignments are included as part of the course examination, we are obliged to report failures to follow these rules.
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Syntax analysis with recursive descent

Recursive methods are well-suited to recursively structured processing data. An example of this is ordinary arithmetic expressions. Consider e.g. the following expression

$$1 + (2.3 + 4) \cdot 3.42 + 0.34 \cdot (1.2 + 13 \cdot 0.7)$$

There are a number of rules for how this should be interpreted, for example "multiplication before addition", "parentheses first" and "from left to right when priority is equal". It is not easy (but doable) to implement these rules in a program which reads and interprets an expression.

However, we can define expressions in a more structured way that in itself details the priority rules:

An *expression*
: is a sequence of one or more *terms* with a plus or minus character in between.

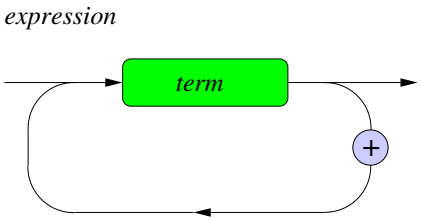
A *term*
: is a sequence of one or more *factors* with a multiplication or division character in between.

A *factor*
: is either a *number* or an *expression* surrounded by parentheses.

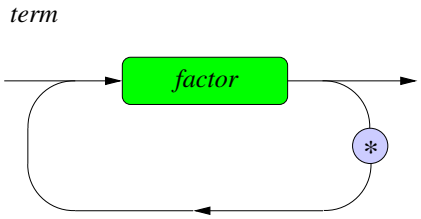
Note that this definition is indirectly recursive.

For the time being, we assume that only syntactically correct expressions are entered. For the sake of simplicity in the demo code, we will limit ourselves for the time being to addition, multiplication and parentheses operations. This does not change the structure — only the details of the code.

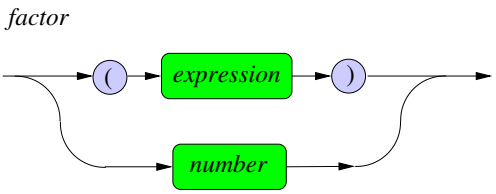
The definition can be illustrated graphically with the following *syntax charts*. There is *pseudocode* to the right of the charts describing how the chart can be translated into code where we mix programming language constructions. The mixed constructions combine `if` and `while` statements with added commented running text for parts to be specified later.




```
def expression():
    sum = term()
    while # next is '+':
        # Get passed '+'
        sum += term()
    return sum
```




```
def term():
    sum = factor()
    while # next is '*':
        # Get passed '*'
        sum += factor()
    return sum
```




```
def factor():
    if # next is '(':
        # Get passed '('
        result = expression()
        # Get passed ')'
    else:
        result = # read number
    return result
```

We have not drawn a chart for *numbers* but assume that someone else can find out how a number is defined using digits, decimal point etc.

Note the recursion again: an *expression* is defined by *terms* which are defined by *factors* which, maybe, are defined by an *expression*.

All charts contain "junctions". It is the next character (plus, times and parentheses) which decides which path we should choose. If, for example, in the *expression* there is a plus character after the first term, we will go back and take a new term. If there is no plus-character, the expression is done **no matter what comes** — it's someone else's problem to handle!

The input to the program is basically a sequence of characters (10 digits as well as `'.'`, `'+'`, `'*'`, `'('` and `')'`). We want to handle *numbers*, not individual digits, decimal point etc. For this we will use a so-called *tokenizer*.

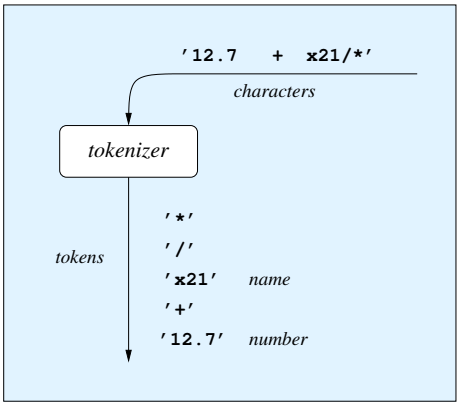
Tokenizer

A *tokenizer* is used to group individual characters into larger units such as words and numbers, so-called *tokens*. Different applications have different rules for how the tokens are formed. Of course, a tokenizer for programming code has different rules from a tokenizer for natural language processing.

The Python module `tokenize` is useful for our purposes but to simplify the usage, we

provide a wrapper class `TokenizeWrapper`. An object from the wrapper class is coupled with a character string (such as an input line) and produces a sequence of tokens. There is a *current token*, methods to get information about this and a method of stepping up to the next token.

This figure exemplifies how a tokenizer receives the string `'12 .7 + x21 / * '` with 15 characters and produces a sequence of 5 different string tokens.



The most important methods in the `TokenizeWrapper` are:

`TokenizeWrapper(line)`	Creates a tokenizer object and connects it to `line`
`next()`	Advances to the next token (number, character, word, ...)
`has_next()`	Returns `True` if there are more tokens on the line, otherwise `False`
`get_current()`	Returns the current token as a string
`get_previous()`	Returns the previous token as a string
`is_number()`	Returns `True` if the current token is a number, otherwise `False`.
`is_name()`	Returns `True` if the current token is a name, otherwise `False`.
`is_at_end()`	Returns `True` if end of line otherwise `False`.

Note that `next()` is the *only* method that advances the tokenizer. The other methods just provide information about the current or previous token.

Here is a small demo code. The output is shown in the adjacent pane.

```
hej     NAME
hopp    NAME
+       OPERATOR
234     NUMBER
*       OPERATOR
26.4    NUMBER
=       OPERATOR
        NEWLINE
```

```python
def main():
    line = 'hej hopp + 234 * 26.4  ='
    wtok = TokenizeWrapper(line)
    while wtok.has_next():
        print(wtok.get_current(), end='\t')
        if wtok.is_name():
            print('NAME')
        elif wtok.is_number():
            print('NUMBER')
        elif wtok.is_newline():
            print('NEWLINE')
        else:
            print('OPERATOR')
        wtok.next()
    print(wtok.get_current())
```

Using these methods, we can express the commented running text of the pseudocode seen on Page 3 in Python code. We will then get following simple calculator:

```python
def expression(wtok):
    result = term(wtok)
    while wtok.get_current() == '+':
        wtok.next()                  # bypass +
        result = result + term(wtok)
    return result

def term(wtok):
    result = factor(wtok)
    while wtok.get_current() == '*':
        wtok.next()                  # bypass *
        result = result * factor(wtok)
    return result

def factor(wtok):
    if wtok.get_current() == '(':
        wtok.next()                  # bypass (
        result = expression(wtok)
        wtok.next()                  # bypass )
    else:                            # should be a number
        result = float(wtok.get_current())
        wtok.next()                  # bypass the number
    return result

def main():
```

```
    print("Very simple calculator")
    while True:
        line = input("Input : ")
        wtok = TokenizeWrapper(line)
        if wtok.get_current() == 'quit':
            break
        else:
            res = expression(wtok)
            print('Result: ', res)
    print("Bye!")

if __name__ == "__main__":
    main()

```

What can go wrong?

```
3*2 ++ 1
2-3
-1
1 2 3
1**2
2*(1+3-+4
```

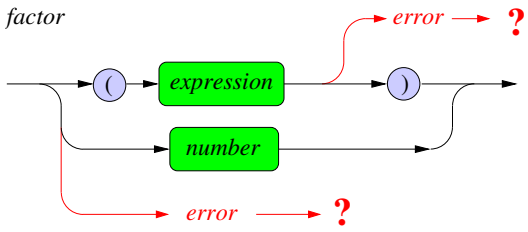
The program above is included when accessing the file `MA2micro.py`. Try, in turn, these incorrect input lines:

Try to understand the output!

There are two places in the code where things can go wrong, and both are when dealing with factors:

1) The factor begins neither with a left parenthesis nor with a number.

2) There is no matching right parentheses after *expression*.



The errors can easily be detected by the code:

```
1  def factor(wtok):
2      if wtok.get_current() == '(':
3          wtok.next()            # bypass (
4          result = expression(wtok)
5          if wtok.get_current() == ')':
6              wtok.next()        # bypass )
7          else:
8              pass # What shall we do here
9      elif wtok.is_number():
10         result = float(wtok.get_current())
11         wtok.next()            # bypass the number
12     else:
13         pass  # What shall we do here?
14     return result
15
```

It is possible to produce an error message here but how should the program continue? The function is expected to return a number that is to be used higher up in the code. Once an error has been detected, it is probably pointless to continue calculating the expression. However, we do not want the program to exit but to print the error message, ignore the rest of the expression and continue with a new expression on a new line.

To handle such situation, *exceptions* are well-suited.

Error handling in the calculator

To handle syntax errors in the calculator, we will make our *own* exception class. It must be written as a subclass of the built-in class `Exception`. Exception classes are easy to write. In this case we only need:

```
1  class SyntaxError(Exception):
2      def __init__(self, arg):
3          self.arg = arg
4          super().__init__(self.arg)
```

Thus, the class has only one constructor which receives and saves a message. The word `Exception` in parentheses in line 1 indicates that this is a subclass of the `Exception` class.

To cause an exception, we use the command `raise`. We use `raise` in the `factor` function and handle the exceptions in `main`:

```
1  def factor(wtok):
2      if wtok.get_current() == '(':
3          wtok.next()                  # bypass (
4          result = expression(wtok)
5          if wtok.get_current() == ')':
```

```
            wtok.next()              # bypass )
        else:
            raise SyntaxError("Expected ')'")
    elif wtok.is_number():
        result = float(wtok.get_current())
        wtok.next()                  # bypass the number
    else:
        raise SyntaxError('Expected number or (')
    return result

def main():
    print("Very simple calculator")
    while True:
        line = input("Input : ")
        wtok = TokenizeWrapper(line)
        try:
            if wtok.get_current() == 'quit':
                break
            else:
                result = expression(wtok)
                if wtok.is_at_end():
                    print('Result: ', result)
                else:
                    raise SyntaxError('Unexpected token')
        except SyntaxError as se:
            print("*** Syntax: ", se.arg)
            print(f"Error ocurred at '{wtok.get_current()}'" +
                  f" just after '{wtok.get_previous()}'")
        except TokenError:
            print('*** Syntax: Unbalanced parentheses')
    print('Bye!')
```

We have also added handling of a `TokenError` that can occur in case of unbalanced parentheses.

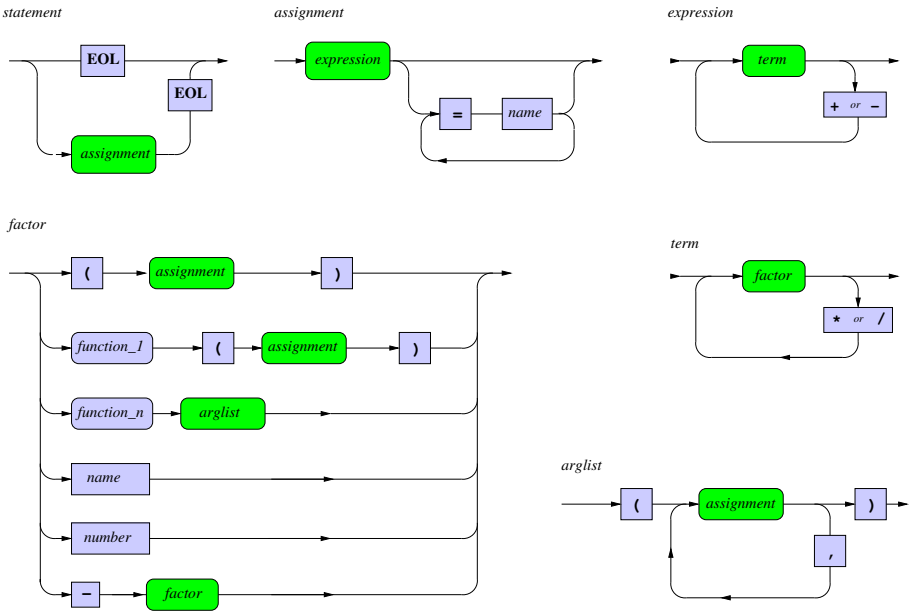
Mandatory assignment: Calculator

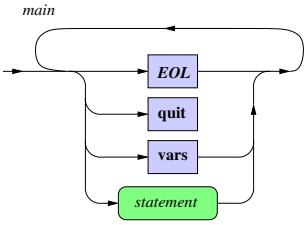
We start by exemplifying a run of the program and the complete syntax charts:

```
Input : 3-1+3-1/2                          # Float type
Result: 4.5
Input : 1 - (5-2*2)/(1+1) - (-2 + 1)       # Float type
Result: 1.5
Input : sin(3.14159265)                    # Standard functions
Result: 3.5897930298416118e-09
Input : cos(PI)                            # Predefined constant
Result: -1.0
Input : log(exp(4*0.5 - 1))                # Standard functions
Result: 1.0
Input : 1 + 2 + 3 = x                      # Variable. Assignment goes RIGHT!
Result: 6.0
Input : x/2 + x
Result: 9.0
Input : (1=x) + sin(2=y)                   # Assignments
Result: 1.9092974268256817
Input : vars                               # Prints variable values
   E     : 2.718281828459045
   PI    : 3.141592653589793
   ans   : 1.9092974268256817
   x     : 1.0
   y     : 2.0
Input : 1+2
Result: 3.0
Input : 2*ans + 5                          # Result of last computation
Result: 11.0
Input : ans
Result: 11.0
Input : z                                  # Undefined variable
*** Evaluation error:  Undefined variable: 'z'
Input : 1 + max(sin(x+y), cos(1), log(0.5))
Result: 1.5403023058681398
Input : fac(5)                            # Factorial. Note integer
Result: 120
Input : fac(2.5)                           # Illegal argument
*** Evaluation error:  Argument to fac is 2.5. Must integer >= 0
Input : fac(40)                            # Larger integer
Result: 815915283247897734345611269596115894272000000000
Input : 2 ++ 4*ans/0                       # Syntax error before evaluation error
*** Syntax error:  Expected number, word or '('
Error ocurred at '+' just after '+'
Input : ans/0 + * x                        # Evaluation error before syntax error
*** Evaluation error:  Division by zero
```

Syntax charts

The syntax of the expressions is defined by the following charts:





The commands `vars` and `quit` are handled in the `main`-function according to this figure:

This function also handles exceptions.

The task is to complement `MA2.py` to handle several operations and tasks as follows

1. The program should be able to handle expressions with constants, variables, the arithmetic operators `+`, `-`, `*`, `/` as well as a number of functions, including `sin`, `cos`, `exp`, `log`.
2. The usual priority rules apply and when used, parentheses should change the calculation order.
3. Variable assignment must be made *from left to right.*
   Example: The expression
   `1+2*3 = y`
   will give the value `7` to `y` .
4. Subexpressions should be able to handle variable assignment.
   Example:
   `(2=x) + (3=y=z) = a`
   will give values to `x`, `y`, `z` and `a`.
5. The predefined variable `ans` should contain the value of the last calculated complete expression. This variable can then be used in the next expression.
   Example:

```
Input : 1+1
Result: 2.0
Input : ans
Result: 2.0
Input : exp(2)
Result: 7.38905609893065
Input : ans
Result: 7.38905609893065
Input : ans + 3
Result: 10.38905609893065
Input : 3 + ans
Result: 13.38905609893065
```

6. The program must detect and diagnose errors. Example:

```
Input : 1++2
*** Error. Expected number, name or '('
*** The error occurred at token '+' just after token '+'
Input : 1+-2
Result: -1.0
Input : 1--2
Result: 3.0
Input : 1**2
*** Error: Unexpected token
*** The error occurred at token '**'
Input : 1/0
*** Error. Division by zero
Input : 1+2*y-4
Result: 1.0
Input : 1+2*k-4
*** Error. Undefined variable: k
Input : 1+2=3+4**x - 1/0
*** Error. Expected variable after '='
*** The error occurred at token '3.0' just after token '='
Input : 1+2*(3-1 a
*** Error: Unbalanced parentheses
*** The error occurred at token 'a' just after token '1.0'
Input : 1+2+3+
*** Error: Expected number, name or '('
*** The error occurred at token '*EOL*' just after token '+'
Input :
```

7. The command `vars` shows all stored variables with values and the command `quit` ends the run. Example:

```
Input : vars
 ans    : 13.38905609893065
 E      : 2.718281828459045
 PI     : 3.141592653589793
 x      : 1.0
 y      : 2.0
Input : quit
Bye!
```

Functions

8. In addition to the functions `sin`, `cos`, `exp`, `log`, the following functions must be available:

Function	Meaning	Example
fac(n)	$n!$ Integer argument and result.	fac(0) = 1, fac(1) =1, fac(3) = 6
sum($a_1, a_2, \ldots$)	Sum of arguments	sum(1,2,3,4) = 10
max($a_1, a_2, \ldots$)	Largest argument	max(1,2,3,4) = 4

   Functions should be implemented using a dictionary with *function names* as keys and *function objects* as values. It is a good idea to use different dictionaries for *FUNCTIONS_1* and *FUNCTION_N*.
   These dictionaries could be placed either locally in `factor` or on the top level as global constants.
   To add a new function, there must be *no changes* in the code needed other than adding a new key-value pair to the dictionary. The function definition itself must of course be included.

As the syntax charts show, there are two different groups of functions:

1. Those with exactly one argument: `sin`, `cos`, `exp`, `log`, `fac` which are called *function_1* in the charts.
2. Those with several arguments: `max` and `sum` which are called *function_n* in the charts.

This example demonstrates how function objects can be stored and transferred.
Note that the example deals with *function objects*, not function values!

```
1  def demo(f, x):
2      return f(x)
3
4  print(demo(sqrt, 4))
5  print(demo(log, 1))
6
7  foo = sqrt
8  print(foo(9))         # Prints the square root of 9
9
10 d = {'f':sqrt, 'g':log}
11 print(d['f'](25))     # Prints the square root of 25
```

More about handling functions as objects can be found at Corey Schafer's YouTube-lesson!

Program parts

The program must have the following components (with specified names):

- The class `TokenizeWrapper`. This class is given and you do not need to modify it in any way.
- A number of functions which handle the parsing and calculations. There should be a function for each syntactic element (i.e. *assignment*, *expression*, *term*, *factor*, ...) These functions should exactly follow the syntax charts!
  All must have exactly the two given parameters `wtok` (the tokenizer object) and `variables` (the variable list).
  All parser functions should return a number (`float` or `int`) except for `arglist` which should return a list of numbers.
- Functions for the built: `fac`, ... Of course, you can directly use functions built into Python (`cos`, `max`, ...)

Variable values

To keep track of the values of variables, a dictionary should be used. The dictionary should be created in the `main`-function and sent as an argument to all parser function. Also add the constants `PI` and `E` and the predefined variable `ans` to the dictionary! This makes the handling as uniform as possible. However, the variable `ans` needs to be updated in the `main` function.

Error handling

The user of the program can make two types of errors: *syntax errors* and *evaluation errors*. The expression `x+*y` is an example of incorrect syntax while the expression `log(2*x-x-x)` is example of a calculation error (because the argument to `log` will be 0).
In the first expression the error can be detected *before* the summation is to be done but in the second case, the argument must be calculated before the error can be detected. In the latter case, information about the current token is usually not relevant.
Errors are caught in the `main` function. When an error occurs, the rest of the line is ignored and a new expression is begun.

Syntax error

If the user writes an expression which does not match the syntax according to the syntax charts (e.g. `a ++ b` or `sin + 4` or `2 * 3) + 8`) it is a *syntax error*.

The program should detect such errors and deal with them with an exception of type `SyntaxError`.

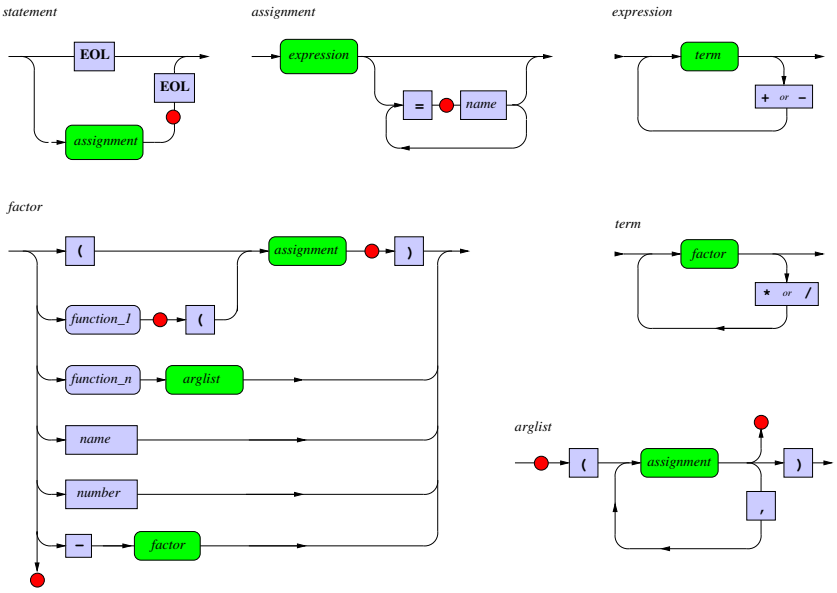
It can be tempting to look for errors everywhere but it only makes sense in a few places:

- In *assignment*: the equals sign is not followed by a variable name.
- In *factor*:
  1. The right parenthesis after *assignment* is missing.

2. The left parenthesis after *function_1* is missing.
3. None of the five cases, i.e. not a parenthesis, not a *function_1* or *function_n* name, not a number, not a minus sign and not a name.

- In *arglist*:
  1. The argument list does not start with a left parenthesis
  2. An argument is not followed by a comma or a parenthesis.
- In *statement*: There are more items on the line.

The red circles indicates places to check the syntax.



In *expression* and *term*, nothing can go wrong and these methods should therefore not look for errors.

Evaluation errors

Even if an expression is syntactically correct, it may be incomputable. Examples of such errors:

- Division by 0
- Argument to `log` less than or equal to 0.
- Incorrect type of argument (e.g. `fac(2.5)`)

These errors should be handled with the exception class `EvaluationError`. If it is an incorrect argument (i.e. all examples except the first) then the function name and the argument should be specified in the error message.

Important coding hint:

Checking that the arguments are correct is best done in the individual functions (`log`, `fac`, ...) and *not* in the parser function `factor`.

Since all calculation is done with type `float` then it is the *value* and not the *type* that

determines whether arguments in `fac` are correct or not. See the examples!

Include the error checks *from the beginning*! This greatly facilitates your own troubleshooting and testing of the program! It is good to implement this feature in an early stage. You can then successively add test cases for each feature you implement instead of manually entering test data each time.