



pgRouting Manual

Release v2.6.0

pgRouting Contributors

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1	General	3
1.1	Introduction	3
1.2	Installation	5
1.3	Support	9
1.4	Sample Data	10
2	Pgrouting Concepts	19
2.1	pgRouting Concepts	19
2.2	pgr_version	32
3	Data Types	33
3.1	pgRouting Data Types	33
4	Topology Functions	37
4.1	Topology - Family of Functions	37
5	Routing functions	63
5.1	Routing Functions	63
6	Available Functions but not official pgRouting functions	149
6.1	Stable Proposed Functions	149
6.2	Experimental Functions	226
7	Change Log	393
7.1	Release Notes	393
	Bibliography	407

pgRouting extends the [PostGIS](http://postgis.net)¹/[PostgreSQL](http://postgresql.org)² geospatial database to provide geospatial routing and other network analysis functionality.

This is the manual for pgRouting v2.6.0.



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¹<http://postgis.net>

²<http://postgresql.org>

³<http://creativecommons.org/licenses/by-sa/3.0/>

1.1 Introduction

pgRouting is an extension of [PostGIS](http://postgis.net)¹ and [PostgreSQL](http://postgresql.org)² geospatial database and adds routing and other network analysis functionality. A predecessor of pgRouting – pgDijkstra, written by Sylvain Pasche from [Camptocamp](http://camptocamp.com)³, was later extended by [Orkney](http://www.orkney.co.jp)⁴ and renamed to pgRouting. The project is now supported and maintained by [Georepublic](http://georepublic.info)⁵, [iMaptools](http://imaptools.com/)⁶ and a broad user community.

pgRouting is part of [OSGeo Community Projects](http://wiki.osgeo.org/wiki/OSGeo_Community_Projects)⁷ from the [OSGeo Foundation](http://osgeo.org)⁸ and included on [OSGeo Live](http://live.osgeo.org)⁹.

1.1.1 Licensing

The following licenses can be found in pgRouting:

License	
GNU General Public License, version 2	Most features of pgRouting are available under GNU General Public License, version 2 ¹⁰ .
Boost Software License - Version 1.0	Some Boost extensions are available under Boost Software License - Version 1.0 ¹¹ .
MIT-X License	Some code contributed by iMaptools.com is available under MIT-X license.
Creative Commons Attribution-Share Alike 3.0 License	The pgRouting Manual is licensed under a Creative Commons Attribution-Share Alike 3.0 License ¹² .

In general license information should be included in the header of each source file.

1.1.2 Contributors

This Release Contributors

¹<http://postgis.net>

²<http://postgresql.org>

³<http://camptocamp.com>

⁴<http://www.orkney.co.jp>

⁵<http://georepublic.info>

⁶<http://imaptools.com/>

⁷http://wiki.osgeo.org/wiki/OSGeo_Community_Projects

⁸<http://osgeo.org>

⁹<http://live.osgeo.org/>

¹⁰<http://www.gnu.org/licenses/gpl-2.0.html>

¹¹http://www.boost.org/LICENSE_1_0.txt

¹²<http://creativecommons.org/licenses/by-sa/3.0/>

Individuals (in alphabetical order)

Anthony Tasca, Virginia Vergara

And all the people that give us a little of their time making comments, finding issues, making pull requests etc.

Corporate Sponsors (in alphabetical order)

These are corporate entities that have contributed developer time, hosting, or direct monetary funding to the pgRouting project:

- [Georepublic](#)¹³
- [Google Summer of Code](#)¹⁴
- [iMaptools](#)¹⁵
- [Paragon Corporation](#)¹⁶
- [Versaterm Inc.](#)¹⁷

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- [Camptocamp](#)
- [CSIS \(University of Tokyo\)](#)
- [Georepublic](#)
- [Google Summer of Code](#)
- [iMaptools](#)
- [Orkney](#)
- [Paragon Corporation](#)
- [Versaterm Inc.](#)

¹³<https://georepublic.info/en/>

¹⁴<https://developers.google.com/open-source/gsoc/>

¹⁵<http://imaptools.com>

¹⁶<http://www.paragoncorporation.com/>

¹⁷<http://www.versaterm.com/>

1.1.3 More Information

- The latest software, documentation and news items are available at the pgRouting web site <http://pgrouting.org>.
- PostgreSQL database server at the PostgreSQL main site <http://www.postgresql.org>.
- PostGIS extension at the PostGIS project web site <http://postgis.net>.
- Boost C++ source libraries at <http://www.boost.org>.
- Computational Geometry Algorithms Library (CGAL) at <http://www.cgal.org>.
- The Migration guide can be found at <https://github.com/pgRouting/pgrouting/wiki/Migration-Guide>.

1.2 Installation

Table of Contents

- *Short Version*
- *Get the sources*
- *Enabling and upgrading in the database*
- *Dependencies*
- *Configuring*
- *Building*
- *Testing*

Instructions for downloading and installing binaries for different Operative systems instructions and additional notes and corrections not included in this documentation can be found in [Installation wiki](#)¹⁸

To use pgRouting postGIS needs to be installed, please read the information about installation in this [Install Guide](#)¹⁹

1.2.1 Short Version

Extracting the tar ball

```
tar xvfz pgrouting-2.6.0.tar.gz
cd pgrouting-2.6.0
```

To compile assuming you have all the dependencies in your search path:

```
mkdir build
cd build
cmake ..
make
sudo make install
```

Once pgRouting is installed, it needs to be enabled in each individual database you want to use it in.

```
createdb routing
psql routing -c 'CREATE EXTENSION postGIS'
psql routing -c 'CREATE EXTENSION pgRouting'
```

¹⁸<https://github.com/pgRouting/pgrouting/wiki/Notes-on-Download%2C-Installation-and-building-pgRouting>

¹⁹http://www.postgis.us/presentations/postgis_install_guide_22.html

1.2.2 Get the sources

The pgRouting latest release can be found in <https://github.com/pgRouting/pgrouting/releases/latest>

wget

To download this release:

```
wget -O pgrouting-2.6.0.tar.gz https://github.com/pgRouting/pgrouting/archive/v2.6.0.tar.gz
```

Goto *Short Version* to the extract and compile instructions.

git

To download the repository

```
git clone git://github.com/pgRouting/pgrouting.git
cd pgrouting
git checkout v2.6.0
```

Goto *Short Version* to the compile instructions (there is no tar ball).

1.2.3 Enabling and upgrading in the database

Enabling the database

pgRouting is an extension and depends on postGIS. Enabling postGIS before enabling pgRouting in the database

```
CREATE EXTENSION postgis;
CREATE EXTENSION pgrouting;
```

Upgrading the database

To upgrade pgRouting in the database to version 2.6.0 use the following command:

```
ALTER EXTENSION pgrouting UPDATE TO "2.6.0";
```

More information can be found in <https://www.postgresql.org/docs/current/static/sql-createextension.html>

1.2.4 Dependencies

Compilation Dependencies

To be able to compile pgRouting, make sure that the following dependencies are met:

- C and C++ compilers * g++ version >= 4.8
- Postgresql version >= 9.3
- PostGIS version >= 2.2
- The Boost Graph Library (BGL). Version >= 1.53
- CMake >= 3.2
- CGAL >= 4.2

optional dependencies

For user's documentation

- Sphinx >= 1.1
- Latex

For developer's documentation

- Doxygen >= 1.7

For testing

- pgtap
- pg_prove

Example: Installing dependencies on linux

Installing the compilation dependencies

Database dependencies

```
sudo apt-get install
    postgresql-10 \
    postgresql-server-dev-10 \
    postgresql-10-postgis
```

Build dependencies

```
sudo apt-get install
    cmake \
    g++ \
    libboost-graph-dev \
    libcglib-dev
```

Optional dependencies

For documentation and testing

```
sudo apt-get install -y python-sphinx \
    texlive \
    doxygen \
    libtap-parser-sourcehandler-pgtap-perl \
    postgresql-10-pgtap
```

1.2.5 Configuring

pgRouting uses the *cmake* system to do the configuration.

The build directory is different from the source directory

Create the build directory

```
$ mkdir build
```

Configurable variables

To see the variables that can be configured

```
$ cd build
$ cmake -L ..
```

Configuring The Documentation

Most of the effort of the documentation has being on the HTML files. Some variables for the documentation:

Variable	Default	Comment
WITH_DOC	BOOL=OFF	Turn on/off building the documentation
BUILD_HTML	BOOL=ON	If ON, turn on/off building HTML for user's documentation
BUILD_DOXY	BOOL=ON	If ON, turn on/off building HTML for developer's documentation
BUILD_LATEX	BOOL=OFF	If ON, turn on/off building PDF
BUILD_MAN	BOOL=OFF	If ON, turn on/off building MAN pages
DOC_USE_BOOTSTRAP	BOOL=OFF	If ON, use sphinx-bootstrap for HTML pages of the users documentation

Configuring with documentation

```
$ cmake -DWITH_DOC=ON ..
```

Note: Most of the effort of the documentation has being on the html files.

1.2.6 Building

Using make to build the code and the documentation

The following instructions start from *path/to/pgrouting/build*

```
$ make          # build the code but not the documentation
$ make doc      # build only the documentation
$ make all doc  # build both the code and the documentation
```

We have tested on several platforms, For installing or reinstalling all the steps are needed.

Warning: The sql signatures are configured and build in the cmake command.

MinGW on Windows

```
$ mkdir build
$ cd build
$ cmake -G"MSYS Makefiles" ..
$ make
$ make install
```

Linux

The following instructions start from *path/to/pgrouting*

```
mkdir build
cd build
cmake ..
make
sudo make install
```

When the configuration changes:

```
rm -rf build
```

and start the build process as mentioned above.

1.2.7 Testing

Currently there is no `make test` and testing is done as follows

The following instructions start from *path/to/pgrouting/*

```
tools/testers/algorithm-tester.pl
createdb -U <user> __pgr__test__
sh ./tools/testers/pg_prove_tests.sh <user>
dropdb -U <user> __pgr__test__
```

1.2.8 See Also

Indices and tables

- [genindex](#)
- [search](#)

1.3 Support

pgRouting community support is available through the [pgRouting website](#)²⁰, [documentation](#)²¹, tutorials, mailing lists and others. If you're looking for *commercial support*, find below a list of companies providing pgRouting development and consulting services.

1.3.1 Reporting Problems

Bugs are reported and managed in an [issue tracker](#)²². Please follow these steps:

1. Search the tickets to see if your problem has already been reported. If so, add any extra context you might have found, or at least indicate that you too are having the problem. This will help us prioritize common issues.
2. If your problem is unreported, create a [new issue](#)²³ for it.
3. In your report include explicit instructions to replicate your issue. The best tickets include the exact SQL necessary to replicate a problem.
4. If you can test older versions of PostGIS for your problem, please do. On your ticket, note the earliest version the problem appears.

²⁰<http://pgrouting.org/support.html>

²¹<http://docs.pgrouting.org>

²²<https://github.com/pgrouting/pgrouting/issues>

²³<https://github.com/pgRouting/pgrouting/issues/new>

- For the versions where you can replicate the problem, note the operating system and version of pgRouting, PostGIS and PostgreSQL.
- It is recommended to use the following wrapper on the problem to pin point the step that is causing the problem.

```
SET client_min_messages TO debug;  
<your code>  
SET client_min_messages TO notice;
```

1.3.2 Mailing List and GIS StackExchange

There are two mailing lists for pgRouting hosted on OSGeo mailing list server:

- User mailing list: <http://lists.osgeo.org/mailman/listinfo/pgrouting-users>
- Developer mailing list: <http://lists.osgeo.org/mailman/listinfo/pgrouting-dev>

For general questions and topics about how to use pgRouting, please write to the user mailing list.

You can also ask at [GIS StackExchange](#)²⁴ and tag the question with `pgrouting`. Find all questions tagged with `pgrouting` under <http://gis.stackexchange.com/questions/tagged/pgrouting> or subscribe to the [pgRouting questions feed](#)²⁵.

1.3.3 Commercial Support

For users who require professional support, development and consulting services, consider contacting any of the following organizations, which have significantly contributed to the development of pgRouting:

Company	Offices in	Website
Georepublic	Germany, Japan	https://georepublic.info
iMaptools	United States	http://imaptools.com
Paragon Corporation	United States	http://www.paragoncorporation.com
Camptocamp	Switzerland, France	http://www.camptocamp.com

- [Sample Data](#) that is used in the examples of this manual.

1.4 Sample Data

The documentation provides very simple example queries based on a small sample network. To be able to execute the sample queries, run the following SQL commands to create a table with a small network data set.

Create table

```
CREATE TABLE edge_table (  
  id BIGSERIAL,  
  dir character varying,  
  source BIGINT,  
  target BIGINT,  
  cost FLOAT,  
  reverse_cost FLOAT,  
  capacity BIGINT,  
  reverse_capacity BIGINT,  
  category_id INTEGER,  
  reverse_category_id INTEGER,  
  x1 FLOAT,
```

²⁴<http://gis.stackexchange.com/>

²⁵<http://gis.stackexchange.com/feeds/tag?tagnames=pgrouting&sort=newest>

```

y1 FLOAT,
x2 FLOAT,
y2 FLOAT,
the_geom geometry
);

```

Insert data

```

INSERT INTO edge_table (
    category_id, reverse_category_id,
    cost, reverse_cost,
    capacity, reverse_capacity,
    x1, y1,
    x2, y2) VALUES
(3, 1, 1, 1, 80, 130, 2, 0, 2, 1),
(3, 2, -1, 1, -1, 100, 2, 1, 3, 1),
(2, 1, -1, 1, -1, 130, 3, 1, 4, 1),
(2, 4, 1, 1, 100, 50, 2, 1, 2, 2),
(1, 4, 1, -1, 130, -1, 3, 1, 3, 2),
(4, 2, 1, 1, 50, 100, 0, 2, 1, 2),
(4, 1, 1, 1, 50, 130, 1, 2, 2, 2),
(2, 1, 1, 1, 100, 130, 2, 2, 3, 2),
(1, 3, 1, 1, 130, 80, 3, 2, 4, 2),
(1, 4, 1, 1, 130, 50, 2, 2, 2, 3),
(1, 2, 1, -1, 130, -1, 3, 2, 3, 3),
(2, 3, 1, -1, 100, -1, 2, 3, 3, 3),
(2, 4, 1, -1, 100, -1, 3, 3, 4, 3),
(3, 1, 1, 1, 80, 130, 2, 3, 2, 4),
(3, 4, 1, 1, 80, 50, 4, 2, 4, 3),
(3, 3, 1, 1, 80, 80, 4, 1, 4, 2),
(1, 2, 1, 1, 130, 100, 0.5, 3.5, 1.9999999999999999, 3.5),
(4, 1, 1, 1, 50, 130, 3.5, 2.3, 3.5, 4);

UPDATE edge_table SET the_geom = st_makeline(st_point(x1,y1),st_point(x2,y2)),
dir = CASE WHEN (cost>0 AND reverse_cost>0) THEN 'B' -- both ways
           WHEN (cost>0 AND reverse_cost<0) THEN 'FT' -- direction of the LINESTRING
           WHEN (cost<0 AND reverse_cost>0) THEN 'TF' -- reverse direction of the LINESTRING
           ELSE '' END;

```

Topology

- Before you test a routing function use this query to create a topology (fills the source and target columns).

```
SELECT pgr_createTopology('edge_table',0.001);
```

Points of interest

- When points outside of the graph.
- Used with the *withPoints - Family of functions* functions.

```

CREATE TABLE pointsOfInterest (
    pid BIGSERIAL,
    x FLOAT,
    y FLOAT,
    edge_id BIGINT,

```

```
side CHAR,
fraction FLOAT,
the_geom geometry,
newPoint geometry
);

INSERT INTO pointsOfInterest (x, y, edge_id, side, fraction) VALUES
(1.8, 0.4, 1, 'l', 0.4),
(4.2, 2.4, 15, 'r', 0.4),
(2.6, 3.2, 12, 'l', 0.6),
(0.3, 1.8, 6, 'r', 0.3),
(2.9, 1.8, 5, 'l', 0.8),
(2.2, 1.7, 4, 'b', 0.7);
UPDATE pointsOfInterest SET the_geom = st_makePoint(x,y);

UPDATE pointsOfInterest
SET newPoint = ST_LineInterpolatePoint(e.the_geom, fraction)
FROM edge_table AS e WHERE edge_id = id;
```

Restrictions

- Used with the *pgr_trsp - Turn Restriction Shortest Path (TRSP)* functions.

```
CREATE TABLE restrictions (
    rid BIGINT NOT NULL,
    to_cost FLOAT,
    target_id BIGINT,
    from_edge BIGINT,
    via_path TEXT
);

INSERT INTO restrictions (rid, to_cost, target_id, from_edge, via_path) VALUES
(1, 100, 7, 4, NULL),
(1, 100, 11, 8, NULL),
(1, 100, 10, 7, NULL),
(2, 4, 8, 3, 5),
(3, 100, 9, 16, NULL);
```

Categories

- Used with the *Flow - Family of functions* functions.

```
/*
CREATE TABLE categories (
    category_id INTEGER,
    category text,
    capacity BIGINT
);

INSERT INTO categories VALUES
(1, 'Category 1', 130),
(2, 'Category 2', 100),
(3, 'Category 3', 80),
(4, 'Category 4', 50);
*/
```


Vertex table

- Used in some deprecated signatures or deprecated functions.

```
-- TODO check if this table is still used
CREATE TABLE vertex_table (
    id SERIAL,
    x FLOAT,
    y FLOAT
);
INSERT INTO vertex_table VALUES
(1,2,0), (2,2,1), (3,3,1), (4,4,1), (5,0,2), (6,1,2), (7,2,2),
(8,3,2), (9,4,2), (10,2,3), (11,3,3), (12,4,3), (13,2,4);
```

1.4.1 Images

- Red arrows correspond when `cost > 0` in the edge table.
- Blue arrows correspond when `reverse_cost > 0` in the edge table.
- Points are outside the graph.
- Click on the graph to enlarge.

Network for queries marked as directed and cost and reverse_cost columns are used

When working with city networks, this is recommended for point of view of vehicles.

Network for queries marked as undirected and cost and reverse_cost columns are used

When working with city networks, this is recommended for point of view of pedestrians.

Network for queries marked as directed and only cost column is used

Network for queries marked as undirected and only cost column is used

Pick & Deliver Data

```
DROP TABLE IF EXISTS customer CASCADE;
CREATE TABLE customer (
    id BIGINT not null primary key,
    x DOUBLE PRECISION,
    y DOUBLE PRECISION,
    demand INTEGER,
    opentime INTEGER,
    closetime INTEGER,
    servicetime INTEGER,
    pindex BIGINT,
    dindex BIGINT
);

INSERT INTO customer(
    id,      x,      y, demand, opentime, closetime, servicetime, pindex, dindex) VALUES
( 0,    40,    50,    0,    0,  1236,    0,    0,    0),
( 1,    45,    68,   -10,   912,   967,    90,   11,    0),
( 2,    45,    70,   -20,   825,   870,    90,    6,    0),
```

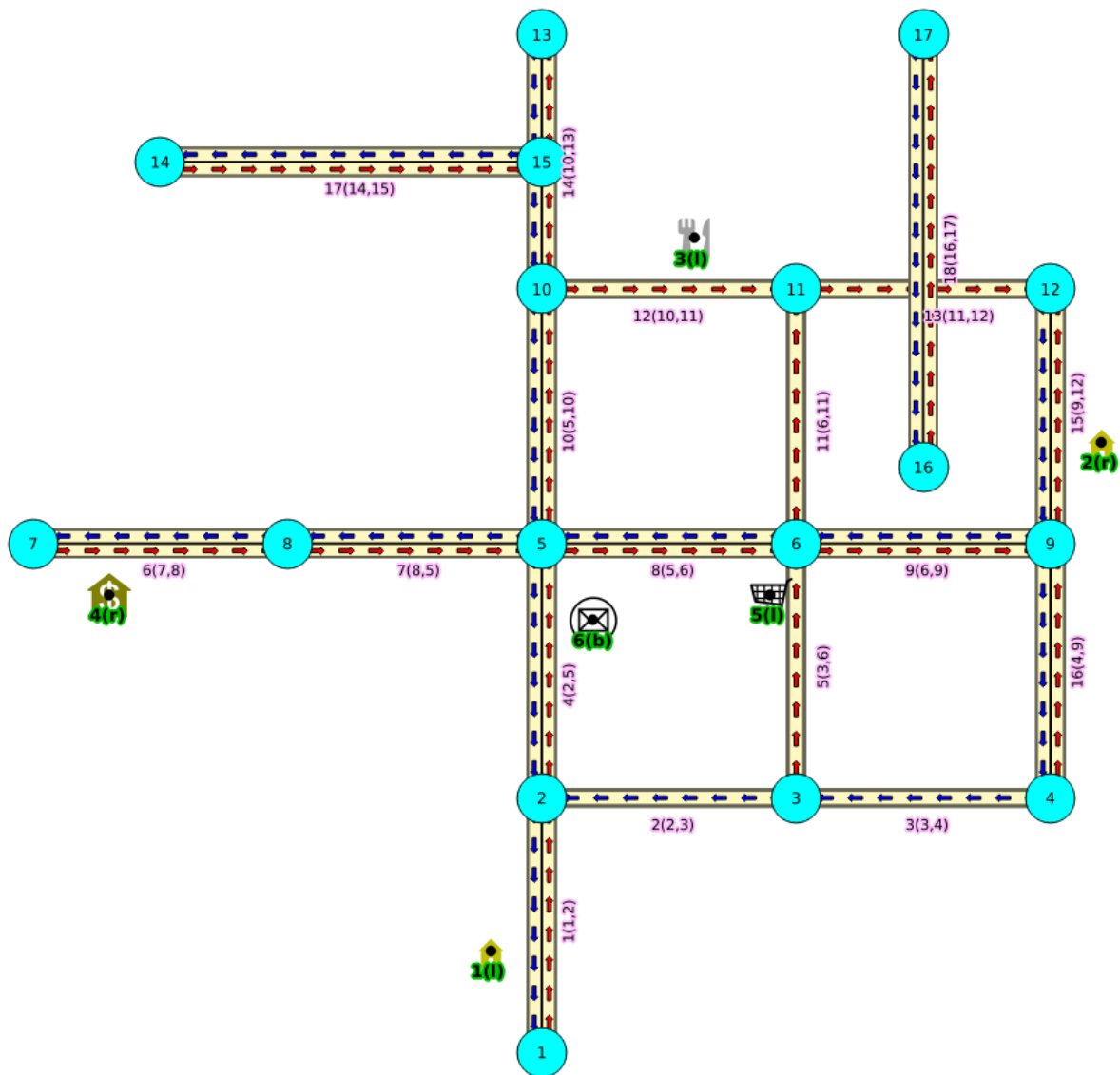


Fig. 1.1: Graph 1: Directed, with cost and reverse cost

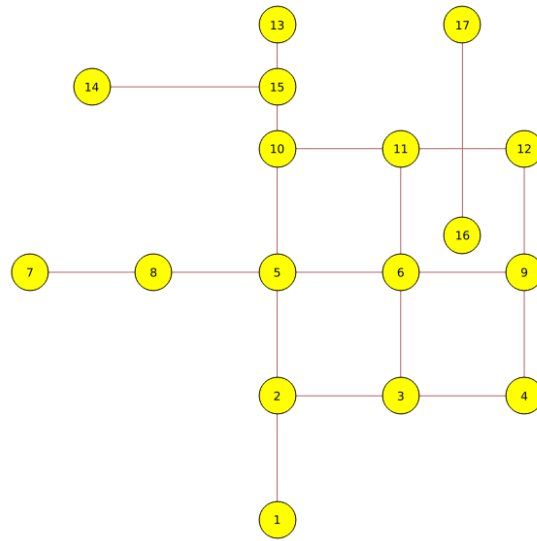


Fig. 1.2: **Graph 2: Undirected, with cost and reverse cost**

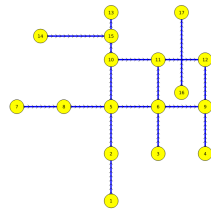


Fig. 1.3: **Graph 3: Directed, with cost**

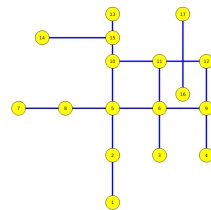


Fig. 1.4: **Graph 4: Undirected, with cost**

```

( 3, 42, 66, 10, 65, 146, 90, 0, 75),
( 4, 42, 68, -10, 727, 782, 90, 9, 0),
( 5, 42, 65, 10, 15, 67, 90, 0, 7),
( 6, 40, 69, 20, 621, 702, 90, 0, 2),
( 7, 40, 66, -10, 170, 225, 90, 5, 0),
( 8, 38, 68, 20, 255, 324, 90, 0, 10),
( 9, 38, 70, 10, 534, 605, 90, 0, 4),
(10, 35, 66, -20, 357, 410, 90, 8, 0),
(11, 35, 69, 10, 448, 505, 90, 0, 1),
(12, 25, 85, -20, 652, 721, 90, 18, 0),
(13, 22, 75, 30, 30, 92, 90, 0, 17),
(14, 22, 85, -40, 567, 620, 90, 16, 0),
(15, 20, 80, -10, 384, 429, 90, 19, 0),
(16, 20, 85, 40, 475, 528, 90, 0, 14),
(17, 18, 75, -30, 99, 148, 90, 13, 0),
(18, 15, 75, 20, 179, 254, 90, 0, 12),
(19, 15, 80, 10, 278, 345, 90, 0, 15),
(20, 30, 50, 10, 10, 73, 90, 0, 24),
(21, 30, 52, -10, 914, 965, 90, 30, 0),
(22, 28, 52, -20, 812, 883, 90, 28, 0),
(23, 28, 55, 10, 732, 777, 0, 0, 103),
(24, 25, 50, -10, 65, 144, 90, 20, 0),
(25, 25, 52, 40, 169, 224, 90, 0, 27),
(26, 25, 55, -10, 622, 701, 90, 29, 0),
(27, 23, 52, -40, 261, 316, 90, 25, 0),
(28, 23, 55, 20, 546, 593, 90, 0, 22),
(29, 20, 50, 10, 358, 405, 90, 0, 26),
(30, 20, 55, 10, 449, 504, 90, 0, 21),
(31, 10, 35, -30, 200, 237, 90, 32, 0),
(32, 10, 40, 30, 31, 100, 90, 0, 31),
(33, 8, 40, 40, 87, 158, 90, 0, 37),
(34, 8, 45, -30, 751, 816, 90, 38, 0),
(35, 5, 35, 10, 283, 344, 90, 0, 39),
(36, 5, 45, 10, 665, 716, 0, 0, 105),
(37, 2, 40, -40, 383, 434, 90, 33, 0),
(38, 0, 40, 30, 479, 522, 90, 0, 34),
(39, 0, 45, -10, 567, 624, 90, 35, 0),
(40, 35, 30, -20, 264, 321, 90, 42, 0),
(41, 35, 32, -10, 166, 235, 90, 43, 0),
(42, 33, 32, 20, 68, 149, 90, 0, 40),
(43, 33, 35, 10, 16, 80, 90, 0, 41),
(44, 32, 30, 10, 359, 412, 90, 0, 46),
(45, 30, 30, 10, 541, 600, 90, 0, 48),
(46, 30, 32, -10, 448, 509, 90, 44, 0),
(47, 30, 35, -10, 1054, 1127, 90, 49, 0),
(48, 28, 30, -10, 632, 693, 90, 45, 0),
(49, 28, 35, 10, 1001, 1066, 90, 0, 47),
(50, 26, 32, 10, 815, 880, 90, 0, 52),
(51, 25, 30, 10, 725, 786, 0, 0, 101),
(52, 25, 35, -10, 912, 969, 90, 50, 0),
(53, 44, 5, 20, 286, 347, 90, 0, 58),
(54, 42, 10, 40, 186, 257, 90, 0, 60),
(55, 42, 15, -40, 95, 158, 90, 57, 0),
(56, 40, 5, 30, 385, 436, 90, 0, 59),
(57, 40, 15, 40, 35, 87, 90, 0, 55),
(58, 38, 5, -20, 471, 534, 90, 53, 0),
(59, 38, 15, -30, 651, 740, 90, 56, 0),
(60, 35, 5, -40, 562, 629, 90, 54, 0),
(61, 50, 30, -10, 531, 610, 90, 67, 0),
(62, 50, 35, 20, 262, 317, 90, 0, 68),
(63, 50, 40, 50, 171, 218, 90, 0, 74),
(64, 48, 30, 10, 632, 693, 0, 0, 102),
(65, 48, 40, 10, 76, 129, 90, 0, 72),

```

```

( 66, 47, 35, 10, 826, 875, 90, 0, 69),
( 67, 47, 40, 10, 12, 77, 90, 0, 61),
( 68, 45, 30, -20, 734, 777, 90, 62, 0),
( 69, 45, 35, -10, 916, 969, 90, 66, 0),
( 70, 95, 30, -30, 387, 456, 90, 81, 0),
( 71, 95, 35, 20, 293, 360, 90, 0, 77),
( 72, 53, 30, -10, 450, 505, 90, 65, 0),
( 73, 92, 30, -10, 478, 551, 90, 76, 0),
( 74, 53, 35, -50, 353, 412, 90, 63, 0),
( 75, 45, 65, -10, 997, 1068, 90, 3, 0),
( 76, 90, 35, 10, 203, 260, 90, 0, 73),
( 77, 88, 30, -20, 574, 643, 90, 71, 0),
( 78, 88, 35, 20, 109, 170, 0, 0, 104),
( 79, 87, 30, 10, 668, 731, 90, 0, 80),
( 80, 85, 25, -10, 769, 820, 90, 79, 0),
( 81, 85, 35, 30, 47, 124, 90, 0, 70),
( 82, 75, 55, 20, 369, 420, 90, 0, 85),
( 83, 72, 55, -20, 265, 338, 90, 87, 0),
( 84, 70, 58, 20, 458, 523, 90, 0, 89),
( 85, 68, 60, -20, 555, 612, 90, 82, 0),
( 86, 66, 55, 10, 173, 238, 90, 0, 91),
( 87, 65, 55, 20, 85, 144, 90, 0, 83),
( 88, 65, 60, -10, 645, 708, 90, 90, 0),
( 89, 63, 58, -20, 737, 802, 90, 84, 0),
( 90, 60, 55, 10, 20, 84, 90, 0, 88),
( 91, 60, 60, -10, 836, 889, 90, 86, 0),
( 92, 67, 85, 20, 368, 441, 90, 0, 93),
( 93, 65, 85, -20, 475, 518, 90, 92, 0),
( 94, 65, 82, -10, 285, 336, 90, 96, 0),
( 95, 62, 80, -20, 196, 239, 90, 98, 0),
( 96, 60, 80, 10, 95, 156, 90, 0, 94),
( 97, 60, 85, 30, 561, 622, 0, 0, 106),
( 98, 58, 75, 20, 30, 84, 90, 0, 95),
( 99, 55, 80, -20, 743, 820, 90, 100, 0),
( 100, 55, 85, 20, 647, 726, 90, 0, 99),
( 101, 25, 30, -10, 725, 786, 90, 51, 0),
( 102, 48, 30, -10, 632, 693, 90, 64, 0),
( 103, 28, 55, -10, 732, 777, 90, 23, 0),
( 104, 88, 35, -20, 109, 170, 90, 78, 0),
( 105, 5, 45, -10, 665, 716, 90, 36, 0),
( 106, 60, 85, -30, 561, 622, 90, 97, 0);

```

Pgrouting Concepts

2.1 pgRouting Concepts

Contents

- *pgRouting Concepts*
 - *Getting Started*
 - * *Create a routing Database*
 - * *Load Data*
 - * *Build a Routing Topology*
 - * *Check the Routing Topology*
 - * *Compute a Path*
 - *Inner Queries*
 - * *Description of the edges_sql query for dijkstra like functions*
 - * *Description of the edges_sql query (id is not necessary)*
 - * *Description of the parameters of the signatures*
 - * *Description of the edges_sql query for astar like functions*
 - * *Description of the edges_sql query for Max-flow like functions*
 - * *Description of the Points SQL query*
 - *Return columns & values*
 - * *Description of the return values for a path*
 - * *Description of the return values for a Cost function*
 - * *Description of the Return Values*
 - *Advanced Topics*
 - * *Routing Topology*
 - * *Graph Analytics*
 - * *Analyze a Graph*
 - * *Analyze One Way Streets*
 - *Example*
 - *Performance Tips*
 - * *For the Routing functions*
 - * *For the topology functions:*
 - *How to contribute*

2.1.1 Getting Started

This is a simple guide to walk you through the steps of getting started with pgRouting. In this guide we will cover:

- *Create a routing Database*
- *Load Data*
- *Build a Routing Topology*
- *Check the Routing Topology*
- *Compute a Path*

Create a routing Database

The first thing we need to do is create a database and load pgrouting in the database. Typically you will create a database for each project. Once you have a database to work in, you can load your data and build your application in that database. This makes it easy to move your project later if you want to to say a production server.

For Postgresql 9.2 and later versions

```
createdb mydatabase
psql mydatabase -c "create extension postgis"
psql mydatabase -c "create extension pgrouting"
```

Load Data

How you load your data will depend in what form it comes in. There are various OpenSource tools that can help you, like:

osm2pgrouting

- this is a tool for loading OSM data into postgresql with pgRouting requirements

shp2pgsql

- this is the postgresql shapefile loader

ogr2ogr

- this is a vector data conversion utility

osm2pgsql

- this is a tool for loading OSM data into postgresql

So these tools and probably others will allow you to read vector data so that you may then load that data into your database as a table of some kind. At this point you need to know a little about your data structure and content. One easy way to browse your new data table is with pgAdmin3 or phpPgAdmin.

Build a Routing Topology

Next we need to build a topology for our street data. What this means is that for any given edge in your street data the ends of that edge will be connected to a unique node and to other edges that are also connected to that same unique node. Once all the edges are connected to nodes we have a graph that can be used for routing with pgrouting. We provide a tool that will help with this:

Note: this step is not needed if data is loaded with *osm2pgrouting*

```
select pgr_createTopology('myroads', 0.000001);
```

- *pgr_createTopology*

Check the Routing Topology

There are lots of possible sources for errors in a graph. The data that you started with may not have been designed with routing in mind. A graph has some very specific requirements. One is that it is *NODED*, this means that except for some very specific use cases, each road segment starts and ends at a node and that in general it does not cross another road segment that it should be connected to.

There can be other errors like the direction of a one-way street being entered in the wrong direction. We do not have tools to search for all possible errors but we have some basic tools that might help.

```
select pgr_analyzeGraph('myroads', 0.000001);
select pgr_analyzeOneway('myroads', s_in_rules, s_out_rules,
                             t_in_rules, t_out_rules,
                             direction)
select pgr_nodeNetwork('myroads', 0.001);
```

- *pgr_analyzeGraph*
- *pgr_analyzeOneway*
- *pgr_nodeNetwork*

Compute a Path

Once you have all the preparation work done above, computing a route is fairly easy. We have a lot of different algorithms that can work with your prepared road network. The general form of a route query is:

```
select pgr_dijkstra(`SELECT * FROM myroads`, 1, 2)
```

As you can see this is fairly straight forward and you can look at the specific algorithms for the details of the signatures and how to use them. These results have information like edge id and/or the node id along with the cost or geometry for the step in the path from *start* to *end*. Using the ids you can join these results back to your edge table to get more information about each step in the path.

- *pgr_dijkstra*

2.1.2 Inner Queries

- *Description of the edges_sql query for dijkstra like functions*
- *Description of the edges_sql query (id is not necessary)*
- *Description of the parameters of the signatures*
- *Description of the edges_sql query for astar like functions*
- *Description of the edges_sql query for Max-flow like functions*
- *Description of the Points SQL query*

There are several kinds of valid inner queries and also the columns returned are depending on the function. Which kind of inner query will depend on the function(s) requirements. To simplify variety of types, ANY-INTEGER and ANY-NUMERICAL is used.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none">• When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none">• When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the `edges_sql` query (id is not necessary)

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none">• When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none">• When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Default	Description
edges_sql	TEXT		SQL query as described above.
via_vertices	ARRAY [ANY-INTEGER]		Array of ordered vertices identifiers that are going to be visited.
directed	BOOLEAN	true	<ul style="list-style-type: none"> When <code>true</code> Graph is considered <i>Directed</i> When <code>false</code> the graph is considered as Undirected.
strict	BOOLEAN	false	<ul style="list-style-type: none"> When <code>false</code> ignores missing paths returning all paths found When <code>true</code> if a path is missing stops and returns <i>EMPTY SET</i>
U_turn_on_edge	BOOLEAN	true	<ul style="list-style-type: none"> When <code>true</code> departing from a visited vertex will not try to avoid using the edge used to reach it. In other words, U turn using the edge with same <i>id</i> is allowed. When <code>false</code> when a departing from a visited vertex tries to avoid using the edge used to reach it. In other words, U turn using the edge with same <i>id</i> is used when no other path is found.

Description of the edges_sql query for astar like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source</i> , <i>target</i>) <ul style="list-style-type: none">• When negative: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target</i> , <i>source</i>), <ul style="list-style-type: none">• When negative: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.
x1	ANY-NUMERICAL		X coordinate of <i>source</i> vertex.
y1	ANY-NUMERICAL		Y coordinate of <i>source</i> vertex.
x2	ANY-NUMERICAL		X coordinate of <i>target</i> vertex.
y2	ANY-NUMERICAL		Y coordinate of <i>target</i> vertex.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the `edges_sql` query for Max-flow like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
capacity	ANY-INTEGER		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_capacity	ANY-INTEGER	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

Description of the Points SQL query

points_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Description
pid	ANY-INTEGER	(optional) Identifier of the point. <ul style="list-style-type: none"> If column present, it can not be NULL. If column not present, a sequential identifier will be given automatically.
edge_id	ANY-INTEGER	Identifier of the “closest” edge to the point.
fraction	ANY-NUMERICAL	Value in <0,1> that indicates the relative position from the first end point of the edge.
side	CHAR	(optional) Value in ['b', 'r', 'l', NULL] indicating if the point is: <ul style="list-style-type: none"> In the right, left of the edge or If it doesn't matter with 'b' or NULL. If column not present 'b' is considered.

Where:

ANY-INTEGER smallint, int, bigint

ANY-NUMERICAL smallint, int, bigint, real, float

2.1.3 Return columns & values

- *Description of the return values for a path*
- *Description of the return values for a Cost function*
- *Description of the Return Values*

There are several kinds of columns returned are depending of the function.

Description of the return values for a path

Returns set of (seq, path_seq [, start_vid] [, end_vid], node, edge, cost, agg_cost)

Column	Type	Description
seq	INT	Sequential value starting from 1 .
path_id	INT	Path identifier. Has value 1 for the first of a path. Used when there are multiple paths for the same start_vid to end_vid combination.
path_seq	INT	Relative position in the path. Has value 1 for the beginning of a path.
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
node	BIGINT	Identifier of the node in the path from start_vid to end_vid.
edge	BIGINT	Identifier of the edge used to go from node to the next node in the path sequence. -1 for the last node of the path.
cost	FLOAT	Cost to traverse from node using edge to the next node in the path sequence.
agg_cost	FLOAT	Aggregate cost from start_v to node.

Description of the return values for a Cost function

Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
agg_cost	FLOAT	Aggregate cost from start_vid to end_vid.

Description of the Return Values

Column	Type	Description
seq	INT	Sequential value starting from 1 .
edge_id	BIGINT	Identifier of the edge in the original query(edges_sql).
source	BIGINT	Identifier of the first end point vertex of the edge.
target	BIGINT	Identifier of the second end point vertex of the edge.
flow	BIGINT	Flow through the edge in the direction (source, target).
residual_capacity	BIGINT	Residual capacity of the edge in the direction (source, target).

2.1.4 Advanced Topics

- *Routing Topology*
- *Graph Analytics*
- *Analyze a Graph*
- *Analyze One Way Streets*
 - *Example*

Routing Topology

Overview

Typically when GIS files are loaded into the data database for use with pgRouting they do not have topology information associated with them. To create a useful topology the data needs to be “noded”. This means that where two or more roads form an intersection there it needs to be a node at the intersection and all the road segments need to be broken at the intersection, assuming that you can navigate from any of these segments to any other segment via that intersection.

You can use the *graph analysis functions* to help you see where you might have topology problems in your data. If you need to node your data, we also have a function `pgr_nodeNetwork()` that might work for you. This function splits ALL crossing segments and nodes them. There are some cases where this might NOT be the right thing to do.

For example, when you have an overpass and underpass intersection, you do not want these noded, but `pgr_nodeNetwork` does not know that is the case and will node them which is not good because then the router will be able to turn off the overpass onto the underpass like it was a flat 2D intersection. To deal with this problem some data sets use z-levels at these types of intersections and other data might not node these intersection which would be ok.

For those cases where topology needs to be added the following functions may be useful. One way to prep the data for pgRouting is to add the following columns to your table and then populate them as appropriate. This example makes a lot of assumption like that you original data tables already has certain columns in it like `one_way`, `fcc`, and possibly others and that they contain specific data values. This is only to give you an idea of what you can do with your data.

```
ALTER TABLE edge_table
  ADD COLUMN source integer,
  ADD COLUMN target integer,
  ADD COLUMN cost_len double precision,
  ADD COLUMN cost_time double precision,
  ADD COLUMN rcost_len double precision,
  ADD COLUMN rcost_time double precision,
  ADD COLUMN x1 double precision,
  ADD COLUMN y1 double precision,
  ADD COLUMN x2 double precision,
  ADD COLUMN y2 double precision,
  ADD COLUMN to_cost double precision,
  ADD COLUMN rule text,
  ADD COLUMN isolated integer;

SELECT pgr_createTopology('edge_table', 0.000001, 'the_geom', 'id');
```

The function `pgr_createTopology()` will create the `vertices_tmp` table and populate the `source` and `target` columns. The following example populated the remaining columns. In this example, the `fcc` column contains feature class code and the CASE statements converts it to an average speed.

```
UPDATE edge_table SET x1 = st_x(st_startpoint(the_geom)),
  y1 = st_y(st_startpoint(the_geom)),
  x2 = st_x(st_endpoint(the_geom)),
  y2 = st_y(st_endpoint(the_geom)),
  cost_len = st_length_spheroid(the_geom, 'SPHEROID["WGS84",6378137,298.25728]');
```

```
rcost_len = st_length_spheroid(the_geom, 'SPHEROID["WGS84",6378137,298.25728]'),
len_km = st_length_spheroid(the_geom, 'SPHEROID["WGS84",6378137,298.25728]')/1000.0,
len_miles = st_length_spheroid(the_geom, 'SPHEROID["WGS84",6378137,298.25728]')
            / 1000.0 * 0.6213712,
speed_mph = CASE WHEN fcc='A10' THEN 65
                 WHEN fcc='A15' THEN 65
                 WHEN fcc='A20' THEN 55
                 WHEN fcc='A25' THEN 55
                 WHEN fcc='A30' THEN 45
                 WHEN fcc='A35' THEN 45
                 WHEN fcc='A40' THEN 35
                 WHEN fcc='A45' THEN 35
                 WHEN fcc='A50' THEN 25
                 WHEN fcc='A60' THEN 25
                 WHEN fcc='A61' THEN 25
                 WHEN fcc='A62' THEN 25
                 WHEN fcc='A64' THEN 25
                 WHEN fcc='A70' THEN 15
                 WHEN fcc='A69' THEN 10
                 ELSE null END,
speed_kmh = CASE WHEN fcc='A10' THEN 104
                 WHEN fcc='A15' THEN 104
                 WHEN fcc='A20' THEN 88
                 WHEN fcc='A25' THEN 88
                 WHEN fcc='A30' THEN 72
                 WHEN fcc='A35' THEN 72
                 WHEN fcc='A40' THEN 56
                 WHEN fcc='A45' THEN 56
                 WHEN fcc='A50' THEN 40
                 WHEN fcc='A60' THEN 50
                 WHEN fcc='A61' THEN 40
                 WHEN fcc='A62' THEN 40
                 WHEN fcc='A64' THEN 40
                 WHEN fcc='A70' THEN 25
                 WHEN fcc='A69' THEN 15
                 ELSE null END;

-- UPDATE the cost information based on oneway streets

UPDATE edge_table SET
    cost_time = CASE
        WHEN one_way='TF' THEN 10000.0
        ELSE cost_len/1000.0/speed_kmh::numeric*3600.0
    END,
    rcost_time = CASE
        WHEN one_way='FT' THEN 10000.0
        ELSE cost_len/1000.0/speed_kmh::numeric*3600.0
    END;

-- clean up the database because we have updated a lot of records

VACUUM ANALYZE VERBOSE edge_table;
```

Now your database should be ready to use any (most?) of the pgRouting algorithms.

Graph Analytics

Overview

It is common to find problems with graphs that have not been constructed fully noded or in graphs with z-levels at intersection that have been entered incorrectly. An other problem is one way streets that have been entered in the

wrong direction. We can not detect errors with respect to “ground” truth, but we can look for inconsistencies and some anomalies in a graph and report them for additional inspections.

We do not current have any visualization tools for these problems, but I have used mapserver to render the graph and highlight potential problem areas. Someone familiar with graphviz might contribute tools for generating images with that.

Analyze a Graph

With *pgr_analyzeGraph* the graph can be checked for errors. For example for table “mytab” that has “mytab_vertices_pgr” as the vertices table:

```
SELECT pgr_analyzeGraph('mytab', 0.000002);
NOTICE: Performing checks, pelase wait...
NOTICE: Analyzing for dead ends. Please wait...
NOTICE: Analyzing for gaps. Please wait...
NOTICE: Analyzing for isolated edges. Please wait...
NOTICE: Analyzing for ring geometries. Please wait...
NOTICE: Analyzing for intersections. Please wait...
NOTICE: ANALYSIS RESULTS FOR SELECTED EDGES:
NOTICE: Isolated segments: 158
NOTICE: Dead ends: 20028
NOTICE: Potential gaps found near dead ends: 527
NOTICE: Intersections detected: 2560
NOTICE: Ring geometries: 0
pgr_analyzeGraph
-----
      OK
(1 row)
```

In the vertices table “mytab_vertices_pgr”:

- Deadends are identified by cnt=1
- Potencial gap problems are identified with chk=1.

```
SELECT count(*) as deadends FROM mytab_vertices_pgr WHERE cnt = 1;
deadends
-----
    20028
(1 row)

SELECT count(*) as gaps FROM mytab_vertices_pgr WHERE chk = 1;
gaps
-----
    527
(1 row)
```

For isolated road segments, for example, a segment where both ends are deadends. you can find these with the following query:

```
SELECT *
FROM mytab a, mytab_vertices_pgr b, mytab_vertices_pgr c
WHERE a.source=b.id AND b.cnt=1 AND a.target=c.id AND c.cnt=1;
```

If you want to visualize these on a graphic image, then you can use something like mapserver to render the edges and the vertices and style based on cnt or if they are isolated, etc. You can also do this with a tool like graphviz, or geoserver or other similar tools.

Analyze One Way Streets

pgr_analyzeOneway analyzes one way streets in a graph and identifies any flipped segments. Basically if you count the edges coming into a node and the edges exiting a node the number has to be greater than one.

This query will add two columns to the `vertices_tmp` table `ein int` and `eout int` and populate it with the appropriate counts. After running this on a graph you can identify nodes with potential problems with the following query.

The rules are defined as an array of text strings that if match the `col` value would be counted as true for the source or target in or out condition.

Example

Lets assume we have a table “st” of edges and a column “one_way” that might have values like:

- ‘FT’ - oneway from the source to the target node.
- ‘TF’ - oneway from the target to the source node.
- ‘B’ - two way street.
- ‘’ - empty field, assume twoway.
- <NULL> - NULL field, use `two_way_if_null` flag.

Then we could form the following query to analyze the oneway streets for errors.

```
SELECT pgr_analyzeOneway('mytab',
    ARRAY['', 'B', 'TF'],
    ARRAY['', 'B', 'FT'],
    ARRAY['', 'B', 'FT'],
    ARRAY['', 'B', 'TF'],
);

-- now we can see the problem nodes
SELECT * FROM mytab_vertices_pgr WHERE ein=0 OR eout=0;

-- and the problem edges connected to those nodes
SELECT gid FROM mytab a, mytab_vertices_pgr b WHERE a.source=b.id AND ein=0 OR eout=0
UNION
SELECT gid FROM mytab a, mytab_vertices_pgr b WHERE a.target=b.id AND ein=0 OR eout=0;
```

Typically these problems are generated by a break in the network, the one way direction set wrong, maybe an error related to z-levels or a network that is not properly noded.

The above tools do not detect all network issues, but they will identify some common problems. There are other problems that are hard to detect because they are more global in nature like multiple disconnected networks. Think of an island with a road network that is not connected to the mainland network because the bridge or ferry routes are missing.

2.1.5 Performance Tips

- *For the Routing functions*
- *For the topology functions:*

For the Routing functions

To get faster results bound your queries to the area of interest of routing to have, for example, no more than one million rows.

Use an inner query SQL that does not include some edges in the routing function

```
SELECT id, source, target from edge_table WHERE
    id < 17 and
    the_geom && (select st_buffer(the_geom,1) as myarea FROM edge_table where id = 5)
```

Integrating the inner query to the pgRouting function:

```
SELECT * FROM pgr_dijkstra(
    'SELECT id, source, target from edge_table WHERE
        id < 17 and
        the_geom && (select st_buffer(the_geom,1) as myarea FROM edge_table where id = 5)',
    1, 2)
```

For the topology functions:

When “you know” that you are going to remove a set of edges from the edges table, and without those edges you are going to use a routing function you can do the following:

Analyze the new topology based on the actual topology:

```
pgr_analyzegraph('edge_table', rows_where:='id < 17');
```

Or create a new topology if the change is permanent:

```
pgr_createTopology('edge_table', rows_where:='id < 17');
pgr_analyzegraph('edge_table', rows_where:='id < 17');
```

2.1.6 How to contribute

Wiki

- Edit an existing [pgRouting Wiki](#)¹ page.
- Or create a new Wiki page
 - Create a page on the [pgRouting Wiki](#)²
 - Give the title an appropriate name
- [Example](#)³

Adding Functionaity to pgRouting

Consult the [developer's documentation](#)⁴

Indices and tables

- [genindex](#)
- [search](#)

Reference

pgr_version - to get pgRouting's version information.

¹<https://github.com/pgRouting/pgrouting/wiki>

²<https://github.com/pgRouting/pgrouting/wiki>

³[https://github.com/pgRouting/pgrouting/wiki/How-to:-Handle-parallel-edges-\(KSP\)](https://github.com/pgRouting/pgrouting/wiki/How-to:-Handle-parallel-edges-(KSP))

⁴<http://docs.pgrouting.org/doxy/2.4/index.html>

2.2 pgr_version

2.2.1 Name

`pgr_version` — Query for pgRouting version information.

2.2.2 Synopsis

Returns a table with pgRouting version information.

```
table() pgr_version();
```

2.2.3 Description

Returns a table with:

Column	Type	Description
version	varchar	pgRouting version
tag	varchar	Git tag of pgRouting build
hash	varchar	Git hash of pgRouting build
branch	varchar	Git branch of pgRouting build
boost	varchar	Boost version

History

- New in version 2.0.0

2.2.4 Examples

- Query for the version string

```
SELECT version FROM pgr_version();
 version
-----
 2.6.0
(1 row)
```

2.2.5 See Also

Indices and tables

- genindex
- search

Data Types

- *pgr_costResult[]* - A set of records to describe a path result with cost attribute.
- *pgr_costResult3[]* - A set of records to describe a path result with cost attribute.
- *pgr_geomResult* - A set of records to describe a path result with geometry attribute.

3.1 pgRouting Data Types

The following are commonly used data types for some of the pgRouting functions.

- *pgr_costResult[]* - A set of records to describe a path result with cost attribute.
- *pgr_costResult3[]* - A set of records to describe a path result with cost attribute.
- *pgr_geomResult* - A set of records to describe a path result with geometry attribute.

3.1.1 pgr_costResult[]

Name

`pgr_costResult[]` — A set of records to describe a path result with cost attribute.

Description

```
CREATE TYPE pgr_costResult AS
(
    seq integer,
    id1 integer,
    id2 integer,
    cost float8
);
```

seq sequential ID indicating the path order

id1 generic name, to be specified by the function, typically the node id

id2 generic name, to be specified by the function, typically the edge id

cost cost attribute

3.1.2 pgr_costResult3[] - Multiple Path Results with Cost

Name

`pgr_costResult3[]` — A set of records to describe a path result with cost attribute.

Description

```
CREATE TYPE pgr_costResult3 AS
(
    seq integer,
    id1 integer,
    id2 integer,
    id3 integer,
    cost float8
);
```

seq sequential ID indicating the path order

id1 generic name, to be specified by the function, typically the path id

id2 generic name, to be specified by the function, typically the node id

id3 generic name, to be specified by the function, typically the edge id

cost cost attribute

History

- New in version 2.0.0
- Replaces `path_result`

See Also

- *Introduction*

Indices and tables

- `genindex`
- `search`

3.1.3 pgr_geomResult[]

Name

`pgr_geomResult[]` — A set of records to describe a path result with geometry attribute.

Description

```
CREATE TYPE pgr_geomResult AS
(
    seq integer,
    id1 integer,
    id2 integer,
```

```
geom geometry  
);
```

seq sequential ID indicating the path order

id1 generic name, to be specified by the function

id2 generic name, to be specified by the function

geom geometry attribute

History

- New in version 2.0.0
- Replaces geoms

See Also

- *Introduction*

Indices and tables

- genindex
- search

3.1.4 See Also

Indices and tables

- genindex
- search

Topology Functions

- *pgr_createTopology* - to create a topology based on the geometry.
- *pgr_createVerticesTable* - to reconstruct the vertices table based on the source and target information.
- *pgr_analyzeGraph* - to analyze the edges and vertices of the edge table.
- *pgr_analyzeOneway* - to analyze directionality of the edges.
- *pgr_nodeNetwork* -to create nodes to a not noded edge table.

4.1 Topology - Family of Functions

The pgRouting's topology of a network, represented with an edge table with source and target attributes and a vertices table associated with it. Depending on the algorithm, you can create a topology or just reconstruct the vertices table, You can analyze the topology, We also provide a function to node an unoded network.

- *pgr_createTopology* - to create a topology based on the geometry.
- *pgr_createVerticesTable* - to reconstruct the vertices table based on the source and target information.
- *pgr_analyzeGraph* - to analyze the edges and vertices of the edge table.
- *pgr_analyzeOneway* - to analyze directionality of the edges.
- *pgr_nodeNetwork* -to create nodes to a not noded edge table.

4.1.1 pgr_createTopology

Name

`pgr_createTopology` — Builds a network topology based on the geometry information.

Synopsis

The function returns:

- OK after the network topology has been built and the vertices table created.
- FAIL when the network topology was not built due to an error.

```
vchar pgr_createTopology(text edge_table, double precision tolerance,
                        text the_geom='the_geom', text id='id',
                        text source='source',text target='target',
                        text rows_where='true', boolean clean:=false)
```

Description

Parameters

The topology creation function accepts the following parameters:

- edge_table** text Network table name. (may contain the schema name AS well)
- tolerance** float8 Snapping tolerance of disconnected edges. (in projection unit)
- the_geom** text Geometry column name of the network table. Default value is `the_geom`.
- id** text Primary key column name of the network table. Default value is `id`.
- source** text Source column name of the network table. Default value is `source`.
- target** text Target column name of the network table. Default value is `target`.
- rows_where** text Condition to SELECT a subset or rows. Default value is `true` to indicate all rows that where `source` or `target` have a null value, otherwise the condition is used.
- clean** boolean Clean any previous topology. Default value is `false`.

Warning: The `edge_table` will be affected

- The `source` column values will change.
- The `target` column values will change.
 - An index will be created, if it doesn't exists, to speed up the process to the following columns:
 - * `id`
 - * `the_geom`
 - * `source`
 - * `target`

The function returns:

- OK after the network topology has been built.
 - Creates a vertices table: `<edge_table>_vertices_pgr`.
 - Fills `id` and `the_geom` columns of the vertices table.
 - Fills the `source` and `target` columns of the edge table referencing the `id` of the vertices table.
- FAIL when the network topology was not built due to an error:
 - A required column of the Network table is not found or is not of the appropriate type.
 - The condition is not well formed.
 - The names of `source` , `target` or `id` are the same.
 - The SRID of the geometry could not be determined.

The Vertices Table

The vertices table is a requirement of the *pgr_analyzeGraph* and the *pgr_analyzeOneway* functions.

The structure of the vertices table is:

- id** bigint Identifier of the vertex.
- cnt** integer Number of vertices in the `edge_table` that reference this vertex. See *pgr_analyzeGraph*.
- chk** integer Indicator that the vertex might have a problem. See *pgr_analyzeGraph*.
- ein** integer Number of vertices in the `edge_table` that reference this vertex AS incoming. See *pgr_analyzeOneway*.

out integer Number of vertices in the edge_table that reference this vertex AS outgoing. See *pgr_analyzeOneway*.

the_geom geometry Point geometry of the vertex.

History

- Renamed in version 2.0.0

Usage when the edge table's columns MATCH the default values:

The simplest way to use `pgr_createTopology` is:

```
SELECT pgr_createTopology('edge_table', 0.001);
NOTICE:  PROCESSING:
NOTICE:  pgr_createTopology('edge_table', 0.001, 'the_geom', 'id', 'source', 'target', rows_where
NOTICE:  Performing checks, please wait .....
NOTICE:  Creating Topology, Please wait...
NOTICE:  -----> TOPOLOGY CREATED FOR 18 edges
NOTICE:  Rows with NULL geometry or NULL id: 0
NOTICE:  Vertices table for table public.edge_table is: public.edge_table_vertices_pgr
NOTICE:  -----
pgr_createtopology
-----
OK
(1 row)
```

When the arguments are given in the order described in the parameters:

We get the same result AS the simplest way to use the function.

```
SELECT pgr_createTopology('edge_table', 0.001,
    'the_geom', 'id', 'source', 'target');
NOTICE:  PROCESSING:
NOTICE:  pgr_createTopology('edge_table', 0.001, 'the_geom', 'id', 'source', 'target', rows_where
NOTICE:  Performing checks, please wait .....
NOTICE:  Creating Topology, Please wait...
NOTICE:  -----> TOPOLOGY CREATED FOR 18 edges
NOTICE:  Rows with NULL geometry or NULL id: 0
NOTICE:  Vertices table for table public.edge_table is: public.edge_table_vertices_pgr
NOTICE:  -----
pgr_createtopology
-----
OK
(1 row)
```

Warning:

An error would occur when the arguments are not given in the appropriate order:

In this example, the column `id` of the table `edge_table` is passed to the function as the geometry column, and the geometry column `the_geom` is passed to the function as the `id` column.

```
SELECT pgr_createTopology('edge_table', 0.001,
    'id', 'the_geom');
NOTICE: PROCESSING:
NOTICE: pgr_createTopology('edge_table', 0.001, 'id', 'the_geom', 'source', 'target', rows_where)
NOTICE: Performing checks, please wait .....
NOTICE: ----> PGR ERROR in pgr_createTopology: Wrong type of Column id:the_geom
NOTICE: Unexpected error raise_exception
pgr_createtopology
-----
FAIL
(1 row)
```

When using the named notation

Parameters defined with a default value can be omitted, as long as the value matches the default And The order of the parameters would not matter.

```
SELECT pgr_createTopology('edge_table', 0.001,
    the_geom:='the_geom', id:='id', source:='source', target:='target');
pgr_createtopology
-----
OK
(1 row)
```

```
SELECT pgr_createTopology('edge_table', 0.001,
    source:='source', id:='id', target:='target', the_geom:='the_geom');
pgr_createtopology
-----
OK
(1 row)
```

```
SELECT pgr_createTopology('edge_table', 0.001, source:='source');
pgr_createtopology
-----
OK
(1 row)
```

Selecting rows using `rows_where` parameter

Selecting rows based on the `id`.

```
SELECT pgr_createTopology('edge_table', 0.001, rows_where:='id < 10');
pgr_createtopology
-----
OK
(1 row)
```

Selecting the rows where the geometry is near the geometry of row with `id = 5`.

```
SELECT pgr_createTopology('edge_table', 0.001,
    rows_where:='the_geom && (SELECT st_buffer(the_geom, 0.05) FROM edge_table WHERE id=5)');
pgr_createtopology
-----
OK
(1 row)
```

Selecting the rows where the geometry is near the geometry of the row with gid=100 of the table othertable.

```
CREATE TABLE otherTable AS (SELECT 100 AS gid, st_point(2.5, 2.5) AS other_geom);
SELECT 1
SELECT pgr_createTopology('edge_table', 0.001,
    rows_where:='the_geom && (SELECT st_buffer(other_geom, 1) FROM otherTable WHERE gid=100)');
pgr_createtopology
-----
OK
(1 row)
```

Usage when the edge table's columns DO NOT MATCH the default values:

For the following table

```
CREATE TABLE mytable AS (SELECT id AS gid, the_geom AS mygeom, source AS src , target AS tgt FROM
SELECT 18
```

Using positional notation:

The arguments need to be given in the order described in the parameters.

Note that this example uses clean flag. So it recreates the whole vertices table.

```
SELECT pgr_createTopology('mytable', 0.001, 'mygeom', 'gid', 'src', 'tgt', clean := TRUE);
pgr_createtopology
-----
OK
(1 row)
```

Warning:

An error would occur when the arguments are not given in the appropriate order:

In this example, the column gid of the table mytable is passed to the function AS the geometry column, and the geometry column mygeom is passed to the function AS the id column.

```
SELECT pgr_createTopology('mytable', 0.001, 'gid', 'mygeom', 'src', 'tgt');
NOTICE: PROCESSING:
NOTICE: pgr_createTopology('mytable', 0.001, 'gid', 'mygeom', 'src', 'tgt', rows_where := 'true
NOTICE: Performing checks, please wait .....
NOTICE: ----> PGR ERROR in pgr_createTopology: Wrong type of Column id:mygeom
NOTICE: Unexpected error raise_exception
pgr_createtopology
-----
FAIL
(1 row)
```

When using the named notation

In this scenario omitting a parameter would create an error because the default values for the column names do not match the column names of the table. The order of the parameters do not matter:

```
SELECT pgr_createTopology('mytable', 0.001, the_geom:='mygeom', id:='gid', source:='src', target:='tgt',
pgr_createtopology
-----
OK
(1 row)
```

```
SELECT pgr_createTopology('mytable', 0.001, source:='src', id:='gid', target:='tgt', the_geom:='mygeom',
pgr_createtopology
-----
OK
(1 row)
```

Selecting rows using rows_where parameter

Based on id:

```
SELECT pgr_createTopology('mytable', 0.001, 'mygeom', 'gid', 'src', 'tgt', rows_where:='gid < 10',
pgr_createtopology
-----
OK
(1 row)

SELECT pgr_createTopology('mytable', 0.001, source:='src', id:='gid', target:='tgt', the_geom:='mygeom',
pgr_createtopology
-----
OK
(1 row)

SELECT pgr_createTopology('mytable', 0.001, 'mygeom', 'gid', 'src', 'tgt',
rows_where:='mygeom && (SELECT st_buffer(mygeom, 1) FROM mytable WHERE gid=5)');
pgr_createtopology
-----
OK
(1 row)

SELECT pgr_createTopology('mytable', 0.001, source:='src', id:='gid', target:='tgt', the_geom:='mygeom',
rows_where:='mygeom && (SELECT st_buffer(mygeom, 1) FROM mytable WHERE gid=5)');
pgr_createtopology
-----
OK
(1 row)
```

Selecting the rows where the geometry is near the geometry of the row with gid=100 of the table othertable.

```
SELECT pgr_createTopology('mytable', 0.001, 'mygeom', 'gid', 'src', 'tgt',
rows_where:='mygeom && (SELECT st_buffer(other_geom, 1) FROM otherTable WHERE gid=100)');
pgr_createtopology
-----
OK
(1 row)

SELECT pgr_createTopology('mytable', 0.001, source:='src', id:='gid', target:='tgt', the_geom:='mygeom',
rows_where:='mygeom && (SELECT st_buffer(other_geom, 1) FROM otherTable WHERE gid=100)');
pgr_createtopology
```

```
-----
OK
(1 row)
```

Examples with full output

This example start a clean topology, with 5 edges, and then its incremented to the rest of the edges.

```
SELECT pgr_createTopology('edge_table', 0.001, rows_where:='id < 6', clean := true);
NOTICE:  PROCESSING:
NOTICE:  pgr_createTopology('edge_table', 0.001, 'the_geom', 'id', 'source', 'target', rows_where
NOTICE:  Performing checks, please wait .....
NOTICE:  Creating Topology, Please wait...
NOTICE:  -----> TOPOLOGY CREATED FOR 5 edges
NOTICE:  Rows with NULL geometry or NULL id: 0
NOTICE:  Vertices table for table public.edge_table is: public.edge_table_vertices_pgr
NOTICE:  -----
pgr_createtopology
-----
OK
(1 row)

SELECT pgr_createTopology('edge_table', 0.001);
NOTICE:  PROCESSING:
NOTICE:  pgr_createTopology('edge_table', 0.001, 'the_geom', 'id', 'source', 'target', rows_where
NOTICE:  Performing checks, please wait .....
NOTICE:  Creating Topology, Please wait...
NOTICE:  -----> TOPOLOGY CREATED FOR 13 edges
NOTICE:  Rows with NULL geometry or NULL id: 0
NOTICE:  Vertices table for table public.edge_table is: public.edge_table_vertices_pgr
NOTICE:  -----
pgr_createtopology
-----
OK
(1 row)
```

The example uses the [Sample Data](#) network.

See Also

- [Routing Topology](#) for an overview of a topology for routing algorithms.
- [pgr_createVerticesTable](#) to reconstruct the vertices table based on the source and target information.
- [pgr_analyzeGraph](#) to analyze the edges and vertices of the edge table.

Indices and tables

- [genindex](#)
- [search](#)

4.1.2 pgr_createVerticesTable

Name

`pgr_createVerticesTable` — Reconstructs the vertices table based on the source and target information.

Synopsis

The function returns:

- OK after the vertices table has been reconstructed.
- FAIL when the vertices table was not reconstructed due to an error.

```
pgr_createVerticesTable(edge_table, the_geom, source, target, rows_where)
```

RETURNS VARCHAR

Description

Parameters

The reconstruction of the vertices table function accepts the following parameters:

- edge_table** text Network table name. (may contain the schema name as well)
- the_geom** text Geometry column name of the network table. Default value is `the_geom`.
- source** text Source column name of the network table. Default value is `source`.
- target** text Target column name of the network table. Default value is `target`.
- rows_where** text Condition to SELECT a subset or rows. Default value is `true` to indicate all rows.

Warning: The `edge_table` will be affected

- An index will be created, if it doesn't exists, to speed up the process to the following columns:
 - `the_geom`
 - `source`
 - `target`

The function returns:

- OK after the vertices table has been reconstructed.
 - Creates a vertices table: `<edge_table>_vertices_pgr`.
 - Fills `id` and `the_geom` columns of the vertices table based on the `source` and `target` columns of the edge table.
- FAIL when the vertices table was not reconstructed due to an error.
 - A required column of the Network table is not found or is not of the appropriate type.
 - The condition is not well formed.
 - The names of `source`, `target` are the same.
 - The SRID of the geometry could not be determined.

The Vertices Table

The vertices table is a requirement of the *pgr_analyzeGraph* and the *pgr_analyzeOneway* functions.

The structure of the vertices table is:

- id** bigint Identifier of the vertex.
- cnt** integer Number of vertices in the `edge_table` that reference this vertex. See *pgr_analyzeGraph*.
- chk** integer Indicator that the vertex might have a problem. See *pgr_analyzeGraph*.

ein integer Number of vertices in the edge_table that reference this vertex as incoming. See *pgr_analyzeOneway*.

eout integer Number of vertices in the edge_table that reference this vertex as outgoing. See *pgr_analyzeOneway*.

the_geom geometry Point geometry of the vertex.

History

- Renamed in version 2.0.0

Usage when the edge table's columns MATCH the default values:

The simplest way to use `pgr_createVerticesTable` is:

```
SELECT pgr_createVerticesTable('edge_table');
```

When the arguments are given in the order described in the parameters:

```
SELECT pgr_createVerticesTable('edge_table','the_geom','source','target');
```

We get the same result as the simplest way to use the function.

Warning: An error would occur when the arguments are not given in the appropriate order: In this example, the column source column source of the table mytable is passed to the function as the geometry column, and the geometry column the_geom is passed to the function as the source column.

```
SELECT pgr_createVerticesTable('edge_table','source','the_geom','target');
NOTICE: pgr_createVerticesTable('edge_table','source','the_geom','target','true')
NOTICE: Performing checks, please wait .....
NOTICE: ----> PGR ERROR in pgr_createVerticesTable: Wrong type of Column source: the_geom
HINT:      ----> Expected type of the_geom is integer,smallint or bigint but USER-DEFINED was fou
NOTICE: Unexpected error raise_exception
pgr_createverticestable
-----
      FAIL
(1 row)
```

When using the named notation

The order of the parameters do not matter:

```
SELECT pgr_createVerticesTable('edge_table',the_geom:='the_geom',source:='source',target:='target');
```

```
SELECT pgr_createVerticesTable('edge_table',source:='source',target:='target',the_geom:='the_geom');
```

Parameters defined with a default value can be omitted, as long as the value matches the default:

```
SELECT pgr_createVerticesTable('edge_table',source:='source');
```

Selecting rows using rows_where parameter

Selecting rows based on the id.

```
SELECT pgr_createVerticesTable('edge_table',rows_where:='id < 10');
```

Selecting the rows where the geometry is near the geometry of row with id =5 .

```
SELECT pgr_createVerticesTable('edge_table',rows_where:='the_geom && (select st_buffer(the_geom,
```

Selecting the rows where the geometry is near the geometry of the row with gid=100 of the table othertable.

```
DROP TABLE IF EXISTS otherTable;
CREATE TABLE otherTable AS (SELECT 100 AS gid, st_point(2.5,2.5) AS other_geom) ;
SELECT pgr_createVerticesTable('edge_table',rows_where:='the_geom && (select st_buffer(othergeom,
```

Usage when the edge table's columns DO NOT MATCH the default values:

For the following table

```
DROP TABLE IF EXISTS mytable;
CREATE TABLE mytable AS (SELECT id AS gid, the_geom AS mygeom, source AS src ,target AS tgt FROM e
```

Using positional notation:

The arguments need to be given in the order described in the parameters:

```
SELECT pgr_createVerticesTable('mytable','mygeom','src','tgt');
```

Warning:

An error would occur when the arguments are not given in the appropriate order: In this example, the column src of the table mytable is passed to the function as the geometry column, and the geometry column mygeom is passed to the function as the source column.

```
SELECT pgr_createVerticesTable('mytable','src','mygeom','tgt');
NOTICE:  PROCESSING:
NOTICE:  pgr_createVerticesTable('mytable','src','mygeom','tgt','true')
NOTICE:  Performing checks, please wait .....
NOTICE:  ----> PGR ERROR in pgr_createVerticesTable: Table mytable not found
HINT:    ----> Check your table name
NOTICE:  Unexpected error raise_exception
pgr_createverticestable
-----
      FAIL
(1 row)
```

When using the named notation

The order of the parameters do not matter:

```
SELECT pgr_createVerticesTable('mytable',the_geom:='mygeom',source:='src',target:='tgt');
```

```
SELECT pgr_createVerticesTable('mytable',source:='src',target:='tgt',the_geom:='mygeom');
```

In this scenario omitting a parameter would create an error because the default values for the column names do not match the column names of the table.

Selecting rows using rows_where parameter

Selecting rows based on the gid.

```
SELECT pgr_createVerticesTable('mytable','mygeom','src','tgt',rows_where:='gid < 10');
```

```
SELECT pgr_createVerticesTable('mytable',source:='src',target:='tgt',the_geom:='mygeom',rows_where:='gid < 10');
```

Selecting the rows where the geometry is near the geometry of row with gid=5 .

```
SELECT pgr_createVerticesTable('mytable','mygeom','src','tgt',
                               rows_where:='the_geom && (SELECT st_buffer(mygeom,0.5) FROM mytable WHERE gid=5)');
```

```
SELECT pgr_createVerticesTable('mytable',source:='src',target:='tgt',the_geom:='mygeom',
                               rows_where:='mygeom && (SELECT st_buffer(mygeom,0.5) FROM mytable WHERE gid=100)');
```

Selecting the rows where the geometry is near the geometry of the row with gid=100 of the table othertable.

```
DROP TABLE IF EXISTS otherTable;
CREATE TABLE otherTable AS (SELECT 100 AS gid, st_point(2.5,2.5) AS other_geom) ;
SELECT pgr_createVerticesTable('mytable','mygeom','src','tgt',
                               rows_where:='the_geom && (SELECT st_buffer(othergeom,0.5) FROM otherTable WHERE gid=100)');
```

```
SELECT pgr_createVerticesTable('mytable',source:='src',target:='tgt',the_geom:='mygeom',
                               rows_where:='the_geom && (SELECT st_buffer(othergeom,0.5) FROM otherTable WHERE gid=100)');
```

Examples

```
SELECT pgr_createVerticesTable('edge_table');
NOTICE:  PROCESSING:
NOTICE:  pgr_createVerticesTable('edge_table','the_geom','source','target','true')
NOTICE:  Performing checks, pelase wait .....
NOTICE:  Populating public.edge_table_vertices_pgr, please wait...
NOTICE:  ----->  VERTICES TABLE CREATED WITH 17 VERTICES
NOTICE:                                     FOR 18 EDGES
NOTICE:  Edges with NULL geometry,source or target: 0
NOTICE:                                     Edges processed: 18
NOTICE:  Vertices table for table public.edge_table is: public.edge_table_vertices_pgr
NOTICE:  -----

pgr_createVerticesTable
-----
OK
(1 row)
```

The example uses the [Sample Data](#) network.

See Also

- [Routing Topology](#) for an overview of a topology for routing algorithms.
- [pgr_createTopology](#) to create a topology based on the geometry.
- [pgr_analyzeGraph](#) to analyze the edges and vertices of the edge table.
- [pgr_analyzeOneway](#) to analyze directionality of the edges.

Indices and tables

- [genindex](#)
- [search](#)

4.1.3 pgr_analyzeGraph

Name

pgr_analyzeGraph — Analyzes the network topology.

Synopsis

The function returns:

- OK after the analysis has finished.
- FAIL when the analysis was not completed due to an error.

```
varchar pgr_analyzeGraph(text edge_table, double precision tolerance,  
                        text the_geom='the_geom', text id='id',  
                        text source='source', text target='target', text rows_where='true')
```

Description

Prerequisites

The edge table to be analyzed must contain a source column and a target column filled with id's of the vertices of the segments and the corresponding vertices table <edge_table>_vertices_pgr that stores the vertices information.

- Use *pgr_createVerticesTable* to create the vertices table.
- Use *pgr_createTopology* to create the topology and the vertices table.

Parameters

The analyze graph function accepts the following parameters:

- edge_table** text Network table name. (may contain the schema name as well)
- tolerance** float8 Snapping tolerance of disconnected edges. (in projection unit)
- the_geom** text Geometry column name of the network table. Default value is the_geom.
- id** text Primary key column name of the network table. Default value is id.
- source** text Source column name of the network table. Default value is source.
- target** text Target column name of the network table. Default value is target.
- rows_where** text Condition to select a subset or rows. Default value is true to indicate all rows.

The function returns:

- OK after the analysis has finished.
 - Uses the vertices table: <edge_table>_vertices_pgr.
 - Fills completely the cnt and chk columns of the vertices table.
 - Returns the analysis of the section of the network defined by rows_where
- FAIL when the analysis was not completed due to an error.
 - The vertices table is not found.
 - A required column of the Network table is not found or is not of the appropriate type.
 - The condition is not well formed.
 - The names of source , target or id are the same.

- The SRID of the geometry could not be determined.

The Vertices Table

The vertices table can be created with *pgr_createVerticesTable* or *pgr_createTopology*

The structure of the vertices table is:

- id** bigint Identifier of the vertex.
- cnt** integer Number of vertices in the edge_table that reference this vertex.
- chk** integer Indicator that the vertex might have a problem.
- ein** integer Number of vertices in the edge_table that reference this vertex as incoming. See *pgr_analyzeOneway*.
- eout** integer Number of vertices in the edge_table that reference this vertex as outgoing. See *pgr_analyzeOneway*.
- the_geom** geometry Point geometry of the vertex.

History

- New in version 2.0.0

Usage when the edge table's columns MATCH the default values:

The simplest way to use *pgr_analyzeGraph* is:

```
SELECT pgr_createTopology('edge_table',0.001);
SELECT pgr_analyzeGraph('edge_table',0.001);
```

When the arguments are given in the order described in the parameters:

```
SELECT pgr_analyzeGraph('edge_table',0.001,'the_geom','id','source','target');
```

We get the same result as the simplest way to use the function.

Warning:

An error would occur when the arguments are not given in the appropriate order: In this example, the column `id` of the table `mytable` is passed to the function as the geometry column, and the geometry column `the_geom` is passed to the function as the `id` column.

```
SELECT pgr_analyzeGraph('edge_table',0.001,'id','the_geom','source','target');
NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('edge_table',0.001,'id','the_geom','source','target','true')
NOTICE:  Performing checks, please wait ...
NOTICE:  Got function st_srid(bigint) does not exist
NOTICE:  ERROR: something went wrong when checking for SRID of id in table public.edge_table
pgr_analyzegraph
-----
      FAIL
(1 row)
```

When using the named notation

The order of the parameters do not matter:

```
SELECT pgr_analyzeGraph('edge_table',0.001,the_geom:='the_geom',id:='id',source:='source',target:='target');
```

```
SELECT pgr_analyzeGraph('edge_table',0.001,source:='source',id:='id',target:='target',the_geom:='the_geom');
```

Parameters defined with a default value can be omitted, as long as the value matches the default:

```
SELECT pgr_analyzeGraph('edge_table',0.001,source:='source');
```

Selecting rows using rows_where parameter

Selecting rows based on the id. Displays the analysis a the section of the network.

```
SELECT pgr_analyzeGraph('edge_table',0.001,rows_where:='id < 10');
```

Selecting the rows where the geometry is near the geometry of row with id =5 .

```
SELECT pgr_analyzeGraph('edge_table',0.001,rows_where:='the_geom && (SELECT st_buffer(the_geom,0.001) <= the_geom)');
```

Selecting the rows where the geometry is near the geometry of the row with gid=100 of the table othertable.

```
DROP TABLE IF EXISTS otherTable;
CREATE TABLE otherTable AS (SELECT 100 AS gid, st_point(2.5,2.5) AS other_geom) ;
SELECT pgr_analyzeGraph('edge_table',0.001,rows_where:='the_geom && (SELECT st_buffer(other_geom,0.001) <= the_geom)');
```

Usage when the edge table's columns DO NOT MATCH the default values:

For the following table

```
DROP TABLE IF EXISTS mytable;
CREATE TABLE mytable AS (SELECT id AS gid, source AS src ,target AS tgt , the_geom AS mygeom FROM edge_table);
SELECT pgr_createTopology('mytable',0.001,'mygeom','gid','src','tgt');
```

Using positional notation:

The arguments need to be given in the order described in the parameters:

```
SELECT pgr_analyzeGraph('mytable',0.001,'mygeom','gid','src','tgt');
```

Warning:

An error would occur when the arguments are not given in the appropriate order: In this example, the column gid of the table mytable is passed to the function as the geometry column, and the geometry column mygeom is passed to the function as the id column.

```
SELECT pgr_analyzeGraph('mytable',0.001,'gid','mygeom','src','tgt');
NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('mytable',0.001,'gid','mygeom','src','tgt','true')
NOTICE:  Performing checks, please wait ...
NOTICE:  Got function st_srid(bigint) does not exist
NOTICE:  ERROR: something went wrong when checking for SRID of gid in table public.mytable
pgr_analyzegraph
-----
      FAIL
(1 row)
```

When using the named notation

The order of the parameters do not matter:

```
SELECT pgr_analyzeGraph('mytable',0.001,the_geom:='mygeom',id:='gid',source:='src',target:='tgt');
```

```
SELECT pgr_analyzeGraph('mytable',0.001,source:='src',id:='gid',target:='tgt',the_geom:='mygeom');
```

In this scenario omitting a parameter would create an error because the default values for the column names do not match the column names of the table.

Selecting rows using rows_where parameter

Selecting rows based on the id.

```
SELECT pgr_analyzeGraph('mytable',0.001,'mygeom','gid','src','tgt',rows_where:='gid < 10');
```

```
SELECT pgr_analyzeGraph('mytable',0.001,source:='src',id:='gid',target:='tgt',the_geom:='mygeom');
```

Selecting the rows WHERE the geometry is near the geometry of row with id=5 .

```
SELECT pgr_analyzeGraph('mytable',0.001,'mygeom','gid','src','tgt',
    rows_where:='mygeom && (SELECT st_buffer(mygeom,1) FROM mytable WHERE id=5);
```

```
SELECT pgr_analyzeGraph('mytable',0.001,source:='src',id:='gid',target:='tgt',the_geom:='mygeom',
    rows_where:='mygeom && (SELECT st_buffer(mygeom,1) FROM mytable WHERE id=5);
```

Selecting the rows WHERE the geometry is near the place='myhouse' of the table othertable. (note the use of quote_literal)

```
DROP TABLE IF EXISTS otherTable;
CREATE TABLE otherTable AS (SELECT 'myhouse'::text AS place, st_point(2.5,2.5) AS other_geom) ;
SELECT pgr_analyzeGraph('mytable',0.001,'mygeom','gid','src','tgt',
    rows_where:='mygeom && (SELECT st_buffer(other_geom,1) FROM otherTable WHERE place=quote_literal('myhouse'))');
```

```
SELECT pgr_analyzeGraph('mytable',0.001,source:='src',id:='gid',target:='tgt',the_geom:='mygeom',
    rows_where:='mygeom && (SELECT st_buffer(other_geom,1) FROM otherTable WHERE place=quote_literal('myhouse'))');
```

Examples

```
SELECT pgr_createTopology('edge_table',0.001);
SELECT pgr_analyzeGraph('edge_table', 0.001);
NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('edge_table',0.001,'the_geom','id','source','target','true')
NOTICE:  Performing checks, pelase wait...
NOTICE:  Analyzing for dead ends. Please wait...
NOTICE:  Analyzing for gaps. Please wait...
NOTICE:  Analyzing for isolated edges. Please wait...
NOTICE:  Analyzing for ring geometries. Please wait...
NOTICE:  Analyzing for intersections. Please wait...
NOTICE:  ANALYSIS RESULTS FOR SELECTED EDGES:
NOTICE:  Isolated segments: 2
NOTICE:  Dead ends: 7
NOTICE:  Potential gaps found near dead ends: 1
NOTICE:  Intersections detected: 1
NOTICE:  Ring geometries: 0

pgr_analyzeGraph
-----
OK
```

```

(1 row)

SELECT pgr_analyzeGraph('edge_table',0.001,rows_where:='id < 10');
NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('edge_table',0.001,'the_geom','id','source','target','id < 10')
NOTICE:  Performing checks, pelase wait...
NOTICE:  Analyzing for dead ends. Please wait...
NOTICE:  Analyzing for gaps. Please wait...
NOTICE:  Analyzing for isolated edges. Please wait...
NOTICE:  Analyzing for ring geometries. Please wait...
NOTICE:  Analyzing for intersections. Please wait...
NOTICE:  ANALYSIS RESULTS FOR SELECTED EDGES:
NOTICE:  Isolated segments: 0
NOTICE:  Dead ends: 4
NOTICE:  Potential gaps found near dead ends: 0
NOTICE:  Intersections detected: 0
NOTICE:  Ring geometries: 0

pgr_analyzeGraph
-----
OK
(1 row)

SELECT pgr_analyzeGraph('edge_table',0.001,rows_where:='id >= 10');
NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('edge_table',0.001,'the_geom','id','source','target','id >= 10')
NOTICE:  Performing checks, pelase wait...
NOTICE:  Analyzing for dead ends. Please wait...
NOTICE:  Analyzing for gaps. Please wait...
NOTICE:  Analyzing for isolated edges. Please wait...
NOTICE:  Analyzing for ring geometries. Please wait...
NOTICE:  Analyzing for intersections. Please wait...
NOTICE:  ANALYSIS RESULTS FOR SELECTED EDGES:
NOTICE:  Isolated segments: 2
NOTICE:  Dead ends: 8
NOTICE:  Potential gaps found near dead ends: 1
NOTICE:  Intersections detected: 1
NOTICE:  Ring geometries: 0

pgr_analyzeGraph
-----
OK
(1 row)

-- Simulate removal of edges
SELECT pgr_createTopology('edge_table', 0.001,rows_where:='id <17');
SELECT pgr_analyzeGraph('edge_table', 0.001);
NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('edge_table',0.001,'the_geom','id','source','target','true')
NOTICE:  Performing checks, pelase wait...
NOTICE:  Analyzing for dead ends. Please wait...
NOTICE:  Analyzing for gaps. Please wait...
NOTICE:  Analyzing for isolated edges. Please wait...
NOTICE:  Analyzing for ring geometries. Please wait...
NOTICE:  Analyzing for intersections. Please wait...
NOTICE:  ANALYSIS RESULTS FOR SELECTED EDGES:
NOTICE:  Isolated segments: 0
NOTICE:  Dead ends: 3
NOTICE:  Potential gaps found near dead ends: 0
NOTICE:  Intersections detected: 0
NOTICE:  Ring geometries: 0

pgr_analyzeGraph

```



```

-----
      OK
      (1 row)
SELECT pgr_createTopology('edge_table', 0.001,rows_where:='id <17');
NOTICE:  PROCESSING:
NOTICE:  pgr_createTopology('edge_table',0.001,'the_geom','id','source','target','id <17')
NOTICE:  Performing checks, pelase wait .....
NOTICE:  Creating Topology, Please wait...
NOTICE:  -----> TOPOLOGY CREATED FOR 16 edges
NOTICE:  Rows with NULL geometry or NULL id: 0
NOTICE:  Vertices table for table public.edge_table is: public.edge_table_vertices_pgr
NOTICE:  -----

      pgr_analyzeGraph
      -----
      OK
      (1 row)

SELECT pgr_analyzeGraph('edge_table', 0.001);
NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('edge_table',0.001,'the_geom','id','source','target','true')
NOTICE:  Performing checks, pelase wait...
NOTICE:  Analyzing for dead ends. Please wait...
NOTICE:  Analyzing for gaps. Please wait...
NOTICE:  Analyzing for isolated edges. Please wait...
NOTICE:  Analyzing for ring geometries. Please wait...
NOTICE:  Analyzing for intersections. Please wait...
NOTICE:  ANALYSIS RESULTS FOR SELECTED EDGES:
NOTICE:  Isolated segments: 0
NOTICE:  Dead ends: 3
NOTICE:  Potential gaps found near dead ends: 0
NOTICE:  Intersections detected: 0
NOTICE:  Ring geometries: 0

      pgr_analyzeGraph
      -----
      OK
      (1 row)

```

The examples use the [Sample Data](#) network.

See Also

- [Routing Topology](#) for an overview of a topology for routing algorithms.
- [pgr_analyzeOneway](#) to analyze directionality of the edges.
- [pgr_createVerticesTable](#) to reconstruct the vertices table based on the source and target information.
- [pgr_nodeNetwork](#) to create nodes to a not noded edge table.

Indices and tables

- [genindex](#)
- [search](#)

4.1.4 pgr_analyzeOneway

Name

`pgr_analyzeOneway` — Analyzes oneway Sstreets and identifies flipped segments.

Synopsis

This function analyzes oneway streets in a graph and identifies any flipped segments.

```
text pgr_analyzeOneway (geom_table text,  
                        text[] s_in_rules, text[] s_out_rules,  
                        text[] t_in_rules, text[] t_out_rules,  
                        text oneway='oneway', text source='source', text target='target',  
                        boolean two_way_if_null=true);
```

Description

The analyses of one way segments is pretty simple but can be a powerful tools to identifying some the potential problems created by setting the direction of a segment the wrong way. A node is a *source* if it has edges the exit from that node and no edges enter that node. Conversely, a node is a *sink* if all edges enter the node but none exit that node. For a *source* type node it is logically impossible to exist because no vehicle can exit the node if no vehicle and enter the node. Likewise, if you had a *sink* node you would have an infinite number of vehicle piling up on this node because you can enter it but not leave it.

So why do we care if the are not feasible? Well if the direction of an edge was reversed by mistake we could generate exactly these conditions. Think about a divided highway and on the north bound lane one segment got entered wrong or maybe a sequence of multiple segments got entered wrong or maybe this happened on a round-about. The result would be potentially a *source* and/or a *sink* node.

So by counting the number of edges entering and exiting each node we can identify both *source* and *sink* nodes so that you can look at those areas of your network to make repairs and/or report the problem back to your data vendor.

Prerequisites

The edge table to be analyzed must contain a source column and a target column filled with id's of the vertices of the segments and the corresponding vertices table `<edge_table>_vertices_pgr` that stores the vertices information.

- Use [`pgr_createVerticesTable`](#) to create the vertices table.
- Use [`pgr_createTopology`](#) to create the topology and the vertices table.

Parameters

edge_table text Network table name. (may contain the schema name as well)

s_in_rules text[] source node **in** rules

s_out_rules text[] source node **out** rules

t_in_rules text[] target node **in** rules

t_out_rules text[] target node **out** rules

oneway text oneway column name name of the network table. Default value is `oneway`.

source text Source column name of the network table. Default value is `source`.

target text Target column name of the network table. Default value is `target`.

two_way_if_null boolean flag to treat oneway NULL values as bi-directional. Default value is `true`.

Note: It is strongly recommended to use the named notation. See *pgr_createVerticesTable* or *pgr_createTopology* for examples.

The function returns:

- OK after the analysis has finished.
 - Uses the vertices table: <edge_table>_vertices_pgr.
 - Fills completely the `ein` and `eout` columns of the vertices table.
- FAIL when the analysis was not completed due to an error.
 - The vertices table is not found.
 - A required column of the Network table is not found or is not of the appropriate type.
 - The names of source , target or oneway are the same.

The rules are defined as an array of text strings that if match the `oneway` value would be counted as `true` for the source or target **in** or **out** condition.

The Vertices Table

The vertices table can be created with *pgr_createVerticesTable* or *pgr_createTopology*

The structure of the vertices table is:

id bigint Identifier of the vertex.

cnt integer Number of vertices in the `edge_table` that reference this vertex. See *pgr_analyzeGgraph*.

chk integer Indicator that the vertex might have a problem. See *pgr_analyzeGraph*.

ein integer Number of vertices in the `edge_table` that reference this vertex as incoming.

eout integer Number of vertices in the `edge_table` that reference this vertex as outgoing.

the_geom geometry Point geometry of the vertex.

History

- New in version 2.0.0

Examples

```
SELECT pgr_analyzeOneway('edge_table',
ARRAY['', 'B', 'TF'],
ARRAY['', 'B', 'FT'],
ARRAY['', 'B', 'FT'],
ARRAY['', 'B', 'TF'],
oneway:='dir');
NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('edge_table',{'",B,TF}','",B,FT}','",B,FT}','",B,TF','dir','sou
NOTICE:  Analyzing graph for one way street errors.
NOTICE:  Analysis 25% complete ...
NOTICE:  Analysis 50% complete ...
NOTICE:  Analysis 75% complete ...
NOTICE:  Analysis 100% complete ...
NOTICE:  Found 0 potential problems in directionality

pgr_analyzeoneway
```

```
-----
OK
(1 row)
```

The queries use the [Sample Data](#) network.

See Also

- *Routing Topology* for an overview of a topology for routing algorithms.
- *Graph Analytics* for an overview of the analysis of a graph.
- *pgr_analyzeGraph* to analyze the edges and vertices of the edge table.
- *pgr_createVerticesTable* to reconstruct the vertices table based on the source and target information.

Indices and tables

- `genindex`
- `search`

4.1.5 pgr_nodeNetwork

Name

`pgr_nodeNetwork` - Nodes an network edge table.

Author Nicolas Ribot

Copyright Nicolas Ribot, The source code is released under the MIT-X license.

Synopsis

The function reads edges from a not “noded” network table and writes the “noded” edges into a new table.

```
pgr_nodenetwork(edge_table, tolerance, id, text the_geom, table_ending, rows_where, outall)
RETURNS TEXT
```

Description

A common problem associated with bringing GIS data into pgRouting is the fact that the data is often not “noded” correctly. This will create invalid topologies, which will result in routes that are incorrect.

What we mean by “noded” is that at every intersection in the road network all the edges will be broken into separate road segments. There are cases like an over-pass and under-pass intersection where you can not traverse from the over-pass to the under-pass, but this function does not have the ability to detect and accommodate those situations.

This function reads the `edge_table` table, that has a primary key column `id` and geometry column named `the_geom` and intersect all the segments in it against all the other segments and then creates a table `edge_table_noded`. It uses the `tolerance` for deciding that multiple nodes within the tolerance are considered the same node.

Parameters

edge_table `text` Network table name. (may contain the schema name as well)

tolerance `float8` tolerance for coincident points (in projection unit)

id `text` Primary key column name of the network table. Default value is `id`.

the_geom text Geometry column name of the network table. Default value is the_geom.

table_ending text Suffix for the new table's. Default value is noded.

The output table will have for edge_table_noded

id bigint Unique identifier for the table

old_id bigint Identifier of the edge in original table

sub_id integer Segment number of the original edge

source integer Empty source column to be used with *pgr_createTopology* function

target integer Empty target column to be used with *pgr_createTopology* function

the_geom geometry Geometry column of the noded network

History

- New in version 2.0.0

Example

Let's create the topology for the data in [Sample Data](#)

```
SELECT pgr_createTopology('edge_table', 0.001);
NOTICE:  PROCESSING:
NOTICE:  pgr_createTopology('edge_table',0.001,'the_geom','id','source','target','true')
NOTICE:  Performing checks, pelase wait .....
NOTICE:  Creating Topology, Please wait...
NOTICE:  -----> TOPOLOGY CREATED FOR 18 edges
NOTICE:  Rows with NULL geometry or NULL id: 0
NOTICE:  Vertices table for table public.edge_table is: public.edge_table_vertices_pgr
NOTICE:  -----
pgr_createtopology
-----
OK
(1 row)
```

Now we can analyze the network.

```
SELECT pgr_analyzeGraph('edge_table', 0.001);
NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('edge_table',0.001,'the_geom','id','source','target','true')
NOTICE:  Performing checks, pelase wait...
NOTICE:  Analyzing for dead ends. Please wait...
NOTICE:  Analyzing for gaps. Please wait...
NOTICE:  Analyzing for isolated edges. Please wait...
NOTICE:  Analyzing for ring geometries. Please wait...
NOTICE:  Analyzing for intersections. Please wait...
NOTICE:  ANALYSIS RESULTS FOR SELECTED EDGES:
NOTICE:  Isolated segments: 2
NOTICE:  Dead ends: 7
NOTICE:  Potential gaps found near dead ends: 1
NOTICE:  Intersections detected: 1
NOTICE:  Ring geometries: 0
pgr_analyzegraph
-----
OK
(1 row)
```

The analysis tell us that the network has a gap and an intersection. We try to fix the problem using:

```

SELECT pgr_nodeNetwork('edge_table', 0.001);
NOTICE:  PROCESSING:
NOTICE:  pgr_nodeNetwork('edge_table',0.001,'the_geom','id','noded')
NOTICE:  Performing checks, pelase wait .....
NOTICE:  Processing, pelase wait .....
NOTICE:  Split Edges: 3
NOTICE:  Untouched Edges: 15
NOTICE:  Total original Edges: 18
NOTICE:  Edges generated: 6
NOTICE:  Untouched Edges: 15
NOTICE:  Total New segments: 21
NOTICE:  New Table: public.edge_table_noded
NOTICE:  -----
pgr_nodenetwork
-----
OK
(1 row)

```

Inspecting the generated table, we can see that edges 13,14 and 18 has been segmented

```

SELECT old_id,sub_id FROM edge_table_noded ORDER BY old_id,sub_id;
old_id | sub_id
-----+-----
1      | 1
2      | 1
3      | 1
4      | 1
5      | 1
6      | 1
7      | 1
8      | 1
9      | 1
10     | 1
11     | 1
12     | 1
13     | 1
13     | 2
14     | 1
14     | 2
15     | 1
16     | 1
17     | 1
18     | 1
18     | 2
(21 rows)

```

We can create the topology of the new network

```

SELECT pgr_createTopology('edge_table_noded', 0.001);
NOTICE:  PROCESSING:
NOTICE:  pgr_createTopology('edge_table_noded',0.001,'the_geom','id','source','target','true')
NOTICE:  Performing checks, pelase wait .....
NOTICE:  Creating Topology, Please wait...
NOTICE:  -----> TOPOLOGY CREATED FOR 21 edges
NOTICE:  Rows with NULL geometry or NULL id: 0
NOTICE:  Vertices table for table public.edge_table_noded is: public.edge_table_noded_vertices_pgr
NOTICE:  -----
pgr_createtopology
-----
OK
(1 row)

```

Now let's analyze the new topology

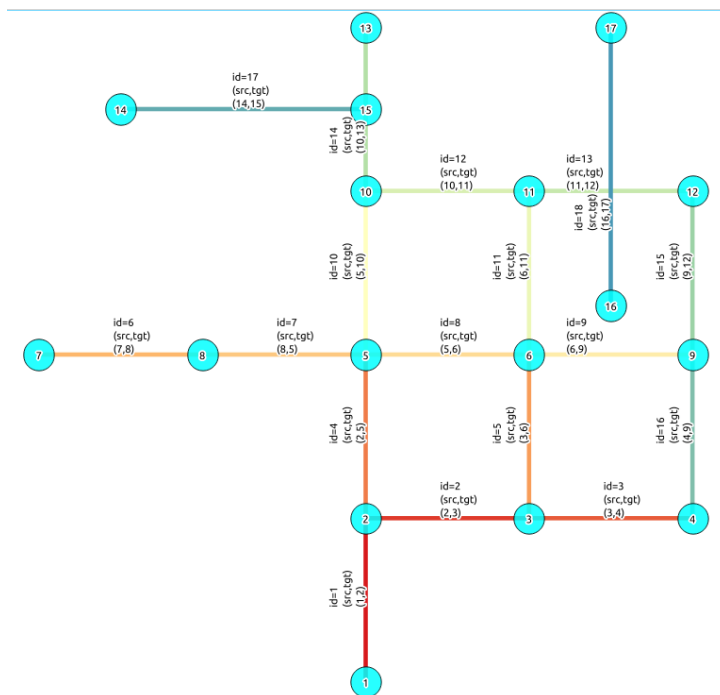
```

SELECT pgr_analyzeGraph('edge_table_noded', 0.001);
NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('edge_table_noded',0.001,'the_geom','id','source','target','true')
NOTICE:  Performing checks, pelase wait...
NOTICE:  Analyzing for dead ends. Please wait...
NOTICE:  Analyzing for gaps. Please wait...
NOTICE:  Analyzing for isolated edges. Please wait...
NOTICE:  Analyzing for ring geometries. Please wait...
NOTICE:  Analyzing for intersections. Please wait...
NOTICE:  ANALYSIS RESULTS FOR SELECTED EDGES:
NOTICE:  Isolated segments: 0
NOTICE:  Dead ends: 6
NOTICE:  Potential gaps found near dead ends: 0
NOTICE:  Intersections detected: 0
NOTICE:  Ring geometries: 0
pgr_createtopology
-----
OK
(1 row)

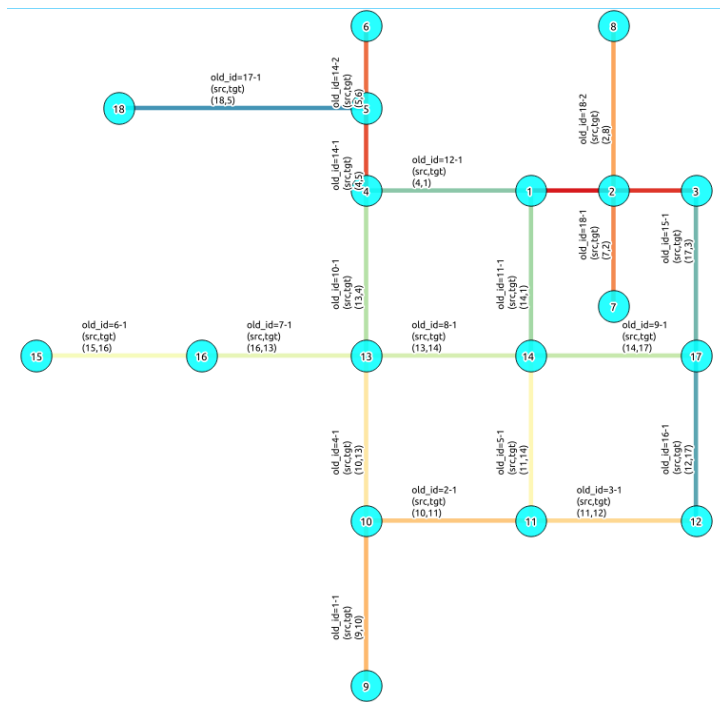
```

Images

Before Image



After Image



Comparing the results

Comparing with the Analysis in the original edge_table, we see that.

	Before	After
Table name	edge_table	edge_table_noded
Fields	All original fields	Has only basic fields to do a topology analysis
Dead ends	<ul style="list-style-type: none"> Edges with 1 dead end: 1,6,24 Edges with 2 dead ends 17,18 <p>Edge 17's right node is a dead end because there is no other edge sharing that same node. (cnt=1)</p>	Edges with 1 dead end: 1-1 ,6-1,14-2, 18-1 17-1 18-2
Isolated segments	two isolated segments: 17 and 18 both they have 2 dead ends	No Isolated segments <ul style="list-style-type: none"> Edge 17 now shares a node with edges 14-1 and 14-2 Edges 18-1 and 18-2 share a node with edges 13-1 and 13-2
Gaps	There is a gap between edge 17 and 14 because edge 14 is near to the right node of edge 17	Edge 14 was segmented Now edges: 14-1 14-2 17 share the same node The tolerance value was taken in account
Intersections	Edges 13 and 18 were intersecting	Edges were segmented, So, now in the intersection's point there is a node and the following edges share it: 13-1 13-2 18-1 18-2

Now, we are going to include the segments 13-1, 13-2 14-1, 14-2 ,18-1 and 18-2 into our edge-table, copying the data for dir,cost,and reverse cost with the following steps:

- Add a column old_id into edge_table, this column is going to keep track the id of the original edge
- Insert only the segmented edges, that is, the ones whose max(sub_id) >1

```
alter table edge_table drop column if exists old_id;
alter table edge_table add column old_id integer;
insert into edge_table (old_id,dir,cost,reverse_cost,the_geom)
    (with
        segmented as (select old_id,count(*) as i from edge_table_noded group by old_id)
    select  segments.old_id,dir,cost,reverse_cost,segments.the_geom
        from edge_table as edges join edge_table_noded as segments on (edges.id = segment
        where edges.id in (select old_id from segmented where i>1) );
```

We recreate the topology:

```
SELECT pgr_createTopology('edge_table', 0.001);

NOTICE:  PROCESSING:
NOTICE:  pgr_createTopology('edge_table',0.001,'the_geom','id','source','target','true')
NOTICE:  Performing checks, pelase wait .....
NOTICE:  Creating Topology, Please wait...
NOTICE:  -----> TOPOLOGY CREATED FOR 24 edges
NOTICE:  Rows with NULL geometry or NULL id: 0
NOTICE:  Vertices table for table public.edge_table is: public.edge_table_vertices_pgr
NOTICE:  -----
pgr_createtopology
-----
OK
(1 row)
```

To get the same analysis results as the topology of edge_table_noded, we do the following query:

```
SELECT pgr_analyzeGraph('edge_table', 0.001,rows_where:='id not in (select old_id from edge_table
NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('edge_table',0.001,'the_geom','id','source','target',
        'id not in (select old_id from edge_table where old_id is not null)')
NOTICE:  Performing checks, pelase wait...
NOTICE:  Analyzing for dead ends. Please wait...
NOTICE:  Analyzing for gaps. Please wait...
NOTICE:  Analyzing for isolated edges. Please wait...
NOTICE:  Analyzing for ring geometries. Please wait...
NOTICE:  Analyzing for intersections. Please wait...
NOTICE:  ANALYSIS RESULTS FOR SELECTED EDGES:
NOTICE:  Isolated segments: 0
NOTICE:  Dead ends: 6
NOTICE:  Potential gaps found near dead ends: 0
NOTICE:  Intersections detected: 0
NOTICE:  Ring geometries: 0
pgr_createtopology
-----
OK
(1 row)
```

To get the same analysis results as the original edge_table, we do the following query:

```
SELECT pgr_analyzeGraph('edge_table', 0.001,rows_where:='old_id is null')

NOTICE:  PROCESSING:
NOTICE:  pgr_analyzeGraph('edge_table',0.001,'the_geom','id','source','target','old_id is null')
NOTICE:  Performing checks, pelase wait...
NOTICE:  Analyzing for dead ends. Please wait...
```

```
NOTICE: Analyzing for gaps. Please wait...
NOTICE: Analyzing for isolated edges. Please wait...
NOTICE: Analyzing for ring geometries. Please wait...
NOTICE: Analyzing for intersections. Please wait...
NOTICE: ANALYSIS RESULTS FOR SELECTED EDGES:
NOTICE: Isolated segments: 2
NOTICE: Dead ends: 7
NOTICE: Potential gaps found near dead ends: 1
NOTICE: Intersections detected: 1
NOTICE: Ring geometries: 0
pgr_createtopology
-----
OK
(1 row)
```

Or we can analyze everything because, maybe edge 18 is an overpass, edge 14 is an under pass and there is also a street level junction, and the same happens with edges 17 and 13.

```
SELECT pgr_analyzegraph('edge_table', 0.001);

NOTICE: PROCESSING:
NOTICE: pgr_analyzeGraph('edge_table',0.001,'the_geom','id','source','target','true')
NOTICE: Performing checks, please wait...
NOTICE: Analyzing for dead ends. Please wait...
NOTICE: Analyzing for gaps. Please wait...
NOTICE: Analyzing for isolated edges. Please wait...
NOTICE: Analyzing for ring geometries. Please wait...
NOTICE: Analyzing for intersections. Please wait...
NOTICE: ANALYSIS RESULTS FOR SELECTED EDGES:
NOTICE: Isolated segments: 0
NOTICE: Dead ends: 3
NOTICE: Potential gaps found near dead ends: 0
NOTICE: Intersections detected: 5
NOTICE: Ring geometries: 0
pgr_createtopology
-----
OK
(1 row)
```

See Also

Routing Topology for an overview of a topology for routing algorithms. *pgr_analyzeOneway* to analyze directionality of the edges. *pgr_createTopology* to create a topology based on the geometry. *pgr_analyzeGraph* to analyze the edges and vertices of the edge table.

Indices and tables

- `genindex`
- `search`

4.1.6 See Also

Indices and tables

- `genindex`
- `search`

Routing functions

5.1 Routing Functions

All Pairs - Family of Functions

- *pgr_floydWarshall* - Floyd-Warshall's Algorithm
- *pgr_johnson* - Johnson's Algorithm

pgr_aStar - Shortest Path A*

pgr_bdAstar - Bi-directional A* Shortest Path

pgr_bdDijkstra - Bi-directional Dijkstra Shortest Path

Dijkstra - Family of functions

- *pgr_dijkstra* - Dijkstra's algorithm for the shortest paths.
- *pgr_dijkstraCost* - Get the aggregate cost of the shortest paths.
- *pgr_dijkstraCostMatrix* - *proposed* - Use *pgr_dijkstra* to create a costs matrix.
- *pgr_drivingDistance* - Use *pgr_dijkstra* to calculate catchment information.
- *pgr_KSP* - Use Yen algorithm with *pgr_dijkstra* to get the K shortest paths.
- *pgr_dijkstraVia* - *Proposed* - Get a route of a sequence of vertices.

pgr_KSP - K-Shortest Path

pgr_trsp - Turn Restriction Shortest Path (TRSP)

Traveling Sales Person - Family of functions

- *pgr_TSP* - When input is given as matrix cell information.
- *pgr_eucledianTSP* - When input are coordinates.

Driving Distance - Category

- *pgr_drivingDistance* - Driving Distance based on *pgr_dijkstra*
- *pgr_withPointsDD* - *Proposed* - Driving Distance based on *pgr_withPoints*
- Post processing
 - *pgr_alphaShape* - Alpha shape computation
 - *pgr_pointsAsPolygon* - Polygon around a set of points

5.1.1 All Pairs - Family of Functions

The following functions work on all vertices pair combinations

pgr_floydWarshall

Synopsis

`pgr_floydWarshall` - Returns the sum of the costs of the shortest path for each pair of nodes in the graph using Floyd-Warshall algorithm.



Fig. 5.1: Boost Graph Inside

Availability: 2.0.0

- Renamed on 2.2.0, previous name `pgr_apspWarshall`

The Floyd-Warshall algorithm, also known as Floyd's algorithm, is a good choice to calculate the sum of the costs of the shortest path for each pair of nodes in the graph, for *dense graphs*. We use Boost's implementation which runs in $\Theta(V^3)$ time,

Characteristics

The main Characteristics are:

- It does not return a path.
- Returns the sum of the costs of the shortest path for each pair of nodes in the graph.
- Process is done only on edges with positive costs.
- Boost returns a $V \times V$ matrix, where the infinity values. Represent the distance between vertices for which there is no path.
 - We return only the non infinity values in form of a set of $(start_vid, end_vid, agg_cost)$.
- Let be the case the values returned are stored in a table, so the unique index would be the pair: $(start_vid, end_vid)$.
- For the undirected graph, the results are symmetric.
 - The agg_cost of (u, v) is the same as for (v, u) .
- When $start_vid = end_vid$, the $agg_cost = 0$.
- **Recommended, use a bounding box of no more than 3500 edges.**

Signature Summary

```
pgr_floydWarshall(edges_sql)
pgr_floydWarshall(edges_sql, directed)
RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

Signatures

Minimal Signature

```
pgr_floydWarshall(edges_sql)
RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

Example 1 On a directed graph.

```
SELECT * FROM pgr_floydWarshall(
  'SELECT id, source, target, cost FROM edge_table where id < 5'
);
 start_vid | end_vid | agg_cost
-----+-----+-----
          1 |         2 |         1
          1 |         5 |         2
          2 |         5 |         1
(3 rows)
```

Complete Signature

```
pgr_floydWarshall(edges_sql, directed)
RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

Example 2 On an undirected graph.

```
SELECT * FROM pgr_floydWarshall(
  'SELECT id, source, target, cost FROM edge_table where id < 5',
  false
);
 start_vid | end_vid | agg_cost
-----+-----+-----
          1 |         2 |         1
          1 |         5 |         2
          2 |         1 |         1
          2 |         5 |         1
          5 |         1 |         2
          5 |         2 |         1
(6 rows)
```

Description of the Signatures

Description of the edges_sql query (id is not necessary)

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source</i> , <i>target</i>) <ul style="list-style-type: none">• When negative: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target</i> , <i>source</i>), <ul style="list-style-type: none">• When negative: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures Receives (*edges_sql*, *directed*)

Parameter	Type	Description
edges_sql	TEXT	SQL query as described above.
directed	BOOLEAN	(optional) Default is true (is directed). When set to false the graph is considered as Undirected

Description of the return values Returns set of (*start_vid*, *end_vid*, *agg_cost*)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex.
end_vid	BIGINT	Identifier of the ending vertex.
agg_cost	FLOAT	Total cost from <i>start_vid</i> to <i>end_vid</i> .

History

- Re-design of `pgr_apspWarshall` in Version 2.2.0

See Also

- [*pgr_johnson*](#)
- [Boost floyd-Warshall²](#) algorithm
- Queries uses the [Sample Data](#) network.

²http://www.boost.org/libs/graph/doc/floyd_warshall_shortest.html

Indices and tables

- `genindex`
- `search`

pgr_johnson

Synopsis

`pgr_johnson` - Returns the sum of the costs of the shortest path for each pair of nodes in the graph using Floyd-Warshall algorithm.



Fig. 5.2: Boost Graph Inside

Availability: 2.0.0

- Renamed on 2.2.0, previous name `pgr_apspJohnson`

The Johnson algorithm, is a good choice to calculate the sum of the costs of the shortest path for each pair of nodes in the graph, for *sparse graphs*. It uses the Boost's implementation which runs in $O(VE \log V)$ time,

Characteristics

The main Characteristics are:

- It does not return a path.
- Returns the sum of the costs of the shortest path for each pair of nodes in the graph.
- Process is done only on edges with positive costs.
- Boost returns a $V \times V$ matrix, where the infinity values. Represent the distance between vertices for which there is no path.
 - We return only the non infinity values in form of a set of $(start_vid, end_vid, agg_cost)$.
- Let be the case the values returned are stored in a table, so the unique index would be the pair: $(start_vid, end_vid)$.
- For the undirected graph, the results are symmetric.
 - The agg_cost of (u, v) is the same as for (v, u) .
- When $start_vid = end_vid$, the $agg_cost = 0$.

Signature Summary

```
pgr_johnson(edges_sql)
pgr_johnson(edges_sql, directed)
RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

Signatures

Minimal Signature

```
pgr_johnson(edges_sql)
RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

Example 1 On a directed graph.

```
SELECT * FROM pgr_johnson(
  'SELECT source, target, cost FROM edge_table WHERE id < 5
   ORDER BY id'
);
 start_vid | end_vid | agg_cost
-----+-----+-----
          1 |         2 |         1
          1 |         5 |         2
          2 |         5 |         1
(3 rows)
```

Complete Signature

```
pgr_johnson(edges_sql, directed)
RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

Example 2 On an undirected graph.

```
SELECT * FROM pgr_johnson(
  'SELECT source, target, cost FROM edge_table WHERE id < 5
   ORDER BY id',
  false
);
 start_vid | end_vid | agg_cost
-----+-----+-----
          1 |         2 |         1
          1 |         5 |         2
          2 |         1 |         1
          2 |         5 |         1
          5 |         1 |         2
          5 |         2 |         1
(6 rows)
```

Description of the Signatures

Description of the edges_sql query (id is not necessary)

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source</i> , <i>target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target</i> , <i>source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures Receives (*edges_sql*, *directed*)

Parameter	Type	Description
edges_sql	TEXT	SQL query as described above.
directed	BOOLEAN	(optional) Default is true (is directed). When set to false the graph is considered as Undirected

Description of the return values Returns set of (*start_vid*, *end_vid*, *agg_cost*)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex.
end_vid	BIGINT	Identifier of the ending vertex.
agg_cost	FLOAT	Total cost from <i>start_vid</i> to <i>end_vid</i> .

History

- Re-design of `pgr_apspJohnson` in Version 2.2.0

See Also

- [*pgr_floydWarshall*](#)
- [Boost Johnson⁴](#) algorithm implementation.
- Queries uses the [Sample Data](#) network.

⁴http://www.boost.org/libs/graph/doc/johnson_all_pairs_shortest.html

Indices and tables

- genindex
- search

Performance

The following tests:

- non server computer
- with AMD 64 CPU
- 4G memory
- trusty
- postgresSQL version 9.3

Data

The following data was used

```
BBOX="-122.8,45.4,-122.5,45.6"
wget --progress=dot:mega -O "sampledata.osm" "http://www.overpass-api.de/api/xapi?*[[bbox=]][@meta]
```

Data processing was done with osm2pgrouting-alpha

```
createdb portland
psql -c "create extension postgis" portland
psql -c "create extension pgrouting" portland
osm2pgrouting -f sampledata.osm -d portland -s 0
```

Results

Test One

This test is not with a bounding box The density of the passed graph is extremely low. For each <SIZE> 30 tests were executed to get the average The tested query is:

```
SELECT count(*) FROM pgr_floydWarshall(
    'SELECT gid as id, source, target, cost, reverse_cost FROM ways where id <= <SIZE>');

SELECT count(*) FROM pgr_johnson(
    'SELECT gid as id, source, target, cost, reverse_cost FROM ways where id <= <SIZE>');
```

The results of this tests are presented as:

SIZE is the number of edges given as input.

EDGES is the total number of records in the query.

DENSITY is the density of the data $\frac{E}{V \times (V - 1)}$.

OUT ROWS is the number of records returned by the queries.

Floyd-Warshall is the average execution time in seconds of pgr_floydWarshall.

Johnson is the average execution time in seconds of pgr_johnson.

SIZE	EDGES	DENSITY	OUT ROWS	Floyd-Warshall	Johnson
500	500	0.18E-7	1346	0.14	0.13
1000	1000	0.36E-7	2655	0.23	0.18
1500	1500	0.55E-7	4110	0.37	0.34
2000	2000	0.73E-7	5676	0.56	0.37
2500	2500	0.89E-7	7177	0.84	0.51
3000	3000	1.07E-7	8778	1.28	0.68
3500	3500	1.24E-7	10526	2.08	0.95
4000	4000	1.41E-7	12484	3.16	1.24
4500	4500	1.58E-7	14354	4.49	1.47
5000	5000	1.76E-7	16503	6.05	1.78
5500	5500	1.93E-7	18623	7.53	2.03
6000	6000	2.11E-7	20710	8.47	2.37
6500	6500	2.28E-7	22752	9.99	2.68
7000	7000	2.46E-7	24687	11.82	3.12
7500	7500	2.64E-7	26861	13.94	3.60
8000	8000	2.83E-7	29050	15.61	4.09
8500	8500	3.01E-7	31693	17.43	4.63
9000	9000	3.17E-7	33879	19.19	5.34
9500	9500	3.35E-7	36287	20.77	6.24
10000	10000	3.52E-7	38491	23.26	6.51

Test Two

This test is with a bounding box The density of the passed graph higher than of the Test One. For each <SIZE> 30 tests were executed to get the average The tested edge query is:

```
WITH
  buffer AS (SELECT ST_Buffer(ST_Centroid(ST_Extent(the_geom)), SIZE) AS geom FROM ways),
  bbox AS (SELECT ST_Envelope(ST_Extent(geom)) as box from buffer)
SELECT gid as id, source, target, cost, reverse_cost FROM ways where the_geom && (SELECT box from
```

The tested queries

```
SELECT count(*) FROM pgr_floydWarshall(<edge query>)
SELECT count(*) FROM pgr_johnson(<edge query>)
```

The results of this tests are presented as:

SIZE is the size of the bounding box.

EDGES is the total number of records in the query.

DENSITY is the density of the data $\frac{E}{V \times (V - 1)}$.

OUT ROWS is the number of records returned by the queries.

Floyd-Warshall is the average execution time in seconds of pgr_floydWarshall.

Johnson is the average execution time in seconds of pgr_johnson.

SIZE	EDGES	DENSITY	OUT ROWS	Floyd-Warshall	Johnson
0.001	44	0.0608	1197	0.10	0.10
0.002	99	0.0251	4330	0.10	0.10
0.003	223	0.0122	18849	0.12	0.12
0.004	358	0.0085	71834	0.16	0.16
0.005	470	0.0070	116290	0.22	0.19
0.006	639	0.0055	207030	0.37	0.27
0.007	843	0.0043	346930	0.64	0.38
0.008	996	0.0037	469936	0.90	0.49
0.009	1146	0.0032	613135	1.26	0.62
0.010	1360	0.0027	849304	1.87	0.82
0.011	1573	0.0024	1147101	2.65	1.04
0.012	1789	0.0021	1483629	3.72	1.35
0.013	1975	0.0019	1846897	4.86	1.68
0.014	2281	0.0017	2438298	7.08	2.28
0.015	2588	0.0015	3156007	10.28	2.80
0.016	2958	0.0013	4090618	14.67	3.76
0.017	3247	0.0012	4868919	18.12	4.48

See Also

- *pgr_johnson*
- *pgr_floydWarshall*
- Boost floyd-Warshall⁵ algorithm

Indices and tables

- genindex
- search

5.1.2 pgr_bdAstar

Name

`pgr_bdAstar` — Returns the shortest path using A* algorithm.



Fig. 5.3: Boost Graph Inside

Availability:

- `pgr_bdAstar(one to one)` 2.0.0, Signature change on 2.5.0
- `pgr_bdAstar(other signatures)` 2.5.0

⁵http://www.boost.org/libs/graph/doc/floyd_warshall_shortest.html

Signature Summary

```
pgr_bdAstar(edges_sql, start_vid, end_vid)
pgr_bdAstar(edges_sql, start_vid, end_vid, directed [, heuristic, factor, epsilon])
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost)
OR EMPTY SET
```

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

```
pgr_bdAstar(edges_sql, start_vid, end_vids [, directed, heuristic, factor, epsilon])
pgr_bdAstar(edges_sql, start_vids, end_vid [, directed, heuristic, factor, epsilon])
pgr_bdAstar(edges_sql, start_vids, end_vids [, directed, heuristic, factor, epsilon])

RETURNS SET OF (seq, path_seq [, start_vid] [, end_vid], node, edge, cost, agg_cost)
OR EMPTY SET
```

Using these signatures, will load once the graph and perform several one to one *pgr_bdAstar*

- The result is the union of the results of the one to one *pgr_bdAstar*.
- The extra *start_vid* and/or *end_vid* in the result is used to distinguish to which path it belongs.

Availability

- *pgr_bdAstar*(one to one) 2.0, signature change on 2.5
- *pgr_bdAstar*(other signatures) 2.5

Signatures

Minimal Signature

```
pgr_bdAstar(edges_sql, start_vid, end_vid)
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost)
```

This usage finds the shortest path from the *start_vid* to the *end_vid*

- on a **directed** graph
- with **heuristic**'s value 5
- with **factor**'s value 1
- with **epsilon**'s value 1

Example Using the defaults

```

SELECT * FROM pgr_bdAstar(
  'SELECT id, source, target, cost, reverse_cost, x1,y1,x2,y2
   FROM edge_table',
  2, 3
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         | 1 | 2 | 4 | 1 | 0
  2 |         | 2 | 5 | 8 | 1 | 1
  3 |         | 3 | 6 | 9 | 1 | 2
  4 |         | 4 | 9 | 16 | 1 | 3
  5 |         | 5 | 4 | 3 | 1 | 4
  6 |         | 6 | 3 | -1 | 0 | 5
(6 rows)

```

pgr_bdAstar One to One

```

pgr_bdAstar(edges_sql, start_vid, end_vid, directed [, heuristic, factor, epsilon])
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost)

```

This usage finds the shortest path from the **start_vid** to the **end_vid** allowing the user to choose

- **heuristic**,
- and/or **factor**
- and/or **epsilon**.

Note: In the One to One signature, because of the deprecated signature existence, it is compulsory to indicate if the graph is **directed** or **undirected**.

Example Directed using Heuristic 2

```

SELECT * FROM pgr_bdAstar(
  'SELECT id, source, target, cost, reverse_cost, x1,y1,x2,y2
   FROM edge_table',
  2, 3,
  true, heuristic := 2
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         | 1 | 2 | 4 | 1 | 0
  2 |         | 2 | 5 | 8 | 1 | 1
  3 |         | 3 | 6 | 9 | 1 | 2
  4 |         | 4 | 9 | 16 | 1 | 3
  5 |         | 5 | 4 | 3 | 1 | 4
  6 |         | 6 | 3 | -1 | 0 | 5
(6 rows)

```

pgr_bdAstar One to many

```

pgr_bdAstar(edges_sql, start_vid, end_vids [, directed, heuristic, factor, epsilon])
RETURNS SET OF (seq, path_seq, end_vid, node, edge, cost, agg_cost) or EMPTY SET

```

This usage finds the shortest path from the **start_vid** to each **end_vid** in **end_vids** allowing the user to choose

- if the graph is **directed** or **undirected**

- and/or **heuristic**,
- and/or **factor**
- and/or **epsilon**.

Example Directed using Heuristic 3 and a factor of 3.5

```
SELECT * FROM pgr_bdAstar(
  'SELECT id, source, target, cost, reverse_cost, x1,y1,x2,y2
  FROM edge_table',
  2, ARRAY[3, 11],
  heuristic := 3, factor := 3.5
);
```

seq	path_seq	end_vid	node	edge	cost	agg_cost
1	1	3	2	4	1	0
2	2	3	5	8	1	1
3	3	3	6	9	1	2
4	4	3	9	16	1	3
5	5	3	4	3	1	4
6	6	3	3	-1	0	5
7	1	11	2	4	1	0
8	2	11	5	8	1	1
9	3	11	6	11	1	2
10	4	11	11	-1	0	3

(10 rows)

pg_rbdAstar Many to One

```
pgr_bdAstar(edges_sql, start_vids, end_vid [, directed, heuristic, factor, epsilon])
RETURNS SET OF (seq, path_seq, start_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This usage finds the shortest path from each `start_vid` in `start_vids` to the `end_vid` allowing the user to choose

- if the graph is **directed** or **undirected**
- and/or **heuristic**,
- and/or **factor**
- and/or **epsilon**.

Example Undirected graph with Heuristic 4

```
SELECT * FROM pgr_bdAstar(
  'SELECT id, source, target, cost, reverse_cost, x1,y1,x2,y2
  FROM edge_table',
  ARRAY[2, 7], 3,
  false, heuristic := 4
);
```

seq	path_seq	start_vid	node	edge	cost	agg_cost
1	1	2	2	2	1	0
2	2	2	3	-1	0	1
3	1	7	7	6	1	0
4	2	7	8	7	1	1
5	3	7	5	4	1	2
6	4	7	2	2	1	3
7	5	7	3	-1	0	4

(7 rows)

pgr_bdAstar Many to Many

```
pgr_bdAstar(edges_sql, start_vids, end_vids [, directed, heuristic, factor, epsilon])
RETURNS SET OF (seq, path_seq, start_vid, end_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This usage finds the shortest path from each **start_vid** in **start_vids** to each **end_vid** in **end_vids** allowing the use

- if the graph is **directed** or **undirected**
- and/or **heuristic**,
- and/or **factor**
- and/or **epsilon**.

Example Directed graph with a factor of 0.5

```
SELECT * FROM pgr_bdAstar(
  'SELECT id, source, target, cost, reverse_cost, x1,y1,x2,y2
  FROM edge_table',
  ARRAY[2, 7], ARRAY[3, 11],
  factor := 0.5
);
```

seq	path_seq	start_vid	end_vid	node	edge	cost	agg_cost
1	1	2	3	2	4	1	0
2	2	2	3	5	8	1	1
3	3	2	3	6	9	1	2
4	4	2	3	9	16	1	3
5	5	2	3	4	3	1	4
6	6	2	3	3	-1	0	5
7	1	2	11	2	4	1	0
8	2	2	11	5	8	1	1
9	3	2	11	6	11	1	2
10	4	2	11	11	-1	0	3
11	1	7	3	7	6	1	0
12	2	7	3	8	7	1	1
13	3	7	3	5	8	1	2
14	4	7	3	6	9	1	3
15	5	7	3	9	16	1	4
16	6	7	3	4	3	1	5
17	7	7	3	3	-1	0	6
18	1	7	11	7	6	1	0
19	2	7	11	8	7	1	1
20	3	7	11	5	10	1	2
21	4	7	11	10	12	1	3
22	5	7	11	11	-1	0	4

(22 rows)

Description of the Signatures**Description of the edges_sql query for astar like functions**

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.
x1	ANY-NUMERICAL		X coordinate of <i>source</i> vertex.
y1	ANY-NUMERICAL		Y coordinate of <i>source</i> vertex.
x2	ANY-NUMERICAL		X coordinate of <i>target</i> vertex.
y2	ANY-NUMERICAL		Y coordinate of <i>target</i> vertex.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Description
edges_sql	TEXT	Edges SQL query as described above.
start_vid	ANY-INTEGER	Starting vertex identifier.
start_vids	ARRAY[ANY-INTEGER]	Starting vertices identifiers.
end_vid	ANY-INTEGER	Ending vertex identifier.
end_vids	ARRAY[ANY-INTEGER]	Ending vertices identifiers.
directed	BOOLEAN	<ul style="list-style-type: none"> Optional. <ul style="list-style-type: none"> When <i>false</i> the graph is considered as Undirected. Default is <i>true</i> which considers the graph as Directed.
heuristic	INTEGER	(optional). Heuristic number. Current valid values 0~5. Default 5 <ul style="list-style-type: none"> 0: $h(v) = 0$ (Use this value to compare with <i>pgr_dijkstra</i>) 1: $h(v) = \text{abs}(\max(dx, dy))$ 2: $h(v) = \text{abs}(\min(dx, dy))$ 3: $h(v) = dx * dx + dy * dy$ 4: $h(v) = \text{sqrt}(dx * dx + dy * dy)$ 5: $h(v) = \text{abs}(dx) + \text{abs}(dy)$
factor	FLOAT	(optional). For units manipulation. <i>factor</i> > 0. Default 1. see <i>Factor</i>
epsilon	FLOAT	(optional). For less restricted results. <i>epsilon</i> >= 1. Default 1.

Description of the return values for a path

Returns set of (seq, path_seq [, start_vid] [, end_vid], node, edge, cost, agg_cost)

Column	Type	Description
seq	INT	Sequential value starting from 1 .
path_id	INT	Path identifier. Has value 1 for the first of a path. Used when there are multiple paths for the same start_vid to end_vid combination.
path_seq	INT	Relative position in the path. Has value 1 for the beginning of a path.
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
node	BIGINT	Identifier of the node in the path from start_vid to end_vid.
edge	BIGINT	Identifier of the edge used to go from node to the next node in the path sequence. -1 for the last node of the path.
cost	FLOAT	Cost to traverse from node using edge to the next node in the path sequence.
agg_cost	FLOAT	Aggregate cost from start_v to node.

See Also

- *Bidirectional A* - Family of functions*

- [Sample Data network](#).
- http://www.boost.org/libs/graph/doc/astar_search.html
- http://en.wikipedia.org/wiki/A*_search_algorithm

Indices and tables

- [genindex](#)
- [search](#)

5.1.3 pgr_bdDijkstra

`pgr_bdDijkstra` — Returns the shortest path(s) using Bidirectional Dijkstra algorithm.



Fig. 5.4: Boost Graph Inside

Availability:

- `pgr_bdDijkstra(one to one)` 2.0.0, Signature changed 2.4.0
- `pgr_bdDijkstra(other signatures)` 2.5.0

Signature Summary

```
pgr_bdDijkstra(edges_sql, start_vid, end_vid)
pgr_bdDijkstra(edges_sql, start_vid, end_vid, directed)
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost)
OR EMPTY SET
```

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

```
pgr_bdDijkstra(edges_sql, start_vid, end_vids, directed)
pgr_bdDijkstra(edges_sql, start_vids, end_vid, directed)
pgr_bdDijkstra(edges_sql, start_vids, end_vids, directed)
```

RETURNS SET OF (seq, path_seq [, start_vid] [, end_vid], node, edge, cost, agg_cost)
OR EMPTY SET

Signatures

Minimal signature

```
pgr_bdDijkstra(edges_sql, start_vid, end_vid)
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost) or EMPTY SET
```

The minimal signature is for a **directed** graph from one start_vid to one end_vid:

Example

```
SELECT * FROM pgr_bdDijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 3
);
```

seq	path_seq	node	edge	cost	agg_cost
1		1	2	4	1
2		2	5	8	1
3		3	6	9	1
4		4	9	16	1
5		5	4	3	1
6		6	3	-1	0

(6 rows)

pgr_bdDijkstra One to One

```
pgr_bdDijkstra(edges_sql, start_vid, end_vid, directed)
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from one start_vid to one end_vid:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Example

```
SELECT * FROM pgr_bdDijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 3,
  false
);
```

seq	path_seq	node	edge	cost	agg_cost
1		1	2	2	1
2		2	3	-1	0

(2 rows)

pgr_bdDijkstra One to many

```
pgr_bdDijkstra(edges_sql, start_vid, end_vids, directed)
RETURNS SET OF (seq, path_seq, end_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from one `start_vid` to each `end_vid` in `end_vids`:

- on a **directed** graph when `directed` flag is missing or is set to `true`.
- on an **undirected** graph when `directed` flag is set to `false`.

Using this signature, will load once the graph and perform a one to one *pgr_dijkstra* where the starting vertex is fixed, and stop when all `end_vids` are reached.

- The result is equivalent to the union of the results of the one to one *pgr_dijkstra*.
- The extra `end_vid` in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_bdDijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, ARRAY[3, 11]);
```

seq	path_seq	end_vid	node	edge	cost	agg_cost
1	1	3	2	4	1	0
2	2	3	5	8	1	1
3	3	3	6	9	1	2
4	4	3	9	16	1	3
5	5	3	4	3	1	4
6	6	3	3	-1	0	5
7	1	11	2	4	1	0
8	2	11	5	8	1	1
9	3	11	6	11	1	2
10	4	11	11	-1	0	3

(10 rows)

pgr_bdDijkstra Many to One

```
pgr_bdDijkstra(edges_sql, start_vids, end_vid, directed)
RETURNS SET OF (seq, path_seq, start_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from each `start_vid` in `start_vids` to one `end_vid`:

- on a **directed** graph when `directed` flag is missing or is set to `true`.
- on an **undirected** graph when `directed` flag is set to `false`.

Using this signature, will load once the graph and perform several one to one *pgr_dijkstra* where the ending vertex is fixed.

- The result is the union of the results of the one to one *pgr_dijkstra*.
- The extra `start_vid` in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_bdDijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2, 7], 3);
```

seq	path_seq	start_vid	node	edge	cost	agg_cost
1	1	2	2	4	1	0
2	2	2	5	8	1	1
3	3	2	6	9	1	2
4	4	2	9	16	1	3
5	5	2	4	3	1	4
6	6	2	3	-1	0	5
7	1	7	7	6	1	0
8	2	7	8	7	1	1

9	3	7	5	8	1	2
10	4	7	6	9	1	3
11	5	7	9	16	1	4
12	6	7	4	3	1	5
13	7	7	3	-1	0	6
(13 rows)						

pgr_bdDijkstra Many to Many

```
pgr_bdDijkstra(edges_sql, start_vids, end_vids, directed)
RETURNS SET OF (seq, path_seq, start_vid, end_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from each `start_vid` in `start_vids` to each `end_vid` in `end_vids`:

- on a **directed** graph when `directed` flag is missing or is set to `true`.
- on an **undirected** graph when `directed` flag is set to `false`.

Using this signature, will load once the graph and perform several one to Many *pgr_dijkstra* for all `start_vids`.

- The result is the union of the results of the one to one *pgr_dijkstra*.
- The extra `start_vid` in the result is used to distinguish to which path it belongs.

The extra `start_vid` and `end_vid` in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_bdDijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2, 7], ARRAY[3, 11]);
```

seq	path_seq	start_vid	end_vid	node	edge	cost	agg_cost
1	1	2	3	2	4	1	0
2	2	2	3	5	8	1	1
3	3	2	3	6	9	1	2
4	4	2	3	9	16	1	3
5	5	2	3	4	3	1	4
6	6	2	3	3	-1	0	5
7	1	2	11	2	4	1	0
8	2	2	11	5	8	1	1
9	3	2	11	6	11	1	2
10	4	2	11	11	-1	0	3
11	1	7	3	7	6	1	0
12	2	7	3	8	7	1	1
13	3	7	3	5	8	1	2
14	4	7	3	6	9	1	3
15	5	7	3	9	16	1	4
16	6	7	3	4	3	1	5
17	7	7	3	3	-1	0	6
18	1	7	11	7	6	1	0
19	2	7	11	8	7	1	1
20	3	7	11	5	10	1	2
21	4	7	11	10	12	1	3
22	5	7	11	11	-1	0	4
(22 rows)							

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Column	Type	Default	Description
sql	TEXT		SQL query as described above.
start_vid	BIGINT		Identifier of the starting vertex of the path.
start_vids	ARRAY[BIGINT]		Array of identifiers of starting vertices.
end_vid	BIGINT		Identifier of the ending vertex of the path.
end_vids	ARRAY[BIGINT]		Array of identifiers of ending vertices.
directed	BOOLEAN	true	<ul style="list-style-type: none"> When true Graph is considered <i>Directed</i> When false the graph is considered as <i>Undirected</i>.

Description of the return values for a path

Returns set of (seq, path_seq [, start_vid] [, end_vid], node, edge, cost, agg_cost)

Col- umn	Type	Description
seq	INT	Sequential value starting from 1.
path_id	INT	Path identifier. Has value 1 for the first of a path. Used when there are multiple paths for the same start_vid to end_vid combination.
path_seq	INT	Relative position in the path. Has value 1 for the beginning of a path.
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
node	BIGINT	Identifier of the node in the path from start_vid to end_vid.
edge	BIGINT	Identifier of the edge used to go from node to the next node in the path sequence. -1 for the last node of the path.
cost	FLOAT	Cost to traverse from node using edge to the next node in the path sequence.
agg_cost	FLOAT	Aggregate cost from start_v to node.

See Also

- The queries use the [Sample Data](#) network.
- *Bidirectional Dijkstra - Family of functions*
- <http://www.cs.princeton.edu/courses/archive/spr06/cos423/Handouts/EPP%20shortest%20path%20algorithms.pdf>
- https://en.wikipedia.org/wiki/Bidirectional_search

Indices and tables

- genindex
- search

5.1.4 Dijkstra - Family of functions

- *pgr_dijkstra* - Dijkstra's algorithm for the shortest paths.
- *pgr_dijkstraCost* - Get the aggregate cost of the shortest paths.
- *pgr_dijkstraCostMatrix - proposed* - Use pgr_dijkstra to create a costs matrix.
- *pgr_drivingDistance* - Use pgr_dijkstra to calculate catchment information.
- *pgr_KSP* - Use Yen algorithm with pgr_dijkstra to get the K shortest paths.
- *pgr_dijkstraVia - Proposed* - Get a route of a sequence of vertices.

pgr_dijkstra

pgr_dijkstra — Returns the shortest path(s) using Dijkstra algorithm. In particular, the Dijkstra algorithm implemented by Boost.Graph.

Availability

- *pgr_dijkstra*(one to one) 2.0.0, signature change 2.1.0
- *pgr_dijkstra*(other signatures) 2.1.0



Fig. 5.5: Boost Graph Inside

Synopsis

Dijkstra's algorithm, conceived by Dutch computer scientist Edsger Dijkstra in 1956. It is a graph search algorithm that solves the shortest path problem for a graph with non-negative edge path costs, producing a shortest path from a starting vertex (*start_vid*) to an ending vertex (*end_vid*). This implementation can be used with a directed graph and an undirected graph.

Characteristics

The main Characteristics are:

- Process is done only on edges with positive costs.
- Values are returned when there is a path.
 - When the starting vertex and ending vertex are the same, there is no path.
 - * The *agg_cost* the non included values (*v, v*) is 0
 - When the starting vertex and ending vertex are the different and there is no path:
 - * The *agg_cost* the non included values (*u, v*) is ∞
- For optimization purposes, any duplicated value in the *start_vids* or *end_vids* are ignored.
- The returned values are ordered:
 - *start_vid* ascending
 - *end_vid* ascending
- Running time: $O(|start_vids| * (V \log V + E))$

Signature Summary

```
pgr_dijkstra(edges_sql, start_vid, end_vid)
pgr_dijkstra(edges_sql, start_vid, end_vid, directed:=true)
pgr_dijkstra(edges_sql, start_vid, end_vids, directed:=true)
pgr_dijkstra(edges_sql, start_vids, end_vid, directed:=true)
pgr_dijkstra(edges_sql, start_vids, end_vids, directed:=true)

RETURNS SET OF (seq, path_seq [, start_vid] [, end_vid], node, edge, cost, agg_cost)
OR EMPTY SET
```

Signatures

Minimal signature

```
pgr_dijkstra(TEXT edges_sql, BIGINT start_vid, BIGINT end_vid)
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost) or EMPTY SET
```

The minimal signature is for a **directed** graph from one *start_vid* to one *end_vid*.

Example

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 3
);
```

seq	path_seq	node	edge	cost	agg_cost
1	1	2	4	1	0
2	2	5	8	1	1
3	3	6	9	1	2
4	4	9	16	1	3
5	5	4	3	1	4
6	6	3	-1	0	5

(6 rows)

pgr_dijkstra One to One

```
pgr_dijkstra(TEXT edges_sql, BIGINT start_vid, BIGINT end_vid,
  BOOLEAN directed:=true);
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from one `start_vid` to one `end_vid`:

- on a **directed** graph when `directed` flag is missing or is set to `true`.
- on an **undirected** graph when `directed` flag is set to `false`.

Example

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 3,
  FALSE
);
```

seq	path_seq	node	edge	cost	agg_cost
1	1	2	2	1	0
2	2	3	-1	0	1

(2 rows)

pgr_dijkstra One to many

```
pgr_dijkstra(TEXT edges_sql, BIGINT start_vid, ARRAY[ANY_INTEGER] end_vids,
  BOOLEAN directed:=true);
RETURNS SET OF (seq, path_seq, end_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from one `start_vid` to each `end_vid` in `end_vids`:

- on a **directed** graph when `directed` flag is missing or is set to `true`.
- on an **undirected** graph when `directed` flag is set to `false`.

Using this signature, will load once the graph and perform a one to one *pgr_dijkstra* where the starting vertex is fixed, and stop when all `end_vids` are reached.

- The result is equivalent to the union of the results of the one to one *pgr_dijkstra*.
- The extra `end_vid` in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  2, ARRAY[3,5],
  FALSE
```

```
);
seq | path_seq | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
1 | 1 | 3 | 2 | 4 | 1 | 0
2 | 2 | 3 | 5 | 8 | 1 | 1
3 | 3 | 3 | 6 | 5 | 1 | 2
4 | 4 | 3 | 3 | -1 | 0 | 3
5 | 1 | 5 | 2 | 4 | 1 | 0
6 | 2 | 5 | 5 | -1 | 0 | 1
(6 rows)
```

pgr_dijkstra Many to One

```
pgr_dijkstra(TEXT edges_sql, ARRAY[ANY_INTEGER] start_vids, BIGINT end_vid,
    BOOLEAN directed:=true);
RETURNS SET OF (seq, path_seq, start_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from each **start_vid** in **start_vids** to one **end_vid**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Using this signature, will load once the graph and perform several one to one *pgr_dijkstra* where the ending vertex is fixed.

- The result is the union of the results of the one to one *pgr_dijkstra*.
- The extra start_vid in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_dijkstra(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    ARRAY[2,11], 5
);
seq | path_seq | start_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
1 | 1 | 2 | 2 | 4 | 1 | 0
2 | 2 | 2 | 5 | -1 | 0 | 1
3 | 1 | 11 | 11 | 13 | 1 | 0
4 | 2 | 11 | 12 | 15 | 1 | 1
5 | 3 | 11 | 9 | 9 | 1 | 2
6 | 4 | 11 | 6 | 8 | 1 | 3
7 | 5 | 11 | 5 | -1 | 0 | 4
(7 rows)
```

pgr_dijkstra Many to Many

```
pgr_dijkstra(TEXT edges_sql, ARRAY[ANY_INTEGER] start_vids, ARRAY[ANY_INTEGER] end_vids,
    BOOLEAN directed:=true);
RETURNS SET OF (seq, path_seq, start_vid, end_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from each **start_vid** in **start_vids** to each **end_vid** in **end_vids**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Using this signature, will load once the graph and perform several one to Many *pgr_dijkstra* for all start_vids.

- The result is the union of the results of the one to one *pgr_dijkstra*.
- The extra start_vid in the result is used to distinguish to which path it belongs.

The extra `start_vid` and `end_vid` in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2,11], ARRAY[3,5],
  FALSE
);
```

seq	path_seq	start_vid	end_vid	node	edge	cost	agg_cost
1	1	2	3	2	2	1	0
2	2	2	3	3	-1	0	1
3	1	2	5	2	4	1	0
4	2	2	5	5	-1	0	1
5	1	11	3	11	11	1	0
6	2	11	3	6	5	1	1
7	3	11	3	3	-1	0	2
8	1	11	5	11	11	1	0
9	2	11	5	6	8	1	1
10	3	11	5	5	-1	0	2

(10 rows)

Description of the Signatures

Description of the `edges_sql` query for dijkstra like functions

`edges_sql` an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source</i> , <i>target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target</i> , <i>source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Column	Type	Default
sql	TEXT	
start_vid	BIGINT	
start_vids	ARRAY[BIGINT]	
end_vid	BIGINT	
end_vids	ARRAY[BIGINT]	
directed	BOOLEAN	true

Description of the return values for a path Returns set of (seq, path_seq [, start_vid] [, end_vid], node, edge, cost, agg_cost)

Column	Type	Description
seq	INT	Sequential value starting from 1.
path_id	INT	Path identifier. Has value 1 for the first of a path. Used when there are multiple paths for the same start_vid to end_vid combination.
path_seq	INT	Relative position in the path. Has value 1 for the beginning of a path.
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
node	BIGINT	Identifier of the node in the path from start_vid to end_vid.
edge	BIGINT	Identifier of the edge used to go from node to the next node in the path sequence. -1 for the last node of the path.
cost	FLOAT	Cost to traverse from node using edge to the next node in the path sequence.
agg_cost	FLOAT	Aggregate cost from start_v to node.

Additional Examples

The examples of this section are based on the [Sample Data](#) network.

The examples include combinations from starting vertices 2 and 11 to ending vertices 3 and 5 in a directed and undirected graph with and with out reverse_cost.

Examples for queries marked as directed with cost and reverse_cost columns The examples in this section use the following *Network for queries marked as directed and cost and reverse_cost columns are used*

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 3
);
```

seq	path_seq	node	edge	cost	agg_cost
1	1	2	4	1	0
2	2	5	8	1	1
3	3	6	9	1	2
4	4	9	16	1	3
5	5	4	3	1	4

```

6 |          6 |      3 |    -1 |      0 |          5
(6 rows)

SELECT * FROM pgr_dijkstra(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    2, 5
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         1 |    2 |    4 |    1 |         0
  2 |         2 |    5 |   -1 |    0 |         1
(2 rows)

SELECT * FROM pgr_dijkstra(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    2, ARRAY[3,5]
);
 seq | path_seq | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
  1 |         1 |        3 |    2 |    4 |    1 |         0
  2 |         2 |        3 |    5 |    8 |    1 |         1
  3 |         3 |        3 |    6 |    9 |    1 |         2
  4 |         4 |        3 |    9 |   16 |    1 |         3
  5 |         5 |        3 |    4 |    3 |    1 |         4
  6 |         6 |        3 |    3 |   -1 |    0 |         5
  7 |         1 |        5 |    2 |    4 |    1 |         0
  8 |         2 |        5 |    5 |   -1 |    0 |         1
(8 rows)

SELECT * FROM pgr_dijkstra(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    11, 3
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         1 |   11 |   13 |    1 |         0
  2 |         2 |   12 |   15 |    1 |         1
  3 |         3 |    9 |   16 |    1 |         2
  4 |         4 |    4 |    3 |    1 |         3
  5 |         5 |    3 |   -1 |    0 |         4
(5 rows)

SELECT * FROM pgr_dijkstra(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    11, 5
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         1 |   11 |   13 |    1 |         0
  2 |         2 |   12 |   15 |    1 |         1
  3 |         3 |    9 |    9 |    1 |         2
  4 |         4 |    6 |    8 |    1 |         3
  5 |         5 |    5 |   -1 |    0 |         4
(5 rows)

SELECT * FROM pgr_dijkstra(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    ARRAY[2,11], 5
);
 seq | path_seq | start_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
  1 |         1 |          2 |    2 |    4 |    1 |         0
  2 |         2 |          2 |    5 |   -1 |    0 |         1

```

```

 3 |      1 |      11 |  11 |  13 |    1 |      0
 4 |      2 |      11 |  12 |  15 |    1 |      1
 5 |      3 |      11 |   9 |   9 |    1 |      2
 6 |      4 |      11 |   6 |   8 |    1 |      3
 7 |      5 |      11 |   5 |  -1 |    0 |      4
(7 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2, 11], ARRAY[3,5]
);
 seq | path_seq | start_vid | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----+-----
  1 |         1 |         2 |        3 |    2 |    4 |    1 |         0
  2 |         2 |         2 |        3 |    5 |    8 |    1 |         1
  3 |         3 |         2 |        3 |    6 |    9 |    1 |         2
  4 |         4 |         2 |        3 |    9 |   16 |    1 |         3
  5 |         5 |         2 |        3 |    4 |    3 |    1 |         4
  6 |         6 |         2 |        3 |    3 |   -1 |    0 |         5
  7 |         1 |         2 |        5 |    2 |    4 |    1 |         0
  8 |         2 |         2 |        5 |    5 |   -1 |    0 |         1
  9 |         1 |        11 |        3 |   11 |   13 |    1 |         0
 10 |         2 |        11 |        3 |   12 |   15 |    1 |         1
 11 |         3 |        11 |        3 |    9 |   16 |    1 |         2
 12 |         4 |        11 |        3 |    4 |    3 |    1 |         3
 13 |         5 |        11 |        3 |    3 |   -1 |    0 |         4
 14 |         1 |        11 |        5 |   11 |   13 |    1 |         0
 15 |         2 |        11 |        5 |   12 |   15 |    1 |         1
 16 |         3 |        11 |        5 |    9 |    9 |    1 |         2
 17 |         4 |        11 |        5 |    6 |    8 |    1 |         3
 18 |         5 |        11 |        5 |    5 |   -1 |    0 |         4
(18 rows)

```

Examples for queries marked as undirected with cost and reverse_cost columns The examples in this section use the following *Network for queries marked as undirected and cost and reverse_cost columns are used*

```

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 3,
  FALSE
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         1 |    2 |    2 |    1 |         0
  2 |         2 |    3 |   -1 |    0 |         1
(2 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 5,
  FALSE
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         1 |    2 |    4 |    1 |         0
  2 |         2 |    5 |   -1 |    0 |         1
(2 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',

```

```

11, 3,
FALSE
);
seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
1 | 1 | 11 | 11 | 1 | 0
2 | 2 | 6 | 5 | 1 | 1
3 | 3 | 3 | -1 | 0 | 2
(3 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  11, 5,
  FALSE
);
seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
1 | 1 | 11 | 11 | 1 | 0
2 | 2 | 6 | 8 | 1 | 1
3 | 3 | 5 | -1 | 0 | 2
(3 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2,11], 5,
  FALSE
);
seq | path_seq | start_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
1 | 1 | 1 | 2 | 2 | 4 | 1 | 0
2 | 2 | 2 | 2 | 5 | -1 | 0 | 1
3 | 3 | 1 | 11 | 11 | 12 | 1 | 0
4 | 4 | 2 | 11 | 10 | 10 | 1 | 1
5 | 5 | 3 | 11 | 5 | -1 | 0 | 2
(5 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, ARRAY[3,5],
  FALSE
);
seq | path_seq | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
1 | 1 | 1 | 3 | 2 | 2 | 1 | 0
2 | 2 | 2 | 3 | 3 | -1 | 0 | 1
3 | 3 | 1 | 5 | 2 | 4 | 1 | 0
4 | 4 | 2 | 5 | 5 | -1 | 0 | 1
(4 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2, 11], ARRAY[3,5],
  FALSE
);
seq | path_seq | start_vid | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----+-----
1 | 1 | 1 | 2 | 3 | 2 | 2 | 1 | 0
2 | 2 | 2 | 2 | 3 | 3 | -1 | 0 | 1
3 | 3 | 1 | 2 | 5 | 2 | 4 | 1 | 0
4 | 4 | 2 | 2 | 5 | 5 | -1 | 0 | 1
5 | 5 | 1 | 11 | 3 | 11 | 11 | 1 | 0
6 | 6 | 2 | 11 | 3 | 6 | 5 | 1 | 1
7 | 7 | 3 | 11 | 3 | 3 | -1 | 0 | 2

```


8	1	11	5	11	11	1	0
9	2	11	5	6	8	1	1
10	3	11	5	5	-1	0	2

(10 rows)

Examples for queries marked as directed with cost column The examples in this section use the following *Network for queries marked as directed and only cost column is used*

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  2, 3
);
```

seq	path_seq	node	edge	cost	agg_cost
-----+-----+-----+-----+-----+-----					

(0 rows)

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  2, 5
);
```

seq	path_seq	node	edge	cost	agg_cost
-----+-----+-----+-----+-----+-----					
1	1	2	4	1	0
2	2	5	-1	0	1

(2 rows)

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  11, 3
);
```

seq	path_seq	node	edge	cost	agg_cost
-----+-----+-----+-----+-----+-----					

(0 rows)

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  11, 5
);
```

seq	path_seq	node	edge	cost	agg_cost
-----+-----+-----+-----+-----+-----					

(0 rows)

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  ARRAY[2,11], 5
);
```

seq	path_seq	start_vid	node	edge	cost	agg_cost
-----+-----+-----+-----+-----+-----+-----						
1	1	2	2	4	1	0
2	2	2	5	-1	0	1

(2 rows)

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  2, ARRAY[3,5]
);
```

seq	path_seq	end_vid	node	edge	cost	agg_cost
-----+-----+-----+-----+-----+-----+-----						
1	1	5	2	4	1	0
2	2	5	5	-1	0	1

(2 rows)

```

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  ARRAY[2, 11], ARRAY[3,5]
);
 seq | path_seq | start_vid | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----+-----
  1 |         1 |         2 |         5 |    2 |    4 |    1 |         0
  2 |         2 |         2 |         5 |    5 |   -1 |    0 |         1
(2 rows)

```

Examples for queries marked as undirected with cost column The examples in this section use the following *Network for queries marked as undirected and only cost column is used*

```

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  2, 3,
  FALSE
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         1 |    2 |    4 |    1 |         0
  2 |         2 |    5 |    8 |    1 |         1
  3 |         3 |    6 |    5 |    1 |         2
  4 |         4 |    3 |   -1 |    0 |         3
(4 rows)

```

```

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  2, 5,
  FALSE
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         1 |    2 |    4 |    1 |         0
  2 |         2 |    5 |   -1 |    0 |         1
(2 rows)

```

```

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  11, 3,
  FALSE
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         1 |   11 |   11 |    1 |         0
  2 |         2 |    6 |    5 |    1 |         1
  3 |         3 |    3 |   -1 |    0 |         2
(3 rows)

```

```

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  11, 5,
  FALSE
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         1 |   11 |   11 |    1 |         0
  2 |         2 |    6 |    8 |    1 |         1
  3 |         3 |    5 |   -1 |    0 |         2
(3 rows)

```

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  ARRAY[2,11], 5,
  FALSE
);
```

seq	path_seq	start_vid	node	edge	cost	agg_cost
1	1	2	2	4	1	0
2	2	2	5	-1	0	1
3	1	11	11	12	1	0
4	2	11	10	10	1	1
5	3	11	5	-1	0	2

(5 rows)

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  2, ARRAY[3,5],
  FALSE
);
```

seq	path_seq	end_vid	node	edge	cost	agg_cost
1	1	3	2	4	1	0
2	2	3	5	8	1	1
3	3	3	6	5	1	2
4	4	3	3	-1	0	3
5	1	5	2	4	1	0
6	2	5	5	-1	0	1

(6 rows)

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost FROM edge_table',
  ARRAY[2, 11], ARRAY[3,5],
  FALSE
);
```

seq	path_seq	start_vid	end_vid	node	edge	cost	agg_cost
1	1	2	3	2	4	1	0
2	2	2	3	5	8	1	1
3	3	2	3	6	5	1	2
4	4	2	3	3	-1	0	3
5	1	2	5	2	4	1	0
6	2	2	5	5	-1	0	1
7	1	11	3	11	11	1	0
8	2	11	3	6	5	1	1
9	3	11	3	3	-1	0	2
10	1	11	5	11	11	1	0
11	2	11	5	6	8	1	1
12	3	11	5	5	-1	0	2

(12 rows)

Equivalences between signatures

Examples For queries marked as directed with cost and reverse_cost columns

The examples in this section use the following:

- *Network for queries marked as directed and cost and reverse_cost columns are used*

```
SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 3,
  TRUE
```

```
);
seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
1 | 1 | 2 | 4 | 1 | 0
2 | 2 | 5 | 8 | 1 | 1
3 | 3 | 6 | 9 | 1 | 2
4 | 4 | 9 | 16 | 1 | 3
5 | 5 | 4 | 3 | 1 | 4
6 | 6 | 3 | -1 | 0 | 5
(6 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2,3
);
seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
1 | 1 | 2 | 4 | 1 | 0
2 | 2 | 5 | 8 | 1 | 1
3 | 3 | 6 | 9 | 1 | 2
4 | 4 | 9 | 16 | 1 | 3
5 | 5 | 4 | 3 | 1 | 4
6 | 6 | 3 | -1 | 0 | 5
(6 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, ARRAY[3],
  TRUE
);
seq | path_seq | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
1 | 1 | 3 | 2 | 4 | 1 | 0
2 | 2 | 3 | 5 | 8 | 1 | 1
3 | 3 | 3 | 6 | 9 | 1 | 2
4 | 4 | 3 | 9 | 16 | 1 | 3
5 | 5 | 3 | 4 | 3 | 1 | 4
6 | 6 | 3 | 3 | -1 | 0 | 5
(6 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, ARRAY[3]
);
seq | path_seq | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
1 | 1 | 3 | 2 | 4 | 1 | 0
2 | 2 | 3 | 5 | 8 | 1 | 1
3 | 3 | 3 | 6 | 9 | 1 | 2
4 | 4 | 3 | 9 | 16 | 1 | 3
5 | 5 | 3 | 4 | 3 | 1 | 4
6 | 6 | 3 | 3 | -1 | 0 | 5
(6 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2], ARRAY[3],
  TRUE
);
seq | path_seq | start_vid | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----+-----
1 | 1 | 2 | 3 | 2 | 4 | 1 | 0
2 | 2 | 2 | 3 | 5 | 8 | 1 | 1
```

```

 3 |          3 |          2 |          3 |          6 |          9 |          1 |          2
 4 |          4 |          2 |          3 |          9 |         16 |          1 |          3
 5 |          5 |          2 |          3 |          4 |          3 |          1 |          4
 6 |          6 |          2 |          3 |          3 |         -1 |          0 |          5
(6 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2], ARRAY[3]
);
 seq | path_seq | start_vid | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----+-----
  1 |         1 |         2 |         3 |     2 |     4 |     1 |         0
  2 |         2 |         2 |         3 |     5 |     8 |     1 |         1
  3 |         3 |         2 |         3 |     6 |     9 |     1 |         2
  4 |         4 |         2 |         3 |     9 |    16 |     1 |         3
  5 |         5 |         2 |         3 |     4 |     3 |     1 |         4
  6 |         6 |         2 |         3 |     3 |    -1 |     0 |         5
(6 rows)

```

Examples For queries marked as undirected with cost and reverse_cost columns

The examples in this section use the following:

- *Network for queries marked as undirected and cost and reverse_cost columns are used*

```

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 3,
  FALSE
);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         1 |     2 |     2 |     1 |         0
  2 |         2 |     3 |    -1 |     0 |         1
(2 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, ARRAY[3],
  FALSE
);
 seq | path_seq | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
  1 |         1 |         3 |     2 |     2 |     1 |         0
  2 |         2 |         3 |     3 |    -1 |     0 |         1
(2 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2], 3,
  FALSE
);
 seq | path_seq | start_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
  1 |         1 |         2 |     2 |     2 |     1 |         0
  2 |         2 |         2 |     3 |    -1 |     0 |         1
(2 rows)

SELECT * FROM pgr_dijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2], ARRAY[3],
  FALSE
);

```

```
);
seq | path_seq | start_vid | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----+-----
  1 |         1 |         2 |         3 |     2 |     2 |     1 |         0
  2 |         2 |         2 |         3 |     3 |    -1 |     0 |         1
(2 rows)
```

See Also

- http://en.wikipedia.org/wiki/Dijkstra%27s_algorithm
- The queries use the [Sample Data](#) network.

Indices and tables

- [genindex](#)
- [search](#)

pgr_dijkstraCost

Synopsis

pgr_dijkstraCost

Using Dijkstra algorithm implemented by Boost.Graph, and extract only the aggregate cost of the shortest path(s) found, for the combination of vertices given.



Fig. 5.6: Boost Graph Inside

Availability

- pgr_dijkstraCost(all signatures) 2.2.0

The `pgr_dijkstraCost` algorithm, is a good choice to calculate the sum of the costs of the shortest path for a subset of pairs of nodes of the graph. We make use of the Boost's implementation of dijkstra which runs in $O(V \log V + E)$ time.

Characteristics

The main Characteristics are:

- It does not return a path.
- Returns the sum of the costs of the shortest path for pair combination of nodes in the graph.
- Process is done only on edges with positive costs.
- Values are returned when there is a path.
 - The returned values are in the form of a set of $(start_vid, end_vid, agg_cost)$.

- When the starting vertex and ending vertex are the same, there is no path.
 - * The *agg_cost* in the non included values (v, v) is 0
- When the starting vertex and ending vertex are the different and there is no path.
 - * The *agg_cost* in the non included values (u, v) is ∞
- Let be the case the values returned are stored in a table, so the unique index would be the pair: (*start_vid*, *end_vid*).
- For undirected graphs, the results are symmetric.
 - The *agg_cost* of (u, v) is the same as for (v, u).
- Any duplicated value in the *start_vids* or *end_vids* is ignored.
- The returned values are ordered:
 - *start_vid* ascending
 - *end_vid* ascending
- Running time: $O(|start_vids| * (V \log V + E))$

Signature Summary

```
pgr_dijkstraCost(edges_sql, start_vid, end_vid);
pgr_dijkstraCost(edges_sql, start_vid, end_vid, directed);
pgr_dijkstraCost(edges_sql, start_vids, end_vid, directed);
pgr_dijkstraCost(edges_sql, start_vid, end_vids, directed);
pgr_dijkstraCost(edges_sql, start_vids, end_vids, directed);

RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

Signatures

Minimal signature The minimal signature is for a **directed** graph from one *start_vid* to one *end_vid*:

```
pgr_dijkstraCost(TEXT edges_sql, BIGINT start_vid, BIGINT end_vid)
RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

Example

```
SELECT * FROM pgr_dijkstraCost(
  'select id, source, target, cost, reverse_cost from edge_table',
  2, 3);
 start_vid | end_vid | agg_cost
-----+-----+-----
          2 |        3 |        5
(1 row)
```

pgr_dijkstraCost One to One

This signature performs a Dijkstra from one *start_vid* to one *end_vid*:

- on a **directed** graph when *directed* flag is missing or is set to true.
- on an **undirected** graph when *directed* flag is set to false.

```
pgr_dijkstraCost(TEXT edges_sql, BIGINT start_vid, BIGINT end_vid,
                 BOOLEAN directed:=true);
RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

Example

```
SELECT * FROM pgr_dijkstraCost(
  'select id, source, target, cost, reverse_cost from edge_table',
  2, 3, false);
 start_vid | end_vid | agg_cost
-----+-----+-----
          2 |         3 |         1
(1 row)
```

pgr_dijkstraCost One to Many

```
pgr_dijkstraCost(TEXT edges_sql, BIGINT start_vid, array[ANY_INTEGER] end_vids,
                 BOOLEAN directed:=true);
RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

This signature performs a Dijkstra from one `start_vid` to each `end_vid` in `end_vids`:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Example

```
SELECT * FROM pgr_dijkstraCost(
  'select id, source, target, cost, reverse_cost from edge_table',
  2, ARRAY[3, 11]);
 start_vid | end_vid | agg_cost
-----+-----+-----
          2 |         3 |         5
          2 |        11 |         3
(2 rows)
```

pgr_dijkstraCost Many to One

```
pgr_dijkstraCost(TEXT edges_sql, array[ANY_INTEGER] start_vids, BIGINT end_vid,
                 BOOLEAN directed:=true);
RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

This signature performs a Dijkstra from each `start_vid` in `start_vids` to one `end_vid`:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Example

```
SELECT * FROM pgr_dijkstraCost(
  'select id, source, target, cost, reverse_cost from edge_table',
  ARRAY[2, 7], 3);
 start_vid | end_vid | agg_cost
-----+-----+-----
          2 |         3 |         5
          7 |         3 |         6
(2 rows)
```


pgr_dijkstraCost Many to Many

```
pgr_dijkstraCost(TEXT edges_sql, array[ANY_INTEGER] start_vids, array[ANY_INTEGER] end_vids,
    BOOLEAN directed:=true);
    RETURNS SET OF (start_vid, end_vid, agg_cost) or EMPTY SET
```

This signature performs a Dijkstra from each **start_vid** in **start_vids** to each **end_vid** in **end_vids**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Example

```
SELECT * FROM pgr_dijkstraCost(
    'select id, source, target, cost, reverse_cost from edge_table',
    ARRAY[2, 7], ARRAY[3, 11]);
 start_vid | end_vid | agg_cost
-----+-----+-----
          2 |         3 |         5
          2 |        11 |         3
          7 |         3 |         6
          7 |        11 |         4
(4 rows)
```

Description of the Signatures**Description of the edges_sql query for dijkstra like functions**

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> • When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> • When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Column	Type	Default
sql	TEXT	
start_vid	BIGINT	
start_vids	ARRAY[BIGINT]	
end_vid	BIGINT	
end_vids	ARRAY[BIGINT]	
directed	BOOLEAN	true

Description of the return values for a Cost function Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
agg_cost	FLOAT	Aggregate cost from start_vid to end_vid.

Additional Examples

Example 1 Demonstration of repeated values are ignored, and result is sorted.

```
SELECT * FROM pgr_dijkstraCost(
    'select id, source, target, cost, reverse_cost from edge_table',
    ARRAY[5, 3, 4, 3, 3, 4], ARRAY[3, 5, 3, 4]);
 start_vid | end_vid | agg_cost
-----+-----+-----
          3 |         4 |         3
          3 |         5 |         2
          4 |         3 |         1
          4 |         5 |         3
          5 |         3 |         4
          5 |         4 |         3
(6 rows)
```

Example 2 Making *start_vids* the same as *end_vids*

```
SELECT * FROM pgr_dijkstraCost(
    'select id, source, target, cost, reverse_cost from edge_table',
    ARRAY[5, 3, 4], ARRAY[5, 3, 4]);
 start_vid | end_vid | agg_cost
-----+-----+-----
          3 |         4 |         3
          3 |         5 |         2
          4 |         3 |         1
          4 |         5 |         3
          5 |         3 |         4
          5 |         4 |         3
```

(6 rows)

See Also

- http://en.wikipedia.org/wiki/Dijkstra%27s_algorithm
- [Sample Data](#) network.

Indices and tables

- [genindex](#)
- [search](#)

pgr_dijkstraCostMatrix - proposed

Name

`pgr_dijkstraCostMatrix` - Calculates the a cost matrix using `pgr_dijktras`.

Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.



Fig. 5.7: Boost Graph Inside

Availability: 2.3.0

Synopsis

Using Dijkstra algorithm, calculate and return a cost matrix.

Signature Summary

```
pgr_dijkstraCostMatrix(edges_sql, start_vids)
pgr_dijkstraCostMatrix(edges_sql, start_vids, directed)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Signatures

Minimal Signature

The minimal signature:

- Is for a **directed** graph.

```
pgr_dijkstraCostMatrix(edges_sql, start_vid)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example Cost matrix for vertices 1, 2, 3, and 4.

```
SELECT * FROM pgr_dijkstraCostMatrix(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5)
);
 start_vid | end_vid | agg_cost
-----+-----+-----
          1 |          2 |          1
          1 |          3 |          6
          1 |          4 |          5
          2 |          1 |          1
          2 |          3 |          5
          2 |          4 |          4
          3 |          1 |          2
          3 |          2 |          1
          3 |          4 |          3
          4 |          1 |          3
          4 |          2 |          2
          4 |          3 |          1
(12 rows)
```

Complete Signature

```
pgr_dijkstraCostMatrix(edges_sql, start_vids, directed:=true)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example Cost matrix for an undirected graph for vertices 1, 2, 3, and 4.

This example returns a symmetric cost matrix.

```
SELECT * FROM pgr_dijkstraCostMatrix(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5),
  false
);
 start_vid | end_vid | agg_cost
-----+-----+-----
          1 |          2 |          1
          1 |          3 |          2
          1 |          4 |          3
          2 |          1 |          1
          2 |          3 |          1
          2 |          4 |          2
          3 |          1 |          2
          3 |          2 |          1
          3 |          4 |          1
          4 |          1 |          3
          4 |          2 |          2
          4 |          3 |          1
(12 rows)
```

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Description
edges_sql	TEXT	Edges SQL query as described above.
start_vids	ARRAY[ANY-INTEGER]	Array of identifiers of the vertices.
directed	BOOLEAN	(optional). When false the graph is considered undirected, true which considers the graph as Directed.

Description of the return values for a Cost function Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
agg_cost	FLOAT	Aggregate cost from start_vid to end_vid.

Examples

Example Use with tsp

```
SELECT * FROM pgr_TSP (
    $$
    SELECT * FROM pgr_dijkstraCostMatrix(
        'SELECT id, source, target, cost, reverse_cost FROM edge_table',
```

```
(SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5),
false
)
$$,
randomize := false
);
```

seq	node	cost	agg_cost
1	1	1	0
2	2	1	1
3	3	1	2
4	4	3	3
5	1	0	6

(5 rows)

See Also

- *Dijkstra - Family of functions*
- *Cost Matrix - Category*
- *Traveling Sales Person - Family of functions*
- The queries use the [Sample Data](#) network.

Indices and tables

- [genindex](#)
- [search](#)

pgr_drivingDistance

Name

`pgr_drivingDistance` - Returns the driving distance from a start node.



Fig. 5.8: Boost Graph Inside

Availability

- `pgr_drivingDistance(single vertex)` 2.0.0, signature change 2.1.0
- `pgr_drivingDistance(multiple vertices)` 2.1.0

Synopsis

Using the Dijkstra algorithm, extracts all the nodes that have costs less than or equal to the value `distance`. The edges extracted will conform to the corresponding spanning tree.

Signature Summary

```
pgr_drivingDistance(edges_sql, start_vid, distance)
pgr_drivingDistance(edges_sql, start_vid, distance, directed)
pgr_drivingDistance(edges_sql, start_vids, distance, directed, equicost)

RETURNS SET OF (seq, [start_vid,] node, edge, cost, agg_cost)
```

Signatures

Minimal Use

```
pgr_drivingDistance(edges_sql, start_vid, distance)
RETURNS SET OF (seq, node, edge, cost, agg_cost)
```

Driving Distance From A Single Starting Vertex

```
pgr_drivingDistance(edges_sql, start_vid, distance, directed)
RETURNS SET OF (seq, node, edge, cost, agg_cost)
```

Driving Distance From Multiple Starting Vertices

```
pgr_drivingDistance(edges_sql, start_vids, distance, directed, equicost)
RETURNS SET OF (seq, start_vid, node, edge, cost, agg_cost)
```

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Column	Type	Description
edges_sql	TEXT	SQL query as described above.
start_vid	BIGINT	Identifier of the starting vertex.
start_vids	ARRAY[ANY-INTEGER]	Array of identifiers of the starting vertices.
distance	FLOAT	Upper limit for the inclusion of the node in the result.
directed	BOOLEAN	(optional). When <code>false</code> the graph is considered as Undirected which considers the graph as Directed.
equicost	BOOLEAN	(optional). When <code>true</code> the node will only appear in the result if the cost is the same. Default is <code>false</code> which resembles several calls using different signatures. Tie brakes are arbitrary.

Description of the return values Returns set of (seq [, start_v], node, edge, cost, agg_cost)

Column	Type	Description
seq	INTEGER	Sequential value starting from 1.
start_vid	INTEGER	Identifier of the starting vertex.
node	BIGINT	Identifier of the node in the path within the limits from start_vid.
edge	BIGINT	Identifier of the edge used to arrive to node. 0 when the node is the start_vid.
cost	FLOAT	Cost to traverse edge.
agg_cost	FLOAT	Aggregate cost from start_vid to node.

Additional Examples

Examples for queries marked as directed with cost and reverse_cost columns The examples in this section use the following *Network for queries marked as directed and cost and reverse_cost columns are used*

```
SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    2, 3
);
```

seq	node	edge	cost	agg_cost
1	2	-1	0	0
2	1	1	1	1
3	5	4	1	1
4	6	8	1	2
5	8	7	1	2
6	10	10	1	2
7	7	6	1	3
8	9	9	1	3
9	11	12	1	3
10	13	14	1	3

(10 rows)

```
SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    13, 3
);
```

seq	node	edge	cost	agg_cost
1	13	-1	0	0
2	10	14	1	1
3	5	10	1	2
4	11	12	1	2
5	2	4	1	3
6	6	8	1	3


```

 7 |      8 |      7 |      1 |      3
 8 |     12 |     13 |      1 |      3
(8 rows)

SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    array[2,13], 3
);
 seq | from_v | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |      2 |    2 |   -1 |    0 |         0
  2 |      2 |    1 |    1 |    1 |         1
  3 |      2 |    5 |    4 |    1 |         1
  4 |      2 |    6 |    8 |    1 |         2
  5 |      2 |    8 |    7 |    1 |         2
  6 |      2 |   10 |   10 |    1 |         2
  7 |      2 |    7 |    6 |    1 |         3
  8 |      2 |    9 |    9 |    1 |         3
  9 |      2 |   11 |   12 |    1 |         3
 10 |      2 |   13 |   14 |    1 |         3
 11 |     13 |   13 |   -1 |    0 |         0
 12 |     13 |   10 |   14 |    1 |         1
 13 |     13 |    5 |   10 |    1 |         2
 14 |     13 |   11 |   12 |    1 |         2
 15 |     13 |    2 |    4 |    1 |         3
 16 |     13 |    6 |    8 |    1 |         3
 17 |     13 |    8 |    7 |    1 |         3
 18 |     13 |   12 |   13 |    1 |         3
(18 rows)

SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    array[2,13], 3, equicost:=true
);
 seq | from_v | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |      2 |    2 |   -1 |    0 |         0
  2 |      2 |    1 |    1 |    1 |         1
  3 |      2 |    5 |    4 |    1 |         1
  4 |      2 |    6 |    8 |    1 |         2
  5 |      2 |    8 |    7 |    1 |         2
  6 |      2 |    7 |    6 |    1 |         3
  7 |      2 |    9 |    9 |    1 |         3
  8 |     13 |   13 |   -1 |    0 |         0
  9 |     13 |   10 |   14 |    1 |         1
 10 |     13 |   11 |   12 |    1 |         2
 11 |     13 |   12 |   13 |    1 |         3
(11 rows)

```

Examples for queries marked as undirected with cost and reverse_cost columns The examples in this section use the following *Network for queries marked as undirected and cost and reverse_cost columns are used*

```

SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    2, 3, false
);
 seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----
  1 |      2 |   -1 |    0 |         0
  2 |      1 |    1 |    1 |         1

```

```

3 | 3 | 2 | 1 | 1
4 | 5 | 4 | 1 | 1
5 | 4 | 3 | 1 | 2
6 | 6 | 8 | 1 | 2
7 | 8 | 7 | 1 | 2
8 | 10 | 10 | 1 | 2
9 | 7 | 6 | 1 | 3
10 | 9 | 16 | 1 | 3
11 | 11 | 12 | 1 | 3
12 | 13 | 14 | 1 | 3
(12 rows)

SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    13, 3, false
);
 seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----
  1 | 13 | -1 | 0 | 0
  2 | 10 | 14 | 1 | 1
  3 | 5 | 10 | 1 | 2
  4 | 11 | 12 | 1 | 2
  5 | 2 | 4 | 1 | 3
  6 | 6 | 8 | 1 | 3
  7 | 8 | 7 | 1 | 3
  8 | 12 | 13 | 1 | 3
(8 rows)

SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    array[2,13], 3, false
);
 seq | from_v | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 | 2 | 2 | 2 | -1 | 0 | 0
  2 | 2 | 1 | 1 | 1 | 1
  3 | 2 | 3 | 2 | 1 | 1
  4 | 2 | 5 | 4 | 1 | 1
  5 | 2 | 4 | 3 | 1 | 2
  6 | 2 | 6 | 8 | 1 | 2
  7 | 2 | 8 | 7 | 1 | 2
  8 | 2 | 10 | 10 | 1 | 2
  9 | 2 | 7 | 6 | 1 | 3
 10 | 2 | 9 | 16 | 1 | 3
 11 | 2 | 11 | 12 | 1 | 3
 12 | 2 | 13 | 14 | 1 | 3
 13 | 13 | 13 | -1 | 0 | 0
 14 | 13 | 10 | 14 | 1 | 1
 15 | 13 | 5 | 10 | 1 | 2
 16 | 13 | 11 | 12 | 1 | 2
 17 | 13 | 2 | 4 | 1 | 3
 18 | 13 | 6 | 8 | 1 | 3
 19 | 13 | 8 | 7 | 1 | 3
 20 | 13 | 12 | 13 | 1 | 3
(20 rows)

SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    array[2,13], 3, false, equicost:=true
);
 seq | from_v | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 | 2 | 2 | 2 | -1 | 0 | 0

```

2	2	1	1	1	1
3	2	3	2	1	1
4	2	5	4	1	1
5	2	4	3	1	2
6	2	6	8	1	2
7	2	8	7	1	2
8	2	7	6	1	3
9	2	9	16	1	3
10	13	13	-1	0	0
11	13	10	14	1	1
12	13	11	12	1	2
13	13	12	13	1	3

(13 rows)

Examples for queries marked as *directed with cost column* The examples in this section use the following *Network for queries marked as directed and only cost column is used*

```
SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost FROM edge_table',
    2, 3
);
```

seq	node	edge	cost	agg_cost
1	2	-1	0	0
2	5	4	1	1
3	6	8	1	2
4	10	10	1	2
5	9	9	1	3
6	11	11	1	3
7	13	14	1	3

(7 rows)

```
SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost FROM edge_table',
    13, 3
);
```

seq	node	edge	cost	agg_cost
1	13	-1	0	0

(1 row)

```
SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost FROM edge_table',
    array[2,13], 3
);
```

seq	from_v	node	edge	cost	agg_cost
1	2	2	-1	0	0
2	2	5	4	1	1
3	2	6	8	1	2
4	2	10	10	1	2
5	2	9	9	1	3
6	2	11	11	1	3
7	2	13	14	1	3
8	13	13	-1	0	0

(8 rows)

```
SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost FROM edge_table',
    array[2,13], 3, equicost:=true
);
```

seq	from_v	node	edge	cost	agg_cost
1	2	2	-1	0	0
2	2	5	4	1	1
3	2	6	8	1	2
4	2	10	10	1	2
5	2	9	9	1	3
6	2	11	11	1	3
7	13	13	-1	0	0

(7 rows)

Examples for queries marked as undirected with cost column The examples in this section use the following *Network for queries marked as undirected and only cost column is used*

```
SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost FROM edge_table',
    2, 3, false
);
```

seq	node	edge	cost	agg_cost
1	2	-1	0	0
2	1	1	1	1
3	5	4	1	1
4	6	8	1	2
5	8	7	1	2
6	10	10	1	2
7	3	5	1	3
8	7	6	1	3
9	9	9	1	3
10	11	12	1	3
11	13	14	1	3

(11 rows)

```
SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost FROM edge_table',
    13, 3, false
);
```

seq	node	edge	cost	agg_cost
1	13	-1	0	0
2	10	14	1	1
3	5	10	1	2
4	11	12	1	2
5	2	4	1	3
6	6	8	1	3
7	8	7	1	3
8	12	13	1	3

(8 rows)

```
SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost FROM edge_table',
    array[2,13], 3, false
);
```

seq	from_v	node	edge	cost	agg_cost
1	2	2	-1	0	0
2	2	1	1	1	1
3	2	5	4	1	1
4	2	6	8	1	2
5	2	8	7	1	2
6	2	10	10	1	2

```

 7 |      2 |      3 |      5 |      1 |      3
 8 |      2 |      7 |      6 |      1 |      3
 9 |      2 |      9 |      9 |      1 |      3
10 |      2 |     11 |     12 |      1 |      3
11 |      2 |     13 |     14 |      1 |      3
12 |     13 |     13 |     -1 |      0 |      0
13 |     13 |     10 |     14 |      1 |      1
14 |     13 |      5 |     10 |      1 |      2
15 |     13 |     11 |     12 |      1 |      2
16 |     13 |      2 |      4 |      1 |      3
17 |     13 |      6 |      8 |      1 |      3
18 |     13 |      8 |      7 |      1 |      3
19 |     13 |     12 |     13 |      1 |      3
(19 rows)

SELECT * FROM pgr_drivingDistance(
    'SELECT id, source, target, cost FROM edge_table',
    array[2,13], 3, false, equicost:=true
);
 seq | from_v | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |      2 |      2 |     -1 |      0 |          0
  2 |      2 |      1 |      1 |      1 |          1
  3 |      2 |      5 |      4 |      1 |          1
  4 |      2 |      6 |      8 |      1 |          2
  5 |      2 |      8 |      7 |      1 |          2
  6 |      2 |      3 |      5 |      1 |          3
  7 |      2 |      7 |      6 |      1 |          3
  8 |      2 |      9 |      9 |      1 |          3
  9 |     13 |     13 |     -1 |      0 |          0
 10 |     13 |     10 |     14 |      1 |          1
 11 |     13 |     11 |     12 |      1 |          2
 12 |     13 |     12 |     13 |      1 |          3
(12 rows)

```

See Also

- [*pgr_alphaShape*](#) - Alpha shape computation
- [*pgr_pointsAsPolygon*](#) - Polygon around set of points
- [Sample Data](#) network.

Indices and tables

- [genindex](#)
- [search](#)

pgr_KSP

Name

pgr_KSP — Returns the “K” shortest paths.



Fig. 5.9: Boost Graph Inside

Availability: 2.0.0

- Signature change 2.1.0

Synopsis

The K shortest path routing algorithm based on Yen's algorithm. "K" is the number of shortest paths desired.

Signature Summary

```
pgr_KSP(edges_sql, start_vid, end_vid, K);  
pgr_KSP(edges_sql, start_vid, end_vid, k, directed, heap_paths)  
RETURNS SET OF (seq, path_id, path_seq, node, edge, cost, agg_cost) or EMPTY SET
```

Signatures

Minimal Signature

```
pgr_ksp(edges_sql, start_vid, end_vid, K);  
RETURNS SET OF (seq, path_id, path_seq, node, edge, cost, agg_cost) or EMPTY SET
```

Complete Signature

```
pgr_KSP(edges_sql, start_vid, end_vid, k, directed, heap_paths)  
RETURNS SET OF (seq, path_id, path_seq, node, edge, cost, agg_cost) or EMPTY SET
```

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Column	Type	Description
edges_sql	TEXT	SQL query as described above.
start_vid	BIGINT	Identifier of the starting vertex.
end_vid	BIGINT	Identifier of the ending vertex.
k	INTEGER	The desired number of paths.
directed	BOOLEAN	(optional). When <i>false</i> the graph is considered as Undirected which considers the graph as Directed.
heap_paths	BOOLEAN	(optional). When <i>true</i> returns all the paths stored in the heap, <i>false</i> which only returns <i>k</i> paths.

Roughly, if the shortest path has *N* edges, the heap will contain about $N * k$ paths for small value of *k* and $k > 1$.

Description of the return values Returns set of (*seq, path_seq, path_id, node, edge, cost, agg_cost*)

Column	Type	Description
seq	INTEGER	Sequential value starting from 1 .
path_seq	INTEGER	Relative position in the path of <i>node</i> and <i>edge</i> . Has value 1 for the beginning of a path.
path_id	BIGINT	Path identifier. The ordering of the paths For two paths <i>i, j</i> if $i < j$ then $agg_cost(i) \leq agg_cost(j)$.
node	BIGINT	Identifier of the node in the path.
edge	BIGINT	Identifier of the edge used to go from <i>node</i> to the next node in the path sequence. -1 for the last node of the route.
cost	FLOAT	Cost to traverse from <i>node</i> using <i>edge</i> to the next node in the path sequence.
agg_cost	FLOAT	Aggregate cost from <i>start_vid</i> to <i>node</i> .

Warning: During the transition to 3.0, because pgr_ksp version 2.0 doesn't have defined a directed flag nor a heap_path flag, when pgr_ksp is used with only one flag version 2.0 signature will be used.

Additional Examples

Examples to handle the one flag to choose signatures The examples in this section use the following *Network for queries marked as directed and cost and reverse_cost columns are used*

```
SELECT * FROM pgr_KSP(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 12, 2,
  directed:=true
);
```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	2	4	1	0
2	1	2	5	8	1	1
3	1	3	6	9	1	2
4	1	4	9	15	1	3
5	1	5	12	-1	0	4
6	2	1	2	4	1	0
7	2	2	5	8	1	1
8	2	3	6	11	1	2
9	2	4	11	13	1	3
10	2	5	12	-1	0	4

(10 rows)

```
SELECT * FROM pgr_KSP(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 12, 2
);
```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	2	4	1	0
2	1	2	5	8	1	1
3	1	3	6	9	1	2
4	1	4	9	15	1	3
5	1	5	12	-1	0	4
6	2	1	2	4	1	0
7	2	2	5	8	1	1
8	2	3	6	11	1	2
9	2	4	11	13	1	3
10	2	5	12	-1	0	4

(10 rows)

Examples for queries marked as directed with cost and reverse_cost columns The examples in this section use the following *Network for queries marked as directed and cost and reverse_cost columns are used*

```
SELECT * FROM pgr_KSP(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 12, 2
);
```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	2	4	1	0
2	1	2	5	8	1	1
3	1	3	6	9	1	2
4	1	4	9	15	1	3
5	1	5	12	-1	0	4

6		2		1		2		4		1		0
7		2		2		5		8		1		1
8		2		3		6		11		1		2
9		2		4		11		13		1		3
10		2		5		12		-1		0		4
(10 rows)												
SELECT * FROM pgr_KSP('SELECT id, source, target, cost, reverse_cost FROM edge_table', 2, 12, 2, heap_paths:=true);												
seq		path_id		path_seq		node		edge		cost		agg_cost
-----+-----+-----+-----+-----+-----+-----												
1		1		1		2		4		1		0
2		1		2		5		8		1		1
3		1		3		6		9		1		2
4		1		4		9		15		1		3
5		1		5		12		-1		0		4
6		2		1		2		4		1		0
7		2		2		5		8		1		1
8		2		3		6		11		1		2
9		2		4		11		13		1		3
10		2		5		12		-1		0		4
11		3		1		2		4		1		0
12		3		2		5		10		1		1
13		3		3		10		12		1		2
14		3		4		11		13		1		3
15		3		5		12		-1		0		4
(15 rows)												
SELECT * FROM pgr_KSP('SELECT id, source, target, cost, reverse_cost FROM edge_table', 2, 12, 2, true, true);												
seq		path_id		path_seq		node		edge		cost		agg_cost
-----+-----+-----+-----+-----+-----+-----												
1		1		1		2		4		1		0
2		1		2		5		8		1		1
3		1		3		6		9		1		2
4		1		4		9		15		1		3
5		1		5		12		-1		0		4
6		2		1		2		4		1		0
7		2		2		5		8		1		1
8		2		3		6		11		1		2
9		2		4		11		13		1		3
10		2		5		12		-1		0		4
11		3		1		2		4		1		0
12		3		2		5		10		1		1
13		3		3		10		12		1		2
14		3		4		11		13		1		3
15		3		5		12		-1		0		4
(15 rows)												

Examples for queries marked as undirected with cost and reverse_cost columns The examples in this section use the following *Network for queries marked as undirected and cost and reverse_cost columns are used*

```
SELECT * FROM pgr_KSP(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 12, 2, directed:=false
);
```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	2	2	1	0
2	1	2	3	3	1	1
3	1	3	4	16	1	2
4	1	4	9	15	1	3
5	1	5	12	-1	0	4
6	2	1	2	4	1	0
7	2	2	5	8	1	1
8	2	3	6	11	1	2
9	2	4	11	13	1	3
10	2	5	12	-1	0	4

(10 rows)

```

SELECT * FROM pgr_KSP(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 12, 2, false, true
);

```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	2	2	1	0
2	1	2	3	3	1	1
3	1	3	4	16	1	2
4	1	4	9	15	1	3
5	1	5	12	-1	0	4
6	2	1	2	4	1	0
7	2	2	5	8	1	1
8	2	3	6	11	1	2
9	2	4	11	13	1	3
10	2	5	12	-1	0	4
11	3	1	2	4	1	0
12	3	2	5	10	1	1
13	3	3	10	12	1	2
14	3	4	11	13	1	3
15	3	5	12	-1	0	4
16	4	1	2	4	1	0
17	4	2	5	10	1	1
18	4	3	10	12	1	2
19	4	4	11	11	1	3
20	4	5	6	9	1	4
21	4	6	9	15	1	5
22	4	7	12	-1	0	6

(22 rows)

Examples for queries marked as directed with cost column The examples in this section use the following *Network for queries marked as directed and only cost column is used*

```

SELECT * FROM pgr_KSP(
  'SELECT id, source, target, cost FROM edge_table',
  2, 3, 2
);

```

seq	path_id	path_seq	node	edge	cost	agg_cost
-----	---------	----------	------	------	------	----------

(0 rows)

```

SELECT * FROM pgr_KSP(
  'SELECT id, source, target, cost FROM edge_table',
  2, 12, 2
);

```

seq	path_id	path_seq	node	edge	cost	agg_cost
-----	---------	----------	------	------	------	----------

```

1 |      1 |      1 |      2 |      4 |      1 |      0
2 |      1 |      2 |      5 |      8 |      1 |      1
3 |      1 |      3 |      6 |      9 |      1 |      2
4 |      1 |      4 |      9 |     15 |      1 |      3
5 |      1 |      5 |     12 |     -1 |      0 |      4
6 |      2 |      1 |      2 |      4 |      1 |      0
7 |      2 |      2 |      5 |      8 |      1 |      1
8 |      2 |      3 |      6 |     11 |      1 |      2
9 |      2 |      4 |     11 |     13 |      1 |      3
10 |     2 |      5 |     12 |     -1 |      0 |      4
(10 rows)

```

```

SELECT  * FROM pgr_KSP(
    'SELECT id, source, target, cost FROM edge_table',
    2, 12, 2, heap_paths:=true
);
 seq | path_id | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
  1 |      1 |      1 |      2 |      4 |      1 |      0
  2 |      1 |      2 |      5 |      8 |      1 |      1
  3 |      1 |      3 |      6 |      9 |      1 |      2
  4 |      1 |      4 |      9 |     15 |      1 |      3
  5 |      1 |      5 |     12 |     -1 |      0 |      4
  6 |      2 |      1 |      2 |      4 |      1 |      0
  7 |      2 |      2 |      5 |      8 |      1 |      1
  8 |      2 |      3 |      6 |     11 |      1 |      2
  9 |      2 |      4 |     11 |     13 |      1 |      3
 10 |      2 |      5 |     12 |     -1 |      0 |      4
 11 |      3 |      1 |      2 |      4 |      1 |      0
 12 |      3 |      2 |      5 |     10 |      1 |      1
 13 |      3 |      3 |     10 |     12 |      1 |      2
 14 |      3 |      4 |     11 |     13 |      1 |      3
 15 |      3 |      5 |     12 |     -1 |      0 |      4
(15 rows)

```

```

SELECT  * FROM pgr_KSP(
    'SELECT id, source, target, cost FROM edge_table',
    2, 12, 2, true, true
);
 seq | path_id | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
  1 |      1 |      1 |      2 |      4 |      1 |      0
  2 |      1 |      2 |      5 |      8 |      1 |      1
  3 |      1 |      3 |      6 |      9 |      1 |      2
  4 |      1 |      4 |      9 |     15 |      1 |      3
  5 |      1 |      5 |     12 |     -1 |      0 |      4
  6 |      2 |      1 |      2 |      4 |      1 |      0
  7 |      2 |      2 |      5 |      8 |      1 |      1
  8 |      2 |      3 |      6 |     11 |      1 |      2
  9 |      2 |      4 |     11 |     13 |      1 |      3
 10 |      2 |      5 |     12 |     -1 |      0 |      4
 11 |      3 |      1 |      2 |      4 |      1 |      0
 12 |      3 |      2 |      5 |     10 |      1 |      1
 13 |      3 |      3 |     10 |     12 |      1 |      2
 14 |      3 |      4 |     11 |     13 |      1 |      3
 15 |      3 |      5 |     12 |     -1 |      0 |      4
(15 rows)

```

Examples for queries marked as undirected with cost column The examples in this section use the following *Network for queries marked as undirected and only cost column is used*

```

SELECT * FROM pgr_KSP (
  'SELECT id, source, target, cost FROM edge_table',
  2, 12, 2, directed:=false
);

```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	2	4	1	0
2	1	2	5	8	1	1
3	1	3	6	9	1	2
4	1	4	9	15	1	3
5	1	5	12	-1	0	4
6	2	1	2	4	1	0
7	2	2	5	8	1	1
8	2	3	6	11	1	2
9	2	4	11	13	1	3
10	2	5	12	-1	0	4

(10 rows)

```

SELECT * FROM pgr_KSP (
  'SELECT id, source, target, cost FROM edge_table',
  2, 12, 2, directed:=false, heap_paths:=true
);

```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	2	4	1	0
2	1	2	5	8	1	1
3	1	3	6	9	1	2
4	1	4	9	15	1	3
5	1	5	12	-1	0	4
6	2	1	2	4	1	0
7	2	2	5	8	1	1
8	2	3	6	11	1	2
9	2	4	11	13	1	3
10	2	5	12	-1	0	4
11	3	1	2	4	1	0
12	3	2	5	10	1	1
13	3	3	10	12	1	2
14	3	4	11	13	1	3
15	3	5	12	-1	0	4

(15 rows)

See Also

- http://en.wikipedia.org/wiki/K_shortest_path_routing
- [Sample Data](#) network.

Indices and tables

- [genindex](#)
- [search](#)

pgr_dijkstraVia - Proposed

Name

`pgr_dijkstraVia` — Using dijkstra algorithm, it finds the route that goes through a list of vertices.



Fig. 5.10: Boost Graph Inside

Availability: 2.2.0

Synopsis

Given a list of vertices and a graph, this function is equivalent to finding the shortest path between $vertex_i$ and $vertex_{i+1}$ for all $i < size_of(vertex_ia)$.

The paths represents the sections of the route.

Note: This is a proposed function

Signature Summary

```
pgr_dijkstraVia(edges_sql, via_vertices)
pgr_dijkstraVia(edges_sql, via_vertices, directed, strict, U_turn_on_edge)

RETURNS SET OF (seq, path_pid, path_seq, start_vid, end_vid,
               node, edge, cost, agg_cost, route_agg_cost) or EMPTY SET
```

Signatures

Minimal Signature

```
pgr_dijkstraVia(edges_sql, via_vertices)
RETURNS SET OF (seq, path_pid, path_seq, start_vid, end_vid,
               node, edge, cost, agg_cost, route_agg_cost) or EMPTY SET
```

Example Find the route that visits the vertices 1 3 9 in that order

```
SELECT * FROM pgr_dijkstraVia(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table order by id',
  ARRAY[1, 3, 9]
);
```

seq	path_id	path_seq	start_vid	end_vid	node	edge	cost	agg_cost	route_agg_cost
1	1	1	1	3	1	1	1	0	0
2	1	2	1	3	2	4	1	1	1
3	1	3	1	3	5	8	1	2	2
4	1	4	1	3	6	9	1	3	3
5	1	5	1	3	9	16	1	4	4
6	1	6	1	3	4	3	1	5	5
7	1	7	1	3	3	-1	0	6	6
8	2	1	3	9	3	5	1	0	6
9	2	2	3	9	6	9	1	1	7
10	2	3	3	9	9	-2	0	2	8

(10 rows)

Complete Signature

```
pgr_dijkstraVia(edges_sql, via_vertices, directed, strict, U_turn_on_edge)
RETURNS SET OF (seq, path_pid, path_seq, start_vid, end_vid,
    node, edge, cost, agg_cost, route_agg_cost) or EMPTY SET
```

Example Find the route that visits the vertices 1 3 9 in that order on an undirected graph, avoiding U-turns when possible

```
SELECT * FROM pgr_dijkstraVia(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table order by id',
    ARRAY[1, 3, 9], false, strict:=true, U_turn_on_edge:=false
);
```

seq	path_id	path_seq	start_vid	end_vid	node	edge	cost	agg_cost	route_agg_cost
1	1	1	1	3	1	1	1	0	0
2	1	2	1	3	2	2	1	1	1
3	1	3	1	3	3	-1	0	2	2
4	2	1	3	9	3	5	1	0	2
5	2	2	3	9	6	9	1	1	3
6	2	3	3	9	9	-2	0	2	4

(6 rows)

Description of the Signature

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source</i> , <i>target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target</i> , <i>source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Default
edges_sql	TEXT	
via_vertices	ARRAY [ANY-INTEGER]	
directed	BOOLEAN	true
strict	BOOLEAN	false
U_turn_on_edge	BOOLEAN	true

Description of the parameters of the signatures

Parameter	Type	Description
edges_sql	TEXT	SQL query as described above.
via_vertices	ARRAY [ANY-INTEGER]	Array of vertices identifiers
directed	BOOLEAN	(optional) Default is true (is directed). When set to false as Undirected
strict	BOOLEAN	(optional) ignores if a subsection of the route is missing. Default is true (is directed). When set to false as Undirected
U_turn_on_edge	BOOLEAN	(optional) Default is true (is directed). When set to false as Undirected

Description of the return values Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
seq	BIGINT	Sequential value starting from 1.
path_pid	BIGINT	Identifier of the path.
path_seq	BIGINT	Sequential value starting from 1 for the path.
start_vid	BIGINT	Identifier of the starting vertex of the path.
end_vid	BIGINT	Identifier of the ending vertex of the path.
node	BIGINT	Identifier of the node in the path from start_vid to end_vid.
edge	BIGINT	Identifier of the edge used to go from node to the next node in the path sequence. -1 for the last node of the path. -2 for the last node of the route.
cost	FLOAT	Cost to traverse from node using edge to the next node in the route sequence.
agg_cost	FLOAT	Total cost from start_vid to end_vid of the path.
route_agg_cost	FLOAT	Total cost from start_vid of path_pid = 1 to end_vid of the current path_pid.

Examples

Example 1 Find the route that visits the vertices 1 5 3 9 4 in that order

```
SELECT * FROM pgr_dijkstraVia(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table order by id',
  ARRAY[1, 5, 3, 9, 4]
);
```

seq	path_id	path_seq	start_vid	end_vid	node	edge	cost	agg_cost	route_agg_cost
1	1	1	1	5	1	1	1	0	0
2	1	2	1	5	2	4	1	1	1
3	1	3	1	5	5	-1	0	2	2
4	2	1	5	3	5	8	1	0	2
5	2	2	5	3	6	9	1	1	3
6	2	3	5	3	9	16	1	2	4
7	2	4	5	3	4	3	1	3	5
8	2	5	5	3	3	-1	0	4	6
9	3	1	3	9	3	5	1	0	6
10	3	2	3	9	6	9	1	1	7
11	3	3	3	9	9	-1	0	2	8
12	4	1	9	4	9	16	1	0	8
13	4	2	9	4	4	-2	0	1	9

(13 rows)

Example 2 What's the aggregate cost of the third path?

```
SELECT agg_cost FROM pgr_dijkstraVia(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table order by id',
  ARRAY[1, 5, 3, 9, 4]
)
WHERE path_id = 3 AND edge < 0;
agg_cost
-----
2
(1 row)
```

Example 3 What's the route's aggregate cost of the route at the end of the third path?

```
SELECT route_agg_cost FROM pgr_dijkstraVia(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table order by id',
  ARRAY[1, 5, 3, 9, 4]
)
WHERE path_id = 3 AND edge < 0;
route_agg_cost
```



```

-----
                8
(1 row)

```

Example 4 How are the nodes visited in the route?

```

SELECT row_number() over () as node_seq, node
FROM   pgr_dijkstraVia(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table order by id',
    ARRAY[1, 5, 3, 9, 4]
)
WHERE  edge <> -1 ORDER BY seq;
 node_seq | node
-----+-----
         1 |    1
         2 |    2
         3 |    5
         4 |    6
         5 |    9
         6 |    4
         7 |    3
         8 |    6
         9 |    9
        10 |    4
(10 rows)

```

Example 5 What are the aggregate costs of the route when the visited vertices are reached?

```

SELECT path_id, route_agg_cost FROM pgr_dijkstraVia(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table order by id',
    ARRAY[1, 5, 3, 9, 4]
)
WHERE  edge < 0;
 path_id | route_agg_cost
-----+-----
        1 |             2
        2 |             6
        3 |             8
        4 |             9
(4 rows)

```

Example 6 show the route's seq and aggregate cost and a status of "passes in front" or "visits" node
9

```

SELECT seq, route_agg_cost, node, agg_cost ,
CASE WHEN edge = -1 THEN 'visits'
ELSE 'passes in front'
END as status
FROM   pgr_dijkstraVia(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table order by id',
    ARRAY[1, 5, 3, 9, 4])
WHERE  node = 9 and (agg_cost <> 0 or seq = 1);
 seq | route_agg_cost | node | agg_cost |      status
-----+-----+-----+-----+-----
    6 |             4 |    9 |         2 | passes in front
   11 |             8 |    9 |         2 | visits
(2 rows)

ROLLBACK;
ROLLBACK

```

See Also

- http://en.wikipedia.org/wiki/Dijkstra%27s_algorithm
- [Sample Data](#) network.

Indices and tables

- [genindex](#)
- [search](#)

The problem definition (Advanced documentation)

Given the following query:

```
pgr_dijkstra(sql, start_vid, end_vid, directed)
```

where $sql = \{(id_i, source_i, target_i, cost_i, reverse_cost_i)\}$

and

- $source = \bigcup source_i$,
- $target = \bigcup target_i$,

The graphs are defined as follows:

Directed graph

The weighted directed graph, $G_d(V, E)$, is defined by:

- the set of vertices V
 - $V = source \cup target \cup start_{vid} \cup end_{vid}$
- the set of edges E
 - $E = \begin{cases} \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} & \text{if } reverse_cost = \\ \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} & \text{if } reverse_cost \neq \end{cases}$

Undirected graph

The weighted undirected graph, $G_u(V, E)$, is defined by:

- the set of vertices V
 - $V = source \cup target \cup start_{vid} \cup end_{vid}$
- the set of edges E
 - $E = \begin{cases} \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, cost_i) \text{ when } cost \geq 0\} & \text{if } reverse_cost = \\ \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} \\ \cup \{(source_i, target_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} & \text{if } reverse_cost \neq \end{cases}$

The problem

Given:

- $start_{vid} \in V$ a starting vertex
- $end_{vid} \in V$ an ending vertex
- $G(V, E) = \begin{cases} G_d(V, E) & \text{if } directed = true \\ G_u(V, E) & \text{if } directed = false \end{cases}$

Then:

- $\pi = \{(path_seq_i, node_i, edge_i, cost_i, agg_cost_i)\}$

where:

- $path_seq_i = i$
- $path_seq_{|\pi|} = |\pi|$
- $node_i \in V$
- $node_1 = start_{vid}$
- $node_{|\pi|} = end_{vid}$
- $\forall i \neq |\pi|, (node_i, node_{i+1}, cost_i) \in E$
- $edge_i = \begin{cases} id_{(node_i, node_{i+1}, cost_i)} & \text{when } i \neq |\pi| \\ -1 & \text{when } i = |\pi| \end{cases}$
- $cost_i = cost_{(node_i, node_{i+1})}$
- $agg_cost_i = \begin{cases} 0 & \text{when } i = 1 \\ \sum_{k=1}^i cost_{(node_{k-1}, node_k)} & \text{when } i \neq 1 \end{cases}$

In other words: The algorithm returns a the shortest path between $start_{vid}$ and end_{vid} , if it exists, in terms of a sequence of

- $path_seq$ indicates the relative position in the path of the *node* or *edge*.
- $cost$ is the cost of the edge to be used to go to the next node.
- agg_cost is the cost from the $start_{vid}$ up to the node.

If there is no path, the resulting set is empty.

See Also

Indices and tables

- [genindex](#)
- [search](#)

5.1.5 pgr_trsp - Turn Restriction Shortest Path (TRSP)

Name

`pgr_trsp` — Returns the shortest path with support for turn restrictions.

Synopsis

The turn restricted shortest path (TRSP) is a shortest path algorithm that can optionally take into account complicated turn restrictions like those found in real world navigable road networks. Performamnce wise it is nearly as fast as the A* search but has many additional features like it works with edges rather than the nodes of the network. Returns a set of *pgr_costResult* (seq, id1, id2, cost) rows, that make up a path.

```
pgr_costResult[] pgr_trsp(sql text, source integer, target integer,
    directed boolean, has_rcost boolean [,restrict_sql text]);
```

```
pgr_costResult[] pgr_trsp(sql text, source_edge integer, source_pos float8,
    target_edge integer, target_pos float8,
    directed boolean, has_rcost boolean [,restrict_sql text]);
```

```
pgr_costResult3[] pgr_trspViaVertices(sql text, vids integer[],
    directed boolean, has_rcost boolean
    [, turn_restrict_sql text]);
```

```
pgr_costResult3[] pgr_trspViaEdges(sql text, eids integer[], pcts float8[],
    directed boolean, has_rcost boolean
    [, turn_restrict_sql text]);
```

Description

The Turn Restricted Shortest Path algorithm (TRSP) is similar to the shooting star in that you can specify turn restrictions.

The TRSP setup is mostly the same as *Dijkstra shortest path* with the addition of an optional turn restriction table. This provides an easy way of adding turn restrictions to a road network by placing them in a separate table.

sql a SQL query, which should return a set of rows with the following columns:

```
SELECT id, source, target, cost, [,reverse_cost] FROM edge_table
```

id int4 identifier of the edge

source int4 identifier of the source vertex

target int4 identifier of the target vertex

cost float8 value, of the edge traversal cost. A negative cost will prevent the edge from being inserted in the graph.

reverse_cost (optional) the cost for the reverse traversal of the edge. This is only used when the **directed** and **has_rcost** parameters are **true** (see the above remark about negative costs).

source int4 **NODE id** of the start point

target int4 **NODE id** of the end point

directed true if the graph is directed

has_rcost if **true**, the **reverse_cost** column of the SQL generated set of rows will be used for the cost of the traversal of the edge in the opposite direction.

restrict_sql (optional) a SQL query, which should return a set of rows with the following columns:

```
SELECT to_cost, target_id, via_path FROM restrictions
```

to_cost float8 turn restriction cost

target_id int4 target id

via_path text comma separated list of edges in the reverse order of rule

Another variant of TRSP allows to specify **EDGE id** of source and target together with a fraction to interpolate the position:

source_edge int4 **EDGE id** of the start edge
source_pos float8 fraction of 1 defines the position on the start edge
target_edge int4 **EDGE id** of the end edge
target_pos float8 fraction of 1 defines the position on the end edge

Returns set of *pgr_costResult[]*:

seq row sequence
id1 node ID
id2 edge ID (-1 for the last row)
cost cost to traverse from id1 using id2

History

- New in version 2.0.0

Support for Vias

Warning: The Support for Vias functions are prototypes. Not all corner cases are being considered.

We also have support for vias where you can say generate a from A to B to C, etc. We support both methods above only you pass an array of vertices or an array of edges and percentage position along the edge in two arrays.

sql a SQL query, which should return a set of rows with the following columns:

```
SELECT id, source, target, cost, [,reverse_cost] FROM edge_table
```

id int4 identifier of the edge
source int4 identifier of the source vertex
target int4 identifier of the target vertex
cost float8 value, of the edge traversal cost. A negative cost will prevent the edge from being inserted in the graph.
reverse_cost (optional) the cost for the reverse traversal of the edge. This is only used when the `directed` and `has_rcost` parameters are `true` (see the above remark about negative costs).

vids int4[] An ordered array of **NODE id** the path will go through from start to end.

directed true if the graph is directed

has_rcost if `true`, the `reverse_cost` column of the SQL generated set of rows will be used for the cost of the traversal of the edge in the opposite direction.

restrict_sql (optional) a SQL query, which should return a set of rows with the following columns:

```
SELECT to_cost, target_id, via_path FROM restrictions
```

to_cost float8 turn restriction cost
target_id int4 target id
via_path text comma separated list of edges in the reverse order of rule

Another variant of TRSP allows to specify **EDGE id** together with a fraction to interpolate the position:

eids int4 An ordered array of **EDGE id** that the path has to traverse

pcts float8 An array of fractional positions along the respective edges in **eids**, where 0.0 is the start of the edge and 1.0 is the end of the eadge.

Returns set of *pgr_costResult[]*:

seq row sequence

id1 route ID

id2 node ID

id3 edge ID (-1 for the last row)

cost cost to traverse from id2 using id3

History

- Via Support prototypes new in version 2.1.0

Examples

Without turn restrictions

```
SELECT * FROM pgr_trsp(
    'SELECT id::INTEGER, source::INTEGER, target::INTEGER, cost FROM edge_table',
    7, 12, false, false
);
 seq | id1 | id2 | cost
-----+-----+-----+-----
   0 |   7 |   6 |    1
   1 |   8 |   7 |    1
   2 |   5 |   8 |    1
   3 |   6 |   9 |    1
   4 |   9 |  15 |    1
   5 |  12 |  -1 |    0
(6 rows)
```

With turn restrictions

Then a query with turn restrictions is created as:

```
SELECT * FROM pgr_trsp(
    'SELECT id::INTEGER, source::INTEGER, target::INTEGER, cost FROM edge_table',
    2, 7, false, false,
    'SELECT to_cost, target_id::int4,
    from_edge || coalesce('',' || via_path, '') AS via_path
    FROM restrictions'
);
 seq | id1 | id2 | cost
-----+-----+-----+-----
   0 |   2 |   4 |    1
   1 |   5 |  10 |    1
   2 |  10 |  12 |    1
   3 |  11 |  11 |    1
   4 |   6 |   8 |    1
   5 |   5 |   7 |    1
   6 |   8 |   6 |    1
   7 |   7 |  -1 |    0
(8 rows)

SELECT * FROM pgr_trsp(
```

```

'SELECT id::INTEGER, source::INTEGER, target::INTEGER, cost FROM edge_table',
7, 11, false, false,
'SELECT to_cost, target_id::int4,
from_edge || coalesce('',' || via_path, '') AS via_path
FROM restrictions'
);
seq | id1 | id2 | cost
-----+-----+-----+-----
0 | 7 | 6 | 1
1 | 8 | 7 | 1
2 | 5 | 8 | 1
3 | 6 | 9 | 1
4 | 9 | 15 | 1
5 | 12 | 13 | 1
6 | 11 | -1 | 0
(7 rows)

```

An example query using vertex ids and via points:

```

SELECT * FROM pgr_trspViaVertices(
'SELECT id::INTEGER, source::INTEGER, target::INTEGER, cost FROM edge_table',
ARRAY[2,7,11]::INTEGER[],
false, false,
'SELECT to_cost, target_id::int4, from_edge ||
coalesce('',' || via_path, '') AS via_path FROM restrictions');
seq | id1 | id2 | id3 | cost
-----+-----+-----+-----+-----
1 | 1 | 2 | 4 | 1
2 | 1 | 5 | 10 | 1
3 | 1 | 10 | 12 | 1
4 | 1 | 11 | 11 | 1
5 | 1 | 6 | 8 | 1
6 | 1 | 5 | 7 | 1
7 | 1 | 8 | 6 | 1
8 | 2 | 7 | 6 | 1
9 | 2 | 8 | 7 | 1
10 | 2 | 5 | 8 | 1
11 | 2 | 6 | 9 | 1
12 | 2 | 9 | 15 | 1
13 | 2 | 12 | 13 | 1
14 | 2 | 11 | -1 | 0
(14 rows)

```

An example query using edge ids and vias:

```

SELECT * FROM pgr_trspViaEdges(
'SELECT id::INTEGER, source::INTEGER, target::INTEGER, cost,
reverse_cost FROM edge_table',
ARRAY[2,7,11]::INTEGER[],
ARRAY[0.5, 0.5, 0.5]::FLOAT[],
true,
true,
'SELECT to_cost, target_id::int4, FROM_edge ||
coalesce('',' || via_path, '') AS via_path FROM restrictions');
seq | id1 | id2 | id3 | cost
-----+-----+-----+-----+-----
1 | 1 | -1 | 2 | 0.5
2 | 1 | 2 | 4 | 1
3 | 1 | 5 | 8 | 1
4 | 1 | 6 | 9 | 1
5 | 1 | 9 | 16 | 1
6 | 1 | 4 | 3 | 1

```

7		1		3		5		1
8		1		6		8		1
9		1		5		7		1
10		2		5		8		1
11		2		6		9		1
12		2		9		16		1
13		2		4		3		1
14		2		3		5		1
15		2		6		11		0.5

(15 rows)

The queries use the [Sample Data](#) network.

See Also

- *pgr_costResult[]*

Indices and tables

- [genindex](#)
- [search](#)

5.1.6 Traveling Sales Person - Family of functions

- *pgr_TSP* - When input is given as matrix cell information.
- *pgr_eucledianTSP* - When input are coordinates.

pgr_TSP

Name

- *pgr_TSP* - Returns a route that visits all the nodes exactly once.

Availability: 2.0.0

- Signature changed 2.3.0

Synopsis

The travelling salesman problem (TSP) or travelling salesperson problem asks the following question:

- Given a list of cities and the distances between each pair of cities, what is the shortest possible route that visits each city exactly once and returns to the origin city?

This implementation uses simulated annealing to return the approximate solution when the input is given in the form of matrix cell contents. The matrix information must be symmetrical.

Signature Summary


```
pgr_TSP(matrix_cell_sql)
pgr_TSP(matrix_cell_sql,
        start_id, end_id,
        max_processing_time,
        tries_per_temperature, max_changes_per_temperature, max_consecutive_non_changes,
        initial_temperature, final_temperature, cooling_factor,
        randomize,
        RETURNS SETOF (seq, node, cost, agg_cost)
```

Signatures

Basic Use

```
pgr_TSP(matrix_cell_sql)
RETURNS SETOF (seq, node, cost, agg_cost)
```

Example

Because the documentation examples are auto generated and tested for non changing results, and the default is to have random execution, the example is wrapping the actual call.

```
WITH
query AS (
  SELECT * FROM pgr_TSP(
    $$
    SELECT * FROM pgr_dijkstraCostMatrix(
      'SELECT id, source, target, cost, reverse_cost FROM edge_table',
      (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 14),
      directed := false
    )
    $$
  )
)
SELECT agg_cost < 20 AS under_20 FROM query WHERE seq = 14;
 under_20
-----
 t
(1 row)
```

Complete Signature

```
pgr_TSP(matrix_cell_sql,
        start_id, end_id,
        max_processing_time,
        tries_per_temperature, max_changes_per_temperature, max_consecutive_non_changes,
        initial_temperature, final_temperature, cooling_factor,
        randomize,
        RETURNS SETOF (seq, node, cost, agg_cost)
```

Example:

```
SELECT * FROM pgr_TSP(
  $$
  SELECT * FROM pgr_dijkstraCostMatrix(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 14),
    directed := false
  )
  $$,
```

```

    start_id := 7,
    randomize := false
);
seq | node | cost | agg_cost
-----+-----+-----+-----
  1 |    7 |    1 |      0
  2 |    8 |    1 |      1
  3 |    5 |    1 |      2
  4 |    2 |    1 |      3
  5 |    1 |    2 |      4
  6 |    3 |    1 |      6
  7 |    4 |    1 |      7
  8 |    9 |    1 |      8
  9 |   12 |    1 |      9
 10 |   11 |    1 |     10
 11 |   10 |    1 |     11
 12 |   13 |    3 |     12
 13 |    6 |    3 |     15
 14 |    7 |    0 |     18
(14 rows)

```

Description of the Signatures

Description of the Matrix Cell SQL query

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex.
end_vid	BIGINT	Identifier of the ending vertex.
agg_cost	FLOAT	Cost for going from start_vid to end_vid

Can be Used with:

- *pgr_dijkstraCostMatrix - proposed*
- *pgr_withPointsCostMatrix - proposed*
- *pgr_floydWarshall*
- *pgr_johnson*

To generate a symmetric matrix

- `directed := false`.

If using `directed := true`, the resulting non symmetric matrix must be converted to symmetric by fixing the non symmetric values according to your application needs.

Description Of the Control parameters

.....

The control parameters are optional, and have a default value.

Parameter	Type	Default	Description
start_vid	<code>``BIGINT``</code>	<code>`0`</code>	The greedy part of the implementation v
end_vid	<code>``BIGINT``</code>	<code>`0`</code>	Last visiting vertex before returning t
max_processing_time	<code>``FLOAT``</code>	<code>`+infinity`</code>	Stop the annealing processing when the
tries_per_temperature	<code>``INTEGER``</code>	<code>`500`</code>	Maximum number of times a neighbor(s)
max_changes_per_temperature	<code>``INTEGER``</code>	<code>`60`</code>	Maximum number of times the solution i
max_consecutive_non_changes	<code>``INTEGER``</code>	<code>`100`</code>	Maximum number of consecutive times th
initial_temperature	<code>``FLOAT``</code>	<code>`100`</code>	Starting temperature.
final_temperature	<code>``FLOAT``</code>	<code>`0.1`</code>	Ending temperature.
cooling_factor	<code>``FLOAT``</code>	<code>`0.9`</code>	Value between between 0 and 1 (not inc

```

**randomize**          ``BOOLEAN``  `true`      Choose the random seed

                                - true: Use current time as seed
                                - false: Use `1` as seed. Using this v

```

Description of the return columns

.....

Returns set of ``(seq, node, cost, agg_cost)``

Column	Type	Description
seq	``INTEGER``	Row sequence.
node	``BIGINT``	Identifier of the node/coordinate/point.
cost	``FLOAT``	Cost to traverse from the current ``node`` ito the next ``node`` in the - ``0`` for the last row in the path sequence.
agg_cost	``FLOAT``	Aggregate cost from the ``node`` at ``seq = 1`` to the current node. - ``0`` for the first row in the path sequence.

Examples

Example Using with points of interest.

To generate a symmetric matrix:

- the **side** information of pointsOfInterest is ignored by not including it in the query
- and **directed := false**

```

SELECT * FROM pgr_TSP(
  $$
  SELECT * FROM pgr_withPointsCostMatrix(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
    'SELECT pid, edge_id, fraction from pointsOfInterest',
    array[-1, 3, 5, 6, -6], directed := false);
  $$,
  start_id := 5,
  randomize := false
);
 seq | node | cost | agg_cost
-----+-----+-----+-----
  1 |    5 |    1 |         0
  2 |    6 |    1 |         1
  3 |    3 |  1.6 |         2
  4 |   -1 |  1.3 |        3.6
  5 |   -6 |  0.3 |        4.9
  6 |    5 |    0 |        5.2
(6 rows)

```

The queries use the [Sample Data](#) network.

See Also

- *Traveling Sales Person - Family of functions*
- http://en.wikipedia.org/wiki/Traveling_salesman_problem
- http://en.wikipedia.org/wiki/Simulated_annealing

Indices and tables

- [genindex](#)
- [search](#)

pgr_eucledianTSP

Name

pgr_eucledianTSP - Returns a route that visits all the coordinates pairs exactly once.

Availability: 2.3.0

Synopsis

The travelling salesman problem (TSP) or travelling salesperson problem asks the following question:

- Given a list of cities and the distances between each pair of cities, what is the shortest possible route that visits each city exactly once and returns to the origin city?

This implementation uses simulated annealing to return the approximate solution when the input is given in the form of coordinates.

Signature Summary

```
pgr_eucledianTSP(coordinates_sql)
pgr_eucledianTSP(coordinates_sql,
    start_id, end_id,
    max_processing_time,
    tries_per_temperature, max_changes_per_temperature, max_consecutive_non_changes,
    initial_temperature, final_temperature, cooling_factor,
    randomize,
    RETURNS SETOF (seq, node, cost, agg_cost)
```

Signatures

Minimal Signature

```
pgr_eucledianTSP(coordinates_sql)
RETURNS SETOF (seq, node, cost, agg_cost)
```

Example

Because the documentation examples are auto generated and tested for non changing results, and the default is to have random execution, the example is wrapping the actual call.

```

WITH
query AS (
  SELECT * FROM pgr_euclidianTSP(
    $$
    SELECT id, st_X(the_geom) AS x, st_Y(the_geom) AS y FROM edge_table_vertices_pgr
    $$
  )
)
SELECT agg_cost < 20 AS under_20 FROM query WHERE seq = 18;
  under_20
-----
 t
(1 row)

```

Complete Signature

```

pgr_euclidianTSP(coordinates_sql,
  start_id, end_id,
  max_processing_time,
  tries_per_temperature, max_changes_per_temperature, max_consecutive_non_changes,
  initial_temperature, final_temperature, cooling_factor,
  randomize,
  RETURNS SETOF (seq, node, cost, agg_cost)

```

Example:

```

SELECT* from pgr_euclidianTSP(
  $$
  SELECT id, st_X(the_geom) AS x, st_Y(the_geom) AS y FROM edge_table_vertices_pgr
  $$,
  tries_per_temperature := 3,
  cooling_factor := 0.5,
  randomize := false
);

```

seq	node	cost	agg_cost
1	1	1.4142135623731	0
2	3	1	1.4142135623731
3	4	1	2.41421356237309
4	9	0.58309518948453	3.41421356237309
5	16	0.58309518948453	3.99730875185762
6	6	1	4.58040394134215
7	5	1	5.58040394134215
8	8	1	6.58040394134215
9	7	1.58113883008419	7.58040394134215
10	14	1.49999999999999	9.16154277142634
11	15	0.5	10.6615427714253
12	13	1.5	11.1615427714253
13	17	1.11803398874989	12.6615427714253
14	12	1	13.7795767601752
15	11	1	14.7795767601752
16	10	2	15.7795767601752
17	2	1	17.7795767601752
18	1	0	18.7795767601752

(18 rows)

Description of the Signatures

Description of the coordinates SQL query

Column	Type	Description
id	BIGINT	Identifier of the coordinate. (optional)
x	FLOAT	X value of the coordinate.
y	FLOAT	Y value of the coordinate.

When the value of **id** is not given then the coordinates will receive an **id** starting from 1, in the order given.

Description Of the Control parameters

.....

The control parameters are optional, and have a default value.

Parameter	Type	Default	Description
start_vid	<code>``BIGINT``</code>	<code>`0`</code>	The greedy part of the implementation v
end_vid	<code>``BIGINT``</code>	<code>`0`</code>	Last visiting vertex before returning t
max_processing_time	<code>``FLOAT``</code>	<code>`+infinity`</code>	Stop the annealing processing when the
tries_per_temperature	<code>``INTEGER``</code>	<code>`500`</code>	Maximum number of times a neighbor(s) i
max_changes_per_temperature	<code>``INTEGER``</code>	<code>`60`</code>	Maximum number of times the solution i
max_consecutive_non_changes	<code>``INTEGER``</code>	<code>`100`</code>	Maximum number of consecutive times the
initial_temperature	<code>``FLOAT``</code>	<code>`100`</code>	Starting temperature.
final_temperature	<code>``FLOAT``</code>	<code>`0.1`</code>	Ending temperature.
cooling_factor	<code>``FLOAT``</code>	<code>`0.9`</code>	Value between between 0 and 1 (not inc
randomize	<code>``BOOLEAN``</code>	<code>`true`</code>	Choose the random seed
			- true: Use current time as seed
			- false: Use `1` as seed. Using this v

Description of the return columns

.....

Returns set of ```(seq, node, cost, agg_cost)```

Column	Type	Description
seq	<code>``INTEGER``</code>	Row sequence.
node	<code>``BIGINT``</code>	Identifier of the node/coordinate/point.
cost	<code>``FLOAT``</code>	Cost to traverse from the current <code>``node``</code> ito the next <code>``node``</code> in the - <code>``0``</code> for the last row in the path sequence.
agg_cost	<code>``FLOAT``</code>	Aggregate cost from the <code>``node``</code> at <code>``seq = 1``</code> to the current node. - <code>``0``</code> for the first row in the path sequence.

Examples**Example** Skipping the Simulated Annealing & showing some process information

```
SET client_min_messages TO DEBUG1;
SET
SELECT* from pgr_euclidianTSP(
    $$
    SELECT id, st_X(the_geom) AS x, st_Y(the_geom) AS y FROM edge_table_vertices_pgr
```

```

$$,
  tries_per_temperature := 0,
  randomize := false
);
DEBUG:  pgr_euclidianTSP Processing Information
Initializing tsp class ---> tsp.greedyInitial ---> tsp.annealing ---> OK

Cycle(100)          total changes =0          0 were because  delta energy < 0
Total swaps: 3
Total slides: 0
Total reverses: 0
Times best tour changed: 4
Best cost reached = 18.7796
 seq | node |      cost      |      agg_cost
-----+-----+-----+-----
  1 |   1 | 1.4142135623731 |          0
  2 |   3 |                | 1.4142135623731
  3 |   4 |                | 2.41421356237309
  4 |   9 | 0.58309518948453 | 3.41421356237309
  5 |  16 | 0.58309518948453 | 3.99730875185762
  6 |   6 |                | 4.58040394134215
  7 |   5 |                | 5.58040394134215
  8 |   8 |                | 6.58040394134215
  9 |   7 | 1.58113883008419 | 7.58040394134215
 10 |  14 | 1.49999999999999 | 9.16154277142634
 11 |  15 |                | 10.6615427714253
 12 |  13 |                | 11.1615427714253
 13 |  17 | 1.11803398874989 | 12.6615427714253
 14 |  12 |                | 13.7795767601752
 15 |  11 |                | 14.7795767601752
 16 |  10 |                | 15.7795767601752
 17 |   2 |                | 17.7795767601752
 18 |   1 |                | 18.7795767601752
(18 rows)

```

The queries use the [Sample Data](#) network.

History

- New in version 2.3.0

See Also

- *Traveling Sales Person - Family of functions*
- http://en.wikipedia.org/wiki/Traveling_salesman_problem
- http://en.wikipedia.org/wiki/Simulated_annealing

Indices and tables

- [genindex](#)
- [search](#)

General Information

Origin

The traveling sales person problem was studied in the 18th century by mathematicians Sir William Rowan Hamilton and Thomas Penyngton Kirkman.

A discussion about the work of Hamilton & Kirkman can be found in the book **Graph Theory (Biggs et al. 1976)**.

- ISBN-13: 978-0198539162
- ISBN-10: 0198539169

It is believed that the general form of the TSP have been first studied by Kalr Menger in Vienna and Harvard. The problem was later promoted by Hassler, Whitney & Merrill at Princeton. A detailed description about the connection between Menger & Whitney, and the development of the TSP can be found in [On the history of combinatorial optimization \(till 1960\)](#)¹⁴

Problem Definition

Given a collection of cities and travel cost between each pair, find the cheapest way for visiting all of the cities and returning to the starting point.

Characteristics

- The travel costs are symmetric:
 - traveling costs from city A to city B are just as much as traveling from B to A.
- This problem is an NP-hard optimization problem.
- To calculate the number of different tours through n cities:
 - Given a starting city,
 - There are $n - 1$ choices for the second city,
 - And $n - 2$ choices for the third city, etc.
 - Multiplying these together we get $(n - 1)! = (n - 1)(n - 2)..1$.
 - Now since our travel costs do not depend on the direction we take around the tour:
 - * this number by 2
 - * $(n - 1)!/2$.

TSP & Simulated Annealing

The simulated annealing algorithm was originally inspired from the process of annealing in metal work.

Annealing involves heating and cooling a material to alter its physical properties due to the changes in its internal structure. As the metal cools its new structure becomes fixed, consequently causing the metal to retain its newly obtained properties. [\[C001\]](#)

Pseudocode

Given an initial solution, the simulated annealing process, will start with a high temperature and gradually cool down until the desired temperature is reached.

For each temperature, a neighbouring new solution **snew** is calculated. The higher the temperature the higher the probability of accepting the new solution as a possible better solution.

¹⁴<http://www.cwi.nl/lex/files/histco.ps>

Once the desired temperature is reached, the best solution found is returned

```
Solution = initial_solution;

temperature = initial_temperature;
while (temperature > final_temperature) {

    do tries_per_temperature times {
        snw = neighbour(solution);
        If P(E(solution), E(snw), T) >= random(0, 1)
            solution = snw;
    }

    temperature = temperature * cooling_factor;
}
```

Output: the best solution

pgRouting Implementation

pgRouting's implementation adds some extra parameters to allow some exit controls within the simulated annealing process.

To cool down faster to the next temperature:

- `max_changes_per_temperature`: limits the number of changes in the solution per temperature
- `max_consecutive_non_changes`: limits the number of consecutive non changes per temperature

This is done by doing some book keeping on the times **solution = snw;** is executed.

- `max_changes_per_temperature`: Increases by one when **solution** changes
- `max_consecutive_non_changes`: Reset to 0 when **solution** changes, and increased each **try**

Additionally to stop the algorithm at a higher temperature than the desired one:

- `max_processing_time`: limits the time the simulated annealing is performed.
- book keeping is done to see if there was a change in **solution** on the last temperature

Note that, if no change was found in the first **max_consecutive_non_changes** tries, then the simulated annealing will stop.

```
Solution = initial_solution;

temperature = initial_temperature;
while (temperature > final_temperature) {

    do tries_per_temperature times {
        snw = neighbour(solution);
        If P(E(solution), E(snw), T) >= random(0, 1)
            solution = snw;

        when max_changes_per_temperature is reached
            or max_consecutive_non_changes is reached
            BREAK;
    }

    temperature = temperature * cooling_factor;
    when no changes were done in the current temperature
        or max_processing_time has being reached
        BREAK;
}
```

Output: the best solution

Choosing parameters

There is no exact rule on how the parameters have to be chose, it will depend on the special characteristics of the problem.

- Your computational time is crucial, then put your time limit to **max_processing_time**.
- Make the **tries_per_tempture** depending on the number of cities, for example:
 - Useful to estimate the time it takes to do one cycle: use l
 - * this will help to set a reasonable **max_processing_time**
 - $n * (n - 1)$
 - $500 * n$
- For a faster decreasing the temperature set **cooling_factor** to a smaller number, and set to a higher number for a slower decrease.
- When for the same given data the same results are needed, set **randomize** to *false*.
 - When estimating how long it takes to do one cycle: use *false*

A recommendation is to play with the values and see what fits to the particular data.

Description Of the Control parameters

The control parameters are optional, and have a default value.

Parameter	Type	Default	Description
start_vid	BIGINT	<i>0</i>	The greedy part of the implementation will use this identifier.
end_vid	BIGINT	<i>0</i>	Last visiting vertex before returning to start_vid.
max_processing_time	FLOAT	<i>+infinity</i>	Stop the annealing processing when the value is reached.
tries_per_temperature	INTEGER	<i>500</i>	Maximum number of times a neighbor(s) is searched in each temperature.
max_changes_per_temperature	INTEGER	<i>60</i>	Maximum number of times the solution is changed in each temperature.
max_consecutive_non_changes	INTEGER	<i>100</i>	Maximum number of consecutive times the solution is not changed in each temperature.
initial_temperature	FLOAT	<i>100</i>	Starting temperature.
final_temperature	FLOAT	<i>0.1</i>	Ending temperature.
cooling_factor	FLOAT	<i>0.9</i>	Value between 0 and 1 (not including) used to calculate the next temperature.
randomize	BOOLEAN	<i>true</i>	Choose the random seed <ul style="list-style-type: none"> • true: Use current time as seed • false: Use 1 as seed. Using this value will get the same results with the same data in each execution.

Description of the return columns

Returns set of (seq, node, cost, agg_cost)

Column	Type	Description
seq	INTEGER	Row sequence.
node	BIGINT	Identifier of the node/coordinate/point.
cost	FLOAT	Cost to traverse from the current node to the next node <ul style="list-style-type: none"> • 0 for the last row in the path sequence.
agg_cost	FLOAT	Aggregate cost from the node at seq = 1 to the current node <ul style="list-style-type: none"> • 0 for the first row in the path sequence.

See Also

References

- http://en.wikipedia.org/wiki/Traveling_salesman_problem
- http://en.wikipedia.org/wiki/Simulated_annealing

Indices and tables

- [genindex](#)
- [search](#)

5.1.7 Driving Distance - Category

- *pgr_drivingDistance* - Driving Distance based on *pgr_dijkstra*
- *pgr_withPointsDD* - *Proposed* - Driving Distance based on *pgr_withPoints*
- Post pocessing
 - *pgr_alphaShape* - Alpha shape computation
 - *pgr_pointsAsPolygon* - Polygon around a set of points

pgr_alphaShape

Name

`pgr_alphaShape` — Core function for alpha shape computation.

Synopsis

Returns a table with (x, y) rows that describe the vertices of an alpha shape.

```
table() pgr_alphaShape(text sql [, float8 alpha]);
```

Description

sql text a SQL query, which should return a set of rows with the following columns:

```
SELECT id, x, y FROM vertex_table
```

id int4 identifier of the vertex

x float8 x-coordinate

y float8 y-coordinate

alpha (optional) float8 alpha value. If specified alpha value equals 0 (default), then optimal alpha value is used. For more information, see [CGAL - 2D Alpha Shapes¹⁵](#).

Returns a vertex record for each row:

x x-coordinate

y y-coordinate

¹⁵http://doc.cgal.org/latest/Alpha_shapes_2/group__PkgAlphaShape2.html

If a result includes multiple outer/inner rings, return those with separator row (x=NULL and y=NULL).

History

- Renamed in version 2.0.0
- Added alpha argument with default 0 (use optimal value) in version 2.1.0
- Supported to return multiple outer/inner ring coordinates with separator row (x=NULL and y=NULL) in version 2.1.0

Examples

PgRouting's alpha shape implementation has no way to control the order of the output points, so the actual output might be different for the same input data. The first query, has the output ordered, the second query shows an example usage:

Example: the (ordered) results

```
SELECT * FROM pgr_alphaShape(
  'SELECT id::integer, ST_X(the_geom)::float AS x, ST_Y(the_geom)::float AS y
   FROM edge_table_vertices_pgr') ORDER BY x, y;
```

x	y
0	2
0.5	3.5
2	0
2	4
3.5	4
4	1
4	2
4	3

(8 rows)

Example: calculating the area

Steps:

- **Calculates the alpha shape**
 - the ORDER BY clause is not used.
- constructs a polygon
- and computes the area

```
SELECT round(ST_Area(ST_MakePolygon(ST_AddPoint(foo.openline, ST_StartPoint(foo.openline))))::numeric, 2) AS
FROM (
  SELECT ST_MakeLine(points ORDER BY id) AS openline
  FROM (
    SELECT ST_MakePoint(x, y) AS points, row_number() over() AS id
    FROM pgr_alphaShape(
      'SELECT id::integer, ST_X(the_geom)::float AS x, ST_Y(the_geom)::float AS y
       FROM edge_table_vertices_pgr')
    ) AS a
  ) AS foo;
st_area
-----
11.75
```

(1 row)

The queries use the [Sample Data](#) network.

See Also

- *pgr_drivingDistance* - Driving Distance
- *pgr_pointsAsPolygon* - Polygon around set of points

Indices and tables

- genindex
- search

pgr_pointsAsPolygon

Name

`pgr_pointsAsPolygon` — Draws an alpha shape around given set of points.

Synopsis

Returns the alpha shape as (multi)polygon geometry.

<code>geometry pgr_pointsAsPolygon(text sql [, float8 alpha]);</code>

Description

sql text a SQL query, which should return a set of rows with the following columns:

<code>SELECT id, x, y FROM vertex_result;</code>
--

id int4 identifier of the vertex

x float8 x-coordinate

y float8 y-coordinate

alpha (optional) float8 alpha value. If specified alpha value equals 0 (default), then optimal alpha value is used. For more information, see [CGAL - 2D Alpha Shapes¹⁶](#).

Returns a (multi)polygon geometry (with holes).

History

- Renamed in version 2.0.0
- Added alpha argument with default 0 (use optimal value) in version 2.1.0
- Supported to return a (multi)polygon geometry (with holes) in version 2.1.0

¹⁶http://doc.cgal.org/latest/Alpha_shapes_2/group__PkgAlphaShape2.html

Examples

In the following query there is no way to control which point in the polygon is the first in the list, so you may get similar but different results than the following which are also correct.

```
SELECT ST_AsText(pgr_pointsAsPolygon('SELECT id::integer, ST_X(the_geom)::float AS x, ST_Y(the_geom)::float AS y
FROM edge_table_vertices_pgr'));
      st_astext
-----
POLYGON((2 4,3.5 4,4 3,4 2,4 1,2 0,0 2,0.5 3.5,2 4))
(1 row)
```

The query use the [Sample Data](#) network.

See Also

- *pgr_drivingDistance* - Driving Distance
- *pgr_alphaShape* - Alpha shape computation

Indices and tables

- genindex
- search

See Also

Indices and tables

- genindex
- search

5.1.8 See Also

Indices and tables

- genindex
- search

All Pairs - Family of Functions

- *pgr_floydWarshall* - Floyd-Warshall's Algorithm
- *pgr_johnson* - Johnson's Algorithm

pgr_aStar - Shortest Path A*

pgr_bdAstar - Bi-directional A* Shortest Path

pgr_bdDijkstra - Bi-directional Dijkstra Shortest Path

Dijkstra - Family of functions

- *pgr_dijkstra* - Dijkstra's algorithm for the shortest paths.
- *pgr_dijkstraCost* - Get the aggregate cost of the shortest paths.
- *pgr_dijkstraCostMatrix* - *proposed* - Use *pgr_dijkstra* to create a costs matrix.

- *pgr_drivingDistance* - Use *pgr_dijkstra* to calculate catchment information.
- *pgr_KSP* - Use Yen algorithm with *pgr_dijkstra* to get the K shortest paths.
- *pgr_dijkstraVia* - *Proposed* - Get a route of a sequence of vertices.

pgr_KSP - K-Shortest Path

pgr_trsp - Turn Restriction Shortest Path (TRSP)

Traveling Sales Person - Family of functions

- *pgr_TSP* - When input is given as matrix cell information.
- *pgr_euclidianTSP* - When input are coordinates.

Driving Distance - Category

- *pgr_drivingDistance* - Driving Distance based on *pgr_dijkstra*
- *pgr_withPointsDD* - *Proposed* - Driving Distance based on *pgr_withPoints*
- Post processing
 - *pgr_alphaShape* - Alpha shape computation
 - *pgr_pointsAsPolygon* - Polygon around a set of points

Available Functions but not official pgRouting functions

- *Stable Proposed Functions*
- *Experimental Functions*

6.1 Stable Proposed Functions

Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.

As part of the *Dijkstra - Family of functions*

- *pgr_dijkstraCostMatrix - proposed* Use pgr_dijkstra to calculate a cost matrix.
- *pgr_dijkstraVia - Proposed* - Use pgr_dijkstra to make a route via vertices.

Families

aStar - Family of functions

- *pgr_aStar* - A* algorithm for the shortest path.
- *pgr_aStarCost - proposed* - Get the aggregate cost of the shortest paths.
- *pgr_aStarCostMatrix - proposed* - Get the cost matrix of the shortest paths.

Bidirectional A - Family of functions*

- *pgr_bdAstar* - Bidirectional A* algorithm for obtaining paths.
- *pgr_bdAstarCost - Proposed* - Bidirectional A* algorithm to calculate the cost of the paths.
- *pgr_bdAstarCostMatrix - proposed* - Bidirectional A* algorithm to calculate a cost matrix of paths.

Bidirectional Dijkstra - Family of functions

- *pgr_bdDijkstra* - Bidirectional Dijkstra algorithm for the shortest paths.
- *pgr_bdDijkstraCost - Proposed* - Bidirectional Dijkstra to calculate the cost of the shortest paths

- *pgr_bdDijkstraCostMatrix - proposed* - Bidirectional Dijkstra algorithm to create a matrix of costs of the shortest paths.

Flow - Family of functions

- *pgr_maxFlow - Proposed* - Only the Max flow calculation using Push and Relabel algorithm.
- *pgr_boykovKolmogorov - Proposed* - Boykov and Kolmogorov with details of flow on edges.
- *pgr_edmondsKarp - Proposed* - Edmonds and Karp algorithm with details of flow on edges.
- *pgr_pushRelabel - Proposed* - Push and relabel algorithm with details of flow on edges.
- Applications
 - *pgr_edgeDisjointPaths - Proposed* - Calculates edge disjoint paths between two groups of vertices.
 - *pgr_maxCardinalityMatch - Proposed* - Calculates a maximum cardinality matching in a graph.

withPoints - Family of functions

- *pgr_withPoints - Proposed* - Route from/to points anywhere on the graph.
- *pgr_withPointsCost - Proposed* - Costs of the shortest paths.
- *pgr_withPointsCostMatrix - proposed* - Costs of the shortest paths.
- *pgr_withPointsKSP - Proposed* - K shortest paths.
- *pgr_withPointsDD - Proposed* - Driving distance.

categories

Cost - Category

- *pgr_aStarCost – proposed*
- *pgr_bdAstarCost - Proposed*
- *pgr_bdDijkstraCost - Proposed*
- *pgr_dijkstraCost*
- *pgr_withPointsCost - Proposed*

Cost Matrix - Category

- *pgr_aStarCostMatrix - proposed*
- *pgr_bdAstarCostMatrix - proposed*
- *pgr_bdDijkstraCostMatrix - proposed*
- *pgr_dijkstraCostMatrix - proposed*
- *pgr_withPointsCostMatrix - proposed*

KSP Category

- *pgr_KSP* - Driving Distance based on *pgr_dijkstra*
- *pgr_withPointsKSP - Proposed* - Driving Distance based on *pgr_dijkstra*

6.1.1 aStar - Family of functions

The A* (pronounced “A Star”) algorithm is based on Dijkstra’s algorithm with a heuristic that allow it to solve most shortest path problems by evaluation only a sub-set of the overall graph.

- *pgr_aStar* - A* algorithm for the shortest path.
- *pgr_aStarCost – proposed* - Get the aggregate cost of the shortest paths.

- *pgr_aStarCostMatrix* - *proposed* - Get the cost matrix of the shortest paths.

pgr_aStar

Name

pgr_aStar — Returns the shortest path using A* algorithm.



Fig. 6.1: Boost Graph Inside

Availability:

- pgr_astar(one to one) 2.0.0, Signature changed 2.3.0
- pgr_astar(other signatures) 2.4.0

Characteristics

The main Characteristics are:

- Process is done only on edges with positive costs.
- Vertices of the graph are:
 - **positive** when it belongs to the edges_sql
- Values are returned when there is a path.
 - When the starting vertex and ending vertex are the same, there is no path.
 - * The agg_cost the non included values (v, v) is 0
 - When the starting vertex and ending vertex are the different and there is no path:
 - * The agg_cost the non included values (u, v) is ∞
- When (x,y) coordinates for the same vertex identifier differ:
 - A random selection of the vertex's (x,y) coordinates is used.
- Running time: $O((E + V) * \log V)$

Signature Summary

```
pgr_aStar(edges_sql, start_vid, end_vid)
pgr_aStar(edges_sql, start_vid, end_vid, directed, heuristic, factor, epsilon)
```

Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.

```
pgr_aStar(edges_sql, start_vid, end_vids, directed, heuristic, factor, epsilon) -- proposed
pgr_aStar(edges_sql, starts_vid, end_vid, directed, heuristic, factor, epsilon) -- proposed
pgr_aStar(edges_sql, starts_vid, end_vids, directed, heuristic, factor, epsilon) -- proposed
RETURNS SET OF (seq, path_seq [, start_vid] [, end_vid], node, edge, cost, agg_cost)
OR EMPTY SET
```

Signatures

Minimal Signature

```
pgr_aStar(edges_sql, start_vid, end_vid)
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost)
```

Example Using the defaults

```
SELECT * FROM pgr_astar(
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
  2, 12);
```

seq	path_seq	node	edge	cost	agg_cost
1	1	2	4	1	0
2	2	5	10	1	1
3	3	10	12	1	2
4	4	11	13	1	3
5	5	12	-1	0	4

(5 rows)

One to One

```
pgr_aStar(edges_sql, start_vid, end_vid, directed, heuristic, factor, epsilon)
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost)
```

Example Undirected using Heuristic 2

```
SELECT * FROM pgr_astar(
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
  2, 12,
  directed := false, heuristic := 2);
```

seq	path_seq	node	edge	cost	agg_cost
1	1	2	2	1	0
2	2	3	3	1	1
3	3	4	16	1	2
4	4	9	15	1	3
5	5	12	-1	0	4

(5 rows)

One to many

```
pgr_aStar(edges_sql, start_vid, end_vids, directed, heuristic, factor, epsilon) -- Proposed
RETURNS SET OF (seq, path_seq, end_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from one **start_vid** to each **end_vid** in **end_vids**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Using this signature, will load once the graph and perform a one to one *pgr_astar* where the starting vertex is fixed, and stop when all **end_vids** are reached.

- The result is equivalent to the union of the results of the one to one *pgr_astar*.
- The extra **end_vid** in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_astar(
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
  2, ARRAY[3, 12], heuristic := 2);
```

seq	path_seq	end_vid	node	edge	cost	agg_cost
1	1	3	2	4	1	0
2	2	3	5	8	1	1
3	3	3	6	9	1	2
4	4	3	9	16	1	3
5	5	3	4	3	1	4
6	6	3	3	-1	0	5
7	1	12	2	4	1	0
8	2	12	5	10	1	1
9	3	12	10	12	1	2
10	4	12	11	13	1	3
11	5	12	12	-1	0	4

(11 rows)

Many to One

```
pgr_aStar(edges_sql, starts_vid, end_vid, directed, heuristic, factor, epsilon) -- Proposed
RETURNS SET OF (seq, path_seq, start_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from each **start_vid** in **start_vids** to one **end_vid**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Using this signature, will load once the graph and perform several one to one *pgr_astar* where the ending vertex is fixed.

- The result is the union of the results of the one to one *pgr_astar*.
- The extra **start_vid** in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_astar(
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
  ARRAY[7, 2], 12, heuristic := 0);
```

seq	path_seq	start_vid	node	edge	cost	agg_cost
1	1	2	2	4	1	0
2	2	2	5	10	1	1
3	3	2	10	12	1	2
4	4	2	11	13	1	3
5	5	2	12	-1	0	4

```

 6 |          1 |          7 |    7 |    6 |    1 |    0
 7 |          2 |          7 |    8 |    7 |    1 |    1
 8 |          3 |          7 |    5 |   10 |    1 |    2
 9 |          4 |          7 |   10 |   12 |    1 |    3
10 |          5 |          7 |   11 |   13 |    1 |    4
11 |          6 |          7 |   12 |   -1 |    0 |    5
(11 rows)

```

Many to Many

```

pgr_aStar(edges_sql, starts_vid, end_vids, directed, heuristic, factor, epsilon) -- Proposed
RETURNS SET OF (seq, path_seq, start_vid, end_vid, node, edge, cost, agg_cost) or EMPTY SET

```

This signature finds the shortest path from each **start_vid** in **start_vids** to each **end_vid** in **end_vids**:

- on a **directed** graph when **directed** flag is missing or is set to true.
- on an **undirected** graph when **directed** flag is set to false.

Using this signature, will load once the graph and perform several one to Many *pgr_dijkstra* for all **start_vids**.

- The result is the union of the results of the one to one *pgr_dijkstra*.
- The extra **start_vid** in the result is used to distinguish to which path it belongs.

The extra **start_vid** and **end_vid** in the result is used to distinguish to which path it belongs.

Example

```

SELECT * FROM pgr_astar(
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
  ARRAY[7, 2], ARRAY[3, 12], heuristic := 2);
 seq | path_seq | start_vid | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----+-----
  1 |         1 |         2 |        3 |    2 |    4 |    1 |         0
  2 |         2 |         2 |        3 |    5 |    8 |    1 |         1
  3 |         3 |         2 |        3 |    6 |    9 |    1 |         2
  4 |         4 |         2 |        3 |    9 |   16 |    1 |         3
  5 |         5 |         2 |        3 |    4 |    3 |    1 |         4
  6 |         6 |         2 |        3 |    3 |   -1 |    0 |         5
  7 |         1 |         7 |        3 |    7 |    6 |    1 |         0
  8 |         2 |         7 |        3 |    8 |    7 |    1 |         1
  9 |         3 |         7 |        3 |    5 |    8 |    1 |         2
10 |         4 |         7 |        3 |    6 |    9 |    1 |         3
11 |         5 |         7 |        3 |    9 |   16 |    1 |         4
12 |         6 |         7 |        3 |    4 |    3 |    1 |         5
13 |         7 |         7 |        3 |    3 |   -1 |    0 |         6
14 |         1 |         2 |       12 |    2 |    4 |    1 |         0
15 |         2 |         2 |       12 |    5 |   10 |    1 |         1
16 |         3 |         2 |       12 |   10 |   12 |    1 |         2
17 |         4 |         2 |       12 |   11 |   13 |    1 |         3
18 |         5 |         2 |       12 |   12 |   -1 |    0 |         4
19 |         1 |         7 |       12 |    7 |    6 |    1 |         0
20 |         2 |         7 |       12 |    8 |    7 |    1 |         1
21 |         3 |         7 |       12 |    5 |   10 |    1 |         2
22 |         4 |         7 |       12 |   10 |   12 |    1 |         3
23 |         5 |         7 |       12 |   11 |   13 |    1 |         4
24 |         6 |         7 |       12 |   12 |   -1 |    0 |         5
(24 rows)

```

Description of the Signatures

Description of the edges_sql query for astar like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.
x1	ANY-NUMERICAL		X coordinate of <i>source</i> vertex.
y1	ANY-NUMERICAL		Y coordinate of <i>source</i> vertex.
x2	ANY-NUMERICAL		X coordinate of <i>target</i> vertex.
y2	ANY-NUMERICAL		Y coordinate of <i>target</i> vertex.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type
edges_sql	TEXT
start_vid	ANY-INTEGER
end_vid	ANY-INTEGER
directed	BOOLEAN
heuristic	INTEGER
factor	FLOAT
epsilon	FLOAT

Description of the return values for a path Returns set of (seq, path_seq [, start_vid] [, end_vid], node, edge, cost, agg_cost)

Column	Type	Description
seq	INT	Sequential value starting from 1 .
path_id	INT	Path identifier. Has value 1 for the first of a path. Used when there are multiple paths for the same start_vid to end_vid combination.
path_seq	INT	Relative position in the path. Has value 1 for the beginning of a path.
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
node	BIGINT	Identifier of the node in the path from start_vid to end_vid.
edge	BIGINT	Identifier of the edge used to go from node to the next node in the path sequence. -1 for the last node of the path.
cost	FLOAT	Cost to traverse from node using edge to the next node in the path sequence.
agg_cost	FLOAT	Aggregate cost from start_v to node.

See Also

- *aStar - Family of functions*
- [Sample Data](#)
- http://www.boost.org/libs/graph/doc/astar_search.html
- http://en.wikipedia.org/wiki/A*_search_algorithm

Indices and tables

- [genindex](#)
- [search](#)

pgr_aStarCost – proposed

Name

`pgr_aStarCost` — Returns the aggregate cost shortest path using *aStar - Family of functions* algorithm.



Fig. 6.2: Boost Graph Inside

Availability: 2.4.0

Signature Summary

Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.

```
pgr_aStarCost(edges_sql, start_vid, end_vid) -- Proposed
pgr_aStarCost(edges_sql, start_vid, end_vid, directed, heuristic, factor, epsilon) -- Proposed
pgr_aStarCost(edges_sql, start_vid, end_vids, directed, heuristic, factor, epsilon) -- Proposed
pgr_aStarCost(edges_sql, starts_vid, end_vid, directed, heuristic, factor, epsilon) -- Proposed
pgr_aStarCost(edges_sql, starts_vid, end_vids, directed, heuristic, factor, epsilon) -- Proposed

RETURNS SET OF (start_vid, end_vid, agg_cost) OR EMPTY SET
```

Signatures

Minimal Signature

```
pgr_aStarCost(edges_sql, start_vid, end_vid)
RETURNS SET OF (start_vid, end_vid, agg_cost) OR EMPTY SET
```

Example Using the defaults

```
SELECT * FROM pgr_aStarCost (
    'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
    2, 12);
 start_vid | end_vid | agg_cost
-----+-----+-----
```

```

      2 |      12 |      4
(1 row)

```

One to One

```

pgr_aStarCost(edges_sql, start_vid, end_vid, directed, heuristic, factor, epsilon)
RETURNS SET OF (start_vid, end_vid, agg_cost) OR EMPTY SET

```

Example Setting a Heuristic

```

SELECT * FROM pgr_aStarCost(
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
  2, 12,
  directed := false, heuristic := 2);
start_vid | end_vid | agg_cost
-----+-----+-----
      2 |      12 |      4
(1 row)

```

One to many

```

pgr_aStarCost(edges_sql, start_vid, end_vids, directed, heuristic, factor, epsilon) -- Proposed
RETURNS SET OF (start_vid, end_vid, agg_cost) OR EMPTY SET

```

This signature finds a path from one **start_vid** to each **end_vid** in **end_vids**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Using this signature, will load once the graph and perform a one to one *pgr_astar* where the starting vertex is fixed, and stop when all **end_vids** are reached.

- The result is equivalent to the union of the results of the one to one *pgr_astar*.
- The extra **end_vid** column in the result is used to distinguish to which path it belongs.

Example

```

SELECT * FROM pgr_aStarCost(
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
  2, ARRAY[3, 12], heuristic := 2);
start_vid | end_vid | agg_cost
-----+-----+-----
      2 |      3 |      5
      2 |     12 |      4
(2 rows)

```

Many to One

```

pgr_aStarCost(edges_sql, starts_vid, end_vid, directed, heuristic, factor, epsilon) -- Proposed
RETURNS SET OF (start_vid, end_vid, agg_cost) OR EMPTY SET

```

This signature finds the shortest path from each **start_vid** in **start_vids** to one **end_vid**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Using this signature, will load once the graph and perform several one to one *pgr_astar* where the ending vertex is fixed.

- The result is the union of the results of the one to one *pgr_astar*.

- The extra `start_vid` column in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_aStarCost (
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
  ARRAY[7, 2], 12, heuristic := 0);
start_vid | end_vid | agg_cost
-----+-----+-----
          2 |      12 |         4
          7 |      12 |         5
(2 rows)
```

Many to Many

```
pgr_aStarCost(edges_sql, starts_vid, end_vids, directed, heuristic, factor, epsilon) -- Proposed
RETURNS SET OF (start_vid, end_vid, agg_cost) OR EMPTY SET
```

This signature finds the shortest path from each `start_vid` in `start_vids` to each `end_vid` in `end_vids`:

- on a **directed** graph when `directed` flag is missing or is set to `true`.
- on an **undirected** graph when `directed` flag is set to `false`.

Using this signature, will load once the graph and perform several one to Many *pgr_dijkstra* for all `start_vids`.

- The result is the union of the results of the one to one *pgr_dijkstra*.
- The extra `start_vid` in the result is used to distinguish to which path it belongs.

The extra `start_vid` and `end_vid` in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_aStarCost (
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
  ARRAY[7, 2], ARRAY[3, 12], heuristic := 2);
start_vid | end_vid | agg_cost
-----+-----+-----
          2 |        3 |         5
          2 |      12 |         4
          7 |        3 |         6
          7 |      12 |         5
(4 rows)
```

Description of the Signatures

Description of the `edges_sql` query for astar like functions

`edges_sql` an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source</i> , <i>target</i>) <ul style="list-style-type: none">• When negative: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target</i> , <i>source</i>), <ul style="list-style-type: none">• When negative: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.
x1	ANY-NUMERICAL		X coordinate of <i>source</i> vertex.
y1	ANY-NUMERICAL		Y coordinate of <i>source</i> vertex.
x2	ANY-NUMERICAL		X coordinate of <i>target</i> vertex.
y2	ANY-NUMERICAL		Y coordinate of <i>target</i> vertex.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type
edges_sql	TEXT
start_vid	ANY-INTEGER
end_vid	ANY-INTEGER
directed	BOOLEAN
heuristic	INTEGER
factor	FLOAT
epsilon	FLOAT

Description of the return values for a Cost function Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
agg_cost	FLOAT	Aggregate cost from start_vid to end_vid.

See Also

- *aStar - Family of functions.*
- Sample Data network.
- http://www.boost.org/libs/graph/doc/astar_search.html
- http://en.wikipedia.org/wiki/A*_search_algorithm

Indices and tables

- genindex
- search

pgr_aStarCostMatrix - proposed

Name

`pgr_aStarCostMatrix` - Calculates the a cost matrix using *pgr_aStar*.

Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.



Fig. 6.3: Boost Graph Inside

Availability: 2.4.0

Synopsis

Using aStar algorithm, calculate and return a cost matrix.

Signature Summary

```
pgr_aStarCostMatrix(edges_sql, vids)
pgr_aStarCostMatrix(edges_sql, vids, directed, heuristic, factor, epsilon)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Signatures**Minimal Signature**

The minimal signature:

- Is for a **directed** graph.

```
pgr_aStarCostMatrix(edges_sql, vids)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example Cost matrix for vertices 1, 2, 3, and 4.

```
SELECT * FROM pgr_aStarCostMatrix(
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
  (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5)
);
 start_vid | end_vid | agg_cost
-----+-----+-----
         2 |         1 |         1
         3 |         1 |         2
         4 |         1 |         3
```

1	2	1
3	2	1
4	2	2
1	3	6
2	3	5
4	3	1
1	4	5
2	4	4
3	4	3

(12 rows)

Complete Signature

```
pgr_aStarCostMatrix(edges_sql, vids, directed, heuristic, factor, epsilon)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example Cost matrix for an undirected graph for vertices 1, 2, 3, and 4.

This example returns a symmetric cost matrix.

```
SELECT * FROM pgr_aStarCostMatrix(
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
  (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5),
  directed := false, heuristic := 2
);
 start_vid | end_vid | agg_cost
-----+-----+-----
          2 |          1 |          1
          3 |          1 |          2
          4 |          1 |          3
          1 |          2 |          1
          3 |          2 |          1
          4 |          2 |          2
          1 |          3 |          2
          2 |          3 |          1
          4 |          3 |          1
          1 |          4 |          3
          2 |          4 |          2
          3 |          4 |          1
(12 rows)
```

Description of the Signatures

Description of the edges_sql query for astar like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source</i> , <i>target</i>) <ul style="list-style-type: none">• When negative: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target</i> , <i>source</i>), <ul style="list-style-type: none">• When negative: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.
x1	ANY-NUMERICAL		X coordinate of <i>source</i> vertex.
y1	ANY-NUMERICAL		Y coordinate of <i>source</i> vertex.
x2	ANY-NUMERICAL		X coordinate of <i>target</i> vertex.
y2	ANY-NUMERICAL		Y coordinate of <i>target</i> vertex.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type
edges_sql	TEXT
vids	ARRAY [ANY-INTEGER]
directed	BOOLEAN
heuristic	INTEGER
factor	FLOAT
epsilon	FLOAT

Description of the return values for a Cost function Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
agg_cost	FLOAT	Aggregate cost from start_vid to end_vid.

Examples

Example Use with tsp

```

SELECT * FROM pgr_TSP (
  $$
  SELECT * FROM pgr_aStarCostMatrix(
    'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
    (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5),
    directed:= false, heuristic := 2
  )
  $$,
  randomize := false
);
seq | node | cost | agg_cost
-----+-----+-----+-----
  1 |    1 |    1 |         0
  2 |    2 |    1 |         1
  3 |    3 |    1 |         2
  4 |    4 |    3 |         3
  5 |    1 |    0 |         6

```

(5 rows)

See Also

- [*aStar - Family of functions*](#)
- [*Cost Matrix - Category*](#)
- [*Traveling Sales Person - Family of functions*](#)
- The queries use the [Sample Data](#) network.

Indices and tables

- [genindex](#)
- [search](#)

The problem definition (Advanced documentation)

The A* (pronounced “A Star”) algorithm is based on Dijkstra’s algorithm with a heuristic, that is an estimation of the remaining cost from the vertex to the goal, that allows to solve most shortest path problems by evaluation only a sub-set of the overall graph. Running time: $O((E + V) * \log V)$

Heuristic

Currently the heuristic functions available are:

- 0: $h(v) = 0$ (Use this value to compare with `pgr_dijkstra`)
- 1: $h(v) = \text{abs}(\max(\Delta x, \Delta y))$
- 2: $h(v) = \text{abs}(\min(\Delta x, \Delta y))$
- 3: $h(v) = \Delta x * \Delta x + \Delta y * \Delta y$
- 4: $h(v) = \text{sqrt}(\Delta x * \Delta x + \Delta y * \Delta y)$
- 5: $h(v) = \text{abs}(\Delta x) + \text{abs}(\Delta y)$

where $\Delta x = x_1 - x_0$ and $\Delta y = y_1 - y_0$

Factor

Analysis 1

Working with `cost/reverse_cost` as length in degrees, x/y in lat/lon: Factor = 1 (no need to change units)

Analysis 2

Working with `cost/reverse_cost` as length in meters, x/y in lat/lon: Factor = would depend on the location of the points:

latitude	conversion	Factor
45	1 longitude degree is 78846.81 m	78846
0	1 longitude degree is 111319.46 m	111319

Analysis 3

Working with cost/reverse_cost as time in seconds, x/y in lat/lon: Factor: would depend on the location of the points and on the average speed say 25m/s is the speed.

latitude	conversion	Factor
45	1 longitude degree is (78846.81m)/(25m/s)	3153 s
0	1 longitude degree is (111319.46 m)/(25m/s)	4452 s

See Also

- *pg_r_aStar*
- *pg_r_aStarCost – proposed*
- *pg_r_aStarCostMatrix - proposed*
- http://www.boost.org/libs/graph/doc/astar_search.html
- http://en.wikipedia.org/wiki/A*_search_algorithm

Indices and tables

- [genindex](#)
- [search](#)

6.1.2 Bidirectional A* - Family of functions

- *pg_r_bdAstar* - Bidirectional A* algorithm for obtaining paths.
- *pg_r_bdAstarCost - Proposed* - Bidirectional A* algorithm to calculate the cost of the paths.
- *pg_r_bdAstarCostMatrix - proposed* - Bidirectional A* algorithm to calculate a cost matrix of paths.

pg_r_bdAstarCost - Proposed

Name

`pg_r_bdAstarCost` — Returns the shortest path using A* algorithm.



Fig. 6.4: Boost Graph Inside

Availability: 2.5.0

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Signature Summary

```
pgr_bdAstarCost(edges_sql, start_vid, end_vid)
pgr_bdAstarCost(edges_sql, start_vid, end_vid [, directed , heuristic, factor, epsilon])
pgr_bdAstarCost(edges_sql, start_vid, end_vids [, directed, heuristic, factor, epsilon])
pgr_bdAstarCost(edges_sql, start_vids, end_vid [, directed, heuristic, factor, epsilon])
pgr_bdAstarCost(edges_sql, start_vids, end_vids [, directed, heuristic, factor, epsilon])

RETURNS SET OF (start_vid, end_vid, agg_cost)
OR EMPTY SET
```

Using these signatures, will load once the graph and perform several one to one *pgr_bdAstarCost*

- The result is the union of the results of the one to one *pgr_bdAstarCost*.
- The extra *start_vid* and/or *end_vid* in the result is used to distinguish to which path it belongs.

Signatures

Minimal Signature

```
pgr_bdAstarCost(edges_sql, start_vid, end_vid)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

This usage finds the shortest path from the *start_vid* to the *end_vid*

- on a **directed** graph
- with **heuristic**'s value 5
- with **factor**'s value 1
- with **epsilon**'s value 1

Example Using the defaults

```
SELECT * FROM pgr_bdAstarCost (
  'SELECT id, source, target, cost, reverse_cost, x1,y1,x2,y2
   FROM edge_table',
  2, 3
);
 start_vid | end_vid | agg_cost
-----+-----+-----
```

```

      2 |      3 |      5
(1 row)

```

pgr_bdAstarCost One to One

```

pgr_bdAstarCost(edges_sql, start_vid, end_vid [, directed, heuristic, factor, epsilon])
RETURNS SET OF (start_vid, end_vid, agg_cost)

```

This usage finds the shortest path from the **start_vid** to each **end_vid** in **end_vids** allowing the user to choose

- if the graph is **directed** or **undirected**
- **heuristic**,
- and/or **factor**
- and/or **epsilon**.

Note: In the One to One signature, because of the deprecated signature existence, it is compulsory to indicate if the graph is **directed** or **undirected**.

Example Directed using Heuristic 2

```

SELECT * FROM pgr_bdAstarCost(
  'SELECT id, source, target, cost, reverse_cost, x1,y1,x2,y2
   FROM edge_table',
  2, 3,
  true, heuristic := 2
);
 start_vid | end_vid | agg_cost
-----+-----+-----
      2 |      3 |      5
(1 row)

```

pgr_bdAstarCost One to many

```

pgr_bdAstarCost(edges_sql, start_vid, end_vids [, directed, heuristic, factor, epsilon])
RETURNS SET OF (start_vid, end_vid, agg_cost)

```

This usage finds the shortest path from the **start_vid** to each **end_vid** in **end_vids** allowing the user to choose

- if the graph is **directed** or **undirected**
- and/or **heuristic**,
- and/or **factor**
- and/or **epsilon**.

Example Directed using Heuristic 3 and a factor of 3.5

```

SELECT * FROM pgr_bdAstarCost(
  'SELECT id, source, target, cost, reverse_cost, x1,y1,x2,y2
   FROM edge_table',
  2, ARRAY[3, 11],
  heuristic := 3, factor := 3.5
);
 start_vid | end_vid | agg_cost
-----+-----+-----
      2 |      3 |      5
      2 |     11 |      3

```

```
(2 rows)
```

pgr_bdAstarCost Many to One

```
pgr_bdAstarCost(edges_sql, start_vids, end_vid [, directed, heuristic, factor, epsilon])  
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

This usage finds the shortest path from each **start_vid** in **start_vids** to the **end_vid** allowing the user to choose

- if the graph is **directed** or **undirected**
- and/or **heuristic**,
- and/or **factor**
- and/or **epsilon**.

Example Undirected graph with Heuristic 4

```
SELECT * FROM pgr_bdAstarCost(  
  'SELECT id, source, target, cost, reverse_cost, x1,y1,x2,y2  
  FROM edge_table',  
  ARRAY[2, 7], 3,  
  false, heuristic := 4  
);  
 start_vid | end_vid | agg_cost  
-----+-----+-----  
          2 |        3 |         1  
          7 |        3 |         4  
(2 rows)
```

pgr_bdAstarCost Many to Many

```
pgr_bdAstarCost(edges_sql, start_vids, end_vids [, directed, heuristic, factor, epsilon])  
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

This usage finds the shortest path from each **start_vid** in **start_vids** to each **end_vid** in **end_vids** allowing the user to choose

- if the graph is **directed** or **undirected**
- and/or **heuristic**,
- and/or **factor**
- and/or **epsilon**.

Example Directed graph with a factor of 0.5

```
SELECT * FROM pgr_bdAstarCost(  
  'SELECT id, source, target, cost, reverse_cost, x1,y1,x2,y2  
  FROM edge_table',  
  ARRAY[2, 7], ARRAY[3, 11],  
  factor := 0.5  
);  
 start_vid | end_vid | agg_cost  
-----+-----+-----  
          2 |        3 |         5  
          2 |       11 |         3  
          7 |        3 |         6  
          7 |       11 |         4  
(4 rows)
```

Description of the Signatures

Description of the edges_sql query for astar like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.
x1	ANY-NUMERICAL		X coordinate of <i>source</i> vertex.
y1	ANY-NUMERICAL		Y coordinate of <i>source</i> vertex.
x2	ANY-NUMERICAL		X coordinate of <i>target</i> vertex.
y2	ANY-NUMERICAL		Y coordinate of <i>target</i> vertex.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type
edges_sql	TEXT
start_vid	ANY-INTEGER
start_vids	ARRAY [ANY-INTEGER]
end_vid	ANY-INTEGER
end_vids	ARRAY [ANY-INTEGER]
directed	BOOLEAN
heuristic	INTEGER
factor	FLOAT
epsilon	FLOAT

Description of the return values for a Cost function Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
agg_cost	FLOAT	Aggregate cost from start_vid to end_vid.

See Also

- *Bidirectional A* - Family of functions*
- [Sample Data network](#).
- [Migration Guide](#)⁵
- http://www.boost.org/libs/graph/doc/astar_search.html
- http://en.wikipedia.org/wiki/A*_search_algorithm

Indices and tables

- [genindex](#)
- [search](#)

⁵https://github.com/cvvergara/pgrouting/wiki/Migration-Guide#pgr_bdastar

pgr_bdAstarCostMatrix - proposed**Name**

`pgr_bdAstarCostMatrix` - Calculates the a cost matrix using *pgr_bdAstar*.



Fig. 6.5: Boost Graph Inside

Availability: 2.5.0

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

Using Dijkstra algorithm, calculate and return a cost matrix.

Signature Summary

```
pgr_bdAstarCostMatrix(edges_sql, start_vids)
pgr_bdAstarCostMatrix(edges_sql, start_vids, [, directed , heuristic, factor, epsilon])
RETURNS SET OF (start_vid, end_vid, agg_cost)
OR EMPTY SET
```

Signatures**Minimal Signature**

```
pgr_bdAstarCostMatrix(edges_sql, start_vids)
RETURNS SET OF (start_vid, end_vid, agg_cost)
OR EMPTY SET
```

This usage calculates the cost from the each `start_vid` in `start_vids` to each `start_vid` in `start_vids`

- on a **directed** graph
- with **heuristic**'s value 5
- with **factor**'s value 1
- with **epsilon**'s value 1

Example Cost matrix for vertices 1, 2, 3, and 4.

```
SELECT * FROM pgr_bdAstarCostMatrix(  
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',  
  (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5)  
);  
 start_vid | end_vid | agg_cost  
-----+-----+-----  
          1 |        2 |        1  
          1 |        3 |        6  
          1 |        4 |        5  
          2 |        1 |        1  
          2 |        3 |        5  
          2 |        4 |        4  
          3 |        1 |        2  
          3 |        2 |        1  
          3 |        4 |        3  
          4 |        1 |        3  
          4 |        2 |        2  
          4 |        3 |        1  
(12 rows)
```

Complete Signature

```
pgr_bdAstarCostMatrix(edges_sql, start_vids, [, directed , heuristic, factor, epsilon])  
RETURNS SET OF (start_vid, end_vid, agg_cost)  
OR EMPTY SET
```

This usage calculates the cost from the each **start_vid** in **start_vids** to each **start_vid** in **start_vids** allowing the

- if the graph is **directed** or **undirected**
- **heuristic**,
- and/or **factor**
- and/or **epsilon**.

Example Cost matrix for an undirected graph for vertices 1, 2, 3, and 4.

This example returns a symmetric cost matrix.

```
SELECT * FROM pgr_bdAstarCostMatrix(  
  'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',  
  (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5),  
  false  
);  
 start_vid | end_vid | agg_cost  
-----+-----+-----  
          1 |        2 |        1  
          1 |        3 |        2  
          1 |        4 |        3  
          2 |        1 |        1  
          2 |        3 |        1  
          2 |        4 |        2  
          3 |        1 |        2  
          3 |        2 |        1
```

3		4		1
4		1		3
4		2		2
4		3		1
(12 rows)				

Description of the Signatures

Description of the edges_sql query for astar like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source</i> , <i>target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target</i> , <i>source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.
x1	ANY-NUMERICAL		X coordinate of <i>source</i> vertex.
y1	ANY-NUMERICAL		Y coordinate of <i>source</i> vertex.
x2	ANY-NUMERICAL		X coordinate of <i>target</i> vertex.
y2	ANY-NUMERICAL		Y coordinate of <i>target</i> vertex.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type
edges_sql	TEXT
start_vid	ANY-INTEGER
start_vids	ARRAY[ANY-INTEGER]
end_vid	ANY-INTEGER
end_vids	ARRAY[ANY-INTEGER]
directed	BOOLEAN
heuristic	INTEGER
factor	FLOAT
epsilon	FLOAT

Description of the return values for a Cost function Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
agg_cost	FLOAT	Aggregate cost from start_vid to end_vid.

Examples

Example Use with tsp

```

SELECT * FROM pgr_TSP (
  $$
  SELECT * FROM pgr_bdAstarCostMatrix(
    'SELECT id, source, target, cost, reverse_cost, x1, y1, x2, y2 FROM edge_table',
    (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5),
    false
  )
  $$,
  randomize := false
);
seq | node | cost | agg_cost
-----+-----+-----+-----
  1 |    1 |    1 |         0
  2 |    2 |    1 |         1

```

3	3	1	2
4	4	3	3
5	1	0	6
(5 rows)			

See Also

- *Bidirectional A* - Family of functions*
- *Cost Matrix - Category*
- *Traveling Sales Person - Family of functions*
- The queries use the [Sample Data](#) network.

Indices and tables

- `genindex`
- `search`

Synopsis

Based on A* algorithm, the bidirectional search finds a shortest path from a starting vertex (`start_vid`) to an ending vertex (`end_vid`). It runs two simultaneous searches: one forward from the `start_vid`, and one backward from the `end_vid`, stopping when the two meet in the middle. This implementation can be used with a directed graph and an undirected graph.

Characteristics

The main Characteristics are:

- Process is done only on edges with positive costs.
- Values are returned when there is a path.
- When the starting vertex and ending vertex are the same, there is no path.
 - The *agg_cost* the non included values (v, v) is 0
- When the starting vertex and ending vertex are the different and there is no path:
 - The *agg_cost* the non included values (u, v) is ∞
- Running time (worse case scenario): $O((E + V) * \log V)$
- For large graphs where there is a path between the starting vertex and ending vertex:
 - It is expected to terminate faster than `pgr_astar`

Description of the Signatures

Description of the `edges_sql` query for `astar` like functions

`edges_sql` an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source</i> , <i>target</i>) <ul style="list-style-type: none">• When negative: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target</i> , <i>source</i>), <ul style="list-style-type: none">• When negative: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.
x1	ANY-NUMERICAL		X coordinate of <i>source</i> vertex.
y1	ANY-NUMERICAL		Y coordinate of <i>source</i> vertex.
x2	ANY-NUMERICAL		X coordinate of <i>target</i> vertex.
y2	ANY-NUMERICAL		Y coordinate of <i>target</i> vertex.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Description
edges_sql	TEXT	Edges SQL query as described above.
start_vid	ANY-INTEGER	Starting vertex identifier.
start_vids	ARRAY [ANY-INTEGER]	Starting vertices identifiers.
end_vid	ANY-INTEGER	Ending vertex identifier.
end_vids	ARRAY [ANY-INTEGER]	Ending vertices identifiers.
directed	BOOLEAN	<ul style="list-style-type: none"> Optional. <ul style="list-style-type: none"> When <i>false</i> the graph is considered as Undirected. Default is <i>true</i> which considers the graph as Directed.
heuristic	INTEGER	(optional). Heuristic number. Current valid values 0~5. Default 5 <ul style="list-style-type: none"> 0: $h(v) = 0$ (Use this value to compare with <code>pgr_dijkstra</code>) 1: $h(v) = \text{abs}(\max(dx, dy))$ 2: $h(v) = \text{abs}(\min(dx, dy))$ 3: $h(v) = dx * dx + dy * dy$ 4: $h(v) = \text{sqrt}(dx * dx + dy * dy)$ 5: $h(v) = \text{abs}(dx) + \text{abs}(dy)$
factor	FLOAT	(optional). For units manipulation. <i>factor</i> > 0. Default 1. see <i>Factor</i>
epsilon	FLOAT	(optional). For less restricted results. <i>epsilon</i> >= 1. Default 1.

See Also

Indices and tables

- `genindex`
- `search`

6.1.3 Bidirectional Dijkstra - Family of functions

- `pgr_bdDijkstra` - Bidirectional Dijkstra algorithm for the shortest paths.
- `pgr_bdDijkstraCost` - *Proposed* - Bidirectional Dijkstra to calculate the cost of the shortest paths
- `pgr_bdDijkstraCostMatrix` - *proposed* - Bidirectional Dijkstra algorithm to create a matrix of costs of the shortest paths.

pgr_bdDijkstraCost - Proposed

`pgr_bdDijkstraCost` — Returns the shortest path(s)'s cost using Bidirectional Dijkstra algorithm.



Fig. 6.6: Boost Graph Inside

Availability: 2.5.0**Warning:** Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Signature Summary

```
pgr_dijkstraCost(edges_sql, start_vid, end_vid)
pgr_bdDijkstraCost(edges_sql, start_vid, end_vid, directed)
pgr_bdDijkstraCost(edges_sql, start_vid, end_vids, directed)
pgr_bdDijkstraCost(edges_sql, start_vids, end_vid, directed)
pgr_bdDijkstraCost(edges_sql, start_vids, end_vids, directed)
```

```
RETURNS SET OF (start_vid, end_vid, agg_cost)
OR EMPTY SET
```

Signatures**Minimal signature**

```
pgr_bdDijkstraCost(edges_sql, start_vid, end_vid)
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost) or EMPTY SET
```

The minimal signature is for a **directed** graph from one start_vid to one end_vid:

Example

```
SELECT * FROM pgr_bdDijkstraCost(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 3
);
 start_vid | end_vid | agg_cost
-----+-----+-----
          2 |        3 |        5
(1 row)
```


pgr_bdDijkstraCost One to One

```
pgr_bdDijkstraCost(edges_sql, start_vid, end_vid, directed)
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from one **start_vid** to one **end_vid**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Example

```
SELECT * FROM pgr_bdDijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, 3,
  false
);
```

seq	path_seq	node	edge	cost	agg_cost
1	1	2	2	1	0
2	2	3	-1	0	1

(2 rows)

pgr_bdDijkstraCost One to many

```
pgr_bdDijkstraCost(edges_sql, start_vid, end_vids, directed)
RETURNS SET OF (seq, path_seq, end_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from one **start_vid** to each **end_vid** in **end_vids**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Using this signature, will load once the graph and perform a one to one *pgr_dijkstra* where the starting vertex is fixed, and stop when all **end_vids** are reached.

- The result is equivalent to the union of the results of the one to one *pgr_dijkstra*.
- The extra **end_vid** in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_bdDijkstraCost(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  2, ARRAY[3, 11]);
```

start_vid	end_vid	agg_cost
2	3	5
2	11	3

(2 rows)

pgr_bdDijkstraCost Many to One

```
pgr_bdDijkstraCost(edges_sql, start_vids, end_vid, directed)
RETURNS SET OF (seq, path_seq, start_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from each **start_vid** in **start_vids** to one **end_vid**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

Using this signature, will load once the graph and perform several one to one *pgr_dijkstra* where the ending vertex is fixed.

- The result is the union of the results of the one to one *pgr_dijkstra*.
- The extra *start_vid* in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_bdDijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2, 7], 3);
```

seq	path_seq	start_vid	node	edge	cost	agg_cost
1	1	2	2	4	1	0
2	2	2	5	8	1	1
3	3	2	6	9	1	2
4	4	2	9	16	1	3
5	5	2	4	3	1	4
6	6	2	3	-1	0	5
7	1	7	7	6	1	0
8	2	7	8	7	1	1
9	3	7	5	8	1	2
10	4	7	6	9	1	3
11	5	7	9	16	1	4
12	6	7	4	3	1	5
13	7	7	3	-1	0	6

(13 rows)

pgr_bdDijkstraCost Many to Many

```
pgr_bdDijkstra(edges_sql, start_vids, end_vids, directed)
RETURNS SET OF (seq, path_seq, start_vid, end_vid, node, edge, cost, agg_cost) or EMPTY SET
```

This signature finds the shortest path from each **start_vid** in **start_vids** to each **end_vid** in **end_vids**:

- on a **directed** graph when *directed* flag is missing or is set to true.
- on an **undirected** graph when *directed* flag is set to false.

Using this signature, will load once the graph and perform several one to Many *pgr_dijkstra* for all *start_vids*.

- The result is the union of the results of the one to one *pgr_dijkstra*.
- The extra *start_vid* in the result is used to distinguish to which path it belongs.

The extra *start_vid* and *end_vid* in the result is used to distinguish to which path it belongs.

Example

```
SELECT * FROM pgr_bdDijkstra(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2, 7], ARRAY[3, 11]);
```

seq	path_seq	start_vid	end_vid	node	edge	cost	agg_cost
1	1	2	3	2	4	1	0
2	2	2	3	5	8	1	1
3	3	2	3	6	9	1	2
4	4	2	3	9	16	1	3
5	5	2	3	4	3	1	4
6	6	2	3	3	-1	0	5
7	1	2	11	2	4	1	0
8	2	2	11	5	8	1	1
9	3	2	11	6	11	1	2
10	4	2	11	11	-1	0	3
11	1	7	3	7	6	1	0
12	2	7	3	8	7	1	1
13	3	7	3	5	8	1	2

14		4		7		3		6		9		1		3
15		5		7		3		9		16		1		4
16		6		7		3		4		3		1		5
17		7		7		3		3		-1		0		6
18		1		7		11		7		6		1		0
19		2		7		11		8		7		1		1
20		3		7		11		5		10		1		2
21		4		7		11		10		12		1		3
22		5		7		11		11		-1		0		4
(22 rows)														

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Column	Type	Default
sql	TEXT	
start_vid	BIGINT	
start_vids	ARRAY[BIGINT]	
end_vid	BIGINT	
end_vids	ARRAY[BIGINT]	
directed	BOOLEAN	true

Description of the return values for a Cost function Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
agg_cost	FLOAT	Aggregate cost from start_vid to end_vid.

See Also

- The queries use the [Sample Data](#) network.
- *pgr_bdDijkstra*
- <http://www.cs.princeton.edu/courses/archive/spr06/cos423/Handouts/EPP%20shortest%20path%20algorithms.pdf>
- https://en.wikipedia.org/wiki/Bidirectional_search

Indices and tables

- genindex
- search

pgr_bdDijkstraCostMatrix - proposed**Name**

`pgr_bdDijkstraCostMatrix` - Calculates the a cost matrix using *pgr_bdDijkstra*.



Fig. 6.7: Boost Graph Inside

Availability: 2.5.0

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

Using Dijkstra algorithm, calculate and return a cost matrix.

Signature Summary

```
pgr_bdDijkstraCostMatrix(edges_sql, start_vids)
pgr_bdDijkstraCostMatrix(edges_sql, start_vids, directed)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Signatures

Minimal Signature

The minimal signature:

- Is for a **directed** graph.

```
pgr_bdDijkstraCostMatrix(edges_sql, start_vid)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example Cost matrix for vertices 1, 2, 3, and 4.

```
SELECT * FROM pgr_bdDijkstraCostMatrix(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5)
);
```

start_vid	end_vid	agg_cost
1	2	1
1	3	6
1	4	5
2	1	1
2	3	5
2	4	4
3	1	2
3	2	1
3	4	3
4	1	3

4		2		2
4		3		1

(12 rows)

Complete Signature

```
pgr_bdDijkstraCostMatrix(edges_sql, start_vids, directed:=true)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example Cost matrix for an undirected graph for vertices 1, 2, 3, and 4.

This example returns a symmetric cost matrix.

```
SELECT * FROM pgr_bdDijkstraCostMatrix(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5),
  false
);
 start_vid | end_vid | agg_cost
-----+-----+-----
          1 |          2 |          1
          1 |          3 |          2
          1 |          4 |          3
          2 |          1 |          1
          2 |          3 |          1
          2 |          4 |          2
          3 |          1 |          2
          3 |          2 |          1
          3 |          4 |          1
          4 |          1 |          3
          4 |          2 |          2
          4 |          3 |          1
(12 rows)
```

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Description
edges_sql	TEXT	Edges SQL query as described above.
start_vids	ARRAY [ANY-INTEGER]	Array of identifiers of the vertices.
directed	BOOLEAN	(optional). When false the graph is considered undirected, true which considers the graph as Directed.

Description of the return values for a Cost function Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
agg_cost	FLOAT	Aggregate cost from start_vid to end_vid.

Examples

Example Use with tsp

```
SELECT * FROM pgr_TSP (
  $$
  SELECT * FROM pgr_bdDijkstraCostMatrix(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table',
    (SELECT array_agg(id) FROM edge_table_vertices_pgr WHERE id < 5),
    false
  )
  $$,
  randomize := false
);
```

seq	node	cost	agg_cost
1	1	1	0
2	2	1	1
3	3	1	2
4	4	3	3
5	1	0	6
(5 rows)			

See Also

- *Bidirectional Dijkstra - Family of functions*
- *Cost Matrix - Category*
- *Traveling Sales Person - Family of functions*
- The queries use the [Sample Data](#) network.

Indices and tables

- genindex
- search

Synopsis

Based on Dijkstra's algorithm, the bidirectional search finds a shortest path a starting vertex (`start_vid`) to an ending vertex (`end_vid`). It runs two simultaneous searches: one forward from the source, and one backward from the target, stopping when the two meet in the middle. This implementation can be used with a directed graph and an undirected graph.

Characteristics

The main Characteristics are:

- Process is done only on edges with positive costs.
- Values are returned when there is a path.
- When the starting vertex and ending vertex are the same, there is no path.
 - The *agg_cost* the non included values (v, v) is 0
- When the starting vertex and ending vertex are the different and there is no path:
 - The *agg_cost* the non included values (u, v) is ∞
- Running time (worse case scenario): $O((V \log V + E))$
- For large graphs where there is a path between the starting vertex and ending vertex:
 - It is expected to terminate faster than `pgr_dijkstra`

See Also

Indices and tables

- genindex

- search

6.1.4 withPoints - Family of functions

When points are also given as input:

- *pgr_withPoints - Proposed* - Route from/to points anywhere on the graph.
- *pgr_withPointsCost - Proposed* - Costs of the shortest paths.
- *pgr_withPointsCostMatrix - proposed* - Costs of the shortest paths.
- *pgr_withPointsKSP - Proposed* - K shortest paths.
- *pgr_withPointsDD - Proposed* - Driving distance.

pgr_withPoints - Proposed

Name

`pgr_withPoints` - Returns the shortest path in a graph with additional temporary vertices.

Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.



Fig. 6.8: Boost Graph Inside

Availability: 2.2.0

Synopsis

Modify the graph to include points defined by `points_sql`. Using Dijkstra algorithm, find the shortest path(s)

Characteristics:

The main Characteristics are:

- Process is done only on edges with positive costs.
- Vertices of the graph are:
 - **positive** when it belongs to the `edges_sql`
 - **negative** when it belongs to the `points_sql`

- Values are returned when there is a path.
 - When the starting vertex and ending vertex are the same, there is no path. - The agg_cost the non included values (v, v) is 0
 - When the starting vertex and ending vertex are the different and there is no path: - The agg_cost the non included values (u, v) is ∞
- For optimization purposes, any duplicated value in the start_vids or end_vids are ignored.
- The returned values are ordered: - start_vid ascending - end_vid ascending
- Running time: $O(|start_vids| \times (V \log V + E))$

Signature Summary

```
pgr_withPoints(edges_sql, points_sql, start_vid, end_vid)
pgr_withPoints(edges_sql, points_sql, start_vid, end_vid, directed, driving_side, details)
pgr_withPoints(edges_sql, points_sql, start_vid, end_vids, directed, driving_side, details)
pgr_withPoints(edges_sql, points_sql, start_vids, end_vid, directed, driving_side, details)
pgr_withPoints(edges_sql, points_sql, start_vids, end_vids, directed, driving_side, details)
RETURNS SET OF (seq, path_seq, [start_vid,] [end_vid,] node, edge, cost, agg_cost)
```

Signatures

Minimal Use

The minimal signature:

- Is for a **directed** graph.
- The driving side is set as **b** both. So arriving/departing to/from the point(s) can be in any direction.
- No **details** are given about distance of other points of points_sql query.

```
pgr_withPoints(edges_sql, points_sql, start_vid, end_vid)
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost)
```

Example From point 1 to point 3

```
SELECT * FROM pgr_withPoints(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, -3);
```

seq	path_seq	node	edge	cost	agg_cost
1	1	-1	1	0.6	0
2	2	2	4	1	0.6
3	3	5	10	1	1.6
4	4	10	12	0.6	2.6
5	5	-3	-1	0	3.2

(5 rows)

One to One

```
pgr_withPoints(edges_sql, points_sql, start_vid, end_vid,
  directed:=true, driving_side:='b', details:=false)
RETURNS SET OF (seq, path_seq, node, edge, cost, agg_cost)
```

Example From point 1 to vertex 3

```

SELECT * FROM pgr_withPoints(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, 3,
  details := true);
seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
1 | 1 | -1 | 1 | 0.6 | 0
2 | 2 | 2 | 4 | 0.7 | 0.6
3 | 3 | -6 | 4 | 0.3 | 1.3
4 | 4 | 5 | 8 | 1 | 1.6
5 | 5 | 6 | 9 | 1 | 2.6
6 | 6 | 9 | 16 | 1 | 3.6
7 | 7 | 4 | 3 | 1 | 4.6
8 | 8 | 3 | -1 | 0 | 5.6
(8 rows)

```

One to Many

```

pgr_withPoints(edges_sql, points_sql, start_vid, end_vids,
  directed:=true, driving_side='b', details:=false)
RETURNS SET OF (seq, path_seq, end_vid, node, edge, cost, agg_cost)

```

Example From point 1 to point 3 and vertex 5

```

SELECT * FROM pgr_withPoints(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, ARRAY[-3,5]);
seq | path_seq | end_pid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
1 | 1 | -3 | -1 | 1 | 0.6 | 0
2 | 2 | -3 | 2 | 4 | 1 | 0.6
3 | 3 | -3 | 5 | 10 | 1 | 1.6
4 | 4 | -3 | 10 | 12 | 0.6 | 2.6
5 | 5 | -3 | -3 | -1 | 0 | 3.2
6 | 1 | 5 | -1 | 1 | 0.6 | 0
7 | 2 | 5 | 2 | 4 | 1 | 0.6
8 | 3 | 5 | 5 | -1 | 0 | 1.6
(8 rows)

```

Many to One

```

pgr_withPoints(edges_sql, points_sql, start_vids, end_vid,
  directed:=true, driving_side='b', details:=false)
RETURNS SET OF (seq, path_seq, start_vid, node, edge, cost, agg_cost)

```

Example From point 1 and vertex 2 to point 3

```

SELECT * FROM pgr_withPoints(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  ARRAY[-1,2], -3);
seq | path_seq | start_pid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
1 | 1 | -1 | -1 | 1 | 0.6 | 0
2 | 2 | -1 | 2 | 4 | 1 | 0.6
3 | 3 | -1 | 5 | 10 | 1 | 1.6
4 | 4 | -1 | 10 | 12 | 0.6 | 2.6
5 | 5 | -1 | -3 | -1 | 0 | 3.2
6 | 1 | 2 | 2 | 4 | 1 | 0

```

```

7 |          2 |          2 |    5 |    10 |    1 |          1
8 |          3 |          2 |   10 |   12 |  0.6 |          2
9 |          4 |          2 |   -3 |   -1 |    0 |         2.6
(9 rows)

```

Many to Many

```

pgr_withPoints(edges_sql, points_sql, start_vids, end_vids,
    directed:=true, driving_side:='b', details:=false)
RETURNS SET OF (seq, path_seq, start_vid, end_vid, node, edge, cost, agg_cost)

```

Example From point 1 and vertex 2 to point 3 and vertex 7

```

SELECT * FROM pgr_withPoints(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
    'SELECT pid, edge_id, fraction, side from pointsOfInterest',
    ARRAY[-1,2], ARRAY[-3,7]);
seq | path_seq | start_pid | end_pid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----+-----
1 | 1 | -1 | -3 | -1 | 1 | 0.6 | 0
2 | 2 | -1 | -3 | 2 | 4 | 1 | 0.6
3 | 3 | -1 | -3 | 5 | 10 | 1 | 1.6
4 | 4 | -1 | -3 | 10 | 12 | 0.6 | 2.6
5 | 5 | -1 | -3 | -3 | -1 | 0 | 3.2
6 | 1 | -1 | 7 | -1 | 1 | 0.6 | 0
7 | 2 | -1 | 7 | 2 | 4 | 1 | 0.6
8 | 3 | -1 | 7 | 5 | 7 | 1 | 1.6
9 | 4 | -1 | 7 | 8 | 6 | 1 | 2.6
10 | 5 | -1 | 7 | 7 | -1 | 0 | 3.6
11 | 1 | 2 | -3 | 2 | 4 | 1 | 0
12 | 2 | 2 | -3 | 5 | 10 | 1 | 1
13 | 3 | 2 | -3 | 10 | 12 | 0.6 | 2
14 | 4 | 2 | -3 | -3 | -1 | 0 | 2.6
15 | 1 | 2 | 7 | 2 | 4 | 1 | 0
16 | 2 | 2 | 7 | 5 | 7 | 1 | 1
17 | 3 | 2 | 7 | 8 | 6 | 1 | 2
18 | 4 | 2 | 7 | 7 | -1 | 0 | 3
(18 rows)

```

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the Points SQL query

points_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Description
pid	ANY-INTEGER	(optional) Identifier of the point. <ul style="list-style-type: none"> If column present, it can not be NULL. If column not present, a sequential identifier will be given automatically.
edge_id	ANY-INTEGER	Identifier of the “closest” edge to the point.
fraction	ANY-NUMERICAL	Value in <0,1> that indicates the relative position from the first end point of the edge.
side	CHAR	(optional) Value in ['b', 'r', 'l', NULL] indicating if the point is: <ul style="list-style-type: none"> In the right, left of the edge or If it doesn't matter with 'b' or NULL. If column not present 'b' is considered.

Where:

ANY-INTEGER smallint, int, bigint

ANY-NUMERICAL smallint, int, bigint, real, float

Description of the parameters of the signatures

Parameter	Type
edges_sql	TEXT
points_sql	TEXT
start_vid	ANY-INTEGER
end_vid	ANY-INTEGER
start_vids	ARRAY [ANY-INTEGER]
end_vids	ARRAY [ANY-INTEGER]
directed	BOOLEAN
driving_side	CHAR
details	BOOLEAN

Description of the return values Returns set of (seq, [path_seq,] [start_vid,] [end_vid,]
node, edge, cost, agg_cost)

Column	Type	Description
seq	INTEGER	Row sequence.
path_seq	INTEGER	Path sequence that indicates the relative position on the path.
start_vid	BIGINT	Identifier of the starting vertex. When negative: is a point's pid.
end_vid	BIGINT	Identifier of the ending vertex. When negative: is a point's pid.
node	BIGINT	Identifier of the node: <ul style="list-style-type: none"> • A positive value indicates the node is a vertex of edges_sql. • A negative value indicates the node is a point of points_sql.
edge	BIGINT	Identifier of the edge used to go from node to the next node: <ul style="list-style-type: none"> • -1 for the last row in the path sequence.
cost	FLOAT	Cost to traverse from node using edge to the next node: <ul style="list-style-type: none"> • 0 for the last row in the path sequence.
agg_cost	FLOAT	Aggregate cost from start_pid to node. <ul style="list-style-type: none"> • 0 for the first row in the path sequence.

Examples

Example Which path (if any) passes in front of point 6 or vertex 6 with **right** side driving topology.

```
SELECT ('(' || start_pid || ' => ' || end_pid || ') at ' || path_seq || 'th step:')::TEXT AS path_at,
CASE WHEN edge = -1 THEN ' visits'
ELSE ' passes in front of'
END as status,
CASE WHEN node < 0 THEN 'Point'
ELSE 'Vertex'
END as is_a,
abs(node) as id
FROM pgr_withPoints(
'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
'SELECT pid, edge_id, fraction, side from pointsOfInterest',
ARRAY[1,-1], ARRAY[-2,-3,-6,3,6],
driving_side := 'r',
details := true)
WHERE node IN (-6,6);
```

path_at	status	is_a	id
(-1 => -6) at 4th step:	visits	Point	6
(-1 => -3) at 4th step:	passes in front of	Point	6
(-1 => -2) at 4th step:	passes in front of	Point	6

```
(-1 => -2) at 6th step: | passes in front of | Vertex | 6
(-1 => 3) at 4th step: | passes in front of | Point | 6
(-1 => 3) at 6th step: | passes in front of | Vertex | 6
(-1 => 6) at 4th step: | passes in front of | Point | 6
(-1 => 6) at 6th step: | visits | Vertex | 6
(1 => -6) at 3th step: | visits | Point | 6
(1 => -3) at 3th step: | passes in front of | Point | 6
(1 => -2) at 3th step: | passes in front of | Point | 6
(1 => -2) at 5th step: | passes in front of | Vertex | 6
(1 => 3) at 3th step: | passes in front of | Point | 6
(1 => 3) at 5th step: | passes in front of | Vertex | 6
(1 => 6) at 3th step: | passes in front of | Point | 6
(1 => 6) at 5th step: | visits | Vertex | 6
(16 rows)
```

Example Which path (if any) passes in front of point 6 or vertex 6 with **left** side driving topology.

```
SELECT ((' || start_pid || ' => ' || end_pid ||') at ' || path_seq || 'th step:')::TEXT AS path_
CASE WHEN edge = -1 THEN ' visits'
ELSE ' passes in front of'
END as status,
CASE WHEN node < 0 THEN 'Point'
ELSE 'Vertex'
END as is_a,
abs(node) as id
FROM pgr_withPoints(
'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
'SELECT pid, edge_id, fraction, side from pointsOfInterest',
ARRAY[1,-1], ARRAY[-2,-3,-6,3,6],
driving_side := 'l',
details := true)
WHERE node IN (-6,6);
path_at | status | is_a | id
-----+-----+-----+---
(-1 => -6) at 3th step: | visits | Point | 6
(-1 => -3) at 3th step: | passes in front of | Point | 6
(-1 => -2) at 3th step: | passes in front of | Point | 6
(-1 => -2) at 5th step: | passes in front of | Vertex | 6
(-1 => 3) at 3th step: | passes in front of | Point | 6
(-1 => 3) at 5th step: | passes in front of | Vertex | 6
(-1 => 6) at 3th step: | passes in front of | Point | 6
(-1 => 6) at 5th step: | visits | Vertex | 6
(1 => -6) at 4th step: | visits | Point | 6
(1 => -3) at 4th step: | passes in front of | Point | 6
(1 => -2) at 4th step: | passes in front of | Point | 6
(1 => -2) at 6th step: | passes in front of | Vertex | 6
(1 => 3) at 4th step: | passes in front of | Point | 6
(1 => 3) at 6th step: | passes in front of | Vertex | 6
(1 => 6) at 4th step: | passes in front of | Point | 6
(1 => 6) at 6th step: | visits | Vertex | 6
(16 rows)
```

Example Many to many example with a twist: on undirected graph and showing details.

```
SELECT * FROM pgr_withPoints(
'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
'SELECT pid, edge_id, fraction, side from pointsOfInterest',
ARRAY[-1,2], ARRAY[-3,7],
directed := false,
details := true);
seq | path_seq | start_pid | end_pid | node | edge | cost | agg_cost
```


1	1	-1	-3	-1	1	0.6	0
2	2	-1	-3	2	4	0.7	0.6
3	3	-1	-3	-6	4	0.3	1.3
4	4	-1	-3	5	10	1	1.6
5	5	-1	-3	10	12	0.6	2.6
6	6	-1	-3	-3	-1	0	3.2
7	1	-1	7	-1	1	0.6	0
8	2	-1	7	2	4	0.7	0.6
9	3	-1	7	-6	4	0.3	1.3
10	4	-1	7	5	7	1	1.6
11	5	-1	7	8	6	0.7	2.6
12	6	-1	7	-4	6	0.3	3.3
13	7	-1	7	7	-1	0	3.6
14	1	2	-3	2	4	0.7	0
15	2	2	-3	-6	4	0.3	0.7
16	3	2	-3	5	10	1	1
17	4	2	-3	10	12	0.6	2
18	5	2	-3	-3	-1	0	2.6
19	1	2	7	2	4	0.7	0
20	2	2	7	-6	4	0.3	0.7
21	3	2	7	5	7	1	1
22	4	2	7	8	6	0.7	2
23	5	2	7	-4	6	0.3	2.7
24	6	2	7	7	-1	0	3
(24 rows)							

The queries use the [Sample Data](#) network.

History

- Proposed in version 2.2

See Also

- *withPoints* - Family of functions

Indices and tables

- `genindex`
- `search`

pgr_withPointsCost - Proposed

Name

`pgr_withPointsCost` - Calculates the shortest path and returns only the aggregate cost of the shortest path(s) found, for the combination of points given.

Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.



Fig. 6.9: Boost Graph Inside

Availability: 2.2.0

Synopsis

Modify the graph to include points defined by points_sql. Using Dijkstra algorithm, return only the aggregate cost of the shortest path(s) found.

Characteristics:

The main Characteristics are:

- It does not return a path.
- Returns the sum of the costs of the shortest path for pair combination of vertices in the modified graph.
- Vertices of the graph are:
 - **positive** when it belongs to the edges_sql
 - **negative** when it belongs to the points_sql
- Process is done only on edges with positive costs.
- Values are returned when there is a path.
 - The returned values are in the form of a set of (*start_vid*, *end_vid*, *agg_cost*).
 - When the starting vertex and ending vertex are the same, there is no path.
 - * The *agg_cost* in the non included values (*v*, *v*) is 0
 - When the starting vertex and ending vertex are the different and there is no path.
 - * The *agg_cost* in the non included values (*u*, *v*) is ∞
- If the values returned are stored in a table, the unique index would be the pair: (*start_vid*, *end_vid*).
- For undirected graphs, the results are symmetric.
 - The *agg_cost* of (*u*, *v*) is the same as for (*v*, *u*).
- For optimization purposes, any duplicated value in the *start_vids* or *end_vids* is ignored.
- The returned values are ordered:
 - *start_vid* ascending

– *end_vid* ascending

- Running time: $O(|start_vids| * (V \log V + E))$

Signature Summary

```
pgr_withPointsCost(edges_sql, points_sql, start_vid, end_vid, directed, driving_side)
pgr_withPointsCost(edges_sql, points_sql, start_vid, end_vids, directed, driving_side)
pgr_withPointsCost(edges_sql, points_sql, start_vids, end_vid, directed, driving_side)
pgr_withPointsCost(edges_sql, points_sql, start_vids, end_vids, directed, driving_side)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Note: There is no **details** flag, unlike the other members of the withPoints family of functions.

Signatures

Minimal Use

The minimal signature:

- Is for a **directed** graph.
- The driving side is set as **b** both. So arriving/departing to/from the point(s) can be in any direction.

```
pgr_withPointsCost(edges_sql, points_sql, start_vid, end_vid)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example

```
SELECT * FROM pgr_withPointsCost(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, -3);
 start_pid | end_pid | agg_cost
-----+-----+-----
        -1 |        -3 |        3.2
(1 row)
```

One to One

```
pgr_withPointsCost(edges_sql, points_sql, start_vid, end_vid,
  directed:=true, driving_side:='b')
RETURNS SET OF (seq, node, edge, cost, agg_cost)
```

Example

```
SELECT * FROM pgr_withPointsCost(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, 3,
  directed := false);
 start_pid | end_pid | agg_cost
-----+-----+-----
        -1 |         3 |        1.6
(1 row)
```

One to Many

```
pgr_withPointsCost(edges_sql, points_sql, start_vid, end_vids,  
    directed:=true, driving_side:='b')  
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example

```
SELECT * FROM pgr_withPointsCost(  
    'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',  
    'SELECT pid, edge_id, fraction, side from pointsOfInterest',  
    -1, ARRAY[-3,5]);  
start_pid | end_pid | agg_cost  
-----+-----+-----  
        -1 |      -3 |       3.2  
        -1 |       5 |       1.6  
(2 rows)
```

Many to One

```
pgr_withPointsCost(edges_sql, points_sql, start_vids, end_vid,  
    directed:=true, driving_side:='b')  
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example

```
SELECT * FROM pgr_withPointsCost(  
    'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',  
    'SELECT pid, edge_id, fraction, side from pointsOfInterest',  
    ARRAY[-1,2], -3);  
start_pid | end_pid | agg_cost  
-----+-----+-----  
        -1 |      -3 |       3.2  
         2 |      -3 |       2.6  
(2 rows)
```

Many to Many

```
pgr_withPointsCost(edges_sql, points_sql, start_vids, end_vids,  
    directed:=true, driving_side:='b')  
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example

```
SELECT * FROM pgr_withPointsCost(  
    'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',  
    'SELECT pid, edge_id, fraction, side from pointsOfInterest',  
    ARRAY[-1,2], ARRAY[-3,7]);  
start_pid | end_pid | agg_cost  
-----+-----+-----  
        -1 |      -3 |       3.2  
        -1 |       7 |       3.6  
         2 |      -3 |       2.6  
         2 |       7 |        3  
(4 rows)
```

Description of the Signatures**Description of the edges_sql query for dijkstra like functions**

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source</i> , <i>target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target</i> , <i>source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the Points SQL query

points_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Description
pid	ANY-INTEGER	(optional) Identifier of the point. <ul style="list-style-type: none"> If column present, it can not be NULL. If column not present, a sequential identifier will be given automatically.
edge_id	ANY-INTEGER	Identifier of the “closest” edge to the point.
fraction	ANY-NUMERICAL	Value in <0,1> that indicates the relative position from the first end point of the edge.
side	CHAR	(optional) Value in ['b', 'r', 'l', NULL] indicating if the point is: <ul style="list-style-type: none"> In the right, left of the edge or If it doesn't matter with 'b' or NULL. If column not present 'b' is considered.

Where:

ANY-INTEGER smallint, int, bigint

ANY-NUMERICAL smallint, int, bigint, real, float

Description of the parameters of the signatures

Parameter	Type
edges_sql	TEXT
points_sql	TEXT
start_vid	ANY-INTEGER
end_vid	ANY-INTEGER
start_vids	ARRAY [ANY-INTEGER]
end_vids	ARRAY [ANY-INTEGER]
directed	BOOLEAN
driving_side	CHAR

Description of the return values Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex. When negative: is a point's pid.
end_vid	BIGINT	Identifier of the ending point. When negative: is a point's pid.
agg_cost	FLOAT	Aggregate cost from start_vid to end_vid.

Examples

Example With **right** side driving topology.

```
SELECT * FROM pgr_withPointsCost(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  ARRAY[-1,2], ARRAY[-3,7],
  driving_side := 'l');
start_pid | end_pid | agg_cost
-----+-----+-----
      -1 |      -3 |       3.2
      -1 |       7 |       3.6
       2 |      -3 |       2.6
       2 |       7 |        3
(4 rows)
```

Example With **left** side driving topology.

```
SELECT * FROM pgr_withPointsCost(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
```

```

ARRAY[-1,2], ARRAY[-3,7],
driving_side := 'r');
start_pid | end_pid | agg_cost
-----+-----+-----
      -1 |      -3 |         4
      -1 |       7 |        4.4
       2 |      -3 |        2.6
       2 |       7 |         3
(4 rows)

```

Example Does not matter driving side.

```

SELECT * FROM pgr_withPointsCost(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  ARRAY[-1,2], ARRAY[-3,7],
  driving_side := 'b');
start_pid | end_pid | agg_cost
-----+-----+-----
      -1 |      -3 |        3.2
      -1 |       7 |        3.6
       2 |      -3 |        2.6
       2 |       7 |         3
(4 rows)

```

The queries use the [Sample Data](#) network.

History

- Proposed in version 2.2

See Also

- *withPoints* - Family of functions

Indices and tables

- `genindex`
- `search`

pgr_withPointsCostMatrix - proposed

Name

`pgr_withPointsCostMatrix` - Calculates the shortest path and returns only the aggregate cost of the shortest path(s) found, for the combination of points given.

Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.



Fig. 6.10: Boost Graph Inside

Availability: 2.2.0

Signature Summary

```
pgr_withPointsCostMatrix(edges_sql, points_sql, start_vids)
pgr_withPointsCostMatrix(edges_sql, points_sql, start_vids, directed, driving_side)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Note: There is no **details** flag, unlike the other members of the withPoints family of functions.

Signatures

Minimal Signature

The minimal signature:

- Is for a **directed** graph.
- The driving side is set as **b** both. So arriving/departing to/from the point(s) can be in any direction.

```
pgr_withPointsCostMatrix(edges_sql, points_sql, start_vid)
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example

```
SELECT * FROM pgr_withPointsCostMatrix(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction from pointsOfInterest',
  array[-1, 3, 6, -6]);
 start_vid | end_vid | agg_cost
-----+-----+-----
        -6 |         -1 |         1.3
        -6 |          3 |         4.3
        -6 |          6 |         1.3
        -1 |         -6 |         1.3
        -1 |          3 |         5.6
        -1 |          6 |         2.6
          3 |         -6 |         1.7
          3 |         -1 |         1.6
```


3		6		1
6		-6		1.3
6		-1		2.6
6		3		3

(12 rows)

Complete Signature

```
pgr_withPointsCostMatrix(edges_sql, points_sql, start_vids,
    directed:=true, driving_side:='b')
RETURNS SET OF (start_vid, end_vid, agg_cost)
```

Example returning a symmetrical cost matrix

- Using the default **side** value on the **points_sql** query
- Using an undirected graph
- Using the default **driving_side** value

```
SELECT * FROM pgr_withPointsCostMatrix(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
    'SELECT pid, edge_id, fraction from pointsOfInterest',
    array[-1, 3, 6, -6], directed := false);
start_vid | end_vid | agg_cost
-----+-----+-----
-6 | -1 | 1.3
-6 | 3 | 1.7
-6 | 6 | 1.3
-1 | -6 | 1.3
-1 | 3 | 1.6
-1 | 6 | 2.6
3 | -6 | 1.7
3 | -1 | 1.6
3 | 6 | 1
6 | -6 | 1.3
6 | -1 | 2.6
6 | 3 | 1
(12 rows)
```

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none">• When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none">• When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the Points SQL query

points_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Description
pid	ANY-INTEGER	(optional) Identifier of the point. <ul style="list-style-type: none">• If column present, it can not be NULL.• If column not present, a sequential identifier will be given automatically.
edge_id	ANY-INTEGER	Identifier of the “closest” edge to the point.
fraction	ANY-NUMERICAL	Value in <0,1> that indicates the relative position from the first end point of the edge.
side	CHAR	(optional) Value in ['b', 'r', 'l', NULL] indicating if the point is: <ul style="list-style-type: none">• In the right, left of the edge or• If it doesn't matter with 'b' or NULL.• If column not present 'b' is considered.

Where:

ANY-INTEGER smallint, int, bigint

ANY-NUMERICAL smallint, int, bigint, real, float

Description of the parameters of the signatures

Parameter	Type
edges_sql	TEXT
points_sql	TEXT
start_vids	ARRAY [ANY-INTEGER]
directed	BOOLEAN
driving_side	CHAR

Description of the return values for a Cost function Returns set of (start_vid, end_vid, agg_cost)

Column	Type	Description
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
agg_cost	FLOAT	Aggregate cost from start_vid to end_vid.

Examples

Example Use with tsp

```
SELECT * FROM pgr_TSP (
  $$
  SELECT * FROM pgr_withPointsCostMatrix(
    'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
    'SELECT pid, edge_id, fraction from pointsOfInterest',
    array[-1, 3, 6, -6], directed := false);
  $$,
  randomize := false
);
 seq | node | cost | agg_cost
-----+-----+-----+-----
   1 |   -6 |   1.3 |         0
   2 |   -1 |   1.6 |        1.3
   3 |    3 |    1 |        2.9
   4 |    6 |   1.3 |        3.9
   5 |   -6 |    0 |        5.2
(5 rows)
```

See Also

- *withPoints - Family of functions*
- *Cost Matrix - Category*

- *Traveling Sales Person - Family of functions*
- *sampledata* network.

Indices and tables

- *genindex*
- *search*

pgr_withPointsKSP - Proposed

Name

pgr_withPointsKSP - Find the K shortest paths using Yen's algorithm.

- Warning:** Proposed functions for next mayor release.
- They are not officially in the current release.
 - They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.



Fig. 6.11: Boost Graph Inside

Availability: 2.2.0

Synopsis

Modifies the graph to include the points defined in the `points_sql` and using Yen algorithm, finds the K shortest paths.

Signature Summary

```
pgr_withPointsKSP(edges_sql, points_sql, start_pid, end_pid, K)
pgr_withPointsKSP(edges_sql, points_sql, start_pid, end_pid, K, directed, heap_paths, driving_side)
RETURNS SET OF (seq, path_id, path_seq, node, edge, cost, agg_cost)
```

Signatures

Minimal Usage

The minimal usage:

- Is for a **directed** graph.

- The driving side is set as **b** both. So arriving/departing to/from the point(s) can be in any direction.
- No **details** are given about distance of other points of the query.
- No **heap paths** are returned.

```
pgr_withPointsKSP(edges_sql, points_sql, start_pid, end_pid, K)
RETURNS SET OF (seq, path_id, path_seq, node, edge, cost, agg_cost)
```

Example

```
SELECT * FROM pgr_withPointsKSP(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, -2, 2);
```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	-1	1	0.6	0
2	1	2	2	4	1	0.6
3	1	3	5	8	1	1.6
4	1	4	6	9	1	2.6
5	1	5	9	15	0.4	3.6
6	1	6	-2	-1	0	4
7	2	1	-1	1	0.6	0
8	2	2	2	4	1	0.6
9	2	3	5	8	1	1.6
10	2	4	6	11	1	2.6
11	2	5	11	13	1	3.6
12	2	6	12	15	0.6	4.6
13	2	7	-2	-1	0	5.2

(13 rows)

Complete Signature Finds the K shortest paths depending on the optional parameters setup.

```
pgr_withPointsKSP(edges_sql, points_sql, start_pid, end_pid, K,
  directed:=true, heap_paths:=false, driving_side:='b', details:=false)
RETURNS SET OF (seq, path_id, path_seq, node, edge, cost, agg_cost)
```

Example With details.

```
SELECT * FROM pgr_withPointsKSP(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, 6, 2, details := true);
```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	-1	1	0.6	0
2	1	2	2	4	0.7	0.6
3	1	3	-6	4	0.3	1.3
4	1	4	5	8	1	1.6
5	1	5	6	-1	0	2.6
6	2	1	-1	1	0.6	0
7	2	2	2	4	0.7	0.6
8	2	3	-6	4	0.3	1.3
9	2	4	5	10	1	1.6
10	2	5	10	12	0.6	2.6
11	2	6	-3	12	0.4	3.2
12	2	7	11	13	1	3.6
13	2	8	12	15	0.6	4.6
14	2	9	-2	15	0.4	5.2
15	2	10	9	9	1	5.6
16	2	11	6	-1	0	6.6

(16 rows)

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none">• When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none">• When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the Points SQL query

points_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Description
pid	ANY-INTEGER	(optional) Identifier of the point. <ul style="list-style-type: none"> • If column present, it can not be NULL. • If column not present, a sequential identifier will be given automatically.
edge_id	ANY-INTEGER	Identifier of the “closest” edge to the point.
fraction	ANY-NUMERICAL	Value in <0,1> that indicates the relative position from the first end point of the edge.
side	CHAR	(optional) Value in ['b', 'r', 'l', NULL] indicating if the point is: <ul style="list-style-type: none"> • In the right, left of the edge or • If it doesn't matter with 'b' or NULL. • If column not present 'b' is considered.

Where:

ANY-INTEGER smallint, int, bigint

ANY-NUMERICAL smallint, int, bigint, real, float

Description of the parameters of the signatures

Parameter	Type
edges_sql	TEXT
points_sql	TEXT
start_pid	ANY-INTEGER
end_pid	ANY-INTEGER
K	INTEGER
directed	BOOLEAN
heap_paths	BOOLEAN
driving_side	CHAR
details	BOOLEAN

Description of the return values Returns set of (seq, path_id, path_seq, node, edge, cost, agg_cost)

Column	Type	Description
seq	INTEGER	Row sequence.
path_seq	INTEGER	Relative position in the path of node and edge. Has value 1 for the beginning of a path.
path_id	INTEGER	Path identifier. The ordering of the paths: For two paths i, j if $i < j$ then $\text{agg_cost}(i) \leq \text{agg_cost}(j)$.
node	BIGINT	Identifier of the node in the path. Negative values are the identifiers of a point.
edge	BIGINT	Identifier of the edge used to go from node to the next node. <ul style="list-style-type: none"> • -1 for the last row in the path sequence.
cost	FLOAT	Cost to traverse from node using edge to the next node. <ul style="list-style-type: none"> • 0 for the last row in the path sequence.
agg_cost	FLOAT	Aggregate cost from start_pid to node. <ul style="list-style-type: none"> • 0 for the first row in the path sequence.

Examples

Example Left side driving topology with details.

```
SELECT * FROM pgr_withPointsKSP(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, -2, 2,
  driving_side := 'l', details := true);
```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	-1	1	0.6	0
2	1	2	2	4	0.7	0.6
3	1	3	-6	4	0.3	1.3
4	1	4	5	8	1	1.6
5	1	5	6	9	1	2.6
6	1	6	9	15	1	3.6
7	1	7	12	15	0.6	4.6
8	1	8	-2	-1	0	5.2
9	2	1	-1	1	0.6	0
10	2	2	2	4	0.7	0.6
11	2	3	-6	4	0.3	1.3
12	2	4	5	8	1	1.6
13	2	5	6	11	1	2.6
14	2	6	11	13	1	3.6
15	2	7	12	15	0.6	4.6
16	2	8	-2	-1	0	5.2

(16 rows)

Example Right side driving topology with heap paths and details.

```

SELECT * FROM pgr_withPointsKSP(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, -2, 2,
  heap_paths := true, driving_side := 'r', details := true);
 seq | path_id | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----
  1 |      1 |      1 |   -1 |    1 |  0.4 |         0
  2 |      1 |      2 |    1 |    1 |    1 |         0.4
  3 |      1 |      3 |    2 |    4 |  0.7 |         1.4
  4 |      1 |      4 |   -6 |    4 |  0.3 |         2.1
  5 |      1 |      5 |    5 |    8 |    1 |         2.4
  6 |      1 |      6 |    6 |    9 |    1 |         3.4
  7 |      1 |      7 |    9 |   15 |  0.4 |         4.4
  8 |      1 |      8 |   -2 |   -1 |    0 |         4.8
  9 |      2 |      1 |   -1 |    1 |  0.4 |         0
 10 |      2 |      2 |    1 |    1 |    1 |         0.4
 11 |      2 |      3 |    2 |    4 |  0.7 |         1.4
 12 |      2 |      4 |   -6 |    4 |  0.3 |         2.1
 13 |      2 |      5 |    5 |    8 |    1 |         2.4
 14 |      2 |      6 |    6 |   11 |    1 |         3.4
 15 |      2 |      7 |   11 |   13 |    1 |         4.4
 16 |      2 |      8 |   12 |   15 |    1 |         5.4
 17 |      2 |      9 |    9 |   15 |  0.4 |         6.4
 18 |      2 |     10 |   -2 |   -1 |    0 |         6.8
 19 |      3 |      1 |   -1 |    1 |  0.4 |         0
 20 |      3 |      2 |    1 |    1 |    1 |         0.4
 21 |      3 |      3 |    2 |    4 |  0.7 |         1.4
 22 |      3 |      4 |   -6 |    4 |  0.3 |         2.1
 23 |      3 |      5 |    5 |   10 |    1 |         2.4
 24 |      3 |      6 |   10 |   12 |  0.6 |         3.4
 25 |      3 |      7 |   -3 |   12 |  0.4 |         4
 26 |      3 |      8 |   11 |   13 |    1 |         4.4
 27 |      3 |      9 |   12 |   15 |    1 |         5.4
 28 |      3 |     10 |    9 |   15 |  0.4 |         6.4
 29 |      3 |     11 |   -2 |   -1 |    0 |         6.8
(29 rows)

```

The queries use the [Sample Data](#) network.

History

- Proposed in version 2.2

See Also

- *withPoints* - Family of functions

Indices and tables

- genindex
- search

pgr_withPointsDD - Proposed

Name

pgr_withPointsDD - Returns the driving distance from a starting point.

Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.



Fig. 6.12: Boost Graph Inside

Availability: 2.2.0

Synopsis

Modify the graph to include points and using Dijkstra algorithm, extracts all the nodes and points that have costs less than or equal to the value `distance` from the starting point. The edges extracted will conform the corresponding spanning tree.

Signature Summary

```
pgr_withPointsDD(edges_sql, points_sql, start_vid, distance)
pgr_withPointsDD(edges_sql, points_sql, start_vid, distance, directed, driving_side, details)
pgr_withPointsDD(edges_sql, points_sql, start_vids, distance, directed, driving_side, details, eq)
RETURNS SET OF (seq, node, edge, cost, agg_cost)
```

Signatures

Minimal Use

The minimal signature:

- Is for a **directed** graph.
- The driving side is set as **b** both. So arriving/departing to/from the point(s) can be in any direction.
- No **details** are given about distance of other points of the query.

```
pgr_withPointsDD(edges_sql, points_sql, start_vid, distance)
    directed:=true, driving_side:='b', details:=false)
RETURNS SET OF (seq, node, edge, cost, agg_cost)
```

Example

```
SELECT * FROM pgr_withPointsDD(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, 3.8);
```

seq	node	edge	cost	agg_cost
1	-1	-1	0	0
2	1	1	0.4	0.4
3	2	1	0.6	0.6
4	5	4	1	1.6
5	6	8	1	2.6
6	8	7	1	2.6
7	10	10	1	2.6
8	7	6	1	3.6
9	9	9	1	3.6
10	11	11	1	3.6
11	13	14	1	3.6

(11 rows)

Driving distance from a single point Finds the driving distance depending on the optional parameters setup.

```
pgr_withPointsDD(edges_sql, points_sql, start_vids, distance,
  directed:=true, driving_side:='b', details:=false)
RETURNS SET OF (seq, node, edge, cost, agg_cost)
```

Example Right side driving topology

```
SELECT * FROM pgr_withPointsDD(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, 3.8,
  driving_side := 'r',
  details := true);
```

seq	node	edge	cost	agg_cost
1	-1	-1	0	0
2	1	1	0.4	0.4
3	2	1	1	1.4
4	-6	4	0.7	2.1
5	5	4	0.3	2.4
6	6	8	1	3.4
7	8	7	1	3.4
8	10	10	1	3.4

(8 rows)

Driving distance from many starting points Finds the driving distance depending on the optional parameters setup.

```
pgr_withPointsDD(edges_sql, points_sql, start_vids, distance,
  directed:=true, driving_side:='b', details:=false, equicost:=false)
RETURNS SET OF (seq, node, edge, cost, agg_cost)
```

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none">• When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none">• When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the Points SQL query

points_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Description
pid	ANY-INTEGER	(optional) Identifier of the point. <ul style="list-style-type: none">• If column present, it can not be NULL.• If column not present, a sequential identifier will be given automatically.
edge_id	ANY-INTEGER	Identifier of the “closest” edge to the point.
fraction	ANY-NUMERICAL	Value in <0,1> that indicates the relative position from the first end point of the edge.
side	CHAR	(optional) Value in ['b', 'r', 'l', NULL] indicating if the point is: <ul style="list-style-type: none">• In the right, left of the edge or• If it doesn't matter with 'b' or NULL.• If column not present 'b' is considered.

Where:

ANY-INTEGER smallint, int, bigint

ANY-NUMERICAL smallint, int, bigint, real, float

Description of the parameters of the signatures

Parameter	Type
edges_sql	TEXT
points_sql	TEXT
start_vid	ANY-INTEGER
distance	ANY-NUMERICAL
directed	BOOLEAN
driving_side	CHAR
details	BOOLEAN
equicost	BOOLEAN

Description of the return values Returns set of (seq, node, edge, cost, agg_cost)

Column	Type	Description
seq	INT	row sequence.
node	BIGINT	Identifier of the node within the Distance from start_pid. If details =: true a negative value is the identifier of a point.
edge	BIGINT	Identifier of the edge used to go from node to the next node. <ul style="list-style-type: none"> • -1 when start_vid = node.
cost	FLOAT	Cost to traverse edge. <ul style="list-style-type: none"> • 0 when start_vid = node.
agg_cost	FLOAT	Aggregate cost from start_vid to node. <ul style="list-style-type: none"> • 0 when start_vid = node.

Examples for queries marked as directed with cost and reverse_cost columns

The examples in this section use the following *Network for queries marked as directed and cost and reverse_cost columns are used*

Example Left side driving topology

```
SELECT * FROM pgr_withPointsDD(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, 3.8,
  driving_side := 'l',
  details := true);
```

seq	node	edge	cost	agg_cost
1	-1	-1	0	0
2	2	1	0.6	0.6
3	-6	4	0.7	1.3
4	5	4	0.3	1.6
5	1	1	1	1.6
6	6	8	1	2.6
7	8	7	1	2.6
8	10	10	1	2.6
9	-3	12	0.6	3.2
10	-4	6	0.7	3.3
11	7	6	0.3	3.6
12	9	9	1	3.6
13	11	11	1	3.6
14	13	14	1	3.6

(14 rows)

Example Does not matter driving side.

```
SELECT * FROM pgr_withPointsDD(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table ORDER BY id',
  'SELECT pid, edge_id, fraction, side from pointsOfInterest',
  -1, 3.8,
  driving_side := 'b',
  details := true);
```

seq	node	edge	cost	agg_cost
1	-1	-1	0	0
2	1	1	0.4	0.4
3	2	1	0.6	0.6
4	-6	4	0.7	1.3
5	5	4	0.3	1.6
6	6	8	1	2.6
7	8	7	1	2.6
8	10	10	1	2.6
9	-3	12	0.6	3.2
10	-4	6	0.7	3.3
11	7	6	0.3	3.6
12	9	9	1	3.6
13	11	11	1	3.6
14	13	14	1	3.6

(14 rows)

The queries use the [Sample Data](#) network.

History

- Proposed in version 2.2

See Also

- *pgr_drivingDistance* - Driving distance using dijkstra.
- *pgr_alphaShape* - Alpha shape computation.
- *pgr_pointsAsPolygon* - Polygon around set of points.

Indices and tables

- genindex
- search

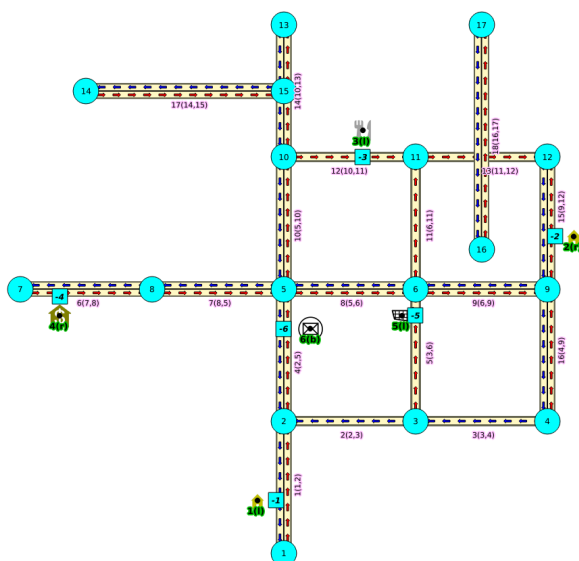
Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.

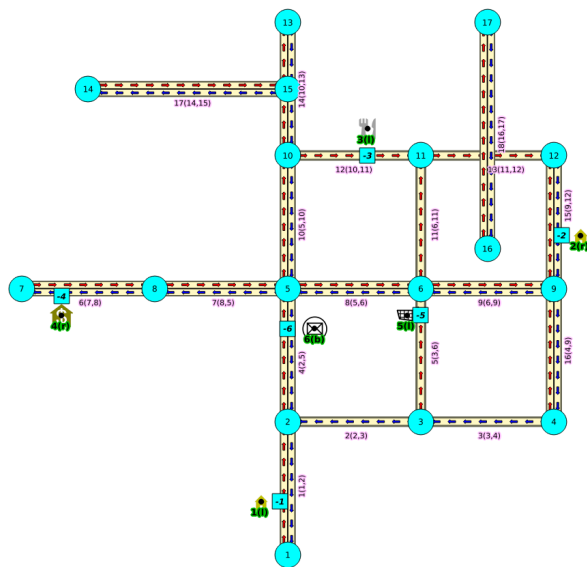
Images

The squared vertices are the temporary vertices, The temporary vertices are added according to the driving side, The following images visually show the differences on how depending on the driving side the data is interpreted.

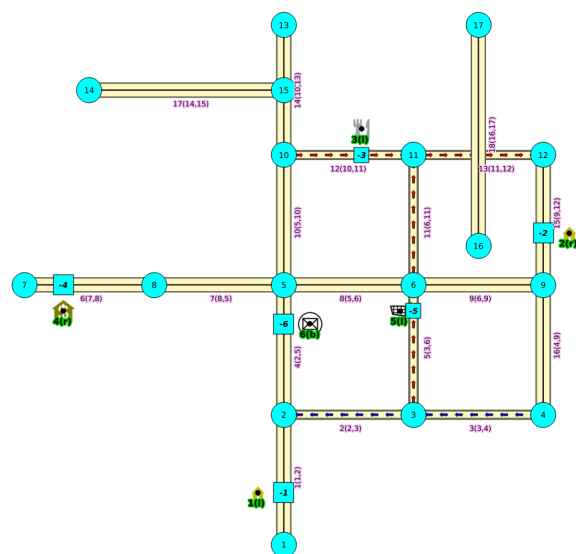
Right driving side



Left driving side



doesn't matter the driving side



Introduction

This family of functions was thought for routing vehicles, but might as well work for some other application that we can not think of.

The with points family of function give you the ability to route between arbitrary points located outside the original graph.

When given a point identified with a *pid* that its being mapped to and edge with an identifier *edge_id*, with a *fraction* along that edge (from the source to the target of the edge) and some additional information about which *side* of the edge the point is on, then routing from arbitrary points more accurately reflect routing vehicles in road networks,

I talk about a family of functions because it includes different functionalities.

- `pgr_withPoints` is `pgr_dijkstra` based
- `pgr_withPointsCost` is `pgr_dijkstraCost` based
- `pgr_withPointsKSP` is `pgr_ksp` based
- `pgr_withPointsDD` is `pgr_drivingDistance` based

In all this functions we have to take care of as many aspects as possible:

- Must work for routing:
 - Cars (directed graph)
 - Pedestrians (undirected graph)
- Arriving at the point:
 - In either side of the street.
 - Compulsory arrival on the side of the street where the point is located.
- Countries with:
 - Right side driving
 - Left side driving
- Some points are:
 - Permanent, for example the set of points of clients stored in a table in the data base
 - Temporal, for example points given through a web application
- The numbering of the points are handled with negative sign.
 - Original point identifiers are to be positive.
 - Transformation to negative is done internally.
 - For results for involving vertices identifiers
 - * positive sign is a vertex of the original graph
 - * negative sign is a point of the temporary points

The reason for doing this is to avoid confusion when there is a vertex with the same number as identifier as the points identifier.

Graph & edges

- Let $G_d(V, E)$ where V is the set of vertices and E is the set of edges be the original directed graph.
 - An edge of the original `edges_sql` is $(id, source, target, cost, reverse_cost)$ will generate internally
 - * $(id, source, target, cost)$
 - * $(id, target, source, reverse_cost)$

Point Definition

- A point is defined by the quadruplet: $(pid, eid, fraction, side)$
 - **pid** is the point identifier
 - **eid** is an edge id of the `edges_sql`
 - **fraction** represents where the edge `eid` will be cut.
 - **side** Indicates the side of the edge where the point is located.

Creating Temporary Vertices in the Graph

For edge (15, 9, 12, 10, 20), & lets insert point (2, 12, 0.3, r)

On a right hand side driving network

From first image above:

- We can arrive to the point only via vertex 9.
- It only affects the edge (15, 9, 12, 10) so that edge is removed.
- Edge (15, 12, 9, 20) is kept.
- Create new edges:
 - (15, 9, -1, 3) edge from vertex 9 to point 1 has cost 3
 - (15, -1, 12, 7) edge from point 1 to vertex 12 has cost 7

On a left hand side driving network

From second image above:

- We can arrive to the point only via vertex 12.
- It only affects the edge (15, 12, 9, 20) so that edge is removed.
- Edge (15, 9, 12, 10) is kept.
- Create new edges:
 - (15, 12, -1, 14) edge from vertex 12 to point 1 has cost 14
 - (15, -1, 9, 6) edge from point 1 to vertex 9 has cost 6

Remember that fraction is from vertex 9 to vertex 12

When driving side does not matter

From third image above:

- We can arrive to the point either via vertex 12 or via vertex 9
- Edge (15, 12, 9, 20) is removed.
- Edge (15, 9, 12, 10) is removed.
- Create new edges:
 - (15, 12, -1, 14) edge from vertex 12 to point 1 has cost 14
 - (15, -1, 9, 6) edge from point 1 to vertex 9 has cost 6
 - (15, 9, -1, 3) edge from vertex 9 to point 1 has cost 3
 - (15, -1, 12, 7) edge from point 1 to vertex 12 has cost 7

See Also

Indices and tables

- [genindex](#)
- [search](#)

6.1.5 Cost - Category

- *pgr_aStarCost – proposed*
- *pgr_bdAstarCost - Proposed*
- *pgr_bdDijkstraCost - Proposed*
- *pgr_dijkstraCost*
- *pgr_withPointsCost - Proposed*

Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.

General Information

Characteristics

The main Characteristics are:

- Each function works as part of the family it belongs to.
- It does not return a path.
- Returns the sum of the costs of the resulting path(s) for pair combination of nodes in the graph.
- Process is done only on edges with positive costs.
- Values are returned when there is a path.
 - The returned values are in the form of a set of $(start_vid, end_vid, agg_cost)$.
 - When the starting vertex and ending vertex are the same, there is no path.
 - * The agg_cost in the non included values (v, v) is 0.
 - When the starting vertex and ending vertex are the different and there is no path.
 - * The agg_cost in the non included values (u, v) is ∞ .
- Let be the case the values returned are stored in a table, so the unique index would be the pair: $(start_vid, end_vid)$.
- Depending on the function and its parameters, the results can be symmetric.
 - The agg_cost of (u, v) is the same as for (v, u) .
- Any duplicated value in the $start_vids$ or in end_vids are ignored.
- The returned values are ordered:
 - $start_vid$ ascending
 - end_vid ascending

See Also

Indices and tables

- [genindex](#)
- [search](#)

6.1.6 Cost Matrix - Category

- *pgr_aStarCostMatrix - proposed*
- *pgr_bdAstarCostMatrix - proposed*
- *pgr_bdDijkstraCostMatrix - proposed*
- *pgr_dijkstraCostMatrix - proposed*
- *pgr_withPointsCostMatrix - proposed*

Warning: Proposed functions for next mayor release.

- They are not officially in the current release.
- They will likely officially be part of the next mayor release:
 - The functions make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might not change. (But still can)
 - Signature might not change. (But still can)
 - Functionality might not change. (But still can)
 - pgTap tests have being done. But might need more.
 - Documentation might need refinement.

General Information

Synopsis

Traveling Sales Person - Family of functions needs as input a symmetric cost matrix and no edge (u, v) must value ∞ .

This collection of functions will return a cost matrix in form of a table.

Characteristics

The main Characteristics are:

- Can be used as input to *pgr_TSP*.
 - **directly** when the resulting matrix is symmetric and there is no ∞ value.
 - It will be the users responsibility to make the matrix symmetric.
 - * By using geometric or harmonic average of the non symmetric values.
 - * By using max or min the non symmetric values.
 - * By setting the upper triangle to be the mirror image of the lower triangle.
 - * By setting the lower triangle to be the mirror image of the upper triangle.
 - It is also the users responsibility to fix an ∞ value.
- Each function works as part of the family it belongs to.
- It does not return a path.

- Returns the sum of the costs of the shortest path for pair combination of nodes in the graph.
- Process is done only on edges with positive costs.
- Values are returned when there is a path.
 - The returned values are in the form of a set of $(start_vid, end_vid, agg_cost)$.
 - When the starting vertex and ending vertex are the same, there is no path.
 - * The agg_cost in the non included values (v, v) is 0 .
 - When the starting vertex and ending vertex are the different and there is no path.
 - * The agg_cost in the non included values (u, v) is ∞ .
- Let be the case the values returned are stored in a table, so the unique index would be the pair: $(start_vid, end_vid)$.
- Depending on the function and its parameters, the results can be symmetric.
 - The agg_cost of (u, v) is the same as for (v, u) .
- Any duplicated value in the $start_vids$ are ignored.
- The returned values are ordered:
 - $start_vid$ ascending
 - end_vid ascending
- Running time: approximately $O(|start_vids| * (V \log V + E))$

See Also

- [*pgr_TSP*](#)

Indices and tables

- [genindex](#)
- [search](#)

6.1.7 KSP Category

- [*pgr_KSP*](#) - Driving Distance based on `pgr_dijkstra`
- [*pgr_withPointsKSP - Proposed*](#) - Driving Distance based on `pgr_dijkstra`

Indices and tables

- [genindex](#)
- [search](#)

6.2 Experimental Functions

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Contraction - Family of functions - Reduce network size using contraction techniques

- *pgr_contractGraph - Experimental* - Reduce network size using contraction techniques

Graph Analysis

- *pgr_labelGraph - Experimental* - Analyze / label subgraphs within a network

Components - Family of functions - Analyze components within a graph

- *pgr_connectedComponents - Experimental* - Return the connected components of an undirected graph
- *pgr_strongComponents - Experimental* - Return the strongly connected components of a directed graph
- *pgr_biconnectedComponents - Experimental* - Return the biconnected components of an undirected graph
- *pgr_articulationPoints - Experimental* - Return the articulation points of an undirected graph
- *pgr_bridges - Experimental* - Return the bridges of an undirected graph

VRP

- *pgr_gsoc_vrppdtw - Experimental*
- *pgr_vrpOneDepot - Experimental*

6.2.1 Contraction - Family of functions

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

pgr_contractGraph - Experimental

pgr_contractGraph - Experimental

`pgr_contractGraph` — Performs graph contraction and returns the contracted vertices and edges.



Fig. 6.13: Boost Graph Inside

Availability: 2.3.0

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

Contraction reduces the size of the graph by removing some of the vertices and edges and, for example, might add edges that represent a sequence of original edges decreasing the total time and space used in graph algorithms.

Characteristics

The main Characteristics are:

- Process is done only on edges with positive costs.
- There are two types of contraction methods used namely,
 - Dead End Contraction
 - Linear Contraction
- The values returned include the added edges and contracted vertices.
- The returned values are ordered as follows:
 - column *id* ascending when type = *v*
 - column *id* descending when type = *e*

Signature Summary:

The `pgr_contractGraph` function has the following signatures:

```
pgr_contractGraph(edges_sql, contraction_order)
pgr_contractGraph(edges_sql, contraction_order, max_cycles, forbidden_vertices, directed)

RETURNS SETOF (seq, type, id, contracted_vertices, source, target, cost)
```

Signatures

Minimal signature

```
pgr_contractGraph(edges_sql, contraction_order)
```

Example Making a dead end contraction and a linear contraction.

```
SELECT * FROM pgr_contractGraph(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[1, 2]);
```

seq	type	id	contracted_vertices	source	target	cost
1	v	5	{7,8}	-1	-1	-1
2	v	15	{14}	-1	-1	-1
3	v	17	{16}	-1	-1	-1
4	e	-1	{1,2}	3	5	2
5	e	-2	{4}	9	3	2
6	e	-3	{10,13}	5	11	2
7	e	-4	{12}	11	9	2

(7 rows)

Complete signature

```
pgr_contractGraph(edges_sql, contraction_order, max_cycles, forbidden_vertices, directed)
```


Example Making a dead end contraction and a linear contraction and vertex 2 is forbidden from contraction

```
SELECT * FROM pgr_contractGraph(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[1, 2], forbidden_vertices:=ARRAY[2]);
seq | type | id | contracted_vertices | source | target | cost
-----+-----+-----+-----+-----+-----+-----
  1 | v   |  2 | {1}                |    -1 |    -1 |   -1
  2 | v   |  5 | {7,8}              |    -1 |    -1 |   -1
  3 | v   | 15 | {14}               |    -1 |    -1 |   -1
  4 | v   | 17 | {16}               |    -1 |    -1 |   -1
  5 | e   | -1 | {4}                |     9 |     3 |    2
  6 | e   | -2 | {10,13}            |     5 |    11 |    2
  7 | e   | -3 | {12}               |    11 |     9 |    2
(7 rows)
```

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Column	Type	Description
edges_sql	TEXT	SQL query as described above.
contraction_order	ARRAY [ANY-INTEGER]	Ordered contraction operations. <ul style="list-style-type: none">• 1 = Dead end contraction• 2 = Linear contraction
forbidden_vertices	ARRAY [ANY-INTEGER]	(optional). Identifiers of vertices forbidden from contraction. Default is an empty array.
max_cycles	INTEGER	(optional). Number of times the contraction operations on <i>contraction_order</i> will be performed. Default is 1.
directed	BOOLEAN	<ul style="list-style-type: none">• When <code>true</code> the graph is considered as <i>Directed</i>.• When <code>false</code> the graph is considered as <i>Undirected</i>.

Description of the return values

RETURNS SETOF (seq, type, id, contracted_vertices, source, target, cost)

The function returns a single row. The columns of the row are:

Column	Type	Description
seq	INTEGER	Sequential value starting from 1 .
type	TEXT	Type of the <i>id</i>. <ul style="list-style-type: none"> • 'v' when <i>id</i> is an identifier of a vertex. • 'e' when <i>id</i> is an identifier of an edge.
id	BIGINT	Identifier of: <ul style="list-style-type: none"> • the vertex when <i>type</i> = 'v'. <ul style="list-style-type: none"> – The vertex belongs to the <i>edge_table</i> passed as a parameter. • the edge when <i>type</i> = 'e'. <ul style="list-style-type: none"> – The <i>id</i> is a decreasing sequence starting from -1. – Representing a pseudo <i>id</i> as is not incorporated into the <i>edge_table</i>.
contracted_vertices	ARRAY[BIGINT]	Array of contracted vertex identifiers.
source	BIGINT	Identifier of the source vertex of the current edge <i>id</i> . Valid values when <i>type</i> = 'e'.
target	BIGINT	Identifier of the target vertex of the current edge <i>id</i> . Valid values when <i>type</i> = 'e'.
cost	FLOAT	Weight of the edge (<i>source</i> , <i>target</i>). Valid values when <i>type</i> = 'e'.

Examples

Example Only dead end contraction

```
SELECT * FROM pgr_contractGraph(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[1]);
```

seq	type	id	contracted_vertices	source	target	cost
1	v	2	{1}	-1	-1	-1
2	v	5	{7,8}	-1	-1	-1
3	v	10	{13}	-1	-1	-1
4	v	15	{14}	-1	-1	-1
5	v	17	{16}	-1	-1	-1

(5 rows)

Example Only linear contraction

```
SELECT * FROM pgr_contractGraph(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[2]);
```

seq	type	id	contracted_vertices	source	target	cost
1	e	-1	{4}	9	3	2
2	e	-2	{8}	5	7	2
3	e	-3	{8}	7	5	2
4	e	-4	{12}	11	9	2
(4 rows)						

Indices and tables

- genindex
- search

Introduction

In big graphs, like the road graphs, or electric networks, graph contraction can be used to speed up some graph algorithms. Contraction reduces the size of the graph by removing some of the vertices and edges and, for example, might add edges that represent a sequence of original edges decreasing the total time and space used in graph algorithms.

This implementation gives a flexible framework for adding contraction algorithms in the future, currently, it supports two algorithms:

1. Dead end contraction
2. Linear contraction

Allowing the user to:

- Forbid contraction on a set of nodes.
- Decide the order of the contraction algorithms and set the maximum number of times they are to be executed.

Note: UNDER DISCUSSION: Forbid contraction on a set of edges

Dead end contraction

In the algorithm, dead end contraction is represented by 1.

Dead end nodes

The definition of a dead end node is different for a directed and an undirected graph.

In case of a undirected graph, a node is considered a dead end node if

- The number of adjacent vertices is 1.

In case of an directed graph, a node is considered a dead end node if

- There are no outgoing edges and has at least one incoming edge.
- There is one incoming and one outgoing edge with the same identifier.

Examples

- The green node B represents a dead end node
- The node A is the only node connecting to B.
- Node A is part of the rest of the graph and has an unlimited number of incoming and outgoing edges.
- Directed graph

Operation: Dead End Contraction

The dead end contraction will stop until there are no more dead end nodes. For example from the following graph:

- Node A is connected to the rest of the graph by an unlimited number of edges.
- Node B is connected to the rest of the graph with one incoming edge.
- Node B is the only node connecting to C.
- The green node C represents a *Dead End* node

After contracting C, node B is now a *Dead End* node and is contracted:

Node B gets contracted

Nodes B and C belong to node A.

Not Dead End nodes

In this graph B is not a *dead end* node.

Linear contraction

In the algorithm, linear contraction is represented by 2.

Linear nodes

A node is considered a linear node if satisfies the following:

- The number of adjacent vertices are 2.
- Should have at least one incoming edge and one outgoing edge.

Examples

- The green node B represents a linear node
- The nodes A and C are the only nodes connecting to B.
- Node A is part of the rest of the graph and has an unlimited number of incoming and outgoing edges.
- Node C is part of the rest of the graph and has an unlimited number of incoming and outgoing edges.
- Directed graph

Operation: Linear Contraction

The linear contraction will stop until there are no more linear nodes. For example from the following graph:

- Node A is connected to the rest of the graph by an unlimited number of edges.
- Node B is connected to the rest of the graph with one incoming edge and one outgoing edge.
- Node C is connected to the rest of the graph with one incoming edge and one outgoing edge.
- Node D is connected to the rest of the graph by an unlimited number of edges.
- The green nodes B and C represents *Linear* nodes.

After contracting B, a new edge gets inserted between A and C which is represented by red color.

Node C is *linear node* and gets contracted.

Nodes B and C belong to edge connecting A and D which is represented by red color.

Not Linear nodes

In this graph B is not a *linear* node.

The cycle

Contracting a graph, can be done with more than one operation. The order of the operations affect the resulting contracted graph, after applying one operation, the set of vertices that can be contracted by another operation changes.

This implementation, cycles `max_cycles` times through `operations_order`.

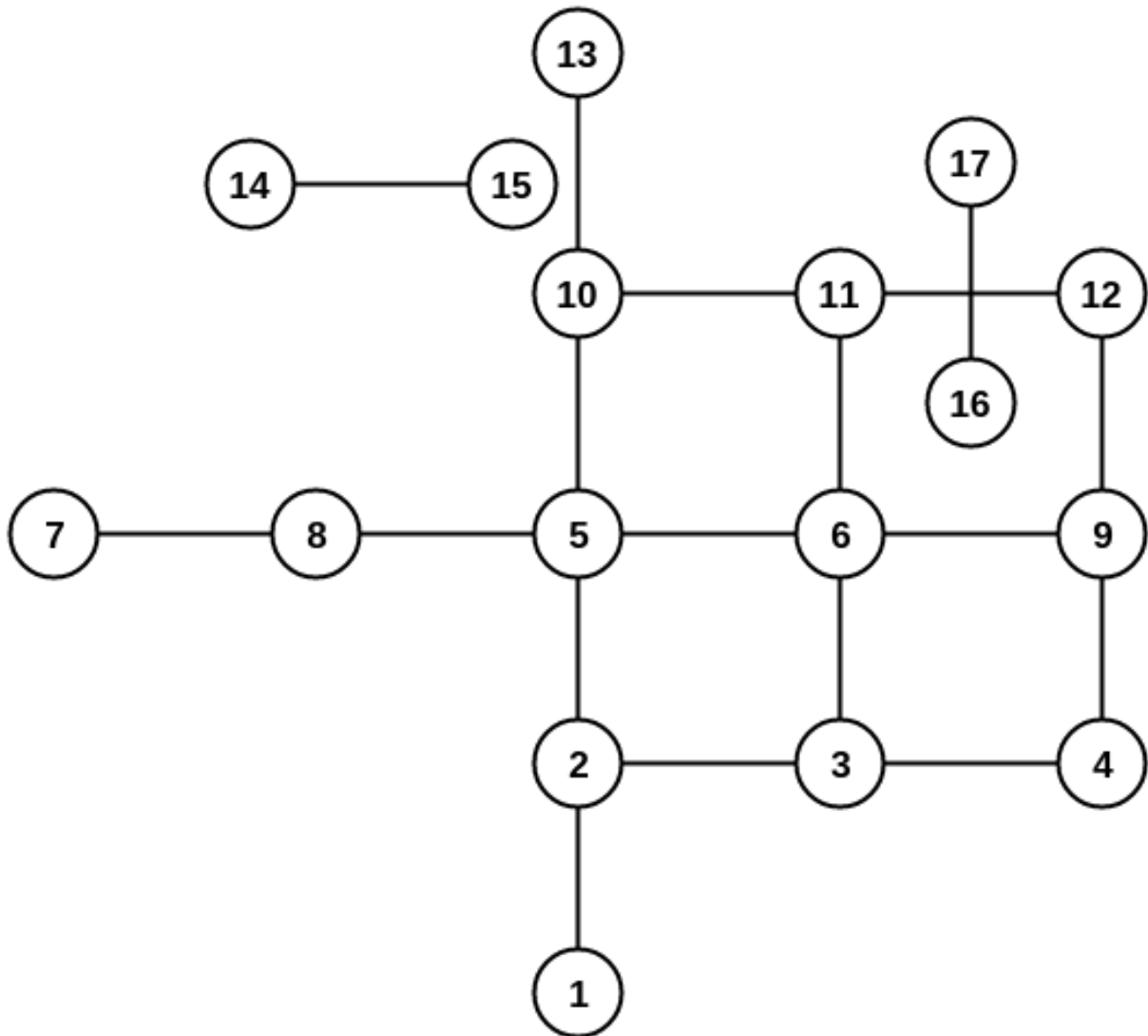
```
<input>
do max_cycles times {
  for (operation in operations_order)
    { do operation }
}
<output>
```

Contracting Sample Data

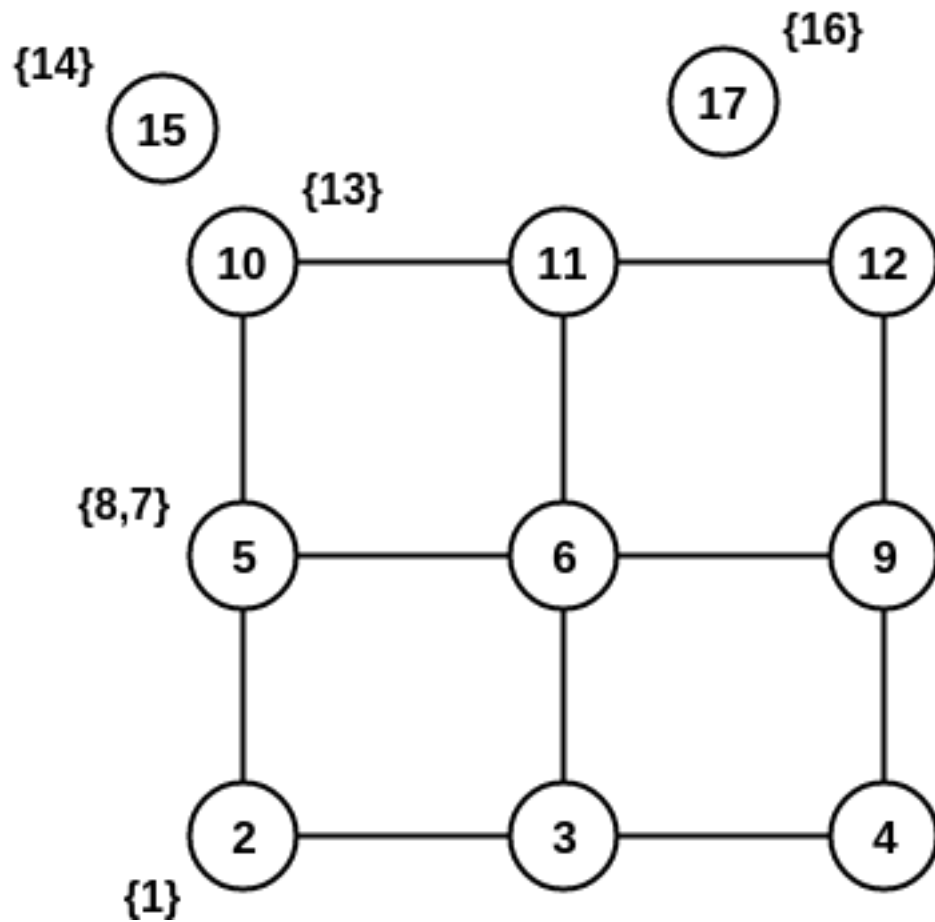
In this section, building and using a contracted graph will be shown by example.

- The [Sample Data](#) for an undirected graph is used
- a dead end operation first followed by a linear operation.

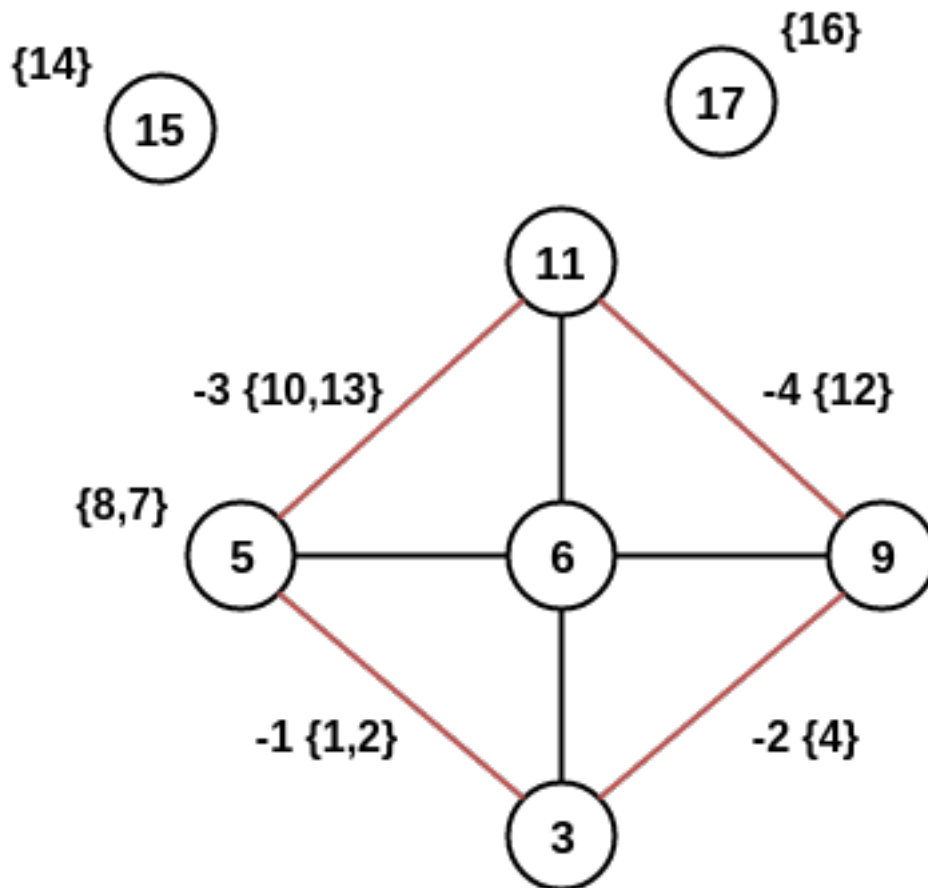
The original graph:



After doing a dead end contraction operation:



Doing a linear contraction operation to the graph above



There are five cases, in this documentation, which arise when calculating the shortest path between a given source and target. In this examples, `pgr_dijkstra` is used.

- **Case 1:** Both source and target belong to the contracted graph.
- **Case 2:** Source belongs to a contracted graph, while target belongs to a edge subgraph.
- **Case 3:** Source belongs to a vertex subgraph, while target belongs to an edge subgraph.
- **Case 4:** Source belongs to a contracted graph, while target belongs to an vertex subgraph.
- **Case 5:** The path contains a new edge added by the contraction algorithm.

Construction of the graph in the database

Original Data

The following query shows the original data involved in the contraction operation.

Contraction Results

```
SELECT * FROM pgr_contractGraph(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  array[1,2], directed:=true);
```

seq	type	id	contracted_vertices	source	target	cost
1	v	5	{7,8}	-1	-1	-1
2	v	15	{14}	-1	-1	-1

3	v	17	{16}		-1		-1		-1
4	e	-1	{1,2}		3		5		2
5	e	-2	{4}		9		3		2
6	e	-3	{10,13}		5		11		2
7	e	-4	{12}		11		9		2
(7 rows)									

The above results do not represent the contracted graph. They represent the changes done to the graph after applying the contraction algorithm. We can see that vertices like 6 and 11 do not appear in the contraction results because they were not affected by the contraction algorithm.

step 1

Adding extra columns to the `edge_table` and `edge_table_vertices_pgr` tables:

Column	Description
contracted_vertices	The vertices set belonging to the vertex/edge
is_contracted	On a <i>vertex</i> table: when <code>true</code> the vertex is contracted, so is not part of the contracted graph.
is_contracted	On an <i>edge</i> table: when <code>true</code> the edge was generated by the contraction algorithm.

Using the following queries:

```
ALTER TABLE edge_table ADD contracted_vertices BIGINT[];
ALTER TABLE
ALTER TABLE edge_table_vertices_pgr ADD contracted_vertices BIGINT[];
ALTER TABLE
ALTER TABLE edge_table ADD is_contracted BOOLEAN DEFAULT false;
ALTER TABLE
ALTER TABLE edge_table_vertices_pgr ADD is_contracted BOOLEAN DEFAULT false;
ALTER TABLE
SET client_min_messages TO NOTICE;
SET
```

step 2

For simplicity, in this documentation, store the results of the call to `pgr_contractGraph` in a temporary table

```
SELECT * INTO contraction_results
FROM pgr_contractGraph(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  array[1,2], directed:=true);
SELECT 7
```

step 3

Update the *vertex* and *edge* tables using the results of the call to `pgr_contraction`

- In `edge_table_vertices_pgr.is_contracted` indicate the vertices that are contracted.

```
UPDATE edge_table_vertices_pgr
SET is_contracted = true
WHERE id IN (SELECT unnest(contracted_vertices) FROM contraction_results);
UPDATE 10
```

- Add to `edge_table_vertices_pgr.contracted_vertices` the contracted vertices belonging to the vertices.

```

UPDATE edge_table_vertices_pgr
SET contracted_vertices = contraction_results.contracted_vertices
FROM contraction_results
WHERE type = 'v' AND edge_table_vertices_pgr.id = contraction_results.id;
UPDATE 3

```

- Insert the new edges generated by `pgr_contractGraph`.

```

INSERT INTO edge_table(source, target, cost, reverse_cost, contracted_vertices, is_contracted)
SELECT source, target, cost, -1, contracted_vertices, true
FROM contraction_results
WHERE type = 'e';
INSERT 0 4

```

step 3.1

Verify visually the updates.

- On the `edge_table_vertices_pgr`

```

SELECT id, contracted_vertices, is_contracted
FROM edge_table_vertices_pgr
ORDER BY id;

```

id	contracted_vertices	is_contracted
1		t
2		t
3		f
4		t
5	{7,8}	f
6		f
7		t
8		t
9		f
10		t
11		f
12		t
13		t
14		t
15	{14}	f
16		t
17	{16}	f

(17 rows)

- On the `edge_table`

```

SELECT id, source, target, cost, reverse_cost, contracted_vertices, is_contracted
FROM edge_table
ORDER BY id;

```

id	source	target	cost	reverse_cost	contracted_vertices	is_contracted
1	1	2	1	1		f
2	2	3	-1	1		f
3	3	4	-1	1		f
4	2	5	1	1		f
5	3	6	1	-1		f
6	7	8	1	1		f
7	8	5	1	1		f
8	5	6	1	1		f
9	6	9	1	1		f
10	5	10	1	1		f
11	6	11	1	-1		f

12		10		11		1		-1				f
13		11		12		1		-1				f
14		10		13		1		1				f
15		9		12		1		1				f
16		4		9		1		1				f
17		14		15		1		1				f
18		16		17		1		1				f
19		3		5		2		-1		{1,2}		t
20		9		3		2		-1		{4}		t
21		5		11		2		-1		{10,13}		t
22		11		9		2		-1		{12}		t

(22 rows)

- vertices that belong to the contracted graph are the non contracted vertices

```
SELECT id FROM edge_table_vertices_pgr
WHERE is_contracted = false
ORDER BY id;
 id
----
  3
  5
  6
  9
 11
 15
 17
(7 rows)
```

case 1: Both source and target belong to the contracted graph.

Inspecting the contracted graph above, vertex 3 and vertex 11 are part of the contracted graph. In the following query:

- vertices_in_graph hold the vertices that belong to the contracted graph.
- when selecting the edges, only edges that have the source and the target in that set are the edges belonging to the contracted graph, that is done in the WHERE clause.

Visually, looking at the original graph, going from 3 to 11: 3 -> 6 -> 11, and in the contracted graph, it is also 3 -> 6 -> 11. The results, on the contracted graph match the results as if it was done on the original graph.

```
SELECT * FROM pgr_dijkstra(
  $$
  WITH
  vertices_in_graph AS (
    SELECT id FROM edge_table_vertices_pgr WHERE is_contracted = false)
  SELECT id, source, target, cost, reverse_cost
  FROM edge_table
  WHERE source IN (SELECT * FROM vertices_in_graph)
  AND target IN (SELECT * FROM vertices_in_graph)
  $$,
  3, 11, false);
 seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |         |  1 |   3 |   5 |         0
  2 |         |  2 |   6 |   1 |         1
  3 |         |  3 |  11 |   0 |         2
(3 rows)
```

case 2: Source belongs to the contracted graph, while target belongs to a edge subgraph.

Inspecting the contracted graph above, vertex 3 is part of the contracted graph and vertex 1 belongs to the contracted subgraph.

- expand1 holds the contracted vertices of the edge where vertex 1 belongs. (belongs to edge 19).
- vertices_in_graph hold the vertices that belong to the contracted graph and also the contracted vertices of edge 19.
- when selecting the edges, only edges that have the source and the target in that set are the edges belonging to the contracted graph, that is done in the WHERE clause.

Visually, looking at the original graph, going from 3 to 1: 3 -> 2 -> 1, and in the contracted graph, it is also 3 -> 2 -> 1. The results, on the contracted graph match the results as if it was done on the original graph.

```
SELECT * FROM pgr_dijkstra(
  $$
  WITH
  expand_edges AS (SELECT id, unnest(contracted_vertices) AS vertex FROM edge_table),
  expand1 AS (SELECT contracted_vertices FROM edge_table
    WHERE id IN (SELECT id FROM expand_edges WHERE vertex = 1)),
  vertices_in_graph AS (
    SELECT id FROM edge_table_vertices_pgr WHERE is_contracted = false
    UNION
    SELECT unnest(contracted_vertices) FROM expand1)
  SELECT id, source, target, cost, reverse_cost
  FROM edge_table
  WHERE source IN (SELECT * FROM vertices_in_graph)
  AND target IN (SELECT * FROM vertices_in_graph)
  $$,
  3, 1, false);
```

seq	path_seq	node	edge	cost	agg_cost
1	1	3	2	1	0
2	2	2	1	1	1
3	3	1	-1	0	2

(3 rows)

case 3: Source belongs to a vertex subgraph, while target belongs to an edge subgraph.

Inspecting the contracted graph above, vertex 7 belongs to the contracted subgraph of vertex 5 and vertex 13 belongs to the contracted subgraph of edge 21. In the following query:

- expand7 holds the contracted vertices of vertex where vertex 7 belongs. (belongs to vertex 5)
- expand13 holds the contracted vertices of edge where vertex 13 belongs. (belongs to edge 21)
- vertices_in_graph hold the vertices that belong to the contracted graph, contracted vertices of vertex 5 and contracted vertices of edge 21.
- when selecting the edges, only edges that have the source and the target in that set are the edges belonging to the contracted graph, that is done in the WHERE clause.

Visually, looking at the original graph, going from 7 to 13: 7 -> 8 -> 5 -> 10 -> 13, and in the contracted graph, it is also 7 -> 8 -> 5 -> 10 -> 13. The results, on the contracted graph match the results as if it was done on the original graph.

```
SELECT * FROM pgr_dijkstra(
  $$
  WITH
  expand_vertices AS (SELECT id, unnest(contracted_vertices) AS vertex FROM edge_table_vertices_pgr
    WHERE id IN (SELECT id FROM expand_edges WHERE vertex = 13)),
  expand7 AS (SELECT contracted_vertices FROM edge_table
    WHERE id IN (SELECT id FROM expand_vertices WHERE vertex = 7)),
  vertices_in_graph AS (
    SELECT id FROM edge_table_vertices_pgr WHERE is_contracted = false
    UNION
    SELECT unnest(contracted_vertices) FROM expand7)
  SELECT id, source, target, cost, reverse_cost
  FROM edge_table
  WHERE source IN (SELECT * FROM vertices_in_graph)
  AND target IN (SELECT * FROM vertices_in_graph)
  $$,
  7, 13, false);
```

```

expand7 AS (SELECT contracted_vertices FROM edge_table_vertices_pgr
             WHERE id IN (SELECT id FROM expand_vertices WHERE vertex = 7)),

expand_edges AS (SELECT id, unnest(contracted_vertices) AS vertex FROM edge_table),
expand13 AS (SELECT contracted_vertices FROM edge_table
             WHERE id IN (SELECT id FROM expand_edges WHERE vertex = 13)),

vertices_in_graph AS (
    SELECT id FROM edge_table_vertices_pgr WHERE is_contracted = false
    UNION
    SELECT unnest(contracted_vertices) FROM expand13
    UNION
    SELECT unnest(contracted_vertices) FROM expand7)

SELECT id, source, target, cost, reverse_cost
FROM edge_table
WHERE source IN (SELECT * FROM vertices_in_graph)
AND target IN (SELECT * FROM vertices_in_graph)
$$,
7, 13, false);

```

seq	path_seq	node	edge	cost	agg_cost
1	1	7	6	1	0
2	2	8	7	1	1
3	3	5	10	1	2
4	4	10	14	1	3
5	5	13	-1	0	4

(5 rows)

case 4: Source belongs to the contracted graph, while target belongs to an vertex subgraph.

Inspecting the contracted graph above, vertex 3 is part of the contracted graph and vertex 7 belongs to the contracted subgraph of vertex 5. In the following query:

- expand7 holds the contracted vertices of vertex where vertex 7 belongs. (belongs to vertex 5)
- vertices_in_graph hold the vertices that belong to the contracted graph and the contracted vertices of vertex 5.
- when selecting the edges, only edges that have the source and the target in that set are the edges belonging to the contracted graph, that is done in the WHERE clause.

Visually, looking at the original graph, going from 3 to 7: 3 -> 2 -> 5 -> 8 -> 7, but in the contracted graph, it is 3 -> 5 -> 8 -> 7. The results, on the contracted graph do not match the results as if it was done on the original graph. This is because the path contains edge 19 which is added by the contraction algorithm.

```

SELECT * FROM pgr_dijkstra(
    $$
    WITH
    expand_vertices AS (SELECT id, unnest(contracted_vertices) AS vertex FROM edge_table_vertices_pgr),
    expand7 AS (SELECT contracted_vertices FROM edge_table_vertices_pgr
                WHERE id IN (SELECT id FROM expand_vertices WHERE vertex = 7)),
    vertices_in_graph AS (
        SELECT id FROM edge_table_vertices_pgr WHERE is_contracted = false
        UNION
        SELECT unnest(contracted_vertices) FROM expand7)
    SELECT id, source, target, cost, reverse_cost
    FROM edge_table
    WHERE source IN (SELECT * FROM vertices_in_graph)
    AND target IN (SELECT * FROM vertices_in_graph)
    $$,

```

```

    3, 7, false);
seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
  1 |           | 1 | 3 | 19 | 2 | 0
  2 |           | 2 | 5 | 7 | 1 | 2
  3 |           | 3 | 8 | 6 | 1 | 3
  4 |           | 4 | 7 | -1 | 0 | 4
(4 rows)

```

case 5: The path contains an edge added by the contraction algorithm.

In the previous example we can see that the path from vertex 3 to vertex 7 contains an edge which is added by the contraction algorithm.

```

WITH
first_dijkstra AS (
  SELECT * FROM pgr_dijkstra(
    $$
    WITH
    expand_vertices AS (SELECT id, unnest(contracted_vertices) AS vertex FROM edge_table_vertices_pgr
    expand7 AS (SELECT contracted_vertices FROM edge_table_vertices_pgr
      WHERE id IN (SELECT id FROM expand_vertices WHERE vertex = 7)),
    vertices_in_graph AS (
      SELECT id FROM edge_table_vertices_pgr WHERE is_contracted = false
    UNION
      SELECT unnest(contracting_vertices) FROM expand7)
    SELECT id, source, target, cost, reverse_cost
    FROM edge_table
    WHERE source IN (SELECT * FROM vertices_in_graph)
    AND target IN (SELECT * FROM vertices_in_graph)
    $$,
    3, 7, false))
SELECT edge, contracting_vertices
  FROM first_dijkstra JOIN edge_table
    ON (edge = id)
  WHERE is_contracted = true;
edge | contracting_vertices
-----+-----
  19 | {1,2}
(1 row)

```

Inspecting the contracted graph above, edge 19 should be expanded. In the following query:

- first_dijkstra holds the results of the dijkstra query.
- edges_to_expand holds the edges added by the contraction algorithm and included in the path.
- vertices_in_graph hold the vertices that belong to the contracted graph, vertices of the contracted solution and the contracted vertices of the edges added by the contraction algorithm and included in the contracted solution.
- when selecting the edges, only edges that have the source and the target in that set are the edges belonging to the contracted graph, that is done in the WHERE clause.

Visually, looking at the original graph, going from 3 to 7: 3 -> 2 -> 5 -> 8 -> 7, and in the contracted graph, it is also 3 -> 2 -> 5 -> 8 -> 7. The results, on the contracted graph match the results as if it was done on the original graph.

```

SELECT * FROM pgr_dijkstra($$
  WITH
  -- This returns the results from case 2

```

```

first_dijkstra AS (
    SELECT * FROM pgr_dijkstra(
        ,
        WITH
        expand_vertices AS (SELECT id, unnest(contracted_vertices) AS vertex FROM edge_table_
        expand7 AS (SELECT contracted_vertices FROM edge_table_vertices_pgr
            WHERE id IN (SELECT id FROM expand_vertices WHERE vertex = 7)),
        vertices_in_graph AS (
            SELECT id FROM edge_table_vertices_pgr WHERE is_contracted = false
            UNION
            SELECT unnest(contracting_vertices) FROM expand7)
        SELECT id, source, target, cost, reverse_cost
        FROM edge_table
        WHERE source IN (SELECT * FROM vertices_in_graph)
        AND target IN (SELECT * FROM vertices_in_graph)
        ,
        3, 7, false)),

-- edges that need expansion and the vertices to be expanded.
edges_to_expand AS (
    SELECT edge, contracting_vertices
    FROM first_dijkstra JOIN edge_table
    ON (edge = id)
    WHERE is_contracted = true),

vertices_in_graph AS (
    -- the nodes of the contracting solution
    SELECT node FROM first_dijkstra
    UNION
    -- the nodes of the expanding sections
    SELECT unnest(contracting_vertices) FROM edges_to_expand)

SELECT id, source, target, cost, reverse_cost
FROM edge_table
WHERE source IN (SELECT * FROM vertices_in_graph)
AND target IN (SELECT * FROM vertices_in_graph)
-- not including the expanded edges
AND id NOT IN (SELECT edge FROM edges_to_expand)
$$,
3, 7, false);
seq | path_seq | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----
1 | 1 | 3 | 2 | 1 | 0
2 | 2 | 2 | 4 | 1 | 1
3 | 3 | 5 | 7 | 1 | 2
4 | 4 | 8 | 6 | 1 | 3
5 | 5 | 7 | -1 | 0 | 4
(5 rows)

```

See Also

- <http://www.cs.cmu.edu/afs/cs/academic/class/15210-f12/www/lectures/lecture16.pdf>
- http://algo2.iti.kit.edu/documents/routeplanning/geisberger_dipl.pdf
- The queries use *pgr_contractGraph - Experimental* function and the [Sample Data](#) network.

Indices and tables

- [genindex](#)

- search

6.2.2 Flow - Family of functions

- *pgr_maxFlow - Proposed* - Only the Max flow calculation using Push and Relabel algorithm.
- *pgr_boykovKolmogorov - Proposed* - Boykov and Kolmogorov with details of flow on edges.
- *pgr_edmondsKarp - Proposed* - Edmonds and Karp algorithm with details of flow on edges.
- *pgr_pushRelabel - Proposed* - Push and relabel algorithm with details of flow on edges.
- Applications
 - *pgr_edgeDisjointPaths - Proposed* - Calculates edge disjoint paths between two groups of vertices.
 - *pgr_maxCardinalityMatch - Proposed* - Calculates a maximum cardinality matching in a graph.

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

pgr_maxFlow - Proposed

Synopsis

`pgr_maxFlow` — Calculates the maximum flow in a directed graph from the source(s) to the targets(s) using the Push Relabel algorithm.



Fig. 6.14: Boost Graph Inside

Availability: 2.4.0

Warning: Experimental functions

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- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Characteristics

- The graph is **directed**.
- When the maximum flow is 0 then there is no flow and **0** is returned.
 - There is no flow when a **source** is the same as a **target**.
- Any duplicated value in the source(s) or target(s) are ignored.
- Uses the *pgr_pushRelabel* algorithm.
- Running time: $O(V^3)$

Signature Summary

```
pgr_maxFlow(edges_sql, source, target)
pgr_maxFlow(edges_sql, sources, target)
pgr_maxFlow(edges_sql, source, targets)
pgr_maxFlow(edges_sql, sources, targets)
RETURNS BIGINT
```

One to One Calculates the maximum flow from the *source* to the *target*.

```
pgr_maxFlow(edges_sql, source, target)
RETURNS BIGINT
```

Example

```
SELECT * FROM pgr_maxFlow(
    'SELECT id,
        source,
        target,
        capacity,
        reverse_capacity
    FROM edge_table'
    , 6, 11
);
pgr_maxflow
-----
```

```

      230
(1 row)

```

One to Many Calculates the maximum flow from the *source* to all of the *targets*.

```

pgr_maxFlow(edges_sql, source, targets)
RETURNS BIGINT

```

Example

```

SELECT * FROM pgr_maxFlow(
  'SELECT id,
    source,
    target,
    capacity,
    reverse_capacity
  FROM edge_table'
  , 6, ARRAY[11, 1, 13]
);
 pgr_maxflow
-----
      340
(1 row)

```

Many to One Calculates the maximum flow from all the *sources* to the *target*.

```

pgr_maxFlow(edges_sql, sources, target)
RETURNS BIGINT

```

Example

```

SELECT * FROM pgr_maxFlow(
  'SELECT id,
    source,
    target,
    capacity,
    reverse_capacity
  FROM edge_table'
  , ARRAY[6, 8, 12], 11
);
 pgr_maxflow
-----
      230
(1 row)

```

Many to Many Calculates the maximum flow from all of the *sources* to all of the *targets*.

```

pgr_maxFlow(edges_sql, sources, targets)
RETURNS BIGINT

```

Example

```

SELECT * FROM pgr_maxFlow(
  'SELECT id,
    source,
    target,
    capacity,
    reverse_capacity

```

```

FROM edge_table'
, ARRAY[6, 8, 12], ARRAY[1, 3, 11]
);
pgr_maxflow
-----
          360
(1 row)

```

Description of the Signatures

Description of the edges_sql query for Max-flow like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
capacity	ANY-INTEGER		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_capacity	ANY-INTEGER	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

Description of the Parameters of the Flow Signatures

Column	Type	Default	Description
edges_sql	TEXT		The edges SQL query as
source	BIGINT		Identifier of the starting
sources	ARRAY[BIGINT]		Array of identifiers of th
target	BIGINT		Identifier of the ending v
targets	ARRAY[BIGINT]		Array of identifiers of th

Description of the return value

Type	Description
BIGINT	Maximum flow possible from the source(s) to the target(s)

See Also

- *Flow - Family of functions*
- http://www.boost.org/libs/graph/doc/push_relabel_max_flow.html

- https://en.wikipedia.org/wiki/Push%E2%80%93relabel_maximum_flow_algorithm

Indices and tables

- [genindex](#)
- [search](#)

pgr_pushRelabel - Proposed

Synopsis

`pgr_pushRelabel` — Calculates the flow on the graph edges that maximizes the flow from the sources to the targets using Push Relabel Algorithm.



Fig. 6.15: Boost Graph Inside

Availability:

- Renamed 2.5.0, Previous name `pgr_maxFlowPushRelabel`
- New in 2.3.0

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Characteristics

- The graph is **directed**.
- Process is done only on edges with positive capacities.
- When the maximum flow is 0 then there is no flow and **EMPTY SET** is returned.
 - There is no flow when a **source** is the same as a **target**.
- Any duplicated value in the source(s) or target(s) are ignored.

- Calculates the flow/residual capacity for each edge. In the output
 - Edges with zero flow are omitted.
- Creates a **super source** and edges to all the source(s), and a **super target** and the edges from all the targets(s).
- The maximum flow through the graph is guaranteed to be the value returned by *pgr_maxFlow* when executed with the same parameters and can be calculated:
 - By aggregation of the outgoing flow from the sources
 - By aggregation of the incoming flow to the targets
- Running time: $O(V^3)$

Signature Summary

```
pgr_pushRelabel(edges_sql, source, target) - Proposed
pgr_pushRelabel(edges_sql, sources, target) - Proposed
pgr_pushRelabel(edges_sql, source, targets) - Proposed
pgr_pushRelabel(edges_sql, sources, targets) - Proposed
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET
```

One to One Calculates the flow on the graph edges that maximizes the flow from the *source* to the *target*.

```
pgr_pushRelabel(edges_sql, source, target)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET
```

Example

```
SELECT * FROM pgr_pushRelabel(
  'SELECT id,
       source,
       target,
       capacity,
       reverse_capacity
  FROM edge_table'
  , 6, 11
);
```

seq	edge	start_vid	end_vid	flow	residual_capacity
1	10	5	10	100	30
2	8	6	5	100	30
3	11	6	11	130	0
4	12	10	11	100	0

(4 rows)

One to Many Calculates the flow on the graph edges that maximizes the flow from the *source* to all of the *targets*.

```
pgr_pushRelabel(edges_sql, source, targets)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET
```

Example

```
SELECT * FROM pgr_pushRelabel(
  'SELECT id,
       source,
```

```

        target,
        capacity,
        reverse_capacity
    FROM edge_table'
    , 6, ARRAY[11, 1, 13]
);
 seq | edge | start_vid | end_vid | flow | residual_capacity
-----+-----+-----+-----+-----+-----
   1 |   1 |         2 |       1 |  130 |                0
   2 |   2 |         3 |       2 |   80 |               20
   3 |   3 |         4 |       3 |   80 |               50
   4 |   4 |         5 |       2 |   50 |                0
   5 |   7 |         5 |       8 |   50 |               80
   6 |  10 |         5 |      10 |   80 |               50
   7 |   8 |         6 |       5 |  130 |                0
   8 |   9 |         6 |       9 |   80 |               50
   9 |  11 |         6 |      11 |  130 |                0
  10 |   6 |         7 |       8 |   50 |                0
  11 |   6 |         8 |       7 |   50 |               50
  12 |   7 |         8 |       5 |   50 |                0
  13 |  16 |         9 |       4 |   80 |                0
  14 |  12 |        10 |      11 |   80 |               20
(14 rows)

```

Many to One Calculates the flow on the graph edges that maximizes the flow from all of the *sources* to the *target*.

```

pgr_pushRelabel(edges_sql, sources, target)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET

```

Example

```

SELECT * FROM pgr_pushRelabel(
    'SELECT id,
        source,
        target,
        capacity,
        reverse_capacity
    FROM edge_table'
    , ARRAY[6, 8, 12], 11
);
 seq | edge | start_vid | end_vid | flow | residual_capacity
-----+-----+-----+-----+-----+-----
   1 |  10 |         5 |      10 |  100 |               30
   2 |   8 |         6 |       5 |  100 |               30
   3 |  11 |         6 |      11 |  130 |                0
   4 |  12 |        10 |      11 |  100 |                0
(4 rows)

```

Many to Many Calculates the flow on the graph edges that maximizes the flow from all of the *sources* to all of the *targets*.

```

pgr_pushRelabel(edges_sql, sources, targets)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET

```

Example

```

SELECT * FROM pgr_pushRelabel(
  'SELECT id,
        source,
        target,
        capacity,
        reverse_capacity
  FROM edge_table'
  , ARRAY[6, 8, 12], ARRAY[1, 3, 11]
);
seq | edge | start_vid | end_vid | flow | residual_capacity
-----+-----+-----+-----+-----+-----
1 | 1 | 2 | 1 | 50 | 80
2 | 3 | 4 | 3 | 80 | 50
3 | 4 | 5 | 2 | 50 | 0
4 | 10 | 5 | 10 | 100 | 30
5 | 8 | 6 | 5 | 130 | 0
6 | 9 | 6 | 9 | 30 | 100
7 | 11 | 6 | 11 | 130 | 0
8 | 7 | 8 | 5 | 20 | 30
9 | 16 | 9 | 4 | 80 | 0
10 | 12 | 10 | 11 | 100 | 0
11 | 15 | 12 | 9 | 50 | 0
(11 rows)

```

Description of the Signatures

Description of the edges_sql query for Max-flow like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
capacity	ANY-INTEGER		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_capacity	ANY-INTEGER	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

Description of the Parameters of the Flow Signatures

Column	Type	Default	Description
edges_sql	TEXT		The edges SQL query as
source	BIGINT		Identifier of the starting
sources	ARRAY[BIGINT]		Array of identifiers of th
target	BIGINT		Identifier of the ending v
targets	ARRAY[BIGINT]		Array of identifiers of th

Description of the Return Values

Column	Type	Description
seq	INT	Sequential value starting from 1 .
edge_id	BIGINT	Identifier of the edge in the original query(edges_sql).
source	BIGINT	Identifier of the first end point vertex of the edge.
target	BIGINT	Identifier of the second end point vertex of the edge.
flow	BIGINT	Flow through the edge in the direction (source, target).
residual_capacity	BIGINT	Residual capacity of the edge in the direction (source, target).

See Also

- *Flow - Family of functions*, *pgr_boykovKolmogorov*, *pgr_edmondsKarp*
- http://www.boost.org/libs/graph/doc/push_relabel_max_flow.html
- https://en.wikipedia.org/wiki/Push%E2%80%93relabel_maximum_flow_algorithm

Indices and tables

- [genindex](#)
- [search](#)

pgr_edmondsKarp - Proposed**Synopsis**

`pgr_edmondsKarp` — Calculates the flow on the graph edges that maximizes the flow from the sources to the targets using Push Relabel Algorithm.



Fig. 6.16: Boost Graph Inside

Availability:

- Renamed 2.5.0, Previous name `pgr_maxFlowEdmondsKarp`
- New in 2.3.0

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Characteristics

- The graph is **directed**.
- Process is done only on edges with positive capacities.
- When the maximum flow is 0 then there is no flow and **EMPTY SET** is returned.
 - There is no flow when a **source** is the same as a **target**.
- Any duplicated value in the source(s) or target(s) are ignored.
- Calculates the flow/residual capacity for each edge. In the output
 - Edges with zero flow are omitted.
- Creates a **super source** and edges to all the source(s), and a **super target** and the edges from all the targets(s).
- The maximum flow through the graph is guaranteed to be the value returned by *pgr_maxFlow* when executed with the same parameters and can be calculated:
 - By aggregation of the outgoing flow from the sources
 - By aggregation of the incoming flow to the targets
- Running time: $O(V * E^2)$

Signature Summary

```
pgr_edmondsKarp(edges_sql, source, target) - Proposed
pgr_edmondsKarp(edges_sql, sources, target) - Proposed
pgr_edmondsKarp(edges_sql, source, targets) - Proposed
pgr_edmondsKarp(edges_sql, sources, targets) - Proposed
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET
```

One to One Calculates the flow on the graph edges that maximizes the flow from the *source* to the *target*.

```
pgr_edmondsKarp(edges_sql, source, target)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET
```

Example

```

SELECT * FROM pgr_edmondsKarp(
  'SELECT id,
       source,
       target,
       capacity,
       reverse_capacity
  FROM edge_table'
  , 6, 11
);

```

seq	edge	start_vid	end_vid	flow	residual_capacity
1	10	5	10	100	30
2	8	6	5	100	30
3	11	6	11	130	0
4	12	10	11	100	0

(4 rows)

One to Many Calculates the flow on the graph edges that maximizes the flow from the *source* to all of the *targets*.

```

pgr_edmondsKarp(edges_sql, source, targets)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET

```

Example

```

SELECT * FROM pgr_edmondsKarp(
  'SELECT id,
       source,
       target,
       capacity,
       reverse_capacity
  FROM edge_table'
  , 6, ARRAY[1, 3, 11]
);

```

seq	edge	start_vid	end_vid	flow	residual_capacity
1	1	2	1	50	80
2	3	4	3	80	50
3	4	5	2	50	0
4	10	5	10	80	50
5	8	6	5	130	0
6	9	6	9	80	50
7	11	6	11	130	0
8	16	9	4	80	0
9	12	10	11	80	20

(9 rows)

Many to One Calculates the flow on the graph edges that maximizes the flow from all of the *sources* to the *target*.

```

pgr_edmondsKarp(edges_sql, sources, target)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET

```

Example

```

SELECT * FROM pgr_edmondsKarp(
  'SELECT id,
       source,

```

```

        target,
        capacity,
        reverse_capacity
    FROM edge_table'
    , ARRAY[6, 8, 12], 11
);
 seq | edge | start_vid | end_vid | flow | residual_capacity
-----+-----+-----+-----+-----+-----
   1 |   10 |         5 |      10 |  100 |              30
   2 |    8 |         6 |       5 |  100 |              30
   3 |   11 |         6 |      11 |  130 |               0
   4 |   12 |        10 |      11 |  100 |               0
(4 rows)

```

Many to Many Calculates the flow on the graph edges that maximizes the flow from all of the *sources* to all of the *targets*.

```

pgr_edmondsKarp(edges_sql, sources, targets)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET

```

Example

```

SELECT * FROM pgr_edmondsKarp(
    'SELECT id,
        source,
        target,
        capacity,
        reverse_capacity
    FROM edge_table'
    , ARRAY[6, 8, 12], ARRAY[1, 3, 11]
);
 seq | edge | start_vid | end_vid | flow | residual_capacity
-----+-----+-----+-----+-----+-----
   1 |    1 |         2 |       1 |   50 |              80
   2 |    3 |         4 |       3 |   80 |              50
   3 |    4 |         5 |       2 |   50 |               0
   4 |   10 |         5 |      10 |  100 |              30
   5 |    8 |         6 |       5 |  130 |               0
   6 |    9 |         6 |       9 |   80 |              50
   7 |   11 |         6 |      11 |  130 |               0
   8 |    7 |         8 |       5 |   20 |              30
   9 |   16 |         9 |       4 |   80 |               0
  10 |   12 |        10 |      11 |  100 |               0
(10 rows)

```

Description of the Signatures

Description of the edges_sql query for Max-flow like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
capacity	ANY-INTEGER		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_capacity	ANY-INTEGER	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

Description of the Parameters of the Flow Signatures

Column	Type	Default	Description
edges_sql	TEXT		The edges SQL query as
source	BIGINT		Identifier of the starting
sources	ARRAY[BIGINT]		Array of identifiers of th
target	BIGINT		Identifier of the ending v
targets	ARRAY[BIGINT]		Array of identifiers of th

Description of the Return Values

Column	Type	Description
seq	INT	Sequential value starting from 1.
edge_id	BIGINT	Identifier of the edge in the original query(edges_sql).
source	BIGINT	Identifier of the first end point vertex of the edge.
target	BIGINT	Identifier of the second end point vertex of the edge.
flow	BIGINT	Flow through the edge in the direction (source, target).
residual_capacity	BIGINT	Residual capacity of the edge in the direction (source, target).

See Also

- *Flow - Family of functions*, *pgr_boykovKolmogorov*, *pgr_PushRelabel*
- http://www.boost.org/libs/graph/doc/edmonds_karp_max_flow.html
- https://en.wikipedia.org/wiki/Edmonds%E2%80%93Karp_algorithm

Indices and tables

- genindex
- search

pgr_boykovKolmogorov - Proposed

Synopsis

`pgr_boykovKolmogorov` — Calculates the flow on the graph edges that maximizes the flow from the sources to the targets using Boykov Kolmogorov algorithm.



Fig. 6.17: Boost Graph Inside

Availability:

- Renamed 2.5.0, Previous name `pgr_maxFlowBoykovKolmogorov`
- New in 2.3.0

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Characteristics

- The graph is **directed**.
- Process is done only on edges with positive capacities.
- When the maximum flow is 0 then there is no flow and **EMPTY SET** is returned.
 - There is no flow when a **source** is the same as a **target**.
- Any duplicated value in the source(s) or target(s) are ignored.
- Calculates the flow/residual capacity for each edge. In the output
 - Edges with zero flow are omitted.
- Creates a **super source** and edges to all the source(s), and a **super target** and the edges from all the targets(s).
- The maximum flow through the graph is guaranteed to be the value returned by `pgr_maxFlow` when executed with the same parameters and can be calculated:
 - By aggregation of the outgoing flow from the sources

- By aggregation of the incoming flow to the targets
- Running time: Polynomial

Signature Summary

```
pgr_boykovKolmogorov(edges_sql, source, target) - Proposed
pgr_boykovKolmogorov(edges_sql, sources, target) - Proposed
pgr_boykovKolmogorov(edges_sql, source, targets) - Proposed
pgr_boykovKolmogorov(edges_sql, sources, targets) - Proposed
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET
```

One to One Calculates the flow on the graph edges that maximizes the flow from the *source* to the *target*.

```
pgr_boykovKolmogorov(edges_sql, source, target)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET
```

Example

```
SELECT * FROM pgr_boykovKolmogorov(
  'SELECT id,
    source,
    target,
    capacity,
    reverse_capacity
  FROM edge_table'
  , 6, 11
);
```

seq	edge	start_vid	end_vid	flow	residual_capacity
1	10	5	10	100	30
2	8	6	5	100	30
3	11	6	11	130	0
4	12	10	11	100	0

(4 rows)

One to Many Calculates the flow on the graph edges that maximizes the flow from the *source* to all of the *targets*.

```
pgr_boykovKolmogorov(edges_sql, source, targets)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET
```

Example

```
SELECT * FROM pgr_boykovKolmogorov(
  'SELECT id,
    source,
    target,
    capacity,
    reverse_capacity
  FROM edge_table'
  , 6, ARRAY[1, 3, 11]
);
```

seq	edge	start_vid	end_vid	flow	residual_capacity
1	1	2	1	50	80
2	3	4	3	80	50

3		4		5		2		50		0
4		10		5		10		80		50
5		8		6		5		130		0
6		9		6		9		80		50
7		11		6		11		130		0
8		16		9		4		80		0
9		12		10		11		80		20
(9 rows)										

Many to One Calculates the flow on the graph edges that maximizes the flow from all of the *sources* to the *target*.

```
pgr_boykovKolmogorov(edges_sql, sources, target)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET
```

Example

```
SELECT * FROM pgr_boykovKolmogorov(
  'SELECT id,
    source,
    target,
    capacity,
    reverse_capacity
  FROM edge_table'
  , ARRAY[6, 8, 12], 11
);
seq | edge | start_vid | end_vid | flow | residual_capacity
-----+-----+-----+-----+-----+-----
  1 |  10 |         5 |      10 | 100 |              30
  2 |   8 |         6 |       5 | 100 |              30
  3 |  11 |         6 |      11 | 130 |               0
  4 |  12 |        10 |      11 | 100 |               0
(4 rows)
```

Many to Many Calculates the flow on the graph edges that maximizes the flow from all of the *sources* to all of the *targets*.

```
pgr_boykovKolmogorov(edges_sql, sources, targets)
RETURNS SET OF (seq, edge, start_vid, end_vid, flow, residual_capacity)
OR EMPTY SET
```

Example

```
SELECT * FROM pgr_boykovKolmogorov(
  'SELECT id,
    source,
    target,
    capacity,
    reverse_capacity
  FROM edge_table'
  , ARRAY[6, 8, 12], ARRAY[1, 3, 11]
);
seq | edge | start_vid | end_vid | flow | residual_capacity
-----+-----+-----+-----+-----+-----
  1 |   1 |         2 |       1 |  50 |              80
  2 |   3 |         4 |       3 |  80 |              50
  3 |   4 |         5 |       2 |  50 |               0
  4 |  10 |         5 |      10 | 100 |              30
  5 |   8 |         6 |       5 | 130 |               0
```


6	9	6	9	80	50
7	11	6	11	130	0
8	7	8	5	20	30
9	16	9	4	80	0
10	12	10	11	100	0
(10 rows)					

Description of the Signatures

Description of the edges_sql query for Max-flow like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
capacity	ANY-INTEGER		Weight of the edge (<i>source</i> , <i>target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_capacity	ANY-INTEGER	-1	Weight of the edge (<i>target</i> , <i>source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

Description of the Parameters of the Flow Signatures

Column	Type	Default	Description
edges_sql	TEXT		The edges SQL query as
source	BIGINT		Identifier of the starting
sources	ARRAY[BIGINT]		Array of identifiers of th
target	BIGINT		Identifier of the ending v
targets	ARRAY[BIGINT]		Array of identifiers of th

Description of the Return Values

Column	Type	Description
seq	INT	Sequential value starting from 1 .
edge_id	BIGINT	Identifier of the edge in the original query(edges_sql).
source	BIGINT	Identifier of the first end point vertex of the edge.
target	BIGINT	Identifier of the second end point vertex of the edge.
flow	BIGINT	Flow through the edge in the direction (source, target).
residual_capacity	BIGINT	Residual capacity of the edge in the direction (source, target).

See Also

- *Flow - Family of functions*, `pgr_pushRelabel`, `pgr_EdmondsKarp`
- http://www.boost.org/libs/graph/doc/boykov_kolmogorov_max_flow.html

Indices and tables

- `genindex`
- `search`

pgr_maxCardinalityMatch - Proposed

Synopsis

`pgr_maxCardinalityMatch` — Calculates a maximum cardinality matching in a graph.

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting



19

Fig. 6.18: Boost Graph Inside

Availability:

- Renamed 2.5.0, Previous name `pgr_maximumCardinalityMatching`
- New in 2.3.0

Characteristics

- A matching or independent edge set in a graph is a set of edges without common vertices.
- A maximum matching is a matching that contains the largest possible number of edges.
 - There may be many maximum matchings.

- Calculates **one** possible maximum cardinality matching in a graph.
- The graph can be **directed** or **undirected**.
- Running time: $O(E * V * \alpha(E, V))$
 - $\alpha(E, V)$ is the inverse of the [Ackermann function](https://en.wikipedia.org/wiki/Ackermann_function)²⁰.

Signature Summary

```
pgr_MaximumCardinalityMatching(edges_sql) - Proposed
pgr_MaximumCardinalityMatching(edges_sql, directed) - Proposed

RETURNS SET OF (seq, edge_id, source, target)
OR EMPTY SET
```

Minimal Use

```
pgr_MaximumCardinalityMatching(edges_sql)
RETURNS SET OF (seq, edge_id, source, target) OR EMPTY SET
```

The minimal use calculates one possible maximum cardinality matching on a **directed** graph.

Example

```
SELECT * FROM pgr_maxCardinalityMatch(
    'SELECT id, source, target, cost AS going, reverse_cost AS coming FROM edge_table'
);
```

seq	edge	source	target
1	1	1	2
2	3	4	3
3	9	6	9
4	6	7	8
5	14	10	13
6	13	11	12
7	17	14	15
8	18	16	17

(8 rows)

Complete signature

```
pgr_MaximumCardinalityMatching(edges_sql, directed)
RETURNS SET OF (seq, edge_id, source, target) OR EMPTY SET
```

The complete signature calculates one possible maximum cardinality matching.

Example

```
SELECT * FROM pgr_maxCardinalityMatch(
    'SELECT id, source, target, cost AS going, reverse_cost AS coming FROM edge_table',
    directed := false
);
```

seq	edge	source	target
1	1	1	2
2	3	3	4
3	9	6	9
4	6	7	8
5	14	10	13
6	13	11	12

²⁰https://en.wikipedia.org/wiki/Ackermann_function

7	17	14	15
8	18	16	17

(8 rows)

Description of the Signatures

Description of the SQL query

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Description
id	ANY-INTEGER	Identifier of the edge.
source	ANY-INTEGER	Identifier of the first end point vertex of the edge.
target	ANY-INTEGER	Identifier of the second end point vertex of the edge.
going	ANY-NUMERIC	A positive value represents the existence of the edge (source, target).
coming	ANY-NUMERIC	A positive value represents the existence of the edge (target, source).

Where:

- **ANY-INTEGER** SMALLINT, INTEGER, BIGINT
- **ANY-NUMERIC** SMALLINT, INTEGER, BIGINT, REAL, DOUBLE PRECISION

Description of the parameters of the signatures

Column	Type	Description
edges_sql	TEXT	SQL query as described above.
directed	BOOLEAN	(optional) Determines the type of the graph. Default

Description of the Result

Column	Type	Description
seq	INT	Sequential value starting from 1 .
edge	BIGINT	Identifier of the edge in the original query(edges_sql).
source	BIGINT	Identifier of the first end point of the edge.
target	BIGINT	Identifier of the second end point of the edge.

See Also

- *Flow - Family of functions*
- http://www.boost.org/libs/graph/doc/maximum_matching.html
- https://en.wikipedia.org/wiki/Matching_%28graph_theory%29
- https://en.wikipedia.org/wiki/Ackermann_function

Indices and tables

- genindex
- search

pgr_edgeDisjointPaths - Proposed

Name

pgr_edgeDisjointPaths — Calculates edge disjoint paths between two groups of vertices.



Fig. 6.19: Boost Graph Inside

Availability: 2.3.0**Warning:** Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

Calculates the edge disjoint paths between two groups of vertices. Utilizes underlying maximum flow algorithms to calculate the paths.

Characteristics:**The main characteristics are:**

- Calculates the edge disjoint paths between any two groups of vertices.
- Returns EMPTY SET when source and destination are the same, or cannot be reached.
- The graph can be directed or undirected.
- One to many, many to one, many to many versions are also supported.
- Uses *pgr_boykovKolmogorov* - *Proposed* to calculate the paths.

Signature Summary

```
pgr_edgeDisjointPaths(edges_sql, start_vid, end_vid)
pgr_edgeDisjointPaths(edges_sql, start_vid, end_vid, directed)
pgr_edgeDisjointPaths(edges_sql, start_vid, end_vids, directed)
pgr_edgeDisjointPaths(edges_sql, start_vids, end_vid, directed)
pgr_edgeDisjointPaths(edges_sql, start_vids, end_vids, directed)

RETURNS SET OF (seq, path_id, path_seq, [start_vid,] [end_vid,] node, edge, cost, agg_cost)
OR EMPTY SET
```

Signatures

Minimal use

```
pgr_edgeDisjointPaths(edges_sql, start_vid, end_vid)
RETURNS SET OF (seq, path_id, path_seq, node, edge, cost, agg_cost)
OR EMPTY SET
```

The minimal use is for a **directed** graph from one start_vid to one end_vid.

Example

```
SELECT * FROM pgr_edgeDisjointPaths(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  3, 5
);
```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	3	2	1	0
2	1	2	2	4	1	1
3	1	3	5	-1	0	2
4	2	1	3	5	1	0
5	2	2	6	8	1	1
6	2	3	5	-1	0	2

(6 rows)

One to One

This signature finds the set of disjoint paths from one start_vid to one end_vid:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.

```
pgr_edgeDisjointPaths(edges_sql, start_vid, end_vid, directed)
RETURNS SET OF (seq, path_id, path_seq, node, edge, cost, agg_cost)
OR EMPTY SET
```

Example

```
SELECT * FROM pgr_edgeDisjointPaths(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  3, 5,
  directed := false
);
```

seq	path_id	path_seq	node	edge	cost	agg_cost
1	1	1	3	2	1	0
2	1	2	2	4	1	1
3	1	3	5	-1	0	2
4	2	1	3	3	-1	0
5	2	2	4	16	1	-1
6	2	3	9	9	1	0
7	2	4	6	8	1	1
8	2	5	5	-1	0	2
9	3	1	3	5	1	0
10	3	2	6	11	1	1
11	3	3	11	12	-1	2
12	3	4	10	10	1	1
13	3	5	5	-1	0	2

(13 rows)

One to Many

This signature finds the sset of disjoint paths from the **start_vid** to each one of the **end_vid** in **end_vids**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.
- The result is equivalent to the union of the results of the one to one *pgr_edgeDisjointPaths*.
- The extra **end_vid** in the result is used to distinguish to which path it belongs.

```
pgr_edgeDisjointPaths(edges_sql, start_vid, end_vids, directed)
RETURNS SET OF (seq, path_id, path_seq, end_vid, node, edge, cost, agg_cost)
OR EMPTY SET
```

Example

```
SELECT * FROM pgr_edgeDisjointPaths(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  3, ARRAY[4, 5, 10]
);
```

seq	path_id	path_seq	end_vid	node	edge	cost	agg_cost
1	1	1	4	3	5	1	0
2	1	2	4	6	9	1	1
3	1	3	4	9	16	1	2
4	1	4	4	4	-1	0	3
5	2	1	5	3	2	1	0
6	2	2	5	2	4	1	1
7	2	3	5	5	-1	0	2
8	3	1	5	3	5	1	0
9	3	2	5	6	8	1	1
10	3	3	5	5	-1	0	2
11	4	1	10	3	2	1	0
12	4	2	10	2	4	1	1
13	4	3	10	5	10	1	2
14	4	4	10	10	-1	0	3

(14 rows)

Many to One

This signature finds the set of disjoint paths from each one of the **start_vid** in **start_vids** to the **end_vid**:

- on a **directed** graph when directed flag is missing or is set to true.
- on an **undirected** graph when directed flag is set to false.
- The result is equivalent to the union of the results of the one to one *pgr_edgeDisjointPaths*.
- The extra **start_vid** in the result is used to distinguish to which path it belongs.

```
pgr_edgeDisjointPaths(edges_sql, start_vids, end_vid, directed)
RETURNS SET OF (seq, path_id, path_seq, start_vid, node, edge, cost, agg_cost)
OR EMPTY SET
```

Example

```
SELECT * FROM pgr_edgeDisjointPaths(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[3, 6], 5
);
```

seq	path_id	path_seq	start_vid	node	edge	cost	agg_cost
1	1	1	3	3	5	1	0
2	1	2	3	6	9	1	1
3	1	3	3	9	16	1	2
4	1	4	3	4	-1	0	3
5	2	1	6	3	2	1	0
6	2	2	6	2	4	1	1
7	2	3	6	5	-1	0	2
8	3	1	3	3	5	1	0
9	3	2	3	6	8	1	1
10	3	3	3	5	-1	0	2
11	4	1	6	3	2	1	0
12	4	2	6	2	4	1	1
13	4	3	6	5	10	1	2
14	4	4	6	10	-1	0	3

1	1	1	0	3	2	1	0
2	1	2	0	2	4	1	1
3	1	3	0	5	-1	0	2
4	2	1	1	3	5	1	0
5	2	2	1	6	8	1	1
6	2	3	1	5	-1	0	2
7	3	1	2	6	8	1	0
8	3	2	2	5	-1	0	1
9	4	1	3	6	9	1	0
10	4	2	3	9	16	1	1
11	4	3	3	4	3	1	2
12	4	4	3	3	2	1	3
13	4	5	3	2	4	1	4
14	4	6	3	5	-1	0	5

(14 rows)

Many to Many

This signature finds the set of disjoint paths from each one of the **start_vid** in **start_vids** to each one of the **end_vid**

- on a **directed** graph when **directed** flag is missing or is set to **true**.
- on an **undirected** graph when **directed** flag is set to **false**.
- The result is equivalent to the union of the results of the one to one *pgr_edgeDisjointPaths*.
- The extra **start_vid** and **end_vid** in the result is used to distinguish to which path it belongs.

```
pgr_edgeDisjointPaths(edges_sql, start_vids, end_vids, directed)
RETURNS SET OF (seq, path_seq, start_vid, end_vid, node, edge, cost, agg_cost)
OR EMPTY SET
```

Example

```
SELECT * FROM pgr_edgeDisjointPaths(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',
  ARRAY[3, 6], ARRAY[4, 5, 10]
);
```

seq	path_id	path_seq	start_vid	end_vid	node	edge	cost	agg_cost
1	1	1	0	4	3	5	1	0
2	1	2	0	4	6	9	1	1
3	1	3	0	4	9	16	1	2
4	1	4	0	4	4	-1	0	3
5	2	1	1	5	3	2	1	0
6	2	2	1	5	2	4	1	1
7	2	3	1	5	5	-1	0	2
8	3	1	2	5	3	5	1	0
9	3	2	2	5	6	8	1	1
10	3	3	2	5	5	-1	0	2
11	4	1	3	10	3	2	1	0
12	4	2	3	10	2	4	1	1
13	4	3	3	10	5	10	1	2
14	4	4	3	10	10	-1	0	3
15	5	1	4	4	6	9	1	0
16	5	2	4	4	9	16	1	1
17	5	3	4	4	4	-1	0	2
18	6	1	5	5	6	8	1	0
19	6	2	5	5	5	-1	0	1
20	7	1	6	5	6	9	1	0
21	7	2	6	5	9	16	1	1
22	7	3	6	5	4	3	1	2

23		7		4		6		5		3		2		1		3
24		7		5		6		5		2		4		1		4
25		7		6		6		5		5		-1		0		5
26		8		1		7		10		6		8		1		0
27		8		2		7		10		5		10		1		1
28		8		3		7		10		10		-1		0		2
(28 rows)																

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Column	Type	Default
sql	TEXT	
start_vid	BIGINT	
start_vids	ARRAY[BIGINT]	
end_vid	BIGINT	
end_vids	ARRAY[BIGINT]	
directed	BOOLEAN	true

Description of the return values for a path Returns set of (seq, path_seq [, start_vid] [, end_vid], node, edge, cost, agg_cost)

Column	Type	Description
seq	INT	Sequential value starting from 1.
path_id	INT	Path identifier. Has value 1 for the first of a path. Used when there are multiple paths for the same start_vid to end_vid combination.
path_seq	INT	Relative position in the path. Has value 1 for the beginning of a path.
start_vid	BIGINT	Identifier of the starting vertex. Used when multiple starting vertices are in the query.
end_vid	BIGINT	Identifier of the ending vertex. Used when multiple ending vertices are in the query.
node	BIGINT	Identifier of the node in the path from start_vid to end_vid.
edge	BIGINT	Identifier of the edge used to go from node to the next node in the path sequence. -1 for the last node of the path.
cost	FLOAT	Cost to traverse from node using edge to the next node in the path sequence.
agg_cost	FLOAT	Aggregate cost from start_v to node.

See Also

- *Flow - Family of functions*

Indices and tables

- genindex
- search

Flow Functions General Information

Characteristics

- The graph is **directed**.
- Process is done only on edges with positive capacities.
- When the maximum flow is 0 then there is no flow and **EMPTY SET** is returned.

- There is no flow when a **source** is the same as a **target**.
- Any duplicated value in the source(s) or target(s) are ignored.
- Calculates the flow/residual capacity for each edge. In the output
 - Edges with zero flow are omitted.
- Creates a **super source** and edges to all the source(s), and a **super target** and the edges from all the targets(s).
- The maximum flow through the graph is guaranteed to be the value returned by *pgr_maxFlow* when executed with the same parameters and can be calculated:
 - By aggregation of the outgoing flow from the sources
 - By aggregation of the incoming flow to the targets

pgr_maxFlow is the maximum Flow and that maximum is guaranteed to be the same on the functions *pgr_pushRelabel*, *pgr_edmondsKarp*, *pgr_boykovKolmogorov*, but the actual flow through each edge may vary.

Problem definition

A flow network is a directed graph where each edge has a capacity and a flow. The flow through an edge must not exceed the capacity of the edge. Additionally, the incoming and outgoing flow of a node must be equal except the for source which only has outgoing flow, and the destination(sink) which only has incoming flow.

Maximum flow algorithms calculate the maximum flow through the graph and the flow of each edge.

The maximum flow through the graph is guaranteed to be the same with all implementations, but the actual flow through each edge may vary. Given the following query:

pgr_maxFlow (*edges_sql*, *source_vertex*, *sink_vertex*)

where *edges_sql* = $\{(id_i, source_i, target_i, capacity_i, reverse_capacity_i)\}$

Graph definition

The weighted directed graph, $G(V, E)$, is defined as:

- the set of vertices V
 - $source_vertex \cup sink_vertex \cup source_i \cup target_i$
- the set of edges E
 - $E = \begin{cases} \{(source_i, target_i, capacity_i) \text{ when } capacity > 0\} & \text{if } reverse_capacity = \\ \{(source_i, target_i, capacity_i) \text{ when } capacity > 0\} \\ \cup \{(target_i, source_i, reverse_capacity_i) \text{ when } reverse_capacity_i > 0\} & \text{if } reverse_capacity \neq \end{cases}$

Maximum flow problem

Given:

- $G(V, E)$
- $source_vertex \in V$ the source vertex
- $sink_vertex \in V$ the sink vertex

Then:

pgr_maxFlow(*edges_sql*, *source*, *sink*) = Φ

$\Phi = (id_i, edge_id_i, source_i, target_i, flow_i, residual_capacity_i)$

Where:

Φ is a subset of the original edges with their residual capacity and flow. The maximum flow through the graph can be obtained by aggregating on the source or sink and summing the flow from/to it. In particular:

- $id_i = i$
- $edge_id = id_i$ in `edges_sql`
- $residual_capacity_i = capacity_i - flow_i$

See Also

- https://en.wikipedia.org/wiki/Maximum_flow_problem

Indices and tables

- `genindex`
- `search`

6.2.3 pgr_labelGraph - Experimental

Name

`pgr_labelGraph` — Locates and labels sub-networks within a network which are not topologically connected.

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

Must be run after `pgr_createTopology()`. No use of geometry column. Only `id`, `source` and `target` columns are required.

The function returns:

- OK when a column with provided name has been generated and populated successfully. All connected edges will have unique similar integer values. In case of `rows_where` condition, non participating rows will have -1 integer values.
- FAIL when the processing cannot be finished due to some error. Notice will be thrown accordingly.
- `rows_where` condition generated 0 rows when passed SQL condition has not been fulfilled by any row.

```
varchar pgr_labelGraph(text, text, text, text, text, text)
```

Description

A network behind any routing query may consist of sub-networks completely isolated from each other. Possible reasons could be:

- An island with no bridge connecting to the mainland.
- An edge or mesh of edges failed to connect to other networks because of human negligence during data generation.
- The data is not properly noded.
- Topology creation failed to succeed.

`pgr_labelGraph()` will create an integer column (with the name provided by the user) and will assign same integer values to all those edges in the network which are connected topologically. Thus better analysis regarding network structure is possible. In case of `rows_where` condition, non participating rows will have -1 integer values.

Prerequisites: Must run `pgr_createTopology()` in order to generate source and target columns. Primary key column `id` should also be there in the network table.

Function accepts the following parameters:

edge_table text Network table name, with optional schema name.

id text Primary key column name of the network table. Default is `id`.

source text Source column name generated after `pgr_createTopology()`. Default is `source`.

target text Target column name generated after `pgr_createTopology()`. Default is `target`.

subgraph text Column name which will hold the integer labels for each sub-graph. Default is `subgraph`.

rows_where text The SQL where condition. Default is `true`, means the processing will be done on the whole table.

Example Usage

The sample data, has 3 subgraphs.

```
SET client_min_messages TO WARNING;
SET
SELECT pgr_labelGraph('edge_table', 'id', 'source', 'target', 'subgraph');
pgr_labelgraph
-----
OK
(1 row)

SELECT DISTINCT subgraph FROM edge_table ORDER BY subgraph;
subgraph
-----
1
2
3
(3 rows)
```

See Also

- `pgr_createTopology`²² to create the topology of a table based on its geometry and tolerance value.

Indices and tables

- `genindex`
- `search`

6.2.4 Components - Family of functions

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

- *`pgr_connectedComponents` - Experimental* - Return the connected components of an undirected graph.
- *`pgr_strongComponents` - Experimental* - Return the strongly connected components of a directed graph.
- *`pgr_biconnectedComponents` - Experimental* - Return the biconnected components of an undirected graph.
- *`pgr_articulationPoints` - Experimental* - Return the articulation points of an undirected graph.
- *`pgr_bridges` - Experimental* - Return the bridges of an undirected graph.

`pgr_connectedComponents` - Experimental

`pgr_connectedComponents` — Return the connected components of an undirected graph using a DFS-based approach. In particular, the algorithm implemented by Boost.Graph.



Fig. 6.20: Boost Graph Inside

²²https://github.com/Zia-/pgrouting/blob/develop/src/common/sql/pgrouting_topology.sql

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

A connected component of an undirected graph is a set of vertices that are all reachable from each other. This implementation can only be used with an undirected graph.

Characteristics

The main Characteristics are:

- Components are described by vertices
- The returned values are ordered:
 - *component* ascending
 - *node* ascending
- Running time: $O(V + E)$

Signatures

```
pgr_connectedComponents (edges_sql)

RETURNS SET OF (seq, component, n_seq, node)
OR EMPTY SET
```

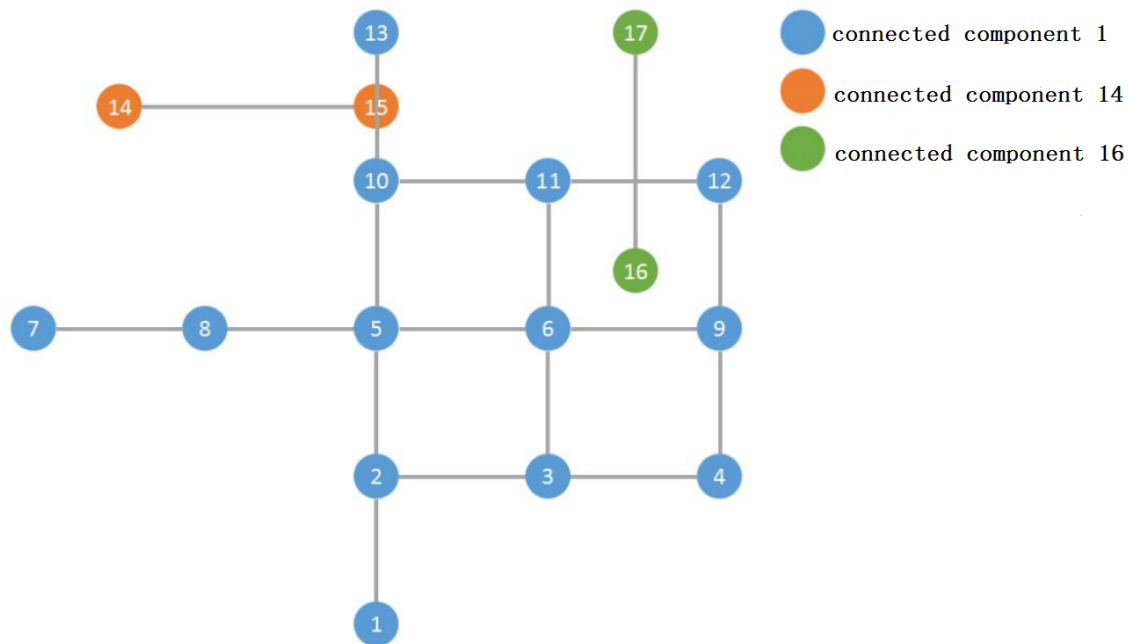
The signature is for a **undirected** graph.

Example

```
SELECT * FROM pgr_connectedComponents (
  'SELECT id, source, target, cost, reverse_cost FROM edge_table'
);
```

seq	component	n_seq	node
1	1	1	1
2	1	2	2
3	1	3	3
4	1	4	4
5	1	5	5
6	1	6	6
7	1	7	7
8	1	8	8

9		1		9		9
10		1		10		10
11		1		11		11
12		1		12		12
13		1		13		13
14		14		1		14
15		14		2		15
16		16		1		16
17		16		2		17
(17 rows)						



Description of the Signatures

Description of the edges_sql query for components functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Default	Description
edges_sql	TEXT		SQL query as described above.

Description of the return values for connected components and strongly connected components Returns set of (*seq, component, n_seq, node*)

Column	Type	Description
seq	INT	Sequential value starting from 1.
component	BIGINT	Component identifier. It is equal to the minimum node identifier in the component.
n_seq	INT	It is a sequential value starting from 1 in a component.
node	BIGINT	Identifier of the vertex.

See Also

- http://en.wikipedia.org/wiki/Connected_component_%28graph_theory%29
- The queries use the [Sample Data](#) network.

Indices and tables

- genindex
- search

pgr_strongComponents - Experimental

`pgr_strongComponents` — Return the strongly connected components of a directed graph using Tarjan's algorithm based on DFS. In particular, the algorithm implemented by Boost.Graph.



Fig. 6.21: Boost Graph Inside

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

A strongly connected component of a directed graph is a set of vertices that are all reachable from each other. This implementation can only be used with a directed graph.

Characteristics

The main Characteristics are:

- Components are described by vertices
- The returned values are ordered:
 - *component* ascending
 - *node* ascending
- Running time: $O(V + E)$

Signatures

```
pgr_strongComponents(edges_sql)

RETURNS SET OF (seq, component, n_seq, node)
OR EMPTY SET
```

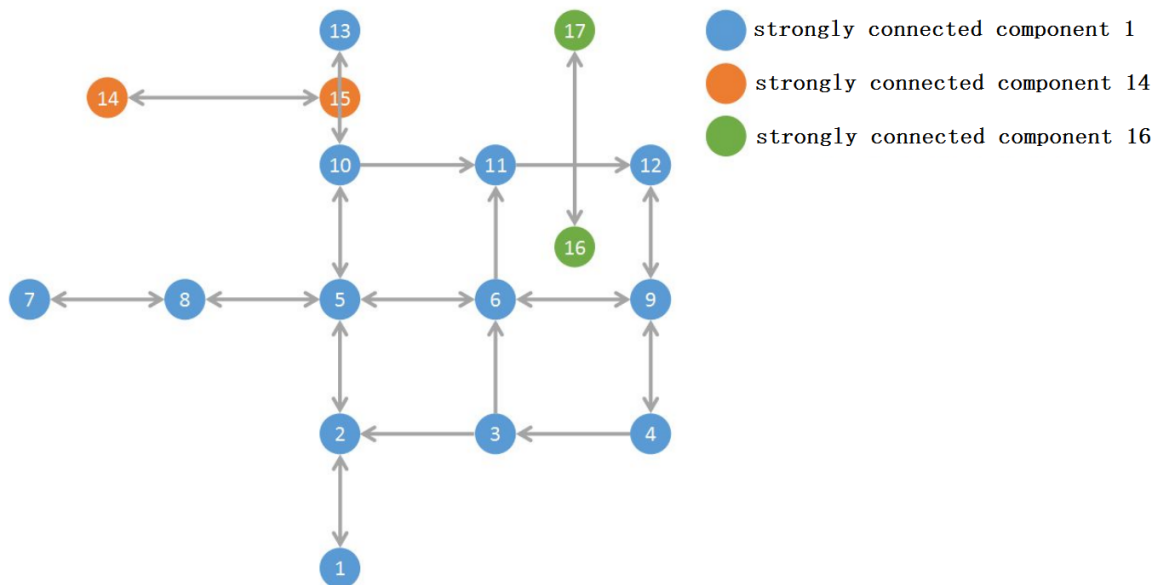
The signature is for a **directed** graph.

Example

```
SELECT * FROM pgr_strongComponents(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table'
);
 seq | component | n_seq | node
```

	+	+	+	+
1		1		1
2		1		2
3		1		3
4		1		4
5		1		5
6		1		6
7		1		7
8		1		8
9		1		9
10		1		10
11		1		11
12		1		12
13		1		13
14		14		1
15		14		2
16		16		1
17		16		2

(17 rows)



Description of the Signatures

Description of the edges_sql query for components functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Default	Description
edges_sql	TEXT		SQL query as described above.

Description of the return values for connected components and strongly connected components Returns set of (*seq, component, n_seq, node*)

Column	Type	Description
seq	INT	Sequential value starting from 1.
component	BIGINT	Component identifier. It is equal to the minimum node identifier in the component.
n_seq	INT	It is a sequential value starting from 1 in a component.
node	BIGINT	Identifier of the vertex.

See Also

- http://en.wikipedia.org/wiki/Strongly_connected_component
- The queries use the [Sample Data](#) network.

Indices and tables

- genindex
- search

pg_r_biconnectedComponents - Experimental

`pg_r_biconnectedComponents` — Return the biconnected components of an undirected graph. In particular, the algorithm implemented by Boost.Graph.



Fig. 6.22: Boost Graph Inside

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

The biconnected components of an undirected graph are the maximal subsets of vertices such that the removal of a vertex from particular component will not disconnect the component. Unlike connected components, vertices may belong to multiple biconnected components. Vertices can be present in multiple biconnected components, but each edge can only be contained in a single biconnected component. So, the output only has edge version.

This implementation can only be used with an undirected graph.

Characteristics

The main Characteristics are:

- Components are described by edges
- The returned values are ordered:
 - *component* ascending
 - *edge* ascending
- Running time: $O(V + E)$

Signatures

```
pgr_biconnectedComponents(edges_sql)

RETURNS SET OF (seq, component, n_seq, edge)
OR EMPTY SET
```

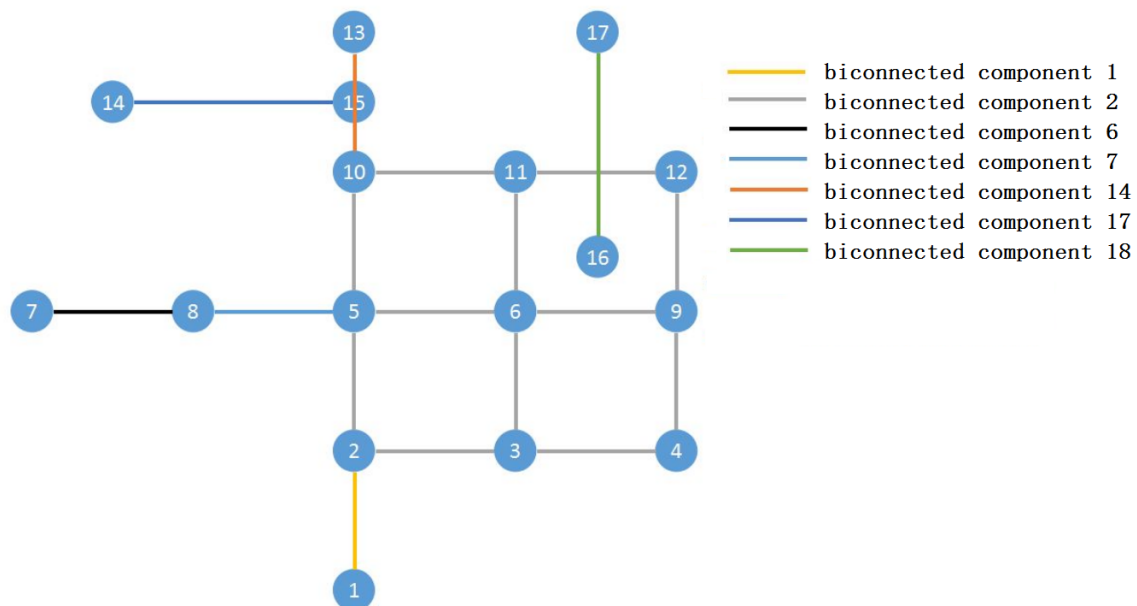
The signature is for a **undirected** graph.

Example

```

SELECT * FROM pgr_biconnectedComponents(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table'
);
 seq | component | n_seq | edge
-----+-----+-----+-----
   1 |           |     1 |    1
   2 |           |     1 |    2
   3 |           |     2 |    3
   4 |           |     3 |    4
   5 |           |     4 |    5
   6 |           |     5 |    8
   7 |           |     6 |    9
   8 |           |     7 |   10
   9 |           |     8 |   11
  10 |           |     9 |   12
  11 |           |    10 |   13
  12 |           |    11 |   15
  13 |           |    12 |   16
  14 |           |     6 |    6
  15 |           |     7 |    7
  16 |          14 |     1 |   14
  17 |          17 |     1 |   17
  18 |          18 |     1 |   18
(18 rows)

```



Description of the Signatures

Description of the `edges_sql` query for components functions

`edges_sql` an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Default	Description
edges_sql	TEXT		SQL query as described above.

Description of the return values for biconnected components, connected components (edge version) and strongly connected components Returns set of (*seq, component, n_seq, edge*)

Column	Type	Description
seq	INT	Sequential value starting from 1.
component	BIGINT	Component identifier. It is equal to the minimum edge identifier in the component.
n_seq	INT	It is a sequential value starting from 1 in a component.
edge	BIGINT	Identifier of the edge.

See Also

- http://en.wikipedia.org/wiki/Biconnected_component
- The queries use the [Sample Data](#) network.

Indices and tables

- genindex
- search

pgr_articulationPoints - Experimental

`pgr_articulationPoints` - Return the articulation points of an undirected graph. In particular, the algorithm implemented by Boost.Graph.



Fig. 6.23: Boost Graph Inside

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

Those vertices that belong to more than one biconnected component are called articulation points or, equivalently, cut vertices. Articulation points are vertices whose removal would increase the number of connected components in the graph. This implementation can only be used with an undirected graph.

Characteristics

The main Characteristics are:

- The returned values are ordered:
 - *node* ascending
- Running time: $O(V + E)$

Signatures

```
pgr_articulationPoints(edges_sql)
```

```
RETURNS SET OF (seq, node)
OR EMPTY SET
```

The signature is for a **undirected** graph.

Example

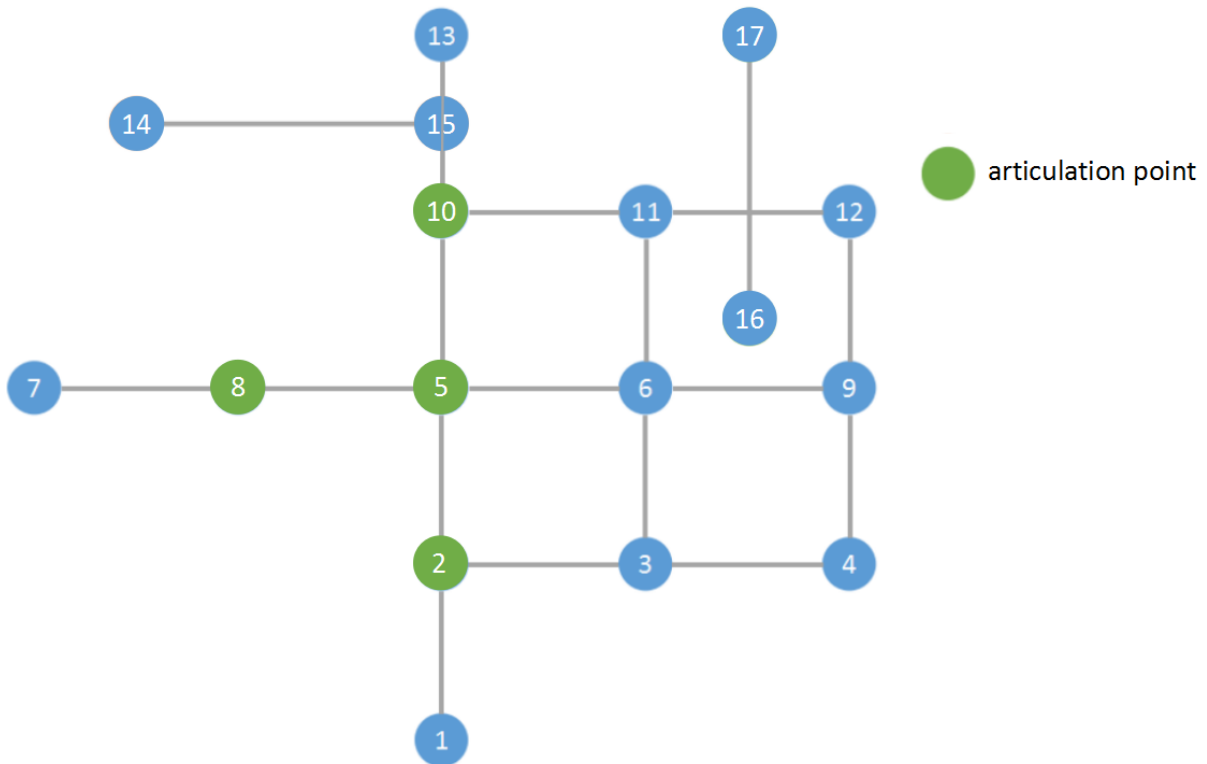
```
SELECT * FROM pgr_articulationPoints(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table'
);
 seq | node
-----+-----
   1 |     2
```



```

2 | 5
3 | 8
4 | 10
(4 rows)

```



Description of the Signatures

Description of the `edges_sql` query for components functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none">When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none">When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Default	Description
edges_sql	TEXT		SQL query as described above.

Description of the return values for articulation points Returns set of (*seq, node*)

Column	Type	Description
seq	INT	Sequential value starting from 1 .
node	BIGINT	Identifier of the vertex.

See Also

- http://en.wikipedia.org/wiki/Biconnected_component
- The queries use the [Sample Data](#) network.

Indices and tables

- [genindex](#)
- [search](#)

pgr_bridges - Experimental

`pgr_bridges` - Return the bridges of an undirected graph.



Fig. 6.24: Boost Graph Inside

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

A bridge is an edge of an undirected graph whose deletion increases its number of connected components. This implementation can only be used with an undirected graph.

Characteristics

The main Characteristics are:

- The returned values are ordered:
 - *edge* ascending
- Running time: $O(E * (V + E))$

Signatures

```
pgr_bridges(edges_sql)

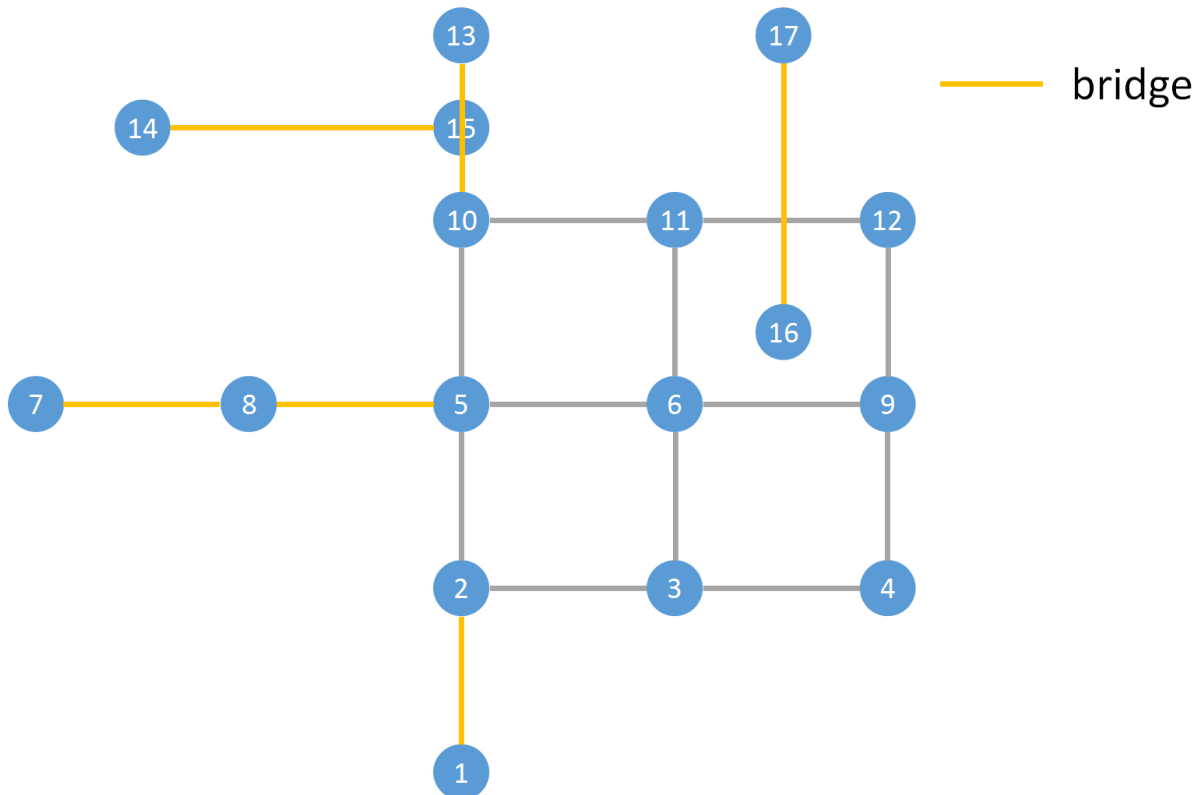
RETURNS SET OF (seq, node)
OR EMPTY SET
```

The signature is for a **undirected** graph.

Example

```
SELECT * FROM pgr_bridges(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table'
);
 seq | edge
-----+-----
   1 |     1
   2 |     6
```

```
3 | 7
4 | 14
5 | 17
6 | 18
(6 rows)
```



Description of the Signatures

Description of the `edges_sql` query for components functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Default	Description
edges_sql	TEXT		SQL query as described above.

Description of the return values for **bridges** Returns set of (*seq, node*)

Column	Type	Description
seq	INT	Sequential value starting from 1 .
edge	BIGINT	Identifier of the edge.

See Also

- http://en.wikipedia.org/wiki/Bridge_%28graph_theory%29
- The queries use the [Sample Data](#) network.

Indices and tables

- [genindex](#)
- [search](#)

The problem definition

Connected components

A connected component of an undirected graph is a set of vertices that are all reachable from each other.

Notice: This problem defines on an undirected graph.

Given the following query:

```
pgr_connectedComponentsV(sql)
```

where $sql = \{(id_i, source_i, target_i, cost_i, reverse_cost_i)\}$

and

- $source = \bigcup source_i,$
- $target = \bigcup target_i,$

The graphs are defined as follows:

The weighted undirected graph, $G(V, E)$, is defined by:

- the set of vertices V
 - $V = source \cup target$
- the set of edges E
 - $E = \begin{cases} \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, cost_i) \text{ when } cost \geq 0\} & \text{if } reverse_cost = \\ \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} \\ \cup \{(source_i, target_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} & \text{if } reverse_cost \neq \end{cases}$

Given:

- $G(V, E)$

Then:

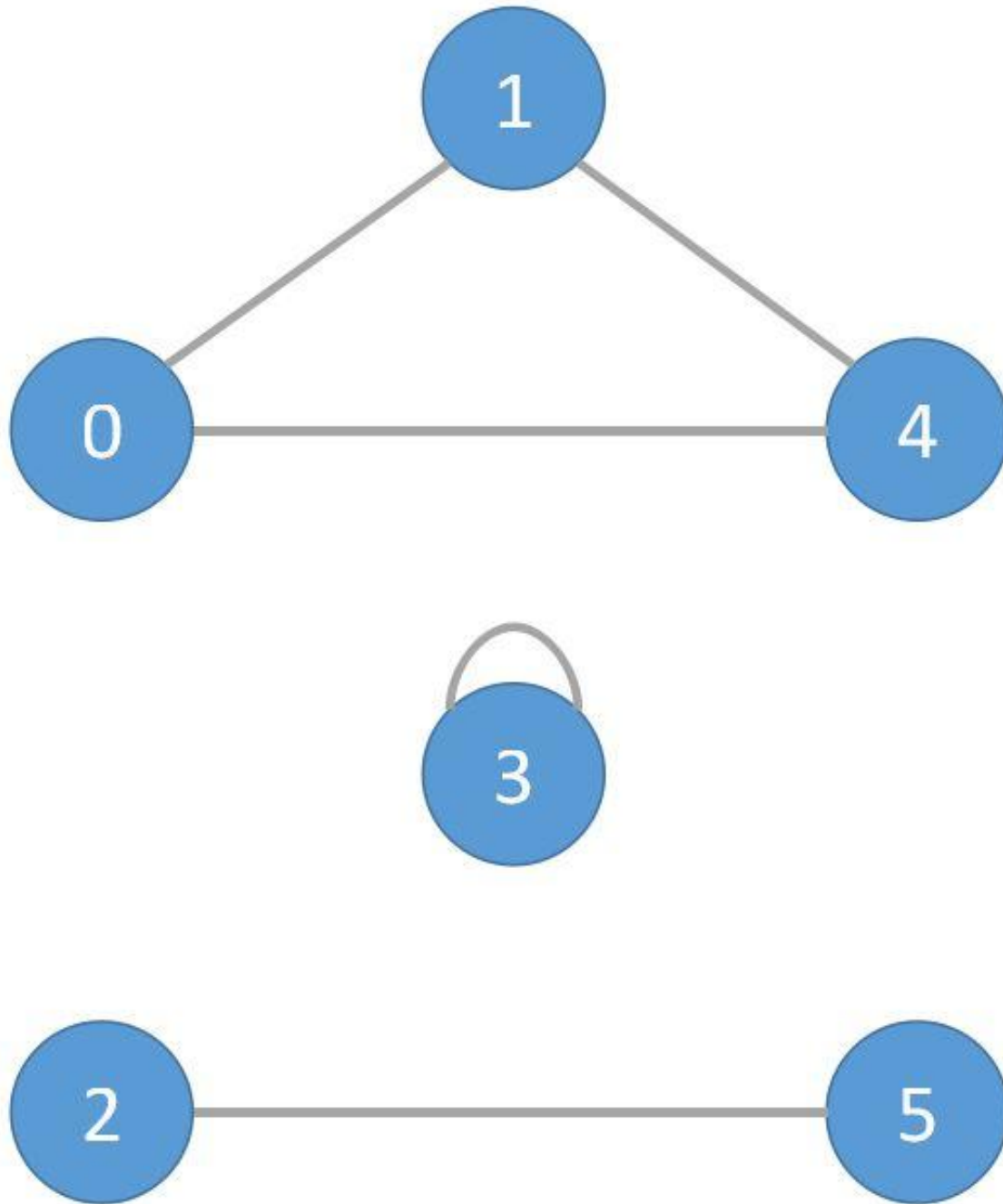
$$\pi = \{(component_i, n_seq_i, node_i)\}$$

where:

- $component_i = \min\{node_j | node_j \in component_i\}$
- n_seq_i is a sequential value starting from **1** in a component.
- $node_i \in component_i$
- The returned values are ordered:
 - *component* ascending
 - *node* ascending

Example:

- The first component is composed of nodes 0, 1 and 4.
- The second component is composed of node 3.
- The third component is composed of nodes 2 and 5.



Strongly connected components

A strongly connected component of a directed graph is a set of vertices that are all reachable from each other.

Notice: This problem defines on a directed graph.

Given the following query:

```
pgr_strongComponentsV(sql)
```

where $sql = \{(id_i, source_i, target_i, cost_i, reverse_cost_i)\}$

and

- $source = \bigcup source_i,$

- $target = \bigcup target_i$,

The graphs are defined as follows:

The weighted directed graph, $G_d(V, E)$, is defined by:

- the set of vertices V
 - $V = source \cup target \cup start_{vid} \cup end_{vid}$
- the set of edges E
 - $E = \begin{cases} \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} & \text{if } reverse_cost = \\ \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} & \text{if } reverse_cost \neq \end{cases}$

Given:

- $G(V, E)$

Then:

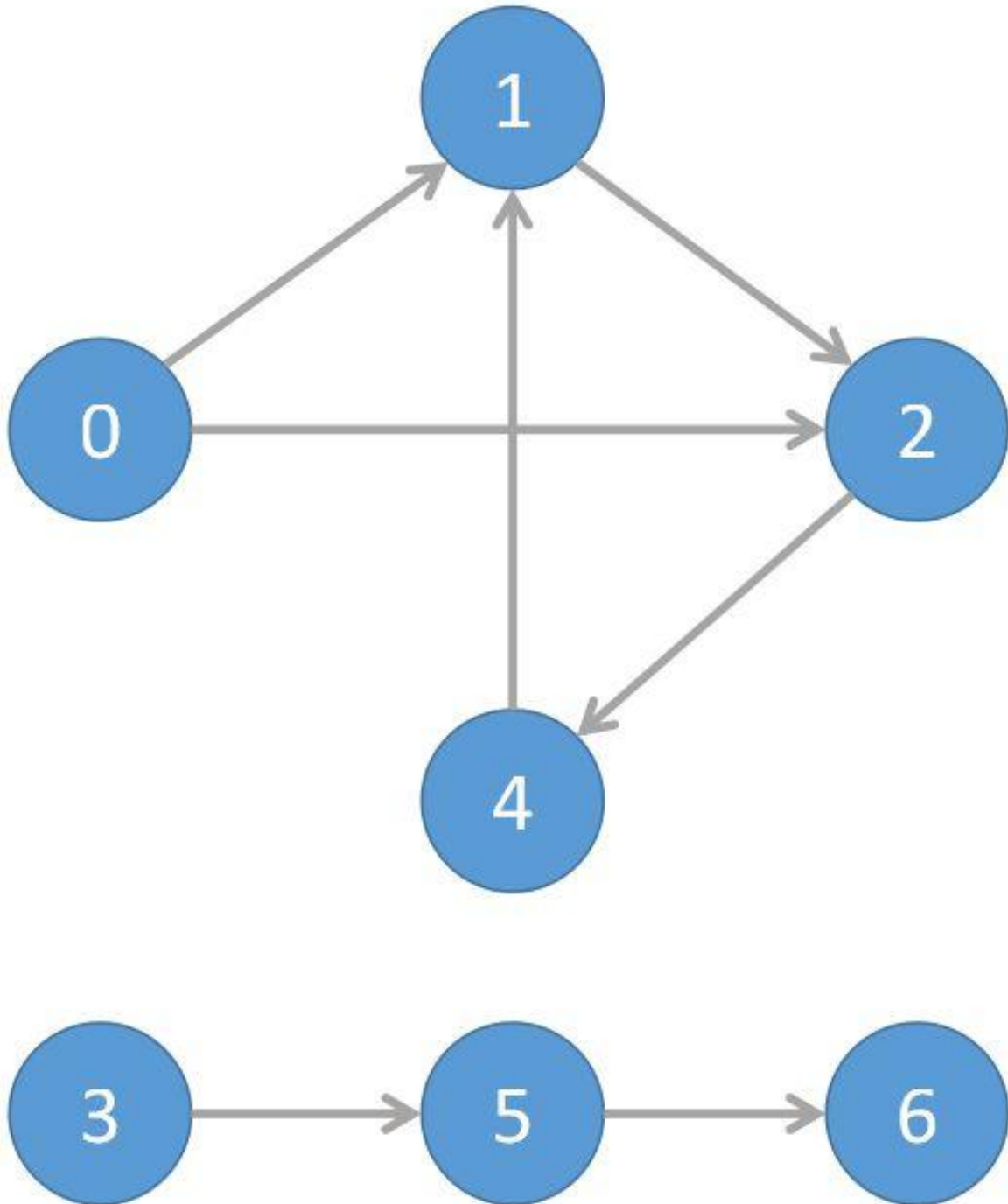
$$\pi = \{(component_i, n_seq_i, node_i)\}$$

where:

- $component_i = \min node_j | node_j \in component_i$
- n_seq_i is a sequential value starting from **1** in a component.
- $node_i \in component_i$
- The returned values are ordered:
 - *component* ascending
 - *node* ascending

Example:

- The first component is composed of nodes 1, 2 and 4.
- The second component is composed of node 0.
- The third component is composed of node 3.
- The fourth component is composed of node 5.
- The fifth component is composed of node 6.



Biconnected components

The biconnected components of an undirected graph are the maximal subsets of vertices such that the removal of a vertex from particular component will not disconnect the component. Unlike connected components, vertices may belong to multiple biconnected components. Vertices can be present in multiple biconnected components, but each edge can only be contained in a single biconnected component. So, the output only has edge version.

Notice: This problem defines on an undirected graph.

Given the following query:

```
pgr_biconnectedComponents(sql)
```

where $sql = \{(id_i, source_i, target_i, cost_i, reverse_cost_i)\}$

and

- $source = \bigcup source_i,$
- $target = \bigcup target_i,$

The graphs are defined as follows:

The weighted undirected graph, $G(V, E)$, is defined by:

- the set of vertices V
 - $V = source \cup target$
- the set of edges E
 - $E = \begin{cases} \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, cost_i) \text{ when } cost \geq 0\} & \text{if } reverse_cost = \\ \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} \\ \cup \{(source_i, target_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} & \text{if } reverse_cost \neq \end{cases}$

Given:

- $G(V, E)$

Then:

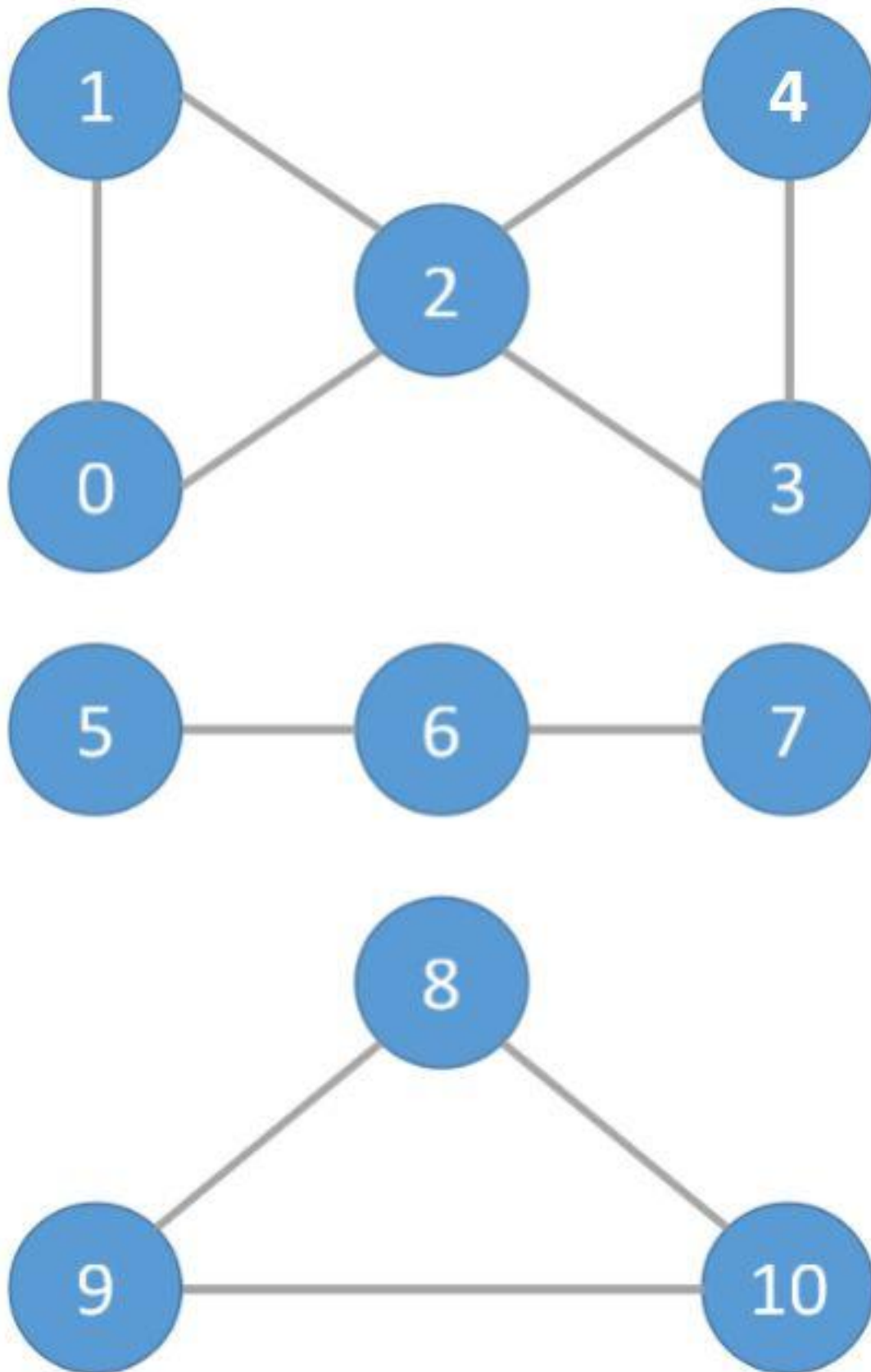
$$\pi = \{(component_i, n_seq_i, node_i)\}$$

where:

- $component_i = \min node_j | node_j \in component_i$
- n_seq_i is a sequential value starting from **1** in a component.
- $edge_i \in component_i$
- The returned values are ordered:
 - $component$ ascending
 - $edge$ ascending

Example:

- The first component is composed of edges 1 – 2, 0 – 1 and 0 – 2.
- The second component is composed of edges 2 – 4, 2 – 3 and 3 – 4.
- The third component is composed of edge 5 – 6.
- The fourth component is composed of edge 6 – 7.
- The fifth component is composed of edges 8 – 9, 9 – 10 and 8 – 10.



Articulation Points

Those vertices that belong to more than one biconnected component are called articulation points or, equivalently, cut vertices. Articulation points are vertices whose removal would increase the number of connected components in the graph.

Notice: This problem defines on an undirected graph.

Given the following query:

```
pgr_articulationPoints(sql)
```

where $sql = \{(id_i, source_i, target_i, cost_i, reverse_cost_i)\}$

and

- $source = \bigcup source_i,$
- $target = \bigcup target_i,$

The graphs are defined as follows:

The weighted undirected graph, $G(V, E)$, is defined by:

- the set of vertices V
 - $V = source \cup target$
- the set of edges E
 - $E = \begin{cases} \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, cost_i) \text{ when } cost \geq 0\} & \text{if } reverse_cost = \\ \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} \\ \cup \{(source_i, target_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} & \text{if } reverse_cost \neq \end{cases}$

Given:

- $G(V, E)$

Then:

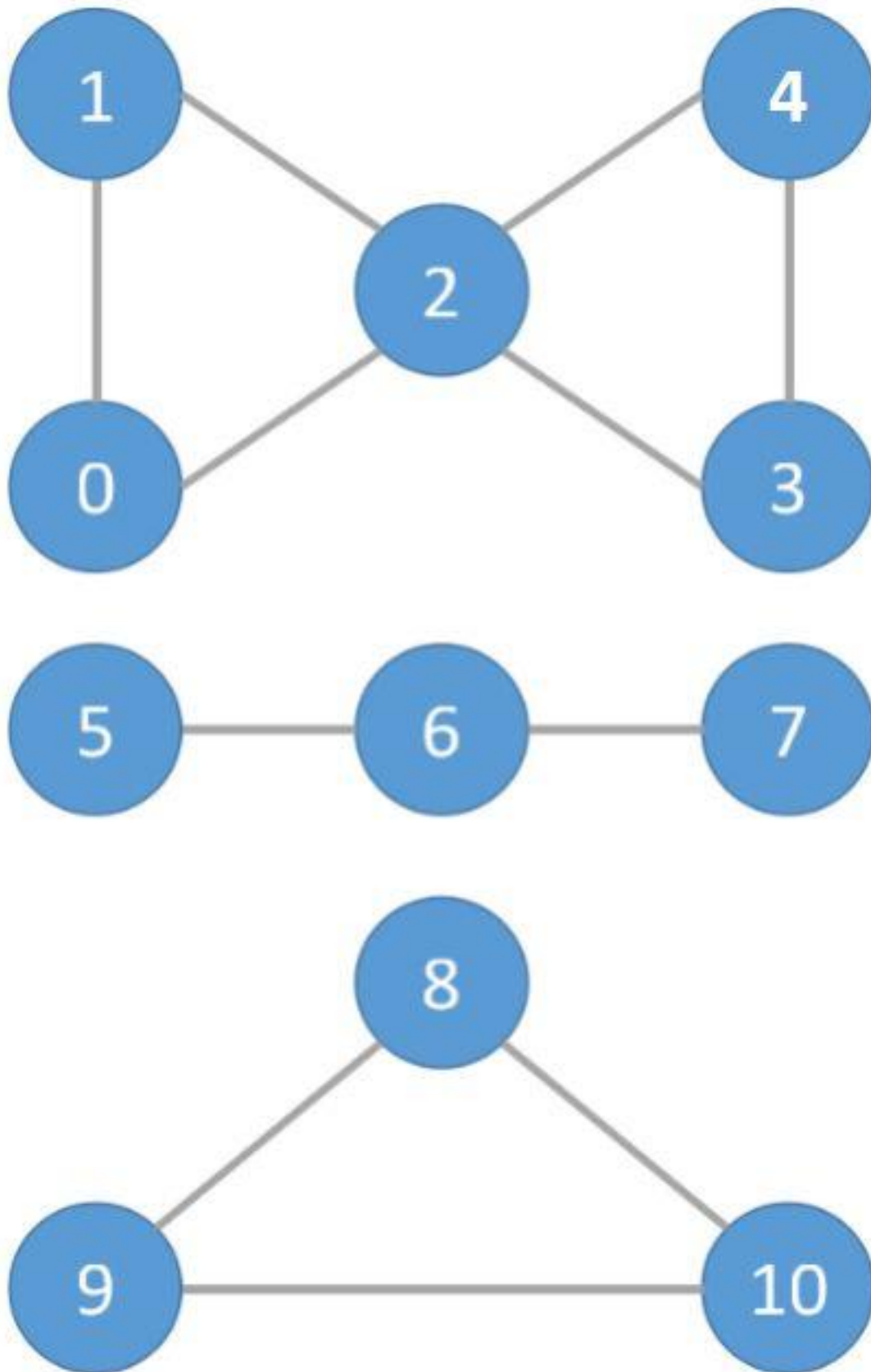
$\pi = \{node_i\}$

where:

- $node_i$ is an articulation point.
- The returned values are ordered:
 - $node$ ascending

Example:

- Articulation points are nodes 2 and 6.



Bridges

A bridge is an edge of an undirected graph whose deletion increases its number of connected components.

Notice: This problem defines on an undirected graph.

Given the following query:

```
pgr_bridges(sql)
```

where $sql = \{(id_i, source_i, target_i, cost_i, reverse_cost_i)\}$

and

- $source = \bigcup source_i$,
- $target = \bigcup target_i$,

The graphs are defined as follows:

The weighted undirected graph, $G(V, E)$, is defined by:

- the set of vertices V
 - $V = source \cup target$
- the set of edges E
 - $E = \begin{cases} \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, cost_i) \text{ when } cost \geq 0\} & \text{if } reverse_cost = \\ \{(source_i, target_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, cost_i) \text{ when } cost \geq 0\} \\ \cup \{(target_i, source_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} \\ \cup \{(source_i, target_i, reverse_cost_i) \text{ when } reverse_cost_i \geq 0\} & \text{if } reverse_cost \neq \end{cases}$

Given:

- $G(V, E)$

Then:

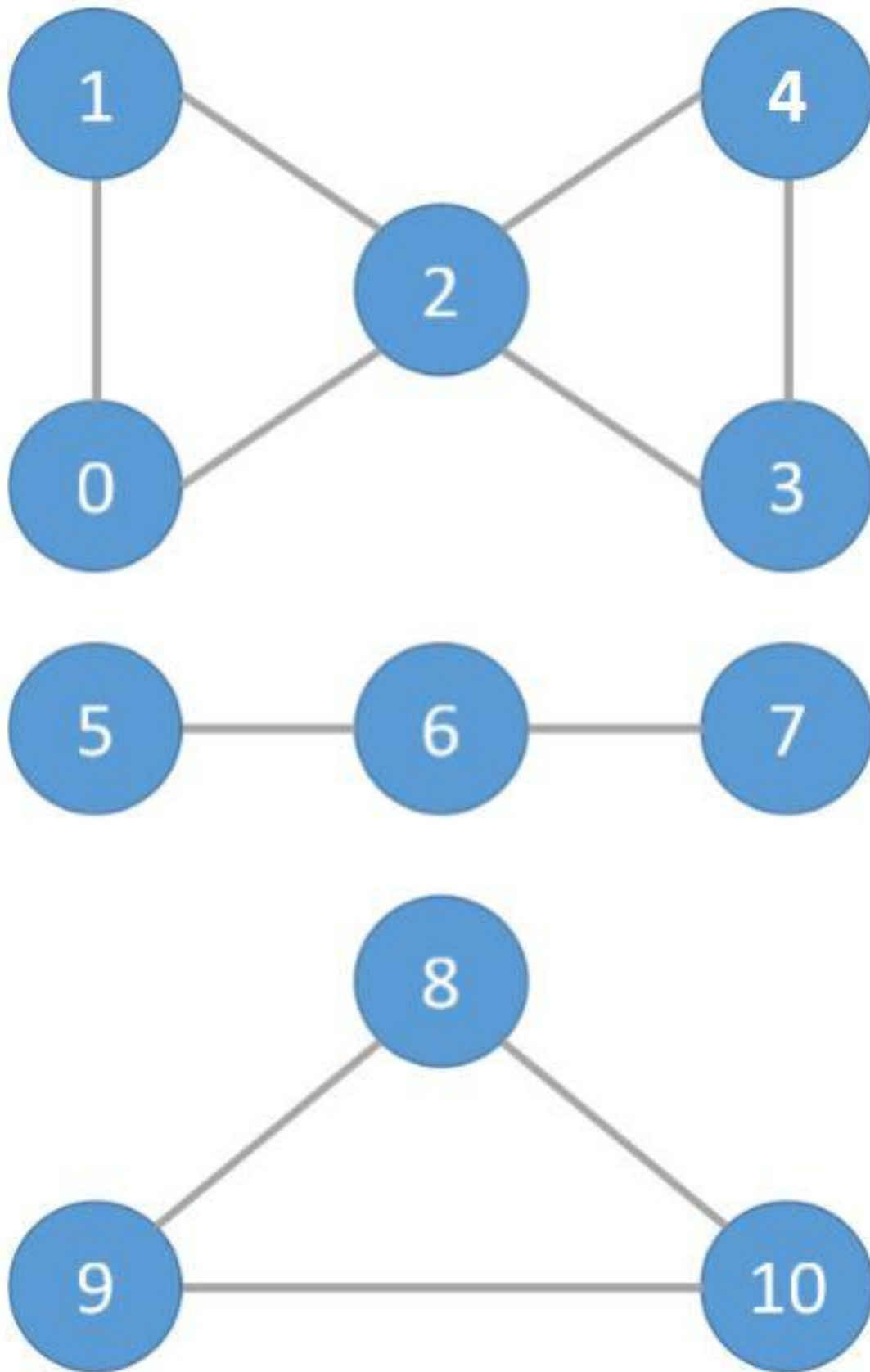
$\pi = \{edge_i\}$

where:

- $edge_i$ is an edge.
- The returned values are ordered:
 - $edge$ ascending

Example:

- Bridges are edges 5 <--> 6 and 6 <--> 7.



Description of the edges_sql query for components functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Parameter	Type	Default	Description
edges_sql	TEXT		SQL query as described above.

Description of the return values for connected components and strongly connected components

Returns set of (*seq, component, n_seq, node*)

Column	Type	Description
seq	INT	Sequential value starting from 1.
component	BIGINT	Component identifier. It is equal to the minimum node identifier in the component.
n_seq	INT	It is a sequential value starting from 1 in a component.
node	BIGINT	Identifier of the vertex.

Description of the return values for biconnected components, connected components (edge version) and strongly connected components

Returns set of (*seq, component, n_seq, edge*)

Column	Type	Description
seq	INT	Sequential value starting from 1.
component	BIGINT	Component identifier. It is equal to the minimum edge identifier in the component.
n_seq	INT	It is a sequential value starting from 1 in a component.
edge	BIGINT	Identifier of the edge.

Description of the return values for articulation points

Returns set of (seq, node)

Column	Type	Description
seq	INT	Sequential value starting from 1 .
node	BIGINT	Identifier of the vertex.

Description of the return values for bridges

Returns set of (seq, node)

Column	Type	Description
seq	INT	Sequential value starting from 1 .
edge	BIGINT	Identifier of the edge.

See Also

Indices and tables

- [genindex](#)
- [search](#)

6.2.5 pgr_gsoc_vrppdtw - Experimental

Name

`pgr_gsoc_vrppdtw` — Returns a solution for *Pick and Delivery with time windows* Vehicle Routing Problem

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Signature Summary

```
pgr_gsoc_vrppdtw(sql, vehicle_num, capacity)
RETURNS SET OF pgr_costResult[]:
```

Signatures

Complete signature

```
pgr_gsoc_vrppdtw(sql, vehicle_num, capacity)
Returns set of pgr_costResult[]:
```

Example: Show the id1

```
SELECT DISTINCT(id1) FROM pgr_gsoc_vrppdtw(
  'SELECT * FROM customer ORDER BY id', 25, 200)
ORDER BY id1;
 id1
-----
   1
   2
   3
   4
   5
   6
   7
   8
   9
  10
(10 rows)
```

Description of the Signatures

Description of the sql query

Column	Type	Description
id	ANY-INTEGER	Identifier of the customer. <ul style="list-style-type: none">• A value of 0 identifies the starting location
x	ANY-NUMERICAL	X coordinate of the location.
y	ANY-NUMERICAL	Y coordinate of the location.
demand	ANY-NUMERICAL	How much is added / removed from the vehicle. <ul style="list-style-type: none">• Negative value is a delivery,• Positive value is a pickup,
openTime	ANY-NUMERICAL	The time relative to 0, when the customer opens.
closeTime	ANY-NUMERICAL	The time relative to 0, when the customer closes.
serviceTime	ANY-NUMERICAL	The duration of the loading / unloading.
pIndex	ANY-INTEGER	Value used when the current customer is a Delivery to find the corresponding Pickup
dIndex	ANY-INTEGER	Value used when the current customer is a Pickup to find the corresponding Delivery

Description of the parameters of the signatures

Column	Type	Description
sql	TEXT	SQL query as described above.
vehicle_num	INTEGER	Maximum number of vehicles in the result. (currently is ignored)
capacity	INTEGER	Capacity of the vehicle.

Description of the result

RETURNS SET OF pgr_costResult[]:

Column	Type	Description
seq	INTEGER	Sequential value starting from 1.
id1	INTEGER	Current vehicle identifier.
id2	INTEGER	Customer identifier.
cost	FLOAT	<p>Previous cost plus travel time plus wait time plus</p> <ul style="list-style-type: none"> when <code>id2 = 0</code> for the second time for the same <code>id1</code>, then has the total time for the current <code>id1</code>

Examples

Example: Total number of rows returned

```
SELECT count(*) FROM pgr_gsoc_vrppdtw(
  'SELECT * FROM customer ORDER BY id', 25, 200);
count
-----
    126
(1 row)
```

Example: Results for only id1 values: 1, 5, and 9

```
SELECT * FROM pgr_gsoc_vrppdtw(
  'SELECT * FROM customer ORDER BY id', 25, 200)
WHERE id1 in (1, 5, 9);
seq | id1 | id2 |      cost
-----+-----+-----+-----
  1 |   1 |   0 |          0
  2 |   1 |  13 | 120.805843601499
  3 |   1 |  17 | 214.805843601499
  4 |   1 |  18 | 307.805843601499
  5 |   1 |  19 | 402.805843601499
  6 |   1 |  15 | 497.805843601499
  7 |   1 |  16 | 592.805843601499
  8 |   1 |  14 | 684.805843601499
  9 |   1 |  12 | 777.805843601499
 10 |   1 |  50 | 920.815276724293
 11 |   1 |  52 | 1013.97755438446
 12 |   1 |  49 | 1106.97755438446
 13 |   1 |  47 | 1198.97755438446
```

```
14 | 1 | 0 | 1217.00531076178
57 | 5 | 0 | 0
58 | 5 | 90 | 110.615528128088
59 | 5 | 87 | 205.615528128088
60 | 5 | 86 | 296.615528128088
61 | 5 | 83 | 392.615528128088
62 | 5 | 82 | 485.615528128088
63 | 5 | 84 | 581.446480022934
64 | 5 | 85 | 674.27490714768
65 | 5 | 88 | 767.27490714768
66 | 5 | 89 | 860.103334272426
67 | 5 | 91 | 953.70888554789
68 | 5 | 0 | 976.069565322888
105 | 9 | 0 | 0
106 | 9 | 67 | 102.206555615734
107 | 9 | 65 | 193.206555615734
108 | 9 | 63 | 285.206555615734
109 | 9 | 62 | 380.206555615734
110 | 9 | 74 | 473.206555615734
111 | 9 | 72 | 568.206555615734
112 | 9 | 61 | 661.206555615734
113 | 9 | 64 | 663.206555615734
114 | 9 | 102 | 753.206555615734
115 | 9 | 68 | 846.206555615734
116 | 9 | 0 | 866.822083743822
(38 rows)
```

See Also

- The examples use *Pick & Deliver Data*
- http://en.wikipedia.org/wiki/Vehicle_routing_problem

Indices and tables

- [genindex](#)
- [search](#)

6.2.6 pgr_vrpOneDepot - Experimental

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

No documentation available

Example:

Current Result

```

BEGIN;
BEGIN
SET client_min_messages TO NOTICE;
SET
SELECT * FROM pgr_vrpOneDepot(
  'SELECT * FROM vrp_orders',
  'SELECT * FROM vrp_vehicles',
  'SELECT * FROM vrp_distance',
  1);
oid | opos | vid | tarrival | tdepart
-----+-----+-----+-----+-----
-1 | 1 | 5 | 0 | 0
66 | 2 | 5 | 0 | 0
25 | 3 | 5 | 0 | 0
21 | 4 | 5 | 0 | 0
84 | 5 | 5 | 0 | 0
50 | 6 | 5 | 0 | 0
49 | 7 | 5 | 0 | 0
24 | 8 | 5 | 0 | 0
22 | 9 | 5 | 0 | 0
20 | 10 | 5 | 0 | 0
19 | 11 | 5 | 0 | 0
66 | 12 | 5 | 11 | 21
84 | 13 | 5 | 30 | 45
24 | 14 | 5 | 71 | 81
22 | 15 | 5 | 83 | 93
20 | 16 | 5 | 98 | 108
19 | 17 | 5 | 114 | 124
50 | 18 | 5 | 131 | 141
21 | 19 | 5 | 144 | 154
25 | 20 | 5 | 158 | 168
49 | 21 | 5 | 179 | 189
-1 | 22 | 5 | 234 | 234
-1 | 1 | 6 | 0 | 0
31 | 2 | 6 | 0 | 0
32 | 3 | 6 | 0 | 0
81 | 4 | 6 | 0 | 0
94 | 5 | 6 | 0 | 0
93 | 6 | 6 | 0 | 0
35 | 7 | 6 | 0 | 0
33 | 8 | 6 | 0 | 0
28 | 9 | 6 | 0 | 0
27 | 10 | 6 | 0 | 0
93 | 11 | 6 | 15 | 25
32 | 12 | 6 | 61 | 71
28 | 13 | 6 | 78 | 88
31 | 14 | 6 | 97 | 107
35 | 15 | 6 | 112 | 122
27 | 16 | 6 | 134 | 144
33 | 17 | 6 | 152 | 162
94 | 18 | 6 | 196 | 206
81 | 19 | 6 | 221 | 231
-1 | 20 | 6 | 238 | 238
-1 | 1 | 3 | 0 | 0
16 | 2 | 3 | 0 | 0

```

14		3		3		0		0
48		4		3		0		0
18		5		3		0		0
17		6		3		0		0
15		7		3		0		0
13		8		3		0		0
11		9		3		0		0
10		10		3		0		0
15		11		3		35		45
48		12		3		48		58
13		13		3		64		74
16		14		3		82		92
17		15		3		94		104
10		16		3		115		125
11		17		3		130		140
14		18		3		147		157
18		19		3		169		179
-1		20		3		219		219
-1		1		8		0		0
71		2		8		0		0
55		3		8		0		0
44		4		8		0		0
43		5		8		0		0
42		6		8		0		0
41		7		8		0		0
40		8		8		0		0
39		9		8		0		0
43		10		8		34		44
40		11		8		49		59
39		12		8		61		85
41		13		8		90		100
42		14		8		111		121
44		15		8		131		141
55		16		8		166		176
71		17		8		198		208
-1		18		8		228		228
-1		1		1		0		0
4		2		1		0		0
101		3		1		0		0
46		4		1		0		0
5		5		1		0		0
3		6		1		0		0
46		7		1		38		48
3		8		1		55		65
2		9		1		96		96
4		10		1		135		145
2		11		1		148		158
5		12		1		165		175
101		13		1		192		202
-1		14		1		222		222
-1		1		13		0		0
92		2		13		0		0
52		3		13		0		0
57		4		13		0		0
85		5		13		0		0
68		6		13		0		0
63		7		13		0		0
63		8		13		29		62
68		9		13		69		80
52		10		13		104		114
85		11		13		123		133
57		12		13		142		152
92		13		13		159		177

-1	14	13	189	189
-1	1	7	0	0
30	2	7	0	0
29	3	7	0	0
38	4	7	0	0
36	5	7	0	0
34	6	7	0	0
34	7	7	51	61
29	8	7	70	80
30	9	7	85	95
38	10	7	149	159
36	11	7	162	172
-1	12	7	217	217
-1	1	2	0	0
89	2	2	0	0
47	3	2	0	0
61	4	2	0	0
9	5	2	0	0
8	6	2	0	0
89	7	2	18	77
8	8	2	96	106
9	9	2	111	121
47	10	2	124	134
61	11	2	154	165
-1	12	2	192	192
-1	1	14	0	0
97	2	14	0	0
64	3	14	0	0
51	4	14	0	0
96	5	14	0	0
77	6	14	0	0
96	7	14	21	44
64	8	14	63	73
77	9	14	83	93
51	10	14	119	129
97	11	14	154	164
-1	12	14	180	180
-1	1	15	0	0
67	2	15	0	0
73	3	15	0	0
95	4	15	0	0
82	5	15	0	0
72	6	15	0	0
73	7	15	27	40
72	8	15	50	75
82	9	15	91	101
95	10	15	114	124
67	11	15	144	154
-1	12	15	167	167
-1	1	11	0	0
78	2	11	0	0
26	3	11	0	0
87	4	11	0	0
23	5	11	0	0
87	6	11	32	97
23	7	11	118	128
78	8	11	149	160
26	9	11	172	182
-1	10	11	227	227
-1	1	4	0	0
60	2	4	0	0
59	3	4	0	0
100	4	4	0	0

54		5		4		0		0
60		6		4		42		52
100		7		4		74		87
54		8		4		103		113
59		9		4		153		163
-1		10		4		211		211
-1		1		10		0		0
86		2		10		0		0
90		3		10		0		0
65		4		10		0		0
53		5		10		0		0
53		6		10		25		62
65		7		10		82		92
86		8		10		111		121
90		9		10		140		154
-1		10		10		206		206
-1		1		12		0		0
6		2		12		0		0
80		3		12		0		0
7		4		12		0		0
56		5		12		0		0
6		6		12		40		51
80		7		12		73		99
7		8		12		113		123
56		9		12		142		152
-1		10		12		166		166
-1		1		19		0		0
88		2		19		0		0
70		3		19		0		0
58		4		19		0		0
99		5		19		0		0
70		6		19		9		51
99		7		19		56		66
88		8		19		97		107
58		9		19		125		135
-1		10		19		162		162
-1		1		17		0		0
75		2		17		0		0
98		3		17		0		0
76		4		17		0		0
76		5		17		57		84
98		6		17		97		130
75		7		17		146		156
-1		8		17		192		192
-1		1		16		0		0
69		2		16		0		0
79		3		16		0		0
74		4		16		0		0
74		5		16		39		87
79		6		16		94		104
69		7		16		136		154
-1		8		16		164		164
-1		1		9		0		0
62		2		9		0		0
37		3		9		0		0
45		4		9		0		0
37		5		9		43		53
45		6		9		63		74
62		7		9		94		104
-1		8		9		120		120
-1		1		18		0		0
91		2		18		0		0
12		3		18		0		0


```

12 |      4 |    18 |      34 |      69
91 |      5 |    18 |      99 |     109
-1 |      6 |    18 |     113 |     113
-1 |      1 |    20 |       0 |       0
83 |      2 |    20 |       0 |       0
83 |      3 |    20 |      15 |      52
-1 |      4 |    20 |      67 |      67
-1 |      0 |     0 |      -1 |    3712
(241 rows)

```

```

ROLLBACK;
ROLLBACK

```

Data

```

drop table if exists vrp_orders cascade;
create table vrp_orders (
    id integer not null primary key,
    order_unit integer,
    open_time integer,
    close_time integer,
    service_time integer,
    x float8,
    y float8
);

copy vrp_orders (id, x, y, order_unit, open_time, close_time, service_time) from stdin;
1      40.000000      50.000000      0      0      240      0
2      25.000000      85.000000     20     145     175     10
3      22.000000      75.000000     30      50      80     10
4      22.000000      85.000000     10     109     139     10
5      20.000000      80.000000     40     141     171     10
6      20.000000      85.000000     20      41      71     10
7      18.000000      75.000000     20      95     125     10
8      15.000000      75.000000     20      79     109     10
9      15.000000      80.000000     10      91     121     10
10     10.000000      35.000000     20      91     121     10
11     10.000000      40.000000     30     119     149     10
12      8.000000      40.000000     40      59      89     10
13      8.000000      45.000000     20      64      94     10
14      5.000000      35.000000     10     142     172     10
15      5.000000      45.000000     10      35      65     10
16      2.000000      40.000000     20      58      88     10
17      0.000000      40.000000     20      72     102     10
18      0.000000      45.000000     20     149     179     10
19     44.000000      5.000000     20      87     117     10
20     42.000000      10.000000     40      72     102     10
21     42.000000      15.000000     10     122     152     10
22     40.000000      5.000000     10      67      97     10
23     40.000000      15.000000     40      92     122     10
24     38.000000      5.000000     30      65      95     10
25     38.000000      15.000000     10     148     178     10
26     35.000000      5.000000     20     154     184     10
27     95.000000      30.000000     30     115     145     10
28     95.000000      35.000000     20      62      92     10
29     92.000000      30.000000     10      62      92     10
30     90.000000      35.000000     10      67      97     10
31     88.000000      30.000000     10      74     104     10
32     88.000000      35.000000     20      61      91     10
33     87.000000      30.000000     10     131     161     10

```

34	85.000000	25.000000	10	51	81	10
35	85.000000	35.000000	30	111	141	10
36	67.000000	85.000000	20	139	169	10
37	65.000000	85.000000	40	43	73	10
38	65.000000	82.000000	10	124	154	10
39	62.000000	80.000000	30	75	105	10
40	60.000000	80.000000	10	37	67	10
41	60.000000	85.000000	30	85	115	10
42	58.000000	75.000000	20	92	122	10
43	55.000000	80.000000	10	33	63	10
44	55.000000	85.000000	20	128	158	10
45	55.000000	82.000000	10	64	94	10
46	20.000000	82.000000	10	37	67	10
47	18.000000	80.000000	10	113	143	10
48	2.000000	45.000000	10	45	75	10
49	42.000000	5.000000	10	151	181	10
50	42.000000	12.000000	10	104	134	10
51	72.000000	35.000000	30	116	146	10
52	55.000000	20.000000	19	83	113	10
53	25.000000	30.000000	3	52	82	10
54	20.000000	50.000000	5	91	121	10
55	55.000000	60.000000	16	139	169	10
56	30.000000	60.000000	16	140	170	10
57	50.000000	35.000000	19	130	160	10
58	30.000000	25.000000	23	96	126	10
59	15.000000	10.000000	20	152	182	10
60	10.000000	20.000000	19	42	72	10
61	15.000000	60.000000	17	155	185	10
62	45.000000	65.000000	9	66	96	10
63	65.000000	35.000000	3	52	82	10
64	65.000000	20.000000	6	39	69	10
65	45.000000	30.000000	17	53	83	10
66	35.000000	40.000000	16	11	41	10
67	41.000000	37.000000	16	133	163	10
68	64.000000	42.000000	9	70	100	10
69	40.000000	60.000000	21	144	174	10
70	31.000000	52.000000	27	41	71	10
71	35.000000	69.000000	23	180	210	10
72	65.000000	55.000000	14	65	95	10
73	63.000000	65.000000	8	30	60	10
74	2.000000	60.000000	5	77	107	10
75	20.000000	20.000000	8	141	171	10
76	5.000000	5.000000	16	74	104	10
77	60.000000	12.000000	31	75	105	10
78	23.000000	3.000000	7	150	180	10
79	8.000000	56.000000	27	90	120	10
80	6.000000	68.000000	30	89	119	10
81	47.000000	47.000000	13	192	222	10
82	49.000000	58.000000	10	86	116	10
83	27.000000	43.000000	9	42	72	10
84	37.000000	31.000000	14	35	65	10
85	57.000000	29.000000	18	96	126	10
86	63.000000	23.000000	2	87	117	10
87	21.000000	24.000000	28	87	117	10
88	12.000000	24.000000	13	90	120	10
89	24.000000	58.000000	19	67	97	10
90	67.000000	5.000000	25	144	174	10
91	37.000000	47.000000	6	86	116	10
92	49.000000	42.000000	13	167	197	10
93	53.000000	43.000000	14	14	44	10
94	61.000000	52.000000	3	178	208	10
95	57.000000	48.000000	23	95	125	10
96	56.000000	37.000000	6	34	64	10

```

97      55.000000      54.000000      26      132      162      10
98      4.000000      18.000000      35      120      150      10
99      26.000000      52.000000      9       46       76      10
100     26.000000      35.000000      15       77      107      10
101     31.000000      67.000000      3       180      210      10
\.
```

```

drop table if exists vrp_vehicles cascade;
create table vrp_vehicles (
    vehicle_id integer not null primary key,
    capacity integer,
    case_no integer
);
```

```
copy vrp_vehicles (vehicle_id, capacity, case_no) from stdin;
```

```

1      200      5
2      200      5
3      200      5
4      200      5
5      200      5
6      200      5
7      200      5
8      200      5
9      200      5
10     200      5
11     200      5
12     200      5
13     200      5
14     200      5
15     200      5
16     200      5
17     200      5
18     200      5
19     200      5
20     200      5
\.
```

```

drop table if exists vrp_distance cascade;
create table vrp_distance (
    src_id integer,
    dest_id integer,
    cost Float8,
    distance Float8,
    traveltime Float8
);
```

```
copy vrp_distance (src_id, dest_id, cost, distance, traveltime) from stdin;
```

```

1      2      38.078866      38.078866      38.078866
1      3      30.805844      30.805844      30.805844
1      4      39.357337      39.357337      39.357337
1      5      36.055513      36.055513      36.055513
1      6      40.311289      40.311289      40.311289
1      7      33.301652      33.301652      33.301652
1      8      35.355339      35.355339      35.355339
1      9      39.051248      39.051248      39.051248
1     10      33.541020      33.541020      33.541020
1     11      31.622777      31.622777      31.622777
1     12      33.526109      33.526109      33.526109
1     13      32.388269      32.388269      32.388269
1     14      38.078866      38.078866      38.078866
1     15      35.355339      35.355339      35.355339
1     16      39.293765      39.293765      39.293765
1     17      41.231056      41.231056      41.231056
```

1	18	40.311289	40.311289	40.311289
1	19	45.177428	45.177428	45.177428
1	20	40.049969	40.049969	40.049969
1	21	35.057096	35.057096	35.057096
1	22	45.000000	45.000000	45.000000
1	23	35.000000	35.000000	35.000000
1	24	45.044423	45.044423	45.044423
1	25	35.057096	35.057096	35.057096
1	26	45.276926	45.276926	45.276926
1	27	58.523500	58.523500	58.523500
1	28	57.008771	57.008771	57.008771
1	29	55.713553	55.713553	55.713553
1	30	52.201533	52.201533	52.201533
1	31	52.000000	52.000000	52.000000
1	32	50.289164	50.289164	50.289164
1	33	51.078371	51.078371	51.078371
1	34	51.478151	51.478151	51.478151
1	35	47.434165	47.434165	47.434165
1	36	44.204072	44.204072	44.204072
1	37	43.011626	43.011626	43.011626
1	38	40.607881	40.607881	40.607881
1	39	37.202150	37.202150	37.202150
1	40	36.055513	36.055513	36.055513
1	41	40.311289	40.311289	40.311289
1	42	30.805844	30.805844	30.805844
1	43	33.541020	33.541020	33.541020
1	44	38.078866	38.078866	38.078866
1	45	35.341194	35.341194	35.341194
1	46	37.735925	37.735925	37.735925
1	47	37.202150	37.202150	37.202150
1	48	38.327536	38.327536	38.327536
1	49	45.044423	45.044423	45.044423
1	50	38.052595	38.052595	38.052595
1	51	35.341194	35.341194	35.341194
1	52	33.541020	33.541020	33.541020
1	53	25.000000	25.000000	25.000000
1	54	20.000000	20.000000	20.000000
1	55	18.027756	18.027756	18.027756
1	56	14.142136	14.142136	14.142136
1	57	18.027756	18.027756	18.027756
1	58	26.925824	26.925824	26.925824
1	59	47.169906	47.169906	47.169906
1	60	42.426407	42.426407	42.426407
1	61	26.925824	26.925824	26.925824
1	62	15.811388	15.811388	15.811388
1	63	29.154759	29.154759	29.154759
1	64	39.051248	39.051248	39.051248
1	65	20.615528	20.615528	20.615528
1	66	11.180340	11.180340	11.180340
1	67	13.038405	13.038405	13.038405
1	68	25.298221	25.298221	25.298221
1	69	10.000000	10.000000	10.000000
1	70	9.219544	9.219544	9.219544
1	71	19.646883	19.646883	19.646883
1	72	25.495098	25.495098	25.495098
1	73	27.459060	27.459060	27.459060
1	74	39.293765	39.293765	39.293765
1	75	36.055513	36.055513	36.055513
1	76	57.008771	57.008771	57.008771
1	77	42.941821	42.941821	42.941821
1	78	49.979996	49.979996	49.979996
1	79	32.557641	32.557641	32.557641
1	80	38.470768	38.470768	38.470768

1	81	7.615773	7.615773	7.615773
1	82	12.041595	12.041595	12.041595
1	83	14.764823	14.764823	14.764823
1	84	19.235384	19.235384	19.235384
1	85	27.018512	27.018512	27.018512
1	86	35.468296	35.468296	35.468296
1	87	32.202484	32.202484	32.202484
1	88	38.209946	38.209946	38.209946
1	89	17.888544	17.888544	17.888544
1	90	52.478567	52.478567	52.478567
1	91	4.242641	4.242641	4.242641
1	92	12.041595	12.041595	12.041595
1	93	14.764823	14.764823	14.764823
1	94	21.095023	21.095023	21.095023
1	95	17.117243	17.117243	17.117243
1	96	20.615528	20.615528	20.615528
1	97	15.524175	15.524175	15.524175
1	98	48.166378	48.166378	48.166378
1	99	14.142136	14.142136	14.142136
1	100	20.518285	20.518285	20.518285
1	101	19.235384	19.235384	19.235384
2	1	38.078866	38.078866	38.078866
2	3	10.440307	10.440307	10.440307
2	4	3.000000	3.000000	3.000000
2	5	7.071068	7.071068	7.071068
2	6	5.000000	5.000000	5.000000
2	7	12.206556	12.206556	12.206556
2	8	14.142136	14.142136	14.142136
2	9	11.180340	11.180340	11.180340
2	10	52.201533	52.201533	52.201533
2	11	47.434165	47.434165	47.434165
2	12	48.104054	48.104054	48.104054
2	13	43.462628	43.462628	43.462628
2	14	53.851648	53.851648	53.851648
2	15	44.721360	44.721360	44.721360
2	16	50.537115	50.537115	50.537115
2	17	51.478151	51.478151	51.478151
2	18	47.169906	47.169906	47.169906
2	19	82.225300	82.225300	82.225300
2	20	76.902536	76.902536	76.902536
2	21	72.034714	72.034714	72.034714
2	22	81.394103	81.394103	81.394103
2	23	71.589105	71.589105	71.589105
2	24	81.049368	81.049368	81.049368
2	25	71.196910	71.196910	71.196910
2	26	80.622577	80.622577	80.622577
2	27	89.022469	89.022469	89.022469
2	28	86.023253	86.023253	86.023253
2	29	86.683332	86.683332	86.683332
2	30	82.006097	82.006097	82.006097
2	31	83.630138	83.630138	83.630138
2	32	80.430094	80.430094	80.430094
2	33	82.879430	82.879430	82.879430
2	34	84.852814	84.852814	84.852814
2	35	78.102497	78.102497	78.102497
2	36	42.000000	42.000000	42.000000
2	37	40.000000	40.000000	40.000000
2	38	40.112342	40.112342	40.112342
2	39	37.336309	37.336309	37.336309
2	40	35.355339	35.355339	35.355339
2	41	35.000000	35.000000	35.000000
2	42	34.481879	34.481879	34.481879
2	43	30.413813	30.413813	30.413813

2	44	30.000000	30.000000	30.000000
2	45	30.149627	30.149627	30.149627
2	46	5.830952	5.830952	5.830952
2	47	8.602325	8.602325	8.602325
2	48	46.141088	46.141088	46.141088
2	49	81.786307	81.786307	81.786307
2	50	74.953319	74.953319	74.953319
2	51	68.622154	68.622154	68.622154
2	52	71.589105	71.589105	71.589105
2	53	55.000000	55.000000	55.000000
2	54	35.355339	35.355339	35.355339
2	55	39.051248	39.051248	39.051248
2	56	25.495098	25.495098	25.495098
2	57	55.901699	55.901699	55.901699
2	58	60.207973	60.207973	60.207973
2	59	75.663730	75.663730	75.663730
2	60	66.708320	66.708320	66.708320
2	61	26.925824	26.925824	26.925824
2	62	28.284271	28.284271	28.284271
2	63	64.031242	64.031242	64.031242
2	64	76.321688	76.321688	76.321688
2	65	58.523500	58.523500	58.523500
2	66	46.097722	46.097722	46.097722
2	67	50.596443	50.596443	50.596443
2	68	58.051701	58.051701	58.051701
2	69	29.154759	29.154759	29.154759
2	70	33.541020	33.541020	33.541020
2	71	18.867962	18.867962	18.867962
2	72	50.000000	50.000000	50.000000
2	73	42.941821	42.941821	42.941821
2	74	33.970576	33.970576	33.970576
2	75	65.192024	65.192024	65.192024
2	76	82.462113	82.462113	82.462113
2	77	80.956779	80.956779	80.956779
2	78	82.024387	82.024387	82.024387
2	79	33.615473	33.615473	33.615473
2	80	25.495098	25.495098	25.495098
2	81	43.908997	43.908997	43.908997
2	82	36.124784	36.124784	36.124784
2	83	42.047592	42.047592	42.047592
2	84	55.317267	55.317267	55.317267
2	85	64.498062	64.498062	64.498062
2	86	72.718636	72.718636	72.718636
2	87	61.131007	61.131007	61.131007
2	88	62.369865	62.369865	62.369865
2	89	27.018512	27.018512	27.018512
2	90	90.354856	90.354856	90.354856
2	91	39.849718	39.849718	39.849718
2	92	49.244289	49.244289	49.244289
2	93	50.477718	50.477718	50.477718
2	94	48.836462	48.836462	48.836462
2	95	48.918299	48.918299	48.918299
2	96	57.140179	57.140179	57.140179
2	97	43.139309	43.139309	43.139309
2	98	70.213959	70.213959	70.213959
2	99	33.015148	33.015148	33.015148
2	100	50.009999	50.009999	50.009999
2	101	18.973666	18.973666	18.973666
3	1	30.805844	30.805844	30.805844
3	2	10.440307	10.440307	10.440307
3	4	10.000000	10.000000	10.000000
3	5	5.385165	5.385165	5.385165
3	6	10.198039	10.198039	10.198039

3	7	4.000000	4.000000	4.000000
3	8	7.000000	7.000000	7.000000
3	9	8.602325	8.602325	8.602325
3	10	41.761226	41.761226	41.761226
3	11	37.000000	37.000000	37.000000
3	12	37.696154	37.696154	37.696154
3	13	33.105891	33.105891	33.105891
3	14	43.462628	43.462628	43.462628
3	15	34.481879	34.481879	34.481879
3	16	40.311289	40.311289	40.311289
3	17	41.340053	41.340053	41.340053
3	18	37.202150	37.202150	37.202150
3	19	73.375745	73.375745	73.375745
3	20	68.007353	68.007353	68.007353
3	21	63.245553	63.245553	63.245553
3	22	72.277244	72.277244	72.277244
3	23	62.641839	62.641839	62.641839
3	24	71.805292	71.805292	71.805292
3	25	62.096699	62.096699	62.096699
3	26	71.196910	71.196910	71.196910
3	27	85.755466	85.755466	85.755466
3	28	83.240615	83.240615	83.240615
3	29	83.216585	83.216585	83.216585
3	30	78.892332	78.892332	78.892332
3	31	79.881162	79.881162	79.881162
3	32	77.175126	77.175126	77.175126
3	33	79.056942	79.056942	79.056942
3	34	80.430094	80.430094	80.430094
3	35	74.625733	74.625733	74.625733
3	36	46.097722	46.097722	46.097722
3	37	44.147480	44.147480	44.147480
3	38	43.566042	43.566042	43.566042
3	39	40.311289	40.311289	40.311289
3	40	38.327536	38.327536	38.327536
3	41	39.293765	39.293765	39.293765
3	42	36.000000	36.000000	36.000000
3	43	33.376639	33.376639	33.376639
3	44	34.481879	34.481879	34.481879
3	45	33.734256	33.734256	33.734256
3	46	7.280110	7.280110	7.280110
3	47	6.403124	6.403124	6.403124
3	48	36.055513	36.055513	36.055513
3	49	72.801099	72.801099	72.801099
3	50	66.098411	66.098411	66.098411
3	51	64.031242	64.031242	64.031242
3	52	64.140471	64.140471	64.140471
3	53	45.099889	45.099889	45.099889
3	54	25.079872	25.079872	25.079872
3	55	36.249138	36.249138	36.249138
3	56	17.000000	17.000000	17.000000
3	57	48.826222	48.826222	48.826222
3	58	50.635956	50.635956	50.635956
3	59	65.375837	65.375837	65.375837
3	60	56.293872	56.293872	56.293872
3	61	16.552945	16.552945	16.552945
3	62	25.079872	25.079872	25.079872
3	63	58.728187	58.728187	58.728187
3	64	69.814039	69.814039	69.814039
3	65	50.537115	50.537115	50.537115
3	66	37.336309	37.336309	37.336309
3	67	42.485292	42.485292	42.485292
3	68	53.413481	53.413481	53.413481
3	69	23.430749	23.430749	23.430749

3	70	24.698178	24.698178	24.698178
3	71	14.317821	14.317821	14.317821
3	72	47.423623	47.423623	47.423623
3	73	42.201896	42.201896	42.201896
3	74	25.000000	25.000000	25.000000
3	75	55.036352	55.036352	55.036352
3	76	72.034714	72.034714	72.034714
3	77	73.573093	73.573093	73.573093
3	78	72.006944	72.006944	72.006944
3	79	23.600847	23.600847	23.600847
3	80	17.464249	17.464249	17.464249
3	81	37.536649	37.536649	37.536649
3	82	31.906112	31.906112	31.906112
3	83	32.388269	32.388269	32.388269
3	84	46.486557	46.486557	46.486557
3	85	57.801384	57.801384	57.801384
3	86	66.219333	66.219333	66.219333
3	87	51.009803	51.009803	51.009803
3	88	51.971146	51.971146	51.971146
3	89	17.117243	17.117243	17.117243
3	90	83.216585	83.216585	83.216585
3	91	31.764760	31.764760	31.764760
3	92	42.638011	42.638011	42.638011
3	93	44.553339	44.553339	44.553339
3	94	45.276926	45.276926	45.276926
3	95	44.204072	44.204072	44.204072
3	96	50.990195	50.990195	50.990195
3	97	39.115214	39.115214	39.115214
3	98	59.774577	59.774577	59.774577
3	99	23.345235	23.345235	23.345235
3	100	40.199502	40.199502	40.199502
3	101	12.041595	12.041595	12.041595
4	1	39.357337	39.357337	39.357337
4	2	3.000000	3.000000	3.000000
4	3	10.000000	10.000000	10.000000
4	5	5.385165	5.385165	5.385165
4	6	2.000000	2.000000	2.000000
4	7	10.770330	10.770330	10.770330
4	8	12.206556	12.206556	12.206556
4	9	8.602325	8.602325	8.602325
4	10	51.419841	51.419841	51.419841
4	11	46.572524	46.572524	46.572524
4	12	47.127487	47.127487	47.127487
4	13	42.379240	42.379240	42.379240
4	14	52.810984	52.810984	52.810984
4	15	43.462628	43.462628	43.462628
4	16	49.244289	49.244289	49.244289
4	17	50.089919	50.089919	50.089919
4	18	45.650849	45.650849	45.650849
4	19	82.969874	82.969874	82.969874
4	20	77.620873	77.620873	77.620873
4	21	72.801099	72.801099	72.801099
4	22	82.000000	82.000000	82.000000
4	23	72.277244	72.277244	72.277244
4	24	81.584312	81.584312	81.584312
4	25	71.805292	71.805292	71.805292
4	26	81.049368	81.049368	81.049368
4	27	91.400219	91.400219	91.400219
4	28	88.481637	88.481637	88.481637
4	29	89.022469	89.022469	89.022469
4	30	84.403791	84.403791	84.403791
4	31	85.912746	85.912746	85.912746
4	32	82.800966	82.800966	82.800966

4	33	85.146932	85.146932	85.146932
4	34	87.000000	87.000000	87.000000
4	35	80.430094	80.430094	80.430094
4	36	45.000000	45.000000	45.000000
4	37	43.000000	43.000000	43.000000
4	38	43.104524	43.104524	43.104524
4	39	40.311289	40.311289	40.311289
4	40	38.327536	38.327536	38.327536
4	41	38.000000	38.000000	38.000000
4	42	37.363083	37.363083	37.363083
4	43	33.376639	33.376639	33.376639
4	44	33.000000	33.000000	33.000000
4	45	33.136083	33.136083	33.136083
4	46	3.605551	3.605551	3.605551
4	47	6.403124	6.403124	6.403124
4	48	44.721360	44.721360	44.721360
4	49	82.462113	82.462113	82.462113
4	50	75.690158	75.690158	75.690158
4	51	70.710678	70.710678	70.710678
4	52	72.897188	72.897188	72.897188
4	53	55.081757	55.081757	55.081757
4	54	35.057096	35.057096	35.057096
4	55	41.400483	41.400483	41.400483
4	56	26.248809	26.248809	26.248809
4	57	57.306195	57.306195	57.306195
4	58	60.530984	60.530984	60.530984
4	59	75.325958	75.325958	75.325958
4	60	66.098411	66.098411	66.098411
4	61	25.961510	25.961510	25.961510
4	62	30.479501	30.479501	30.479501
4	63	65.946948	65.946948	65.946948
4	64	77.935871	77.935871	77.935871
4	65	59.615434	59.615434	59.615434
4	66	46.840154	46.840154	46.840154
4	67	51.623638	51.623638	51.623638
4	68	60.108236	60.108236	60.108236
4	69	30.805844	30.805844	30.805844
4	70	34.205263	34.205263	34.205263
4	71	20.615528	20.615528	20.615528
4	72	52.430907	52.430907	52.430907
4	73	45.617979	45.617979	45.617979
4	74	32.015621	32.015621	32.015621
4	75	65.030762	65.030762	65.030762
4	76	81.786307	81.786307	81.786307
4	77	82.298238	82.298238	82.298238
4	78	82.006097	82.006097	82.006097
4	79	32.202484	32.202484	32.202484
4	80	23.345235	23.345235	23.345235
4	81	45.486262	45.486262	45.486262
4	82	38.183766	38.183766	38.183766
4	83	42.296572	42.296572	42.296572
4	84	56.044625	56.044625	56.044625
4	85	66.037868	66.037868	66.037868
4	86	74.330344	74.330344	74.330344
4	87	61.008196	61.008196	61.008196
4	88	61.814238	61.814238	61.814238
4	89	27.073973	27.073973	27.073973
4	90	91.787799	91.787799	91.787799
4	91	40.853396	40.853396	40.853396
4	92	50.774009	50.774009	50.774009
4	93	52.201533	52.201533	52.201533
4	94	51.088159	51.088159	51.088159
4	95	50.931326	50.931326	50.931326

4	96	58.821765	58.821765	58.821765
4	97	45.276926	45.276926	45.276926
4	98	69.375788	69.375788	69.375788
4	99	33.241540	33.241540	33.241540
4	100	50.159745	50.159745	50.159745
4	101	20.124612	20.124612	20.124612
5	1	36.055513	36.055513	36.055513
5	2	7.071068	7.071068	7.071068
5	3	5.385165	5.385165	5.385165
5	4	5.385165	5.385165	5.385165
5	6	5.000000	5.000000	5.000000
5	7	5.385165	5.385165	5.385165
5	8	7.071068	7.071068	7.071068
5	9	5.000000	5.000000	5.000000
5	10	46.097722	46.097722	46.097722
5	11	41.231056	41.231056	41.231056
5	12	41.761226	41.761226	41.761226
5	13	37.000000	37.000000	37.000000
5	14	47.434165	47.434165	47.434165
5	15	38.078866	38.078866	38.078866
5	16	43.863424	43.863424	43.863424
5	17	44.721360	44.721360	44.721360
5	18	40.311289	40.311289	40.311289
5	19	78.746428	78.746428	78.746428
5	20	73.375745	73.375745	73.375745
5	21	68.622154	68.622154	68.622154
5	22	77.620873	77.620873	77.620873
5	23	68.007353	68.007353	68.007353
5	24	77.129761	77.129761	77.129761
5	25	67.446275	67.446275	67.446275
5	26	76.485293	76.485293	76.485293
5	27	90.138782	90.138782	90.138782
5	28	87.464278	87.464278	87.464278
5	29	87.658428	87.658428	87.658428
5	30	83.216585	83.216585	83.216585
5	31	84.403791	84.403791	84.403791
5	32	81.541401	81.541401	81.541401
5	33	83.600239	83.600239	83.600239
5	34	85.146932	85.146932	85.146932
5	35	79.056942	79.056942	79.056942
5	36	47.265209	47.265209	47.265209
5	37	45.276926	45.276926	45.276926
5	38	45.044423	45.044423	45.044423
5	39	42.000000	42.000000	42.000000
5	40	40.000000	40.000000	40.000000
5	41	40.311289	40.311289	40.311289
5	42	38.327536	38.327536	38.327536
5	43	35.000000	35.000000	35.000000
5	44	35.355339	35.355339	35.355339
5	45	35.057096	35.057096	35.057096
5	46	2.000000	2.000000	2.000000
5	47	2.000000	2.000000	2.000000
5	48	39.357337	39.357337	39.357337
5	49	78.160092	78.160092	78.160092
5	50	71.470274	71.470274	71.470274
5	51	68.767725	68.767725	68.767725
5	52	69.462220	69.462220	69.462220
5	53	50.249378	50.249378	50.249378
5	54	30.000000	30.000000	30.000000
5	55	40.311289	40.311289	40.311289
5	56	22.360680	22.360680	22.360680
5	57	54.083269	54.083269	54.083269
5	58	55.901699	55.901699	55.901699

5	59	70.178344	70.178344	70.178344
5	60	60.827625	60.827625	60.827625
5	61	20.615528	20.615528	20.615528
5	62	29.154759	29.154759	29.154759
5	63	63.639610	63.639610	63.639610
5	64	75.000000	75.000000	75.000000
5	65	55.901699	55.901699	55.901699
5	66	42.720019	42.720019	42.720019
5	67	47.853944	47.853944	47.853944
5	68	58.137767	58.137767	58.137767
5	69	28.284271	28.284271	28.284271
5	70	30.083218	30.083218	30.083218
5	71	18.601075	18.601075	18.601075
5	72	51.478151	51.478151	51.478151
5	73	45.541190	45.541190	45.541190
5	74	26.907248	26.907248	26.907248
5	75	60.000000	60.000000	60.000000
5	76	76.485293	76.485293	76.485293
5	77	78.892332	78.892332	78.892332
5	78	77.058419	77.058419	77.058419
5	79	26.832816	26.832816	26.832816
5	80	18.439089	18.439089	18.439089
5	81	42.638011	42.638011	42.638011
5	82	36.400549	36.400549	36.400549
5	83	37.656341	37.656341	37.656341
5	84	51.865210	51.865210	51.865210
5	85	63.007936	63.007936	63.007936
5	86	71.400280	71.400280	71.400280
5	87	56.008928	56.008928	56.008928
5	88	56.568542	56.568542	56.568542
5	89	22.360680	22.360680	22.360680
5	90	88.509886	88.509886	88.509886
5	91	37.121422	37.121422	37.121422
5	92	47.801674	47.801674	47.801674
5	93	49.578221	49.578221	49.578221
5	94	49.648766	49.648766	49.648766
5	95	48.918299	48.918299	48.918299
5	96	56.080300	56.080300	56.080300
5	97	43.600459	43.600459	43.600459
5	98	64.031242	64.031242	64.031242
5	99	28.635642	28.635642	28.635642
5	100	45.398238	45.398238	45.398238
5	101	17.029386	17.029386	17.029386
6	1	40.311289	40.311289	40.311289
6	2	5.000000	5.000000	5.000000
6	3	10.198039	10.198039	10.198039
6	4	2.000000	2.000000	2.000000
6	5	5.000000	5.000000	5.000000
6	7	10.198039	10.198039	10.198039
6	8	11.180340	11.180340	11.180340
6	9	7.071068	7.071068	7.071068
6	10	50.990195	50.990195	50.990195
6	11	46.097722	46.097722	46.097722
6	12	46.572524	46.572524	46.572524
6	13	41.761226	41.761226	41.761226
6	14	52.201533	52.201533	52.201533
6	15	42.720019	42.720019	42.720019
6	16	48.466483	48.466483	48.466483
6	17	49.244289	49.244289	49.244289
6	18	44.721360	44.721360	44.721360
6	19	83.522452	83.522452	83.522452
6	20	78.160092	78.160092	78.160092
6	21	73.375745	73.375745	73.375745

6	22	82.462113	82.462113	82.462113
6	23	72.801099	72.801099	72.801099
6	24	82.000000	82.000000	82.000000
6	25	72.277244	72.277244	72.277244
6	26	81.394103	81.394103	81.394103
6	27	93.005376	93.005376	93.005376
6	28	90.138782	90.138782	90.138782
6	29	90.603532	90.603532	90.603532
6	30	86.023253	86.023253	86.023253
6	31	87.458562	87.458562	87.458562
6	32	84.403791	84.403791	84.403791
6	33	86.683332	86.683332	86.683332
6	34	88.459030	88.459030	88.459030
6	35	82.006097	82.006097	82.006097
6	36	47.000000	47.000000	47.000000
6	37	45.000000	45.000000	45.000000
6	38	45.099889	45.099889	45.099889
6	39	42.296572	42.296572	42.296572
6	40	40.311289	40.311289	40.311289
6	41	40.000000	40.000000	40.000000
6	42	39.293765	39.293765	39.293765
6	43	35.355339	35.355339	35.355339
6	44	35.000000	35.000000	35.000000
6	45	35.128336	35.128336	35.128336
6	46	3.000000	3.000000	3.000000
6	47	5.385165	5.385165	5.385165
6	48	43.863424	43.863424	43.863424
6	49	82.969874	82.969874	82.969874
6	50	76.243032	76.243032	76.243032
6	51	72.138755	72.138755	72.138755
6	52	73.824115	73.824115	73.824115
6	53	55.226805	55.226805	55.226805
6	54	35.000000	35.000000	35.000000
6	55	43.011626	43.011626	43.011626
6	56	26.925824	26.925824	26.925824
6	57	58.309519	58.309519	58.309519
6	58	60.827625	60.827625	60.827625
6	59	75.166482	75.166482	75.166482
6	60	65.764732	65.764732	65.764732
6	61	25.495098	25.495098	25.495098
6	62	32.015621	32.015621	32.015621
6	63	67.268120	67.268120	67.268120
6	64	79.056942	79.056942	79.056942
6	65	60.415230	60.415230	60.415230
6	66	47.434165	47.434165	47.434165
6	67	52.392748	52.392748	52.392748
6	68	61.522354	61.522354	61.522354
6	69	32.015621	32.015621	32.015621
6	70	34.785054	34.785054	34.785054
6	71	21.931712	21.931712	21.931712
6	72	54.083269	54.083269	54.083269
6	73	47.423623	47.423623	47.423623
6	74	30.805844	30.805844	30.805844
6	75	65.000000	65.000000	65.000000
6	76	81.394103	81.394103	81.394103
6	77	83.240615	83.240615	83.240615
6	78	82.054860	82.054860	82.054860
6	79	31.384710	31.384710	31.384710
6	80	22.022716	22.022716	22.022716
6	81	46.615448	46.615448	46.615448
6	82	39.623226	39.623226	39.623226
6	83	42.579338	42.579338	42.579338
6	84	56.612719	56.612719	56.612719

6	85	67.119297	67.119297	67.119297
6	86	75.451971	75.451971	75.451971
6	87	61.008196	61.008196	61.008196
6	88	61.522354	61.522354	61.522354
6	89	27.294688	27.294688	27.294688
6	90	92.784697	92.784697	92.784697
6	91	41.629317	41.629317	41.629317
6	92	51.865210	51.865210	51.865210
6	93	53.413481	53.413481	53.413481
6	94	52.630789	52.630789	52.630789
6	95	52.325902	52.325902	52.325902
6	96	60.000000	60.000000	60.000000
6	97	46.754679	46.754679	46.754679
6	98	68.883960	68.883960	68.883960
6	99	33.541020	33.541020	33.541020
6	100	50.358713	50.358713	50.358713
6	101	21.095023	21.095023	21.095023
7	1	33.301652	33.301652	33.301652
7	2	12.206556	12.206556	12.206556
7	3	4.000000	4.000000	4.000000
7	4	10.770330	10.770330	10.770330
7	5	5.385165	5.385165	5.385165
7	6	10.198039	10.198039	10.198039
7	8	3.000000	3.000000	3.000000
7	9	5.830952	5.830952	5.830952
7	10	40.792156	40.792156	40.792156
7	11	35.902646	35.902646	35.902646
7	12	36.400549	36.400549	36.400549
7	13	31.622777	31.622777	31.622777
7	14	42.059482	42.059482	42.059482
7	15	32.695565	32.695565	32.695565
7	16	38.483763	38.483763	38.483763
7	17	39.357337	39.357337	39.357337
7	18	34.985711	34.985711	34.985711
7	19	74.672619	74.672619	74.672619
7	20	69.289249	69.289249	69.289249
7	21	64.621978	64.621978	64.621978
7	22	73.375745	73.375745	73.375745
7	23	63.906181	63.906181	63.906181
7	24	72.801099	72.801099	72.801099
7	25	63.245553	63.245553	63.245553
7	26	72.034714	72.034714	72.034714
7	27	89.185201	89.185201	89.185201
7	28	86.769810	86.769810	86.769810
7	29	86.608314	86.608314	86.608314
7	30	82.365041	82.365041	82.365041
7	31	83.216585	83.216585	83.216585
7	32	80.622577	80.622577	80.622577
7	33	82.377181	82.377181	82.377181
7	34	83.600239	83.600239	83.600239
7	35	78.032045	78.032045	78.032045
7	36	50.009999	50.009999	50.009999
7	37	48.052055	48.052055	48.052055
7	38	47.518417	47.518417	47.518417
7	39	44.283180	44.283180	44.283180
7	40	42.296572	42.296572	42.296572
7	41	43.174066	43.174066	43.174066
7	42	40.000000	40.000000	40.000000
7	43	37.336309	37.336309	37.336309
7	44	38.327536	38.327536	38.327536
7	45	37.656341	37.656341	37.656341
7	46	7.280110	7.280110	7.280110
7	47	5.000000	5.000000	5.000000

7	48	34.000000	34.000000	34.000000
7	49	74.000000	74.000000	74.000000
7	50	67.416615	67.416615	67.416615
7	51	67.201190	67.201190	67.201190
7	52	66.287254	66.287254	66.287254
7	53	45.541190	45.541190	45.541190
7	54	25.079872	25.079872	25.079872
7	55	39.924930	39.924930	39.924930
7	56	19.209373	19.209373	19.209373
7	57	51.224994	51.224994	51.224994
7	58	51.419841	51.419841	51.419841
7	59	65.069194	65.069194	65.069194
7	60	55.578773	55.578773	55.578773
7	61	15.297059	15.297059	15.297059
7	62	28.792360	28.792360	28.792360
7	63	61.717096	61.717096	61.717096
7	64	72.346389	72.346389	72.346389
7	65	52.478567	52.478567	52.478567
7	66	38.910153	38.910153	38.910153
7	67	44.418465	44.418465	44.418465
7	68	56.612719	56.612719	56.612719
7	69	26.627054	26.627054	26.627054
7	70	26.419690	26.419690	26.419690
7	71	18.027756	18.027756	18.027756
7	72	51.078371	51.078371	51.078371
7	73	46.097722	46.097722	46.097722
7	74	21.931712	21.931712	21.931712
7	75	55.036352	55.036352	55.036352
7	76	71.196910	71.196910	71.196910
7	77	75.716577	75.716577	75.716577
7	78	72.173402	72.173402	72.173402
7	79	21.470911	21.470911	21.470911
7	80	13.892444	13.892444	13.892444
7	81	40.311289	40.311289	40.311289
7	82	35.355339	35.355339	35.355339
7	83	33.241540	33.241540	33.241540
7	84	47.927028	47.927028	47.927028
7	85	60.307545	60.307545	60.307545
7	86	68.767725	68.767725	68.767725
7	87	51.088159	51.088159	51.088159
7	88	51.351728	51.351728	51.351728
7	89	18.027756	18.027756	18.027756
7	90	85.445889	85.445889	85.445889
7	91	33.837849	33.837849	33.837849
7	92	45.276926	45.276926	45.276926
7	93	47.423623	47.423623	47.423623
7	94	48.764741	48.764741	48.764741
7	95	47.434165	47.434165	47.434165
7	96	53.740115	53.740115	53.740115
7	97	42.544095	42.544095	42.544095
7	98	58.694122	58.694122	58.694122
7	99	24.351591	24.351591	24.351591
7	100	40.792156	40.792156	40.792156
7	101	15.264338	15.264338	15.264338
8	1	35.355339	35.355339	35.355339
8	2	14.142136	14.142136	14.142136
8	3	7.000000	7.000000	7.000000
8	4	12.206556	12.206556	12.206556
8	5	7.071068	7.071068	7.071068
8	6	11.180340	11.180340	11.180340
8	7	3.000000	3.000000	3.000000
8	9	5.000000	5.000000	5.000000
8	10	40.311289	40.311289	40.311289

8	11	35.355339	35.355339	35.355339
8	12	35.693137	35.693137	35.693137
8	13	30.805844	30.805844	30.805844
8	14	41.231056	41.231056	41.231056
8	15	31.622777	31.622777	31.622777
8	16	37.336309	37.336309	37.336309
8	17	38.078866	38.078866	38.078866
8	18	33.541020	33.541020	33.541020
8	19	75.769387	75.769387	75.769387
8	20	70.384657	70.384657	70.384657
8	21	65.795137	65.795137	65.795137
8	22	74.330344	74.330344	74.330344
8	23	65.000000	65.000000	65.000000
8	24	73.681748	73.681748	73.681748
8	25	64.257295	64.257295	64.257295
8	26	72.801099	72.801099	72.801099
8	27	91.787799	91.787799	91.787799
8	28	89.442719	89.442719	89.442719
8	29	89.185201	89.185201	89.185201
8	30	85.000000	85.000000	85.000000
8	31	85.755466	85.755466	85.755466
8	32	83.240615	83.240615	83.240615
8	33	84.905830	84.905830	84.905830
8	34	86.023253	86.023253	86.023253
8	35	80.622577	80.622577	80.622577
8	36	52.952809	52.952809	52.952809
8	37	50.990195	50.990195	50.990195
8	38	50.487622	50.487622	50.487622
8	39	47.265209	47.265209	47.265209
8	40	45.276926	45.276926	45.276926
8	41	46.097722	46.097722	46.097722
8	42	43.000000	43.000000	43.000000
8	43	40.311289	40.311289	40.311289
8	44	41.231056	41.231056	41.231056
8	45	40.607881	40.607881	40.607881
8	46	8.602325	8.602325	8.602325
8	47	5.830952	5.830952	5.830952
8	48	32.695565	32.695565	32.695565
8	49	75.026662	75.026662	75.026662
8	50	68.541958	68.541958	68.541958
8	51	69.634761	69.634761	69.634761
8	52	68.007353	68.007353	68.007353
8	53	46.097722	46.097722	46.097722
8	54	25.495098	25.495098	25.495098
8	55	42.720019	42.720019	42.720019
8	56	21.213203	21.213203	21.213203
8	57	53.150729	53.150729	53.150729
8	58	52.201533	52.201533	52.201533
8	59	65.000000	65.000000	65.000000
8	60	55.226805	55.226805	55.226805
8	61	15.000000	15.000000	15.000000
8	62	31.622777	31.622777	31.622777
8	63	64.031242	64.031242	64.031242
8	64	74.330344	74.330344	74.330344
8	65	54.083269	54.083269	54.083269
8	66	40.311289	40.311289	40.311289
8	67	46.043458	46.043458	46.043458
8	68	59.076222	59.076222	59.076222
8	69	29.154759	29.154759	29.154759
8	70	28.017851	28.017851	28.017851
8	71	20.880613	20.880613	20.880613
8	72	53.851648	53.851648	53.851648
8	73	49.030603	49.030603	49.030603

8	74	19.849433	19.849433	19.849433
8	75	55.226805	55.226805	55.226805
8	76	70.710678	70.710678	70.710678
8	77	77.420927	77.420927	77.420927
8	78	72.443081	72.443081	72.443081
8	79	20.248457	20.248457	20.248457
8	80	11.401754	11.401754	11.401754
8	81	42.520583	42.520583	42.520583
8	82	38.013156	38.013156	38.013156
8	83	34.176015	34.176015	34.176015
8	84	49.193496	49.193496	49.193496
8	85	62.289646	62.289646	62.289646
8	86	70.767224	70.767224	70.767224
8	87	51.351728	51.351728	51.351728
8	88	51.088159	51.088159	51.088159
8	89	19.235384	19.235384	19.235384
8	90	87.200917	87.200917	87.200917
8	91	35.608988	35.608988	35.608988
8	92	47.381431	47.381431	47.381431
8	93	49.678969	49.678969	49.678969
8	94	51.429563	51.429563	51.429563
8	95	49.929951	49.929951	49.929951
8	96	55.901699	55.901699	55.901699
8	97	45.177428	45.177428	45.177428
8	98	58.051701	58.051701	58.051701
8	99	25.495098	25.495098	25.495098
8	100	41.484937	41.484937	41.484937
8	101	17.888544	17.888544	17.888544
9	1	39.051248	39.051248	39.051248
9	2	11.180340	11.180340	11.180340
9	3	8.602325	8.602325	8.602325
9	4	8.602325	8.602325	8.602325
9	5	5.000000	5.000000	5.000000
9	6	7.071068	7.071068	7.071068
9	7	5.830952	5.830952	5.830952
9	8	5.000000	5.000000	5.000000
9	10	45.276926	45.276926	45.276926
9	11	40.311289	40.311289	40.311289
9	12	40.607881	40.607881	40.607881
9	13	35.693137	35.693137	35.693137
9	14	46.097722	46.097722	46.097722
9	15	36.400549	36.400549	36.400549
9	16	42.059482	42.059482	42.059482
9	17	42.720019	42.720019	42.720019
9	18	38.078866	38.078866	38.078866
9	19	80.411442	80.411442	80.411442
9	20	75.026662	75.026662	75.026662
9	21	70.384657	70.384657	70.384657
9	22	79.056942	79.056942	79.056942
9	23	69.641941	69.641941	69.641941
9	24	78.447435	78.447435	78.447435
9	25	68.949257	68.949257	68.949257
9	26	77.620873	77.620873	77.620873
9	27	94.339811	94.339811	94.339811
9	28	91.787799	91.787799	91.787799
9	29	91.809586	91.809586	91.809586
9	30	87.464278	87.464278	87.464278
9	31	88.481637	88.481637	88.481637
9	32	85.755466	85.755466	85.755466
9	33	87.658428	87.658428	87.658428
9	34	89.022469	89.022469	89.022469
9	35	83.216585	83.216585	83.216585
9	36	52.239832	52.239832	52.239832

9	37	50.249378	50.249378	50.249378
9	38	50.039984	50.039984	50.039984
9	39	47.000000	47.000000	47.000000
9	40	45.000000	45.000000	45.000000
9	41	45.276926	45.276926	45.276926
9	42	43.289722	43.289722	43.289722
9	43	40.000000	40.000000	40.000000
9	44	40.311289	40.311289	40.311289
9	45	40.049969	40.049969	40.049969
9	46	5.385165	5.385165	5.385165
9	47	3.000000	3.000000	3.000000
9	48	37.336309	37.336309	37.336309
9	49	79.711982	79.711982	79.711982
9	50	73.164199	73.164199	73.164199
9	51	72.622311	72.622311	72.622311
9	52	72.111026	72.111026	72.111026
9	53	50.990195	50.990195	50.990195
9	54	30.413813	30.413813	30.413813
9	55	44.721360	44.721360	44.721360
9	56	25.000000	25.000000	25.000000
9	57	57.008771	57.008771	57.008771
9	58	57.008771	57.008771	57.008771
9	59	70.000000	70.000000	70.000000
9	60	60.207973	60.207973	60.207973
9	61	20.000000	20.000000	20.000000
9	62	33.541020	33.541020	33.541020
9	63	67.268120	67.268120	67.268120
9	64	78.102497	78.102497	78.102497
9	65	58.309519	58.309519	58.309519
9	66	44.721360	44.721360	44.721360
9	67	50.249378	50.249378	50.249378
9	68	62.008064	62.008064	62.008064
9	69	32.015621	32.015621	32.015621
9	70	32.249031	32.249031	32.249031
9	71	22.825424	22.825424	22.825424
9	72	55.901699	55.901699	55.901699
9	73	50.289164	50.289164	50.289164
9	74	23.853721	23.853721	23.853721
9	75	60.207973	60.207973	60.207973
9	76	75.663730	75.663730	75.663730
9	77	81.541401	81.541401	81.541401
9	78	77.414469	77.414469	77.414469
9	79	25.000000	25.000000	25.000000
9	80	15.000000	15.000000	15.000000
9	81	45.967380	45.967380	45.967380
9	82	40.496913	40.496913	40.496913
9	83	38.897301	38.897301	38.897301
9	84	53.712196	53.712196	53.712196
9	85	66.068147	66.068147	66.068147
9	86	74.518454	74.518454	74.518454
9	87	56.320511	56.320511	56.320511
9	88	56.080300	56.080300	56.080300
9	89	23.769729	23.769729	23.769729
9	90	91.263355	91.263355	91.263355
9	91	39.661064	39.661064	39.661064
9	92	50.990195	50.990195	50.990195
9	93	53.037722	53.037722	53.037722
9	94	53.851648	53.851648	53.851648
9	95	52.801515	52.801515	52.801515
9	96	59.413803	59.413803	59.413803
9	97	47.707442	47.707442	47.707442
9	98	62.968246	62.968246	62.968246
9	99	30.083218	30.083218	30.083218

9	100	46.324939	46.324939	46.324939
9	101	20.615528	20.615528	20.615528
10	1	33.541020	33.541020	33.541020
10	2	52.201533	52.201533	52.201533
10	3	41.761226	41.761226	41.761226
10	4	51.419841	51.419841	51.419841
10	5	46.097722	46.097722	46.097722
10	6	50.990195	50.990195	50.990195
10	7	40.792156	40.792156	40.792156
10	8	40.311289	40.311289	40.311289
10	9	45.276926	45.276926	45.276926
10	11	5.000000	5.000000	5.000000
10	12	5.385165	5.385165	5.385165
10	13	10.198039	10.198039	10.198039
10	14	5.000000	5.000000	5.000000
10	15	11.180340	11.180340	11.180340
10	16	9.433981	9.433981	9.433981
10	17	11.180340	11.180340	11.180340
10	18	14.142136	14.142136	14.142136
10	19	45.343136	45.343136	45.343136
10	20	40.607881	40.607881	40.607881
10	21	37.735925	37.735925	37.735925
10	22	42.426407	42.426407	42.426407
10	23	36.055513	36.055513	36.055513
10	24	41.036569	41.036569	41.036569
10	25	34.409301	34.409301	34.409301
10	26	39.051248	39.051248	39.051248
10	27	85.146932	85.146932	85.146932
10	28	85.000000	85.000000	85.000000
10	29	82.152298	82.152298	82.152298
10	30	80.000000	80.000000	80.000000
10	31	78.160092	78.160092	78.160092
10	32	78.000000	78.000000	78.000000
10	33	77.162167	77.162167	77.162167
10	34	75.663730	75.663730	75.663730
10	35	75.000000	75.000000	75.000000
10	36	75.822160	75.822160	75.822160
10	37	74.330344	74.330344	74.330344
10	38	72.346389	72.346389	72.346389
10	39	68.767725	68.767725	68.767725
10	40	67.268120	67.268120	67.268120
10	41	70.710678	70.710678	70.710678
10	42	62.481997	62.481997	62.481997
10	43	63.639610	63.639610	63.639610
10	44	67.268120	67.268120	67.268120
10	45	65.069194	65.069194	65.069194
10	46	48.052055	48.052055	48.052055
10	47	45.705580	45.705580	45.705580
10	48	12.806248	12.806248	12.806248
10	49	43.863424	43.863424	43.863424
10	50	39.408121	39.408121	39.408121
10	51	62.000000	62.000000	62.000000
10	52	47.434165	47.434165	47.434165
10	53	15.811388	15.811388	15.811388
10	54	18.027756	18.027756	18.027756
10	55	51.478151	51.478151	51.478151
10	56	32.015621	32.015621	32.015621
10	57	40.000000	40.000000	40.000000
10	58	22.360680	22.360680	22.360680
10	59	25.495098	25.495098	25.495098
10	60	15.000000	15.000000	15.000000
10	61	25.495098	25.495098	25.495098
10	62	46.097722	46.097722	46.097722

10	63	55.000000	55.000000	55.000000
10	64	57.008771	57.008771	57.008771
10	65	35.355339	35.355339	35.355339
10	66	25.495098	25.495098	25.495098
10	67	31.064449	31.064449	31.064449
10	68	54.451814	54.451814	54.451814
10	69	39.051248	39.051248	39.051248
10	70	27.018512	27.018512	27.018512
10	71	42.201896	42.201896	42.201896
10	72	58.523500	58.523500	58.523500
10	73	60.901560	60.901560	60.901560
10	74	26.248809	26.248809	26.248809
10	75	18.027756	18.027756	18.027756
10	76	30.413813	30.413813	30.413813
10	77	55.036352	55.036352	55.036352
10	78	34.539832	34.539832	34.539832
10	79	21.095023	21.095023	21.095023
10	80	33.241540	33.241540	33.241540
10	81	38.897301	38.897301	38.897301
10	82	45.276926	45.276926	45.276926
10	83	18.788294	18.788294	18.788294
10	84	27.294688	27.294688	27.294688
10	85	47.381431	47.381431	47.381431
10	86	54.341513	54.341513	54.341513
10	87	15.556349	15.556349	15.556349
10	88	11.180340	11.180340	11.180340
10	89	26.925824	26.925824	26.925824
10	90	64.412732	64.412732	64.412732
10	91	29.546573	29.546573	29.546573
10	92	39.623226	39.623226	39.623226
10	93	43.737855	43.737855	43.737855
10	94	53.758720	53.758720	53.758720
10	95	48.764741	48.764741	48.764741
10	96	46.043458	46.043458	46.043458
10	97	48.846699	48.846699	48.846699
10	98	18.027756	18.027756	18.027756
10	99	23.345235	23.345235	23.345235
10	100	16.000000	16.000000	16.000000
10	101	38.275318	38.275318	38.275318
11	1	31.622777	31.622777	31.622777
11	2	47.434165	47.434165	47.434165
11	3	37.000000	37.000000	37.000000
11	4	46.572524	46.572524	46.572524
11	5	41.231056	41.231056	41.231056
11	6	46.097722	46.097722	46.097722
11	7	35.902646	35.902646	35.902646
11	8	35.355339	35.355339	35.355339
11	9	40.311289	40.311289	40.311289
11	10	5.000000	5.000000	5.000000
11	12	2.000000	2.000000	2.000000
11	13	5.385165	5.385165	5.385165
11	14	7.071068	7.071068	7.071068
11	15	7.071068	7.071068	7.071068
11	16	8.000000	8.000000	8.000000
11	17	10.000000	10.000000	10.000000
11	18	11.180340	11.180340	11.180340
11	19	48.795492	48.795492	48.795492
11	20	43.863424	43.863424	43.863424
11	21	40.607881	40.607881	40.607881
11	22	46.097722	46.097722	46.097722
11	23	39.051248	39.051248	39.051248
11	24	44.821870	44.821870	44.821870
11	25	37.536649	37.536649	37.536649

11	26	43.011626	43.011626	43.011626
11	27	85.586214	85.586214	85.586214
11	28	85.146932	85.146932	85.146932
11	29	82.607506	82.607506	82.607506
11	30	80.156098	80.156098	80.156098
11	31	78.638413	78.638413	78.638413
11	32	78.160092	78.160092	78.160092
11	33	77.646635	77.646635	77.646635
11	34	76.485293	76.485293	76.485293
11	35	75.166482	75.166482	75.166482
11	36	72.622311	72.622311	72.622311
11	37	71.063352	71.063352	71.063352
11	38	69.202601	69.202601	69.202601
11	39	65.604878	65.604878	65.604878
11	40	64.031242	64.031242	64.031242
11	41	67.268120	67.268120	67.268120
11	42	59.405387	59.405387	59.405387
11	43	60.207973	60.207973	60.207973
11	44	63.639610	63.639610	63.639610
11	45	61.554854	61.554854	61.554854
11	46	43.174066	43.174066	43.174066
11	47	40.792156	40.792156	40.792156
11	48	9.433981	9.433981	9.433981
11	49	47.423623	47.423623	47.423623
11	50	42.520583	42.520583	42.520583
11	51	62.201286	62.201286	62.201286
11	52	49.244289	49.244289	49.244289
11	53	18.027756	18.027756	18.027756
11	54	14.142136	14.142136	14.142136
11	55	49.244289	49.244289	49.244289
11	56	28.284271	28.284271	28.284271
11	57	40.311289	40.311289	40.311289
11	58	25.000000	25.000000	25.000000
11	59	30.413813	30.413813	30.413813
11	60	20.000000	20.000000	20.000000
11	61	20.615528	20.615528	20.615528
11	62	43.011626	43.011626	43.011626
11	63	55.226805	55.226805	55.226805
11	64	58.523500	58.523500	58.523500
11	65	36.400549	36.400549	36.400549
11	66	25.000000	25.000000	25.000000
11	67	31.144823	31.144823	31.144823
11	68	54.037024	54.037024	54.037024
11	69	36.055513	36.055513	36.055513
11	70	24.186773	24.186773	24.186773
11	71	38.288379	38.288379	38.288379
11	72	57.008771	57.008771	57.008771
11	73	58.600341	58.600341	58.600341
11	74	21.540659	21.540659	21.540659
11	75	22.360680	22.360680	22.360680
11	76	35.355339	35.355339	35.355339
11	77	57.306195	57.306195	57.306195
11	78	39.217343	39.217343	39.217343
11	79	16.124515	16.124515	16.124515
11	80	28.284271	28.284271	28.284271
11	81	37.656341	37.656341	37.656341
11	82	42.953463	42.953463	42.953463
11	83	17.262677	17.262677	17.262677
11	84	28.460499	28.460499	28.460499
11	85	48.270074	48.270074	48.270074
11	86	55.659680	55.659680	55.659680
11	87	19.416488	19.416488	19.416488
11	88	16.124515	16.124515	16.124515

11	89	22.803509	22.803509	22.803509
11	90	66.887966	66.887966	66.887966
11	91	27.892651	27.892651	27.892651
11	92	39.051248	39.051248	39.051248
11	93	43.104524	43.104524	43.104524
11	94	52.392748	52.392748	52.392748
11	95	47.675990	47.675990	47.675990
11	96	46.097722	46.097722	46.097722
11	97	47.127487	47.127487	47.127487
11	98	22.803509	22.803509	22.803509
11	99	20.000000	20.000000	20.000000
11	100	16.763055	16.763055	16.763055
11	101	34.205263	34.205263	34.205263
12	1	33.526109	33.526109	33.526109
12	2	48.104054	48.104054	48.104054
12	3	37.696154	37.696154	37.696154
12	4	47.127487	47.127487	47.127487
12	5	41.761226	41.761226	41.761226
12	6	46.572524	46.572524	46.572524
12	7	36.400549	36.400549	36.400549
12	8	35.693137	35.693137	35.693137
12	9	40.607881	40.607881	40.607881
12	10	5.385165	5.385165	5.385165
12	11	2.000000	2.000000	2.000000
12	13	5.000000	5.000000	5.000000
12	14	5.830952	5.830952	5.830952
12	15	5.830952	5.830952	5.830952
12	16	6.000000	6.000000	6.000000
12	17	8.000000	8.000000	8.000000
12	18	9.433981	9.433981	9.433981
12	19	50.209561	50.209561	50.209561
12	20	45.343136	45.343136	45.343136
12	21	42.201896	42.201896	42.201896
12	22	47.423623	47.423623	47.423623
12	23	40.607881	40.607881	40.607881
12	24	46.097722	46.097722	46.097722
12	25	39.051248	39.051248	39.051248
12	26	44.204072	44.204072	44.204072
12	27	87.572827	87.572827	87.572827
12	28	87.143560	87.143560	87.143560
12	29	84.593144	84.593144	84.593144
12	30	82.152298	82.152298	82.152298
12	31	80.622577	80.622577	80.622577
12	32	80.156098	80.156098	80.156098
12	33	79.630396	79.630396	79.630396
12	34	78.447435	78.447435	78.447435
12	35	77.162167	77.162167	77.162167
12	36	74.202426	74.202426	74.202426
12	37	72.622311	72.622311	72.622311
12	38	70.802542	70.802542	70.802542
12	39	67.201190	67.201190	67.201190
12	40	65.604878	65.604878	65.604878
12	41	68.767725	68.767725	68.767725
12	42	61.032778	61.032778	61.032778
12	43	61.717096	61.717096	61.717096
12	44	65.069194	65.069194	65.069194
12	45	63.031738	63.031738	63.031738
12	46	43.680659	43.680659	43.680659
12	47	41.231056	41.231056	41.231056
12	48	7.810250	7.810250	7.810250
12	49	48.795492	48.795492	48.795492
12	50	44.045431	44.045431	44.045431
12	51	64.195015	64.195015	64.195015

12	52	51.078371	51.078371	51.078371
12	53	19.723083	19.723083	19.723083
12	54	15.620499	15.620499	15.620499
12	55	51.078371	51.078371	51.078371
12	56	29.732137	29.732137	29.732137
12	57	42.296572	42.296572	42.296572
12	58	26.627054	26.627054	26.627054
12	59	30.805844	30.805844	30.805844
12	60	20.099751	20.099751	20.099751
12	61	21.189620	21.189620	21.189620
12	62	44.654227	44.654227	44.654227
12	63	57.218878	57.218878	57.218878
12	64	60.406953	60.406953	60.406953
12	65	38.327536	38.327536	38.327536
12	66	27.000000	27.000000	27.000000
12	67	33.136083	33.136083	33.136083
12	68	56.035703	56.035703	56.035703
12	69	37.735925	37.735925	37.735925
12	70	25.942244	25.942244	25.942244
12	71	39.623226	39.623226	39.623226
12	72	58.940648	58.940648	58.940648
12	73	60.415230	60.415230	60.415230
12	74	20.880613	20.880613	20.880613
12	75	23.323808	23.323808	23.323808
12	76	35.128336	35.128336	35.128336
12	77	59.059292	59.059292	59.059292
12	78	39.924930	39.924930	39.924930
12	79	16.000000	16.000000	16.000000
12	80	28.071338	28.071338	28.071338
12	81	39.623226	39.623226	39.623226
12	82	44.777226	44.777226	44.777226
12	83	19.235384	19.235384	19.235384
12	84	30.364453	30.364453	30.364453
12	85	50.219518	50.219518	50.219518
12	86	57.567352	57.567352	57.567352
12	87	20.615528	20.615528	20.615528
12	88	16.492423	16.492423	16.492423
12	89	24.083189	24.083189	24.083189
12	90	68.600292	68.600292	68.600292
12	91	29.832868	29.832868	29.832868
12	92	41.048752	41.048752	41.048752
12	93	45.099889	45.099889	45.099889
12	94	54.341513	54.341513	54.341513
12	95	49.648766	49.648766	49.648766
12	96	48.093659	48.093659	48.093659
12	97	49.040799	49.040799	49.040799
12	98	22.360680	22.360680	22.360680
12	99	21.633308	21.633308	21.633308
12	100	18.681542	18.681542	18.681542
12	101	35.468296	35.468296	35.468296
13	1	32.388269	32.388269	32.388269
13	2	43.462628	43.462628	43.462628
13	3	33.105891	33.105891	33.105891
13	4	42.379240	42.379240	42.379240
13	5	37.000000	37.000000	37.000000
13	6	41.761226	41.761226	41.761226
13	7	31.622777	31.622777	31.622777
13	8	30.805844	30.805844	30.805844
13	9	35.693137	35.693137	35.693137
13	10	10.198039	10.198039	10.198039
13	11	5.385165	5.385165	5.385165
13	12	5.000000	5.000000	5.000000
13	14	10.440307	10.440307	10.440307

13	15	3.000000	3.000000	3.000000
13	16	7.810250	7.810250	7.810250
13	17	9.433981	9.433981	9.433981
13	18	8.000000	8.000000	8.000000
13	19	53.814496	53.814496	53.814496
13	20	48.795492	48.795492	48.795492
13	21	45.343136	45.343136	45.343136
13	22	51.224994	51.224994	51.224994
13	23	43.863424	43.863424	43.863424
13	24	50.000000	50.000000	50.000000
13	25	42.426407	42.426407	42.426407
13	26	48.259714	48.259714	48.259714
13	27	88.283634	88.283634	88.283634
13	28	87.572827	87.572827	87.572827
13	29	85.328776	85.328776	85.328776
13	30	82.607506	82.607506	82.607506
13	31	81.394103	81.394103	81.394103
13	32	80.622577	80.622577	80.622577
13	33	80.411442	80.411442	80.411442
13	34	79.555012	79.555012	79.555012
13	35	77.646635	77.646635	77.646635
13	36	71.281134	71.281134	71.281134
13	37	69.634761	69.634761	69.634761
13	38	67.955868	67.955868	67.955868
13	39	64.350602	64.350602	64.350602
13	40	62.681736	62.681736	62.681736
13	41	65.604878	65.604878	65.604878
13	42	58.309519	58.309519	58.309519
13	43	58.600341	58.600341	58.600341
13	44	61.717096	61.717096	61.717096
13	45	59.816386	59.816386	59.816386
13	46	38.897301	38.897301	38.897301
13	47	36.400549	36.400549	36.400549
13	48	6.000000	6.000000	6.000000
13	49	52.497619	52.497619	52.497619
13	50	47.381431	47.381431	47.381431
13	51	64.776539	64.776539	64.776539
13	52	53.235327	53.235327	53.235327
13	53	22.671568	22.671568	22.671568
13	54	13.000000	13.000000	13.000000
13	55	49.335586	49.335586	49.335586
13	56	26.627054	26.627054	26.627054
13	57	43.174066	43.174066	43.174066
13	58	29.732137	29.732137	29.732137
13	59	35.693137	35.693137	35.693137
13	60	25.079872	25.079872	25.079872
13	61	16.552945	16.552945	16.552945
13	62	42.059482	42.059482	42.059482
13	63	57.870545	57.870545	57.870545
13	64	62.241465	62.241465	62.241465
13	65	39.924930	39.924930	39.924930
13	66	27.459060	27.459060	27.459060
13	67	33.955854	33.955854	33.955854
13	68	56.080300	56.080300	56.080300
13	69	35.341194	35.341194	35.341194
13	70	24.041631	24.041631	24.041631
13	71	36.124784	36.124784	36.124784
13	72	57.870545	57.870545	57.870545
13	73	58.523500	58.523500	58.523500
13	74	16.155494	16.155494	16.155494
13	75	27.730849	27.730849	27.730849
13	76	40.112342	40.112342	40.112342
13	77	61.587336	61.587336	61.587336

13	78	44.598206	44.598206	44.598206
13	79	11.000000	11.000000	11.000000
13	80	23.086793	23.086793	23.086793
13	81	39.051248	39.051248	39.051248
13	82	43.011626	43.011626	43.011626
13	83	19.104973	19.104973	19.104973
13	84	32.202484	32.202484	32.202484
13	85	51.546096	51.546096	51.546096
13	86	59.236813	59.236813	59.236813
13	87	24.698178	24.698178	24.698178
13	88	21.377558	21.377558	21.377558
13	89	20.615528	20.615528	20.615528
13	90	71.281134	71.281134	71.281134
13	91	29.068884	29.068884	29.068884
13	92	41.109610	41.109610	41.109610
13	93	45.044423	45.044423	45.044423
13	94	53.460266	53.460266	53.460266
13	95	49.091751	49.091751	49.091751
13	96	48.662100	48.662100	48.662100
13	97	47.853944	47.853944	47.853944
13	98	27.294688	27.294688	27.294688
13	99	19.313208	19.313208	19.313208
13	100	20.591260	20.591260	20.591260
13	101	31.827661	31.827661	31.827661
14	1	38.078866	38.078866	38.078866
14	2	53.851648	53.851648	53.851648
14	3	43.462628	43.462628	43.462628
14	4	52.810984	52.810984	52.810984
14	5	47.434165	47.434165	47.434165
14	6	52.201533	52.201533	52.201533
14	7	42.059482	42.059482	42.059482
14	8	41.231056	41.231056	41.231056
14	9	46.097722	46.097722	46.097722
14	10	5.000000	5.000000	5.000000
14	11	7.071068	7.071068	7.071068
14	12	5.830952	5.830952	5.830952
14	13	10.440307	10.440307	10.440307
14	15	10.000000	10.000000	10.000000
14	16	5.830952	5.830952	5.830952
14	17	7.071068	7.071068	7.071068
14	18	11.180340	11.180340	11.180340
14	19	49.203658	49.203658	49.203658
14	20	44.654227	44.654227	44.654227
14	21	42.059482	42.059482	42.059482
14	22	46.097722	46.097722	46.097722
14	23	40.311289	40.311289	40.311289
14	24	44.598206	44.598206	44.598206
14	25	38.587563	38.587563	38.587563
14	26	42.426407	42.426407	42.426407
14	27	90.138782	90.138782	90.138782
14	28	90.000000	90.000000	90.000000
14	29	87.143560	87.143560	87.143560
14	30	85.000000	85.000000	85.000000
14	31	83.150466	83.150466	83.150466
14	32	83.000000	83.000000	83.000000
14	33	82.152298	82.152298	82.152298
14	34	80.622577	80.622577	80.622577
14	35	80.000000	80.000000	80.000000
14	36	79.649231	79.649231	79.649231
14	37	78.102497	78.102497	78.102497
14	38	76.216796	76.216796	76.216796
14	39	72.622311	72.622311	72.622311
14	40	71.063352	71.063352	71.063352

14	41	74.330344	74.330344	74.330344
14	42	66.400301	66.400301	66.400301
14	43	67.268120	67.268120	67.268120
14	44	70.710678	70.710678	70.710678
14	45	68.622154	68.622154	68.622154
14	46	49.335586	49.335586	49.335586
14	47	46.840154	46.840154	46.840154
14	48	10.440307	10.440307	10.440307
14	49	47.634021	47.634021	47.634021
14	50	43.566042	43.566042	43.566042
14	51	67.000000	67.000000	67.000000
14	52	52.201533	52.201533	52.201533
14	53	20.615528	20.615528	20.615528
14	54	21.213203	21.213203	21.213203
14	55	55.901699	55.901699	55.901699
14	56	35.355339	35.355339	35.355339
14	57	45.000000	45.000000	45.000000
14	58	26.925824	26.925824	26.925824
14	59	26.925824	26.925824	26.925824
14	60	15.811388	15.811388	15.811388
14	61	26.925824	26.925824	26.925824
14	62	50.000000	50.000000	50.000000
14	63	60.000000	60.000000	60.000000
14	64	61.846584	61.846584	61.846584
14	65	40.311289	40.311289	40.311289
14	66	30.413813	30.413813	30.413813
14	67	36.055513	36.055513	36.055513
14	68	59.413803	59.413803	59.413803
14	69	43.011626	43.011626	43.011626
14	70	31.064449	31.064449	31.064449
14	71	45.343136	45.343136	45.343136
14	72	63.245553	63.245553	63.245553
14	73	65.299311	65.299311	65.299311
14	74	25.179357	25.179357	25.179357
14	75	21.213203	21.213203	21.213203
14	76	30.000000	30.000000	30.000000
14	77	59.615434	59.615434	59.615434
14	78	36.715120	36.715120	36.715120
14	79	21.213203	21.213203	21.213203
14	80	33.015148	33.015148	33.015148
14	81	43.680659	43.680659	43.680659
14	82	49.648766	49.648766	49.648766
14	83	23.409400	23.409400	23.409400
14	84	32.249031	32.249031	32.249031
14	85	52.345009	52.345009	52.345009
14	86	59.228372	59.228372	59.228372
14	87	19.416488	19.416488	19.416488
14	88	13.038405	13.038405	13.038405
14	89	29.832868	29.832868	29.832868
14	90	68.876701	68.876701	68.876701
14	91	34.176015	34.176015	34.176015
14	92	44.553339	44.553339	44.553339
14	93	48.662100	48.662100	48.662100
14	94	58.523500	58.523500	58.523500
14	95	53.600373	53.600373	53.600373
14	96	51.039201	51.039201	51.039201
14	97	53.488316	53.488316	53.488316
14	98	17.029386	17.029386	17.029386
14	99	27.018512	27.018512	27.018512
14	100	21.000000	21.000000	21.000000
14	101	41.231056	41.231056	41.231056
15	1	35.355339	35.355339	35.355339
15	2	44.721360	44.721360	44.721360

15	3	34.481879	34.481879	34.481879
15	4	43.462628	43.462628	43.462628
15	5	38.078866	38.078866	38.078866
15	6	42.720019	42.720019	42.720019
15	7	32.695565	32.695565	32.695565
15	8	31.622777	31.622777	31.622777
15	9	36.400549	36.400549	36.400549
15	10	11.180340	11.180340	11.180340
15	11	7.071068	7.071068	7.071068
15	12	5.830952	5.830952	5.830952
15	13	3.000000	3.000000	3.000000
15	14	10.000000	10.000000	10.000000
15	16	5.830952	5.830952	5.830952
15	17	7.071068	7.071068	7.071068
15	18	5.000000	5.000000	5.000000
15	19	55.865911	55.865911	55.865911
15	20	50.931326	50.931326	50.931326
15	21	47.634021	47.634021	47.634021
15	22	53.150729	53.150729	53.150729
15	23	46.097722	46.097722	46.097722
15	24	51.855569	51.855569	51.855569
15	25	44.598206	44.598206	44.598206
15	26	50.000000	50.000000	50.000000
15	27	91.241438	91.241438	91.241438
15	28	90.553851	90.553851	90.553851
15	29	88.283634	88.283634	88.283634
15	30	85.586214	85.586214	85.586214
15	31	84.344532	84.344532	84.344532
15	32	83.600239	83.600239	83.600239
15	33	83.360662	83.360662	83.360662
15	34	82.462113	82.462113	82.462113
15	35	80.622577	80.622577	80.622577
15	36	73.783467	73.783467	73.783467
15	37	72.111026	72.111026	72.111026
15	38	70.491134	70.491134	70.491134
15	39	66.887966	66.887966	66.887966
15	40	65.192024	65.192024	65.192024
15	41	68.007353	68.007353	68.007353
15	42	60.901560	60.901560	60.901560
15	43	61.032778	61.032778	61.032778
15	44	64.031242	64.031242	64.031242
15	45	62.201286	62.201286	62.201286
15	46	39.924930	39.924930	39.924930
15	47	37.336309	37.336309	37.336309
15	48	3.000000	3.000000	3.000000
15	49	54.488531	54.488531	54.488531
15	50	49.578221	49.578221	49.578221
15	51	67.742158	67.742158	67.742158
15	52	55.901699	55.901699	55.901699
15	53	25.000000	25.000000	25.000000
15	54	15.811388	15.811388	15.811388
15	55	52.201533	52.201533	52.201533
15	56	29.154759	29.154759	29.154759
15	57	46.097722	46.097722	46.097722
15	58	32.015621	32.015621	32.015621
15	59	36.400549	36.400549	36.400549
15	60	25.495098	25.495098	25.495098
15	61	18.027756	18.027756	18.027756
15	62	44.721360	44.721360	44.721360
15	63	60.827625	60.827625	60.827625
15	64	65.000000	65.000000	65.000000
15	65	42.720019	42.720019	42.720019
15	66	30.413813	30.413813	30.413813

15	67	36.878178	36.878178	36.878178
15	68	59.076222	59.076222	59.076222
15	69	38.078866	38.078866	38.078866
15	70	26.925824	26.925824	26.925824
15	71	38.418745	38.418745	38.418745
15	72	60.827625	60.827625	60.827625
15	73	61.351447	61.351447	61.351447
15	74	15.297059	15.297059	15.297059
15	75	29.154759	29.154759	29.154759
15	76	40.000000	40.000000	40.000000
15	77	64.140471	64.140471	64.140471
15	78	45.694639	45.694639	45.694639
15	79	11.401754	11.401754	11.401754
15	80	23.021729	23.021729	23.021729
15	81	42.047592	42.047592	42.047592
15	82	45.880279	45.880279	45.880279
15	83	22.090722	22.090722	22.090722
15	84	34.928498	34.928498	34.928498
15	85	54.405882	54.405882	54.405882
15	86	62.032250	62.032250	62.032250
15	87	26.400758	26.400758	26.400758
15	88	22.135944	22.135944	22.135944
15	89	23.021729	23.021729	23.021729
15	90	73.783467	73.783467	73.783467
15	91	32.062439	32.062439	32.062439
15	92	44.102154	44.102154	44.102154
15	93	48.041649	48.041649	48.041649
15	94	56.435804	56.435804	56.435804
15	95	52.086467	52.086467	52.086467
15	96	51.623638	51.623638	51.623638
15	97	50.803543	50.803543	50.803543
15	98	27.018512	27.018512	27.018512
15	99	22.135944	22.135944	22.135944
15	100	23.259407	23.259407	23.259407
15	101	34.058773	34.058773	34.058773
16	1	39.293765	39.293765	39.293765
16	2	50.537115	50.537115	50.537115
16	3	40.311289	40.311289	40.311289
16	4	49.244289	49.244289	49.244289
16	5	43.863424	43.863424	43.863424
16	6	48.466483	48.466483	48.466483
16	7	38.483763	38.483763	38.483763
16	8	37.336309	37.336309	37.336309
16	9	42.059482	42.059482	42.059482
16	10	9.433981	9.433981	9.433981
16	11	8.000000	8.000000	8.000000
16	12	6.000000	6.000000	6.000000
16	13	7.810250	7.810250	7.810250
16	14	5.830952	5.830952	5.830952
16	15	5.830952	5.830952	5.830952
16	17	2.000000	2.000000	2.000000
16	18	5.385165	5.385165	5.385165
16	19	54.671748	54.671748	54.671748
16	20	50.000000	50.000000	50.000000
16	21	47.169906	47.169906	47.169906
16	22	51.662365	51.662365	51.662365
16	23	45.486262	45.486262	45.486262
16	24	50.209561	50.209561	50.209561
16	25	43.829214	43.829214	43.829214
16	26	48.104054	48.104054	48.104054
16	27	93.536089	93.536089	93.536089
16	28	93.134312	93.134312	93.134312
16	29	90.553851	90.553851	90.553851

16	30	88.141931	88.141931	88.141931
16	31	86.579443	86.579443	86.579443
16	32	86.145226	86.145226	86.145226
16	33	85.586214	85.586214	85.586214
16	34	84.344532	84.344532	84.344532
16	35	83.150466	83.150466	83.150466
16	36	79.056942	79.056942	79.056942
16	37	77.420927	77.420927	77.420927
16	38	75.716577	75.716577	75.716577
16	39	72.111026	72.111026	72.111026
16	40	70.455660	70.455660	70.455660
16	41	73.409809	73.409809	73.409809
16	42	66.037868	66.037868	66.037868
16	43	66.400301	66.400301	66.400301
16	44	69.526973	69.526973	69.526973
16	45	67.623960	67.623960	67.623960
16	46	45.694639	45.694639	45.694639
16	47	43.081318	43.081318	43.081318
16	48	5.000000	5.000000	5.000000
16	49	53.150729	53.150729	53.150729
16	50	48.826222	48.826222	48.826222
16	51	70.178344	70.178344	70.178344
16	52	56.648036	56.648036	56.648036
16	53	25.079872	25.079872	25.079872
16	54	20.591260	20.591260	20.591260
16	55	56.648036	56.648036	56.648036
16	56	34.409301	34.409301	34.409301
16	57	48.259714	48.259714	48.259714
16	58	31.764760	31.764760	31.764760
16	59	32.695565	32.695565	32.695565
16	60	21.540659	21.540659	21.540659
16	61	23.853721	23.853721	23.853721
16	62	49.739320	49.739320	49.739320
16	63	63.198101	63.198101	63.198101
16	64	66.098411	66.098411	66.098411
16	65	44.147480	44.147480	44.147480
16	66	33.000000	33.000000	33.000000
16	67	39.115214	39.115214	39.115214
16	68	62.032250	62.032250	62.032250
16	69	42.941821	42.941821	42.941821
16	70	31.384710	31.384710	31.384710
16	71	43.931765	43.931765	43.931765
16	72	64.761099	64.761099	64.761099
16	73	65.924199	65.924199	65.924199
16	74	20.000000	20.000000	20.000000
16	75	26.907248	26.907248	26.907248
16	76	35.128336	35.128336	35.128336
16	77	64.404969	64.404969	64.404969
16	78	42.544095	42.544095	42.544095
16	79	17.088007	17.088007	17.088007
16	80	28.284271	28.284271	28.284271
16	81	45.541190	45.541190	45.541190
16	82	50.328918	50.328918	50.328918
16	83	25.179357	25.179357	25.179357
16	84	36.138622	36.138622	36.138622
16	85	56.089215	56.089215	56.089215
16	86	63.324561	63.324561	63.324561
16	87	24.839485	24.839485	24.839485
16	88	18.867962	18.867962	18.867962
16	89	28.425341	28.425341	28.425341
16	90	73.824115	73.824115	73.824115
16	91	35.693137	35.693137	35.693137
16	92	47.042534	47.042534	47.042534

16	93	51.088159	51.088159	51.088159
16	94	60.207973	60.207973	60.207973
16	95	55.578773	55.578773	55.578773
16	96	54.083269	54.083269	54.083269
16	97	54.817880	54.817880	54.817880
16	98	22.090722	22.090722	22.090722
16	99	26.832816	26.832816	26.832816
16	100	24.515301	24.515301	24.515301
16	101	39.623226	39.623226	39.623226
17	1	41.231056	41.231056	41.231056
17	2	51.478151	51.478151	51.478151
17	3	41.340053	41.340053	41.340053
17	4	50.089919	50.089919	50.089919
17	5	44.721360	44.721360	44.721360
17	6	49.244289	49.244289	49.244289
17	7	39.357337	39.357337	39.357337
17	8	38.078866	38.078866	38.078866
17	9	42.720019	42.720019	42.720019
17	10	11.180340	11.180340	11.180340
17	11	10.000000	10.000000	10.000000
17	12	8.000000	8.000000	8.000000
17	13	9.433981	9.433981	9.433981
17	14	7.071068	7.071068	7.071068
17	15	7.071068	7.071068	7.071068
17	16	2.000000	2.000000	2.000000
17	18	5.000000	5.000000	5.000000
17	19	56.222771	56.222771	56.222771
17	20	51.613952	51.613952	51.613952
17	21	48.877398	48.877398	48.877398
17	22	53.150729	53.150729	53.150729
17	23	47.169906	47.169906	47.169906
17	24	51.662365	51.662365	51.662365
17	25	45.486262	45.486262	45.486262
17	26	49.497475	49.497475	49.497475
17	27	95.524866	95.524866	95.524866
17	28	95.131488	95.131488	95.131488
17	29	92.541882	92.541882	92.541882
17	30	90.138782	90.138782	90.138782
17	31	88.566359	88.566359	88.566359
17	32	88.141931	88.141931	88.141931
17	33	87.572827	87.572827	87.572827
17	34	86.313383	86.313383	86.313383
17	35	85.146932	85.146932	85.146932
17	36	80.709355	80.709355	80.709355
17	37	79.056942	79.056942	79.056942
17	38	77.388630	77.388630	77.388630
17	39	73.783467	73.783467	73.783467
17	40	72.111026	72.111026	72.111026
17	41	75.000000	75.000000	75.000000
17	42	67.742158	67.742158	67.742158
17	43	68.007353	68.007353	68.007353
17	44	71.063352	71.063352	71.063352
17	45	69.202601	69.202601	69.202601
17	46	46.518813	46.518813	46.518813
17	47	43.863424	43.863424	43.863424
17	48	5.385165	5.385165	5.385165
17	49	54.671748	54.671748	54.671748
17	50	50.477718	50.477718	50.477718
17	51	72.173402	72.173402	72.173402
17	52	58.523500	58.523500	58.523500
17	53	26.925824	26.925824	26.925824
17	54	22.360680	22.360680	22.360680
17	55	58.523500	58.523500	58.523500

17	56	36.055513	36.055513	36.055513
17	57	50.249378	50.249378	50.249378
17	58	33.541020	33.541020	33.541020
17	59	33.541020	33.541020	33.541020
17	60	22.360680	22.360680	22.360680
17	61	25.000000	25.000000	25.000000
17	62	51.478151	51.478151	51.478151
17	63	65.192024	65.192024	65.192024
17	64	68.007353	68.007353	68.007353
17	65	46.097722	46.097722	46.097722
17	66	35.000000	35.000000	35.000000
17	67	41.109610	41.109610	41.109610
17	68	64.031242	64.031242	64.031242
17	69	44.721360	44.721360	44.721360
17	70	33.241540	33.241540	33.241540
17	71	45.453273	45.453273	45.453273
17	72	66.708320	66.708320	66.708320
17	73	67.779053	67.779053	67.779053
17	74	20.099751	20.099751	20.099751
17	75	28.284271	28.284271	28.284271
17	76	35.355339	35.355339	35.355339
17	77	66.211781	66.211781	66.211781
17	78	43.566042	43.566042	43.566042
17	79	17.888544	17.888544	17.888544
17	80	28.635642	28.635642	28.635642
17	81	47.518417	47.518417	47.518417
17	82	52.201533	52.201533	52.201533
17	83	27.166155	27.166155	27.166155
17	84	38.078866	38.078866	38.078866
17	85	58.051701	58.051701	58.051701
17	86	65.253352	65.253352	65.253352
17	87	26.400758	26.400758	26.400758
17	88	20.000000	20.000000	20.000000
17	89	30.000000	30.000000	30.000000
17	90	75.591005	75.591005	75.591005
17	91	37.656341	37.656341	37.656341
17	92	49.040799	49.040799	49.040799
17	93	53.084838	53.084838	53.084838
17	94	62.169124	62.169124	62.169124
17	95	57.558666	57.558666	57.558666
17	96	56.080300	56.080300	56.080300
17	97	56.753854	56.753854	56.753854
17	98	22.360680	22.360680	22.360680
17	99	28.635642	28.635642	28.635642
17	100	26.476405	26.476405	26.476405
17	101	41.109610	41.109610	41.109610
18	1	40.311289	40.311289	40.311289
18	2	47.169906	47.169906	47.169906
18	3	37.202150	37.202150	37.202150
18	4	45.650849	45.650849	45.650849
18	5	40.311289	40.311289	40.311289
18	6	44.721360	44.721360	44.721360
18	7	34.985711	34.985711	34.985711
18	8	33.541020	33.541020	33.541020
18	9	38.078866	38.078866	38.078866
18	10	14.142136	14.142136	14.142136
18	11	11.180340	11.180340	11.180340
18	12	9.433981	9.433981	9.433981
18	13	8.000000	8.000000	8.000000
18	14	11.180340	11.180340	11.180340
18	15	5.000000	5.000000	5.000000
18	16	5.385165	5.385165	5.385165
18	17	5.000000	5.000000	5.000000

18	19	59.464275	59.464275	59.464275
18	20	54.671748	54.671748	54.671748
18	21	51.613952	51.613952	51.613952
18	22	56.568542	56.568542	56.568542
18	23	50.000000	50.000000	50.000000
18	24	55.172457	55.172457	55.172457
18	25	48.414874	48.414874	48.414874
18	26	53.150729	53.150729	53.150729
18	27	96.176920	96.176920	96.176920
18	28	95.524866	95.524866	95.524866
18	29	93.214806	93.214806	93.214806
18	30	90.553851	90.553851	90.553851
18	31	89.269256	89.269256	89.269256
18	32	88.566359	88.566359	88.566359
18	33	88.283634	88.283634	88.283634
18	34	87.321246	87.321246	87.321246
18	35	85.586214	85.586214	85.586214
18	36	78.032045	78.032045	78.032045
18	37	76.321688	76.321688	76.321688
18	38	74.793048	74.793048	74.793048
18	39	71.196910	71.196910	71.196910
18	40	69.462220	69.462220	69.462220
18	41	72.111026	72.111026	72.111026
18	42	65.299311	65.299311	65.299311
18	43	65.192024	65.192024	65.192024
18	44	68.007353	68.007353	68.007353
18	45	66.287254	66.287254	66.287254
18	46	42.059482	42.059482	42.059482
18	47	39.357337	39.357337	39.357337
18	48	2.000000	2.000000	2.000000
18	49	58.000000	58.000000	58.000000
18	50	53.413481	53.413481	53.413481
18	51	72.691127	72.691127	72.691127
18	52	60.415230	60.415230	60.415230
18	53	29.154759	29.154759	29.154759
18	54	20.615528	20.615528	20.615528
18	55	57.008771	57.008771	57.008771
18	56	33.541020	33.541020	33.541020
18	57	50.990195	50.990195	50.990195
18	58	36.055513	36.055513	36.055513
18	59	38.078866	38.078866	38.078866
18	60	26.925824	26.925824	26.925824
18	61	21.213203	21.213203	21.213203
18	62	49.244289	49.244289	49.244289
18	63	65.764732	65.764732	65.764732
18	64	69.641941	69.641941	69.641941
18	65	47.434165	47.434165	47.434165
18	66	35.355339	35.355339	35.355339
18	67	41.773197	41.773197	41.773197
18	68	64.070274	64.070274	64.070274
18	69	42.720019	42.720019	42.720019
18	70	31.780497	31.780497	31.780497
18	71	42.438190	42.438190	42.438190
18	72	65.764732	65.764732	65.764732
18	73	66.098411	66.098411	66.098411
18	74	15.132746	15.132746	15.132746
18	75	32.015621	32.015621	32.015621
18	76	40.311289	40.311289	40.311289
18	77	68.476273	68.476273	68.476273
18	78	47.885280	47.885280	47.885280
18	79	13.601471	13.601471	13.601471
18	80	23.769729	23.769729	23.769729
18	81	47.042534	47.042534	47.042534

18	82	50.695167	50.695167	50.695167
18	83	27.073973	27.073973	27.073973
18	84	39.560081	39.560081	39.560081
18	85	59.203040	59.203040	59.203040
18	86	66.730802	66.730802	66.730802
18	87	29.698485	29.698485	29.698485
18	88	24.186773	24.186773	24.186773
18	89	27.294688	27.294688	27.294688
18	90	78.032045	78.032045	78.032045
18	91	37.054015	37.054015	37.054015
18	92	49.091751	49.091751	49.091751
18	93	53.037722	53.037722	53.037722
18	94	61.400326	61.400326	61.400326
18	95	57.078893	57.078893	57.078893
18	96	56.568542	56.568542	56.568542
18	97	55.731499	55.731499	55.731499
18	98	27.294688	27.294688	27.294688
18	99	26.925824	26.925824	26.925824
18	100	27.856777	27.856777	27.856777
18	101	38.013156	38.013156	38.013156
19	1	45.177428	45.177428	45.177428
19	2	82.225300	82.225300	82.225300
19	3	73.375745	73.375745	73.375745
19	4	82.969874	82.969874	82.969874
19	5	78.746428	78.746428	78.746428
19	6	83.522452	83.522452	83.522452
19	7	74.672619	74.672619	74.672619
19	8	75.769387	75.769387	75.769387
19	9	80.411442	80.411442	80.411442
19	10	45.343136	45.343136	45.343136
19	11	48.795492	48.795492	48.795492
19	12	50.209561	50.209561	50.209561
19	13	53.814496	53.814496	53.814496
19	14	49.203658	49.203658	49.203658
19	15	55.865911	55.865911	55.865911
19	16	54.671748	54.671748	54.671748
19	17	56.222771	56.222771	56.222771
19	18	59.464275	59.464275	59.464275
19	20	5.385165	5.385165	5.385165
19	21	10.198039	10.198039	10.198039
19	22	4.000000	4.000000	4.000000
19	23	10.770330	10.770330	10.770330
19	24	6.000000	6.000000	6.000000
19	25	11.661904	11.661904	11.661904
19	26	9.000000	9.000000	9.000000
19	27	56.797887	56.797887	56.797887
19	28	59.169249	59.169249	59.169249
19	29	54.120237	54.120237	54.120237
19	30	54.918121	54.918121	54.918121
19	31	50.606324	50.606324	50.606324
19	32	53.254108	53.254108	53.254108
19	33	49.739320	49.739320	49.739320
19	34	45.617979	45.617979	45.617979
19	35	50.803543	50.803543	50.803543
19	36	83.240615	83.240615	83.240615
19	37	82.710338	82.710338	82.710338
19	38	79.812280	79.812280	79.812280
19	39	77.129761	77.129761	77.129761
19	40	76.687678	76.687678	76.687678
19	41	81.584312	81.584312	81.584312
19	42	71.386273	71.386273	71.386273
19	43	75.802375	75.802375	75.802375
19	44	80.752709	80.752709	80.752709

19	45	77.781746	77.781746	77.781746
19	46	80.653580	80.653580	80.653580
19	47	79.378838	79.378838	79.378838
19	48	58.000000	58.000000	58.000000
19	49	2.000000	2.000000	2.000000
19	50	7.280110	7.280110	7.280110
19	51	41.036569	41.036569	41.036569
19	52	18.601075	18.601075	18.601075
19	53	31.400637	31.400637	31.400637
19	54	51.000000	51.000000	51.000000
19	55	56.089215	56.089215	56.089215
19	56	56.753854	56.753854	56.753854
19	57	30.594117	30.594117	30.594117
19	58	24.413111	24.413111	24.413111
19	59	29.427878	29.427878	29.427878
19	60	37.161808	37.161808	37.161808
19	61	62.177166	62.177166	62.177166
19	62	60.008333	60.008333	60.008333
19	63	36.619667	36.619667	36.619667
19	64	25.806976	25.806976	25.806976
19	65	25.019992	25.019992	25.019992
19	66	36.138622	36.138622	36.138622
19	67	32.140317	32.140317	32.140317
19	68	42.059482	42.059482	42.059482
19	69	55.145263	55.145263	55.145263
19	70	48.764741	48.764741	48.764741
19	71	64.629715	64.629715	64.629715
19	72	54.230987	54.230987	54.230987
19	73	62.936476	62.936476	62.936476
19	74	69.202601	69.202601	69.202601
19	75	28.301943	28.301943	28.301943
19	76	39.000000	39.000000	39.000000
19	77	17.464249	17.464249	17.464249
19	78	21.095023	21.095023	21.095023
19	79	62.425956	62.425956	62.425956
19	80	73.573093	73.573093	73.573093
19	81	42.107007	42.107007	42.107007
19	82	53.235327	53.235327	53.235327
19	83	41.629317	41.629317	41.629317
19	84	26.925824	26.925824	26.925824
19	85	27.294688	27.294688	27.294688
19	86	26.172505	26.172505	26.172505
19	87	29.832868	29.832868	29.832868
19	88	37.215588	37.215588	37.215588
19	89	56.648036	56.648036	56.648036
19	90	23.000000	23.000000	23.000000
19	91	42.579338	42.579338	42.579338
19	92	37.336309	37.336309	37.336309
19	93	39.051248	39.051248	39.051248
19	94	49.979996	49.979996	49.979996
19	95	44.922155	44.922155	44.922155
19	96	34.176015	34.176015	34.176015
19	97	50.219518	50.219518	50.219518
19	98	42.059482	42.059482	42.059482
19	99	50.328918	50.328918	50.328918
19	100	34.985711	34.985711	34.985711
19	101	63.348244	63.348244	63.348244
20	1	40.049969	40.049969	40.049969
20	2	76.902536	76.902536	76.902536
20	3	68.007353	68.007353	68.007353
20	4	77.620873	77.620873	77.620873
20	5	73.375745	73.375745	73.375745
20	6	78.160092	78.160092	78.160092

20	7	69.289249	69.289249	69.289249
20	8	70.384657	70.384657	70.384657
20	9	75.026662	75.026662	75.026662
20	10	40.607881	40.607881	40.607881
20	11	43.863424	43.863424	43.863424
20	12	45.343136	45.343136	45.343136
20	13	48.795492	48.795492	48.795492
20	14	44.654227	44.654227	44.654227
20	15	50.931326	50.931326	50.931326
20	16	50.000000	50.000000	50.000000
20	17	51.613952	51.613952	51.613952
20	18	54.671748	54.671748	54.671748
20	19	5.385165	5.385165	5.385165
20	21	5.000000	5.000000	5.000000
20	22	5.385165	5.385165	5.385165
20	23	5.385165	5.385165	5.385165
20	24	6.403124	6.403124	6.403124
20	25	6.403124	6.403124	6.403124
20	26	8.602325	8.602325	8.602325
20	27	56.648036	56.648036	56.648036
20	28	58.600341	58.600341	58.600341
20	29	53.851648	53.851648	53.851648
20	30	54.120237	54.120237	54.120237
20	31	50.159745	50.159745	50.159745
20	32	52.354560	52.354560	52.354560
20	33	49.244289	49.244289	49.244289
20	34	45.541190	45.541190	45.541190
20	35	49.739320	49.739320	49.739320
20	36	79.056942	79.056942	79.056942
20	37	78.447435	78.447435	78.447435
20	38	75.584390	75.584390	75.584390
20	39	72.801099	72.801099	72.801099
20	40	72.277244	72.277244	72.277244
20	41	77.129761	77.129761	77.129761
20	42	66.940272	66.940272	66.940272
20	43	71.196910	71.196910	71.196910
20	44	76.118329	76.118329	76.118329
20	45	73.164199	73.164199	73.164199
20	46	75.286121	75.286121	75.286121
20	47	74.000000	74.000000	74.000000
20	48	53.150729	53.150729	53.150729
20	49	5.000000	5.000000	5.000000
20	50	2.000000	2.000000	2.000000
20	51	39.051248	39.051248	39.051248
20	52	16.401219	16.401219	16.401219
20	53	26.248809	26.248809	26.248809
20	54	45.650849	45.650849	45.650849
20	55	51.662365	51.662365	51.662365
20	56	51.419841	51.419841	51.419841
20	57	26.248809	26.248809	26.248809
20	58	19.209373	19.209373	19.209373
20	59	27.000000	27.000000	27.000000
20	60	33.526109	33.526109	33.526109
20	61	56.824291	56.824291	56.824291
20	62	55.081757	55.081757	55.081757
20	63	33.970576	33.970576	33.970576
20	64	25.079872	25.079872	25.079872
20	65	20.223748	20.223748	20.223748
20	66	30.805844	30.805844	30.805844
20	67	27.018512	27.018512	27.018512
20	68	38.832976	38.832976	38.832976
20	69	50.039984	50.039984	50.039984
20	70	43.416587	43.416587	43.416587

20	71	59.413803	59.413803	59.413803
20	72	50.537115	50.537115	50.537115
20	73	58.872744	58.872744	58.872744
20	74	64.031242	64.031242	64.031242
20	75	24.166092	24.166092	24.166092
20	76	37.336309	37.336309	37.336309
20	77	18.110770	18.110770	18.110770
20	78	20.248457	20.248457	20.248457
20	79	57.201399	57.201399	57.201399
20	80	68.264193	68.264193	68.264193
20	81	37.336309	37.336309	37.336309
20	82	48.507731	48.507731	48.507731
20	83	36.249138	36.249138	36.249138
20	84	21.587033	21.587033	21.587033
20	85	24.207437	24.207437	24.207437
20	86	24.698178	24.698178	24.698178
20	87	25.238859	25.238859	25.238859
20	88	33.105891	33.105891	33.105891
20	89	51.264022	51.264022	51.264022
20	90	25.495098	25.495098	25.495098
20	91	37.336309	37.336309	37.336309
20	92	32.756679	32.756679	32.756679
20	93	34.785054	34.785054	34.785054
20	94	46.097722	46.097722	46.097722
20	95	40.853396	40.853396	40.853396
20	96	30.413813	30.413813	30.413813
20	97	45.880279	45.880279	45.880279
20	98	38.832976	38.832976	38.832976
20	99	44.944410	44.944410	44.944410
20	100	29.681644	29.681644	29.681644
20	101	58.051701	58.051701	58.051701
21	1	35.057096	35.057096	35.057096
21	2	72.034714	72.034714	72.034714
21	3	63.245553	63.245553	63.245553
21	4	72.801099	72.801099	72.801099
21	5	68.622154	68.622154	68.622154
21	6	73.375745	73.375745	73.375745
21	7	64.621978	64.621978	64.621978
21	8	65.795137	65.795137	65.795137
21	9	70.384657	70.384657	70.384657
21	10	37.735925	37.735925	37.735925
21	11	40.607881	40.607881	40.607881
21	12	42.201896	42.201896	42.201896
21	13	45.343136	45.343136	45.343136
21	14	42.059482	42.059482	42.059482
21	15	47.634021	47.634021	47.634021
21	16	47.169906	47.169906	47.169906
21	17	48.877398	48.877398	48.877398
21	18	51.613952	51.613952	51.613952
21	19	10.198039	10.198039	10.198039
21	20	5.000000	5.000000	5.000000
21	22	10.198039	10.198039	10.198039
21	23	2.000000	2.000000	2.000000
21	24	10.770330	10.770330	10.770330
21	25	4.000000	4.000000	4.000000
21	26	12.206556	12.206556	12.206556
21	27	55.081757	55.081757	55.081757
21	28	56.648036	56.648036	56.648036
21	29	52.201533	52.201533	52.201533
21	30	52.000000	52.000000	52.000000
21	31	48.383882	48.383882	48.383882
21	32	50.159745	50.159745	50.159745
21	33	47.434165	47.434165	47.434165

21	34	44.147480	44.147480	44.147480
21	35	47.423623	47.423623	47.423623
21	36	74.330344	74.330344	74.330344
21	37	73.681748	73.681748	73.681748
21	38	70.837843	70.837843	70.837843
21	39	68.007353	68.007353	68.007353
21	40	67.446275	67.446275	67.446275
21	41	72.277244	72.277244	72.277244
21	42	62.096699	62.096699	62.096699
21	43	66.287254	66.287254	66.287254
21	44	71.196910	71.196910	71.196910
21	45	68.249542	68.249542	68.249542
21	46	70.519501	70.519501	70.519501
21	47	69.289249	69.289249	69.289249
21	48	50.000000	50.000000	50.000000
21	49	10.000000	10.000000	10.000000
21	50	3.000000	3.000000	3.000000
21	51	36.055513	36.055513	36.055513
21	52	13.928388	13.928388	13.928388
21	53	22.671568	22.671568	22.671568
21	54	41.340053	41.340053	41.340053
21	55	46.840154	46.840154	46.840154
21	56	46.572524	46.572524	46.572524
21	57	21.540659	21.540659	21.540659
21	58	15.620499	15.620499	15.620499
21	59	27.459060	27.459060	27.459060
21	60	32.388269	32.388269	32.388269
21	61	52.478567	52.478567	52.478567
21	62	50.089919	50.089919	50.089919
21	63	30.479501	30.479501	30.479501
21	64	23.537205	23.537205	23.537205
21	65	15.297059	15.297059	15.297059
21	66	25.961510	25.961510	25.961510
21	67	22.022716	22.022716	22.022716
21	68	34.828150	34.828150	34.828150
21	69	45.044423	45.044423	45.044423
21	70	38.600518	38.600518	38.600518
21	71	54.451814	54.451814	54.451814
21	72	46.141088	46.141088	46.141088
21	73	54.230987	54.230987	54.230987
21	74	60.207973	60.207973	60.207973
21	75	22.561028	22.561028	22.561028
21	76	38.327536	38.327536	38.327536
21	77	18.248288	18.248288	18.248288
21	78	22.472205	22.472205	22.472205
21	79	53.263496	53.263496	53.263496
21	80	64.070274	64.070274	64.070274
21	81	32.388269	32.388269	32.388269
21	82	43.566042	43.566042	43.566042
21	83	31.764760	31.764760	31.764760
21	84	16.763055	16.763055	16.763055
21	85	20.518285	20.518285	20.518285
21	86	22.472205	22.472205	22.472205
21	87	22.847319	22.847319	22.847319
21	88	31.320920	31.320920	31.320920
21	89	46.615448	46.615448	46.615448
21	90	26.925824	26.925824	26.925824
21	91	32.388269	32.388269	32.388269
21	92	27.892651	27.892651	27.892651
21	93	30.083218	30.083218	30.083218
21	94	41.593269	41.593269	41.593269
21	95	36.249138	36.249138	36.249138
21	96	26.076810	26.076810	26.076810

21	97	41.109610	41.109610	41.109610
21	98	38.118237	38.118237	38.118237
21	99	40.311289	40.311289	40.311289
21	100	25.612497	25.612497	25.612497
21	101	53.150729	53.150729	53.150729
22	1	45.000000	45.000000	45.000000
22	2	81.394103	81.394103	81.394103
22	3	72.277244	72.277244	72.277244
22	4	82.000000	82.000000	82.000000
22	5	77.620873	77.620873	77.620873
22	6	82.462113	82.462113	82.462113
22	7	73.375745	73.375745	73.375745
22	8	74.330344	74.330344	74.330344
22	9	79.056942	79.056942	79.056942
22	10	42.426407	42.426407	42.426407
22	11	46.097722	46.097722	46.097722
22	12	47.423623	47.423623	47.423623
22	13	51.224994	51.224994	51.224994
22	14	46.097722	46.097722	46.097722
22	15	53.150729	53.150729	53.150729
22	16	51.662365	51.662365	51.662365
22	17	53.150729	53.150729	53.150729
22	18	56.568542	56.568542	56.568542
22	19	4.000000	4.000000	4.000000
22	20	5.385165	5.385165	5.385165
22	21	10.198039	10.198039	10.198039
22	23	10.000000	10.000000	10.000000
22	24	2.000000	2.000000	2.000000
22	25	10.198039	10.198039	10.198039
22	26	5.000000	5.000000	5.000000
22	27	60.415230	60.415230	60.415230
22	28	62.649820	62.649820	62.649820
22	29	57.697487	57.697487	57.697487
22	30	58.309519	58.309519	58.309519
22	31	54.120237	54.120237	54.120237
22	32	56.603887	56.603887	56.603887
22	33	53.235327	53.235327	53.235327
22	34	49.244289	49.244289	49.244289
22	35	54.083269	54.083269	54.083269
22	36	84.433406	84.433406	84.433406
22	37	83.815273	83.815273	83.815273
22	38	80.956779	80.956779	80.956779
22	39	78.160092	78.160092	78.160092
22	40	77.620873	77.620873	77.620873
22	41	82.462113	82.462113	82.462113
22	42	72.277244	72.277244	72.277244
22	43	76.485293	76.485293	76.485293
22	44	81.394103	81.394103	81.394103
22	45	78.447435	78.447435	78.447435
22	46	79.555012	79.555012	79.555012
22	47	78.160092	78.160092	78.160092
22	48	55.172457	55.172457	55.172457
22	49	2.000000	2.000000	2.000000
22	50	7.280110	7.280110	7.280110
22	51	43.863424	43.863424	43.863424
22	52	21.213203	21.213203	21.213203
22	53	29.154759	29.154759	29.154759
22	54	49.244289	49.244289	49.244289
22	55	57.008771	57.008771	57.008771
22	56	55.901699	55.901699	55.901699
22	57	31.622777	31.622777	31.622777
22	58	22.360680	22.360680	22.360680
22	59	25.495098	25.495098	25.495098

22	60	33.541020	33.541020	33.541020
22	61	60.415230	60.415230	60.415230
22	62	60.207973	60.207973	60.207973
22	63	39.051248	39.051248	39.051248
22	64	29.154759	29.154759	29.154759
22	65	25.495098	25.495098	25.495098
22	66	35.355339	35.355339	35.355339
22	67	32.015621	32.015621	32.015621
22	68	44.102154	44.102154	44.102154
22	69	55.000000	55.000000	55.000000
22	70	47.853944	47.853944	47.853944
22	71	64.195015	64.195015	64.195015
22	72	55.901699	55.901699	55.901699
22	73	64.257295	64.257295	64.257295
22	74	66.850580	66.850580	66.850580
22	75	25.000000	25.000000	25.000000
22	76	35.000000	35.000000	35.000000
22	77	21.189620	21.189620	21.189620
22	78	17.117243	17.117243	17.117243
22	79	60.207973	60.207973	60.207973
22	80	71.589105	71.589105	71.589105
22	81	42.579338	42.579338	42.579338
22	82	53.758720	53.758720	53.758720
22	83	40.162171	40.162171	40.162171
22	84	26.172505	26.172505	26.172505
22	85	29.410882	29.410882	29.410882
22	86	29.206164	29.206164	29.206164
22	87	26.870058	26.870058	26.870058
22	88	33.837849	33.837849	33.837849
22	89	55.362442	55.362442	55.362442
22	90	27.000000	27.000000	27.000000
22	91	42.107007	42.107007	42.107007
22	92	38.078866	38.078866	38.078866
22	93	40.162171	40.162171	40.162171
22	94	51.478151	51.478151	51.478151
22	95	46.238512	46.238512	46.238512
22	96	35.777088	35.777088	35.777088
22	97	51.244512	51.244512	51.244512
22	98	38.275318	38.275318	38.275318
22	99	49.040799	49.040799	49.040799
22	100	33.105891	33.105891	33.105891
22	101	62.649820	62.649820	62.649820
23	1	35.000000	35.000000	35.000000
23	2	71.589105	71.589105	71.589105
23	3	62.641839	62.641839	62.641839
23	4	72.277244	72.277244	72.277244
23	5	68.007353	68.007353	68.007353
23	6	72.801099	72.801099	72.801099
23	7	63.906181	63.906181	63.906181
23	8	65.000000	65.000000	65.000000
23	9	69.641941	69.641941	69.641941
23	10	36.055513	36.055513	36.055513
23	11	39.051248	39.051248	39.051248
23	12	40.607881	40.607881	40.607881
23	13	43.863424	43.863424	43.863424
23	14	40.311289	40.311289	40.311289
23	15	46.097722	46.097722	46.097722
23	16	45.486262	45.486262	45.486262
23	17	47.169906	47.169906	47.169906
23	18	50.000000	50.000000	50.000000
23	19	10.770330	10.770330	10.770330
23	20	5.385165	5.385165	5.385165
23	21	2.000000	2.000000	2.000000

23	22	10.000000	10.000000	10.000000
23	24	10.198039	10.198039	10.198039
23	25	2.000000	2.000000	2.000000
23	26	11.180340	11.180340	11.180340
23	27	57.008771	57.008771	57.008771
23	28	58.523500	58.523500	58.523500
23	29	54.120237	54.120237	54.120237
23	30	53.851648	53.851648	53.851648
23	31	50.289164	50.289164	50.289164
23	32	52.000000	52.000000	52.000000
23	33	49.335586	49.335586	49.335586
23	34	46.097722	46.097722	46.097722
23	35	49.244289	49.244289	49.244289
23	36	75.026662	75.026662	75.026662
23	37	74.330344	74.330344	74.330344
23	38	71.512237	71.512237	71.512237
23	39	68.622154	68.622154	68.622154
23	40	68.007353	68.007353	68.007353
23	41	72.801099	72.801099	72.801099
23	42	62.641839	62.641839	62.641839
23	43	66.708320	66.708320	66.708320
23	44	71.589105	71.589105	71.589105
23	45	68.658576	68.658576	68.658576
23	46	69.921384	69.921384	69.921384
23	47	68.622154	68.622154	68.622154
23	48	48.414874	48.414874	48.414874
23	49	10.198039	10.198039	10.198039
23	50	3.605551	3.605551	3.605551
23	51	37.735925	37.735925	37.735925
23	52	15.811388	15.811388	15.811388
23	53	21.213203	21.213203	21.213203
23	54	40.311289	40.311289	40.311289
23	55	47.434165	47.434165	47.434165
23	56	46.097722	46.097722	46.097722
23	57	22.360680	22.360680	22.360680
23	58	14.142136	14.142136	14.142136
23	59	25.495098	25.495098	25.495098
23	60	30.413813	30.413813	30.413813
23	61	51.478151	51.478151	51.478151
23	62	50.249378	50.249378	50.249378
23	63	32.015621	32.015621	32.015621
23	64	25.495098	25.495098	25.495098
23	65	15.811388	15.811388	15.811388
23	66	25.495098	25.495098	25.495098
23	67	22.022716	22.022716	22.022716
23	68	36.124784	36.124784	36.124784
23	69	45.000000	45.000000	45.000000
23	70	38.078866	38.078866	38.078866
23	71	54.230987	54.230987	54.230987
23	72	47.169906	47.169906	47.169906
23	73	55.036352	55.036352	55.036352
23	74	58.898217	58.898217	58.898217
23	75	20.615528	20.615528	20.615528
23	76	36.400549	36.400549	36.400549
23	77	20.223748	20.223748	20.223748
23	78	20.808652	20.808652	20.808652
23	79	52.009614	52.009614	52.009614
23	80	62.968246	62.968246	62.968246
23	81	32.756679	32.756679	32.756679
23	82	43.931765	43.931765	43.931765
23	83	30.870698	30.870698	30.870698
23	84	16.278821	16.278821	16.278821
23	85	22.022716	22.022716	22.022716

23	86	24.351591	24.351591	24.351591
23	87	21.023796	21.023796	21.023796
23	88	29.410882	29.410882	29.410882
23	89	45.880279	45.880279	45.880279
23	90	28.792360	28.792360	28.792360
23	91	32.140317	32.140317	32.140317
23	92	28.460499	28.460499	28.460499
23	93	30.870698	30.870698	30.870698
23	94	42.544095	42.544095	42.544095
23	95	37.121422	37.121422	37.121422
23	96	27.202941	27.202941	27.202941
23	97	41.785165	41.785165	41.785165
23	98	36.124784	36.124784	36.124784
23	99	39.560081	39.560081	39.560081
23	100	24.413111	24.413111	24.413111
23	101	52.773099	52.773099	52.773099
24	1	45.044423	45.044423	45.044423
24	2	81.049368	81.049368	81.049368
24	3	71.805292	71.805292	71.805292
24	4	81.584312	81.584312	81.584312
24	5	77.129761	77.129761	77.129761
24	6	82.000000	82.000000	82.000000
24	7	72.801099	72.801099	72.801099
24	8	73.681748	73.681748	73.681748
24	9	78.447435	78.447435	78.447435
24	10	41.036569	41.036569	41.036569
24	11	44.821870	44.821870	44.821870
24	12	46.097722	46.097722	46.097722
24	13	50.000000	50.000000	50.000000
24	14	44.598206	44.598206	44.598206
24	15	51.855569	51.855569	51.855569
24	16	50.209561	50.209561	50.209561
24	17	51.662365	51.662365	51.662365
24	18	55.172457	55.172457	55.172457
24	19	6.000000	6.000000	6.000000
24	20	6.403124	6.403124	6.403124
24	21	10.770330	10.770330	10.770330
24	22	2.000000	2.000000	2.000000
24	23	10.198039	10.198039	10.198039
24	25	10.000000	10.000000	10.000000
24	26	3.000000	3.000000	3.000000
24	27	62.241465	62.241465	62.241465
24	28	64.412732	64.412732	64.412732
24	29	59.506302	59.506302	59.506302
24	30	60.033324	60.033324	60.033324
24	31	55.901699	55.901699	55.901699
24	32	58.309519	58.309519	58.309519
24	33	55.009090	55.009090	55.009090
24	34	51.078371	51.078371	51.078371
24	35	55.758407	55.758407	55.758407
24	36	85.094066	85.094066	85.094066
24	37	84.433406	84.433406	84.433406
24	38	81.596569	81.596569	81.596569
24	39	78.746428	78.746428	78.746428
24	40	78.160092	78.160092	78.160092
24	41	82.969874	82.969874	82.969874
24	42	72.801099	72.801099	72.801099
24	43	76.902536	76.902536	76.902536
24	44	81.786307	81.786307	81.786307
24	45	78.854296	78.854296	78.854296
24	46	79.075913	79.075913	79.075913
24	47	77.620873	77.620873	77.620873
24	48	53.814496	53.814496	53.814496

24	49	4.000000	4.000000	4.000000
24	50	8.062258	8.062258	8.062258
24	51	45.343136	45.343136	45.343136
24	52	22.671568	22.671568	22.671568
24	53	28.178006	28.178006	28.178006
24	54	48.466483	48.466483	48.466483
24	55	57.567352	57.567352	57.567352
24	56	55.578773	55.578773	55.578773
24	57	32.310989	32.310989	32.310989
24	58	21.540659	21.540659	21.540659
24	59	23.537205	23.537205	23.537205
24	60	31.764760	31.764760	31.764760
24	61	59.615434	59.615434	59.615434
24	62	60.406953	60.406953	60.406953
24	63	40.360872	40.360872	40.360872
24	64	30.886890	30.886890	30.886890
24	65	25.961510	25.961510	25.961510
24	66	35.128336	35.128336	35.128336
24	67	32.140317	32.140317	32.140317
24	68	45.221676	45.221676	45.221676
24	69	55.036352	55.036352	55.036352
24	70	47.518417	47.518417	47.518417
24	71	64.070274	64.070274	64.070274
24	72	56.824291	56.824291	56.824291
24	73	65.000000	65.000000	65.000000
24	74	65.734314	65.734314	65.734314
24	75	23.430749	23.430749	23.430749
24	76	33.000000	33.000000	33.000000
24	77	23.086793	23.086793	23.086793
24	78	15.132746	15.132746	15.132746
24	79	59.169249	59.169249	59.169249
24	80	70.661163	70.661163	70.661163
24	81	42.953463	42.953463	42.953463
24	82	54.129474	54.129474	54.129474
24	83	39.560081	39.560081	39.560081
24	84	26.019224	26.019224	26.019224
24	85	30.610456	30.610456	30.610456
24	86	30.805844	30.805844	30.805844
24	87	25.495098	25.495098	25.495098
24	88	32.202484	32.202484	32.202484
24	89	54.817880	54.817880	54.817880
24	90	29.000000	29.000000	29.000000
24	91	42.011903	42.011903	42.011903
24	92	38.600518	38.600518	38.600518
24	93	40.853396	40.853396	40.853396
24	94	52.325902	52.325902	52.325902
24	95	47.010637	47.010637	47.010637
24	96	36.715120	36.715120	36.715120
24	97	51.865210	51.865210	51.865210
24	98	36.400549	36.400549	36.400549
24	99	48.507731	48.507731	48.507731
24	100	32.310989	32.310989	32.310989
24	101	62.393910	62.393910	62.393910
25	1	35.057096	35.057096	35.057096
25	2	71.196910	71.196910	71.196910
25	3	62.096699	62.096699	62.096699
25	4	71.805292	71.805292	71.805292
25	5	67.446275	67.446275	67.446275
25	6	72.277244	72.277244	72.277244
25	7	63.245553	63.245553	63.245553
25	8	64.257295	64.257295	64.257295
25	9	68.949257	68.949257	68.949257
25	10	34.409301	34.409301	34.409301

25	11	37.536649	37.536649	37.536649
25	12	39.051248	39.051248	39.051248
25	13	42.426407	42.426407	42.426407
25	14	38.587563	38.587563	38.587563
25	15	44.598206	44.598206	44.598206
25	16	43.829214	43.829214	43.829214
25	17	45.486262	45.486262	45.486262
25	18	48.414874	48.414874	48.414874
25	19	11.661904	11.661904	11.661904
25	20	6.403124	6.403124	6.403124
25	21	4.000000	4.000000	4.000000
25	22	10.198039	10.198039	10.198039
25	23	2.000000	2.000000	2.000000
25	24	10.000000	10.000000	10.000000
25	26	10.440307	10.440307	10.440307
25	27	58.940648	58.940648	58.940648
25	28	60.406953	60.406953	60.406953
25	29	56.044625	56.044625	56.044625
25	30	55.713553	55.713553	55.713553
25	31	52.201533	52.201533	52.201533
25	32	53.851648	53.851648	53.851648
25	33	51.244512	51.244512	51.244512
25	34	48.052055	48.052055	48.052055
25	35	51.078371	51.078371	51.078371
25	36	75.769387	75.769387	75.769387
25	37	75.026662	75.026662	75.026662
25	38	72.235725	72.235725	72.235725
25	39	69.289249	69.289249	69.289249
25	40	68.622154	68.622154	68.622154
25	41	73.375745	73.375745	73.375745
25	42	63.245553	63.245553	63.245553
25	43	67.186308	67.186308	67.186308
25	44	72.034714	72.034714	72.034714
25	45	69.123079	69.123079	69.123079
25	46	69.375788	69.375788	69.375788
25	47	68.007353	68.007353	68.007353
25	48	46.861498	46.861498	46.861498
25	49	10.770330	10.770330	10.770330
25	50	5.000000	5.000000	5.000000
25	51	39.446166	39.446166	39.446166
25	52	17.720045	17.720045	17.720045
25	53	19.849433	19.849433	19.849433
25	54	39.357337	39.357337	39.357337
25	55	48.104054	48.104054	48.104054
25	56	45.705580	45.705580	45.705580
25	57	23.323808	23.323808	23.323808
25	58	12.806248	12.806248	12.806248
25	59	23.537205	23.537205	23.537205
25	60	28.442925	28.442925	28.442925
25	61	50.537115	50.537115	50.537115
25	62	50.487622	50.487622	50.487622
25	63	33.600595	33.600595	33.600595
25	64	27.459060	27.459060	27.459060
25	65	16.552945	16.552945	16.552945
25	66	25.179357	25.179357	25.179357
25	67	22.203603	22.203603	22.203603
25	68	37.483330	37.483330	37.483330
25	69	45.044423	45.044423	45.044423
25	70	37.656341	37.656341	37.656341
25	71	54.083269	54.083269	54.083269
25	72	48.259714	48.259714	48.259714
25	73	55.901699	55.901699	55.901699
25	74	57.628118	57.628118	57.628118

25	75	18.681542	18.681542	18.681542
25	76	34.481879	34.481879	34.481879
25	77	22.203603	22.203603	22.203603
25	78	19.209373	19.209373	19.209373
25	79	50.803543	50.803543	50.803543
25	80	61.911227	61.911227	61.911227
25	81	33.241540	33.241540	33.241540
25	82	44.384682	44.384682	44.384682
25	83	30.083218	30.083218	30.083218
25	84	16.031220	16.031220	16.031220
25	85	23.600847	23.600847	23.600847
25	86	26.248809	26.248809	26.248809
25	87	19.235384	19.235384	19.235384
25	88	27.513633	27.513633	27.513633
25	89	45.221676	45.221676	45.221676
25	90	30.675723	30.675723	30.675723
25	91	32.015621	32.015621	32.015621
25	92	29.154759	29.154759	29.154759
25	93	31.764760	31.764760	31.764760
25	94	43.566042	43.566042	43.566042
25	95	38.078866	38.078866	38.078866
25	96	28.425341	28.425341	28.425341
25	97	42.544095	42.544095	42.544095
25	98	34.132096	34.132096	34.132096
25	99	38.897301	38.897301	38.897301
25	100	23.323808	23.323808	23.323808
25	101	52.469038	52.469038	52.469038
26	1	45.276926	45.276926	45.276926
26	2	80.622577	80.622577	80.622577
26	3	71.196910	71.196910	71.196910
26	4	81.049368	81.049368	81.049368
26	5	76.485293	76.485293	76.485293
26	6	81.394103	81.394103	81.394103
26	7	72.034714	72.034714	72.034714
26	8	72.801099	72.801099	72.801099
26	9	77.620873	77.620873	77.620873
26	10	39.051248	39.051248	39.051248
26	11	43.011626	43.011626	43.011626
26	12	44.204072	44.204072	44.204072
26	13	48.259714	48.259714	48.259714
26	14	42.426407	42.426407	42.426407
26	15	50.000000	50.000000	50.000000
26	16	48.104054	48.104054	48.104054
26	17	49.497475	49.497475	49.497475
26	18	53.150729	53.150729	53.150729
26	19	9.000000	9.000000	9.000000
26	20	8.602325	8.602325	8.602325
26	21	12.206556	12.206556	12.206556
26	22	5.000000	5.000000	5.000000
26	23	11.180340	11.180340	11.180340
26	24	3.000000	3.000000	3.000000
26	25	10.440307	10.440307	10.440307
26	27	65.000000	65.000000	65.000000
26	28	67.082039	67.082039	67.082039
26	29	62.241465	62.241465	62.241465
26	30	62.649820	62.649820	62.649820
26	31	58.600341	58.600341	58.600341
26	32	60.901560	60.901560	60.901560
26	33	57.697487	57.697487	57.697487
26	34	53.851648	53.851648	53.851648
26	35	58.309519	58.309519	58.309519
26	36	86.162637	86.162637	86.162637
26	37	85.440037	85.440037	85.440037

26	38	82.637764	82.637764	82.637764
26	39	79.711982	79.711982	79.711982
26	40	79.056942	79.056942	79.056942
26	41	83.815273	83.815273	83.815273
26	42	73.681748	73.681748	73.681748
26	43	77.620873	77.620873	77.620873
26	44	82.462113	82.462113	82.462113
26	45	79.555012	79.555012	79.555012
26	46	78.447435	78.447435	78.447435
26	47	76.902536	76.902536	76.902536
26	48	51.855569	51.855569	51.855569
26	49	7.000000	7.000000	7.000000
26	50	9.899495	9.899495	9.899495
26	51	47.634021	47.634021	47.634021
26	52	25.000000	25.000000	25.000000
26	53	26.925824	26.925824	26.925824
26	54	47.434165	47.434165	47.434165
26	55	58.523500	58.523500	58.523500
26	56	55.226805	55.226805	55.226805
26	57	33.541020	33.541020	33.541020
26	58	20.615528	20.615528	20.615528
26	59	20.615528	20.615528	20.615528
26	60	29.154759	29.154759	29.154759
26	61	58.523500	58.523500	58.523500
26	62	60.827625	60.827625	60.827625
26	63	42.426407	42.426407	42.426407
26	64	33.541020	33.541020	33.541020
26	65	26.925824	26.925824	26.925824
26	66	35.000000	35.000000	35.000000
26	67	32.557641	32.557641	32.557641
26	68	47.010637	47.010637	47.010637
26	69	55.226805	55.226805	55.226805
26	70	47.169906	47.169906	47.169906
26	71	64.000000	64.000000	64.000000
26	72	58.309519	58.309519	58.309519
26	73	66.211781	66.211781	66.211781
26	74	64.140471	64.140471	64.140471
26	75	21.213203	21.213203	21.213203
26	76	30.000000	30.000000	30.000000
26	77	25.961510	25.961510	25.961510
26	78	12.165525	12.165525	12.165525
26	79	57.706152	57.706152	57.706152
26	80	69.354164	69.354164	69.354164
26	81	43.680659	43.680659	43.680659
26	82	54.817880	54.817880	54.817880
26	83	38.832976	38.832976	38.832976
26	84	26.076810	26.076810	26.076810
26	85	32.557641	32.557641	32.557641
26	86	33.286634	33.286634	33.286634
26	87	23.600847	23.600847	23.600847
26	88	29.832868	29.832868	29.832868
26	89	54.129474	54.129474	54.129474
26	90	32.000000	32.000000	32.000000
26	91	42.047592	42.047592	42.047592
26	92	39.560081	39.560081	39.560081
26	93	42.047592	42.047592	42.047592
26	94	53.712196	53.712196	53.712196
26	95	48.301139	48.301139	48.301139
26	96	38.275318	38.275318	38.275318
26	97	52.924474	52.924474	52.924474
26	98	33.615473	33.615473	33.615473
26	99	47.853944	47.853944	47.853944
26	100	31.320920	31.320920	31.320920

26	101	62.128898	62.128898	62.128898
27	1	58.523500	58.523500	58.523500
27	2	89.022469	89.022469	89.022469
27	3	85.755466	85.755466	85.755466
27	4	91.400219	91.400219	91.400219
27	5	90.138782	90.138782	90.138782
27	6	93.005376	93.005376	93.005376
27	7	89.185201	89.185201	89.185201
27	8	91.787799	91.787799	91.787799
27	9	94.339811	94.339811	94.339811
27	10	85.146932	85.146932	85.146932
27	11	85.586214	85.586214	85.586214
27	12	87.572827	87.572827	87.572827
27	13	88.283634	88.283634	88.283634
27	14	90.138782	90.138782	90.138782
27	15	91.241438	91.241438	91.241438
27	16	93.536089	93.536089	93.536089
27	17	95.524866	95.524866	95.524866
27	18	96.176920	96.176920	96.176920
27	19	56.797887	56.797887	56.797887
27	20	56.648036	56.648036	56.648036
27	21	55.081757	55.081757	55.081757
27	22	60.415230	60.415230	60.415230
27	23	57.008771	57.008771	57.008771
27	24	62.241465	62.241465	62.241465
27	25	58.940648	58.940648	58.940648
27	26	65.000000	65.000000	65.000000
27	28	5.000000	5.000000	5.000000
27	29	3.000000	3.000000	3.000000
27	30	7.071068	7.071068	7.071068
27	31	7.000000	7.000000	7.000000
27	32	8.602325	8.602325	8.602325
27	33	8.000000	8.000000	8.000000
27	34	11.180340	11.180340	11.180340
27	35	11.180340	11.180340	11.180340
27	36	61.717096	61.717096	61.717096
27	37	62.649820	62.649820	62.649820
27	38	60.033324	60.033324	60.033324
27	39	59.908263	59.908263	59.908263
27	40	61.032778	61.032778	61.032778
27	41	65.192024	65.192024	65.192024
27	42	58.258047	58.258047	58.258047
27	43	64.031242	64.031242	64.031242
27	44	68.007353	68.007353	68.007353
27	45	65.604878	65.604878	65.604878
27	46	91.263355	91.263355	91.263355
27	47	91.809586	91.809586	91.809586
27	48	94.201911	94.201911	94.201911
27	49	58.600341	58.600341	58.600341
27	50	55.973208	55.973208	55.973208
27	51	23.537205	23.537205	23.537205
27	52	41.231056	41.231056	41.231056
27	53	70.000000	70.000000	70.000000
27	54	77.620873	77.620873	77.620873
27	55	50.000000	50.000000	50.000000
27	56	71.589105	71.589105	71.589105
27	57	45.276926	45.276926	45.276926
27	58	65.192024	65.192024	65.192024
27	59	82.462113	82.462113	82.462113
27	60	85.586214	85.586214	85.586214
27	61	85.440037	85.440037	85.440037
27	62	61.032778	61.032778	61.032778
27	63	30.413813	30.413813	30.413813

27	64	31.622777	31.622777	31.622777
27	65	50.000000	50.000000	50.000000
27	66	60.827625	60.827625	60.827625
27	67	54.451814	54.451814	54.451814
27	68	33.241540	33.241540	33.241540
27	69	62.649820	62.649820	62.649820
27	70	67.675697	67.675697	67.675697
27	71	71.561163	71.561163	71.561163
27	72	39.051248	39.051248	39.051248
27	73	47.423623	47.423623	47.423623
27	74	97.718985	97.718985	97.718985
27	75	75.663730	75.663730	75.663730
27	76	93.407708	93.407708	93.407708
27	77	39.357337	39.357337	39.357337
27	78	76.896034	76.896034	76.896034
27	79	90.801982	90.801982	90.801982
27	80	96.772930	96.772930	96.772930
27	81	50.921508	50.921508	50.921508
27	82	53.851648	53.851648	53.851648
27	83	69.231496	69.231496	69.231496
27	84	58.008620	58.008620	58.008620
27	85	38.013156	38.013156	38.013156
27	86	32.756679	32.756679	32.756679
27	87	74.242845	74.242845	74.242845
27	88	83.216585	83.216585	83.216585
27	89	76.321688	76.321688	76.321688
27	90	37.536649	37.536649	37.536649
27	91	60.440053	60.440053	60.440053
27	92	47.539457	47.539457	47.539457
27	93	43.965896	43.965896	43.965896
27	94	40.496913	40.496913	40.496913
27	95	42.047592	42.047592	42.047592
27	96	39.623226	39.623226	39.623226
27	97	46.647615	46.647615	46.647615
27	98	91.787799	91.787799	91.787799
27	99	72.422372	72.422372	72.422372
27	100	69.180922	69.180922	69.180922
27	101	73.925638	73.925638	73.925638
28	1	57.008771	57.008771	57.008771
28	2	86.023253	86.023253	86.023253
28	3	83.240615	83.240615	83.240615
28	4	88.481637	88.481637	88.481637
28	5	87.464278	87.464278	87.464278
28	6	90.138782	90.138782	90.138782
28	7	86.769810	86.769810	86.769810
28	8	89.442719	89.442719	89.442719
28	9	91.787799	91.787799	91.787799
28	10	85.000000	85.000000	85.000000
28	11	85.146932	85.146932	85.146932
28	12	87.143560	87.143560	87.143560
28	13	87.572827	87.572827	87.572827
28	14	90.000000	90.000000	90.000000
28	15	90.553851	90.553851	90.553851
28	16	93.134312	93.134312	93.134312
28	17	95.131488	95.131488	95.131488
28	18	95.524866	95.524866	95.524866
28	19	59.169249	59.169249	59.169249
28	20	58.600341	58.600341	58.600341
28	21	56.648036	56.648036	56.648036
28	22	62.649820	62.649820	62.649820
28	23	58.523500	58.523500	58.523500
28	24	64.412732	64.412732	64.412732
28	25	60.406953	60.406953	60.406953

28	26	67.082039	67.082039	67.082039
28	27	5.000000	5.000000	5.000000
28	29	5.830952	5.830952	5.830952
28	30	5.000000	5.000000	5.000000
28	31	8.602325	8.602325	8.602325
28	32	7.000000	7.000000	7.000000
28	33	9.433981	9.433981	9.433981
28	34	14.142136	14.142136	14.142136
28	35	10.000000	10.000000	10.000000
28	36	57.306195	57.306195	57.306195
28	37	58.309519	58.309519	58.309519
28	38	55.758407	55.758407	55.758407
28	39	55.803226	55.803226	55.803226
28	40	57.008771	57.008771	57.008771
28	41	61.032778	61.032778	61.032778
28	42	54.488531	54.488531	54.488531
28	43	60.207973	60.207973	60.207973
28	44	64.031242	64.031242	64.031242
28	45	61.717096	61.717096	61.717096
28	46	88.509886	88.509886	88.509886
28	47	89.185201	89.185201	89.185201
28	48	93.536089	93.536089	93.536089
28	49	60.901560	60.901560	60.901560
28	50	57.775427	57.775427	57.775427
28	51	23.000000	23.000000	23.000000
28	52	42.720019	42.720019	42.720019
28	53	70.178344	70.178344	70.178344
28	54	76.485293	76.485293	76.485293
28	55	47.169906	47.169906	47.169906
28	56	69.641941	69.641941	69.641941
28	57	45.000000	45.000000	45.000000
28	58	65.764732	65.764732	65.764732
28	59	83.815273	83.815273	83.815273
28	60	86.313383	86.313383	86.313383
28	61	83.815273	83.815273	83.815273
28	62	58.309519	58.309519	58.309519
28	63	30.000000	30.000000	30.000000
28	64	33.541020	33.541020	33.541020
28	65	50.249378	50.249378	50.249378
28	66	60.207973	60.207973	60.207973
28	67	54.037024	54.037024	54.037024
28	68	31.780497	31.780497	31.780497
28	69	60.415230	60.415230	60.415230
28	70	66.219333	66.219333	66.219333
28	71	68.963759	68.963759	68.963759
28	72	36.055513	36.055513	36.055513
28	73	43.863424	43.863424	43.863424
28	74	96.301610	96.301610	96.301610
28	75	76.485293	76.485293	76.485293
28	76	94.868330	94.868330	94.868330
28	77	41.880783	41.880783	41.880783
28	78	78.790862	78.790862	78.790862
28	79	89.498603	89.498603	89.498603
28	80	94.921020	94.921020	94.921020
28	81	49.477268	49.477268	49.477268
28	82	51.429563	51.429563	51.429563
28	83	68.468971	68.468971	68.468971
28	84	58.137767	58.137767	58.137767
28	85	38.470768	38.470768	38.470768
28	86	34.176015	34.176015	34.176015
28	87	74.813100	74.813100	74.813100
28	88	83.725743	83.725743	83.725743
28	89	74.632433	74.632433	74.632433

28	90	41.036569	41.036569	41.036569
28	91	59.228372	59.228372	59.228372
28	92	46.529560	46.529560	46.529560
28	93	42.755117	42.755117	42.755117
28	94	38.013156	38.013156	38.013156
28	95	40.162171	40.162171	40.162171
28	96	39.051248	39.051248	39.051248
28	97	44.283180	44.283180	44.283180
28	98	92.574294	92.574294	92.574294
28	99	71.063352	71.063352	71.063352
28	100	69.000000	69.000000	69.000000
28	101	71.554175	71.554175	71.554175
29	1	55.713553	55.713553	55.713553
29	2	86.683332	86.683332	86.683332
29	3	83.216585	83.216585	83.216585
29	4	89.022469	89.022469	89.022469
29	5	87.658428	87.658428	87.658428
29	6	90.603532	90.603532	90.603532
29	7	86.608314	86.608314	86.608314
29	8	89.185201	89.185201	89.185201
29	9	91.809586	91.809586	91.809586
29	10	82.152298	82.152298	82.152298
29	11	82.607506	82.607506	82.607506
29	12	84.593144	84.593144	84.593144
29	13	85.328776	85.328776	85.328776
29	14	87.143560	87.143560	87.143560
29	15	88.283634	88.283634	88.283634
29	16	90.553851	90.553851	90.553851
29	17	92.541882	92.541882	92.541882
29	18	93.214806	93.214806	93.214806
29	19	54.120237	54.120237	54.120237
29	20	53.851648	53.851648	53.851648
29	21	52.201533	52.201533	52.201533
29	22	57.697487	57.697487	57.697487
29	23	54.120237	54.120237	54.120237
29	24	59.506302	59.506302	59.506302
29	25	56.044625	56.044625	56.044625
29	26	62.241465	62.241465	62.241465
29	27	3.000000	3.000000	3.000000
29	28	5.830952	5.830952	5.830952
29	30	5.385165	5.385165	5.385165
29	31	4.000000	4.000000	4.000000
29	32	6.403124	6.403124	6.403124
29	33	5.000000	5.000000	5.000000
29	34	8.602325	8.602325	8.602325
29	35	8.602325	8.602325	8.602325
29	36	60.415230	60.415230	60.415230
29	37	61.269895	61.269895	61.269895
29	38	58.591808	58.591808	58.591808
29	39	58.309519	58.309519	58.309519
29	40	59.363288	59.363288	59.363288
29	41	63.631753	63.631753	63.631753
29	42	56.400355	56.400355	56.400355
29	43	62.201286	62.201286	62.201286
29	44	66.287254	66.287254	66.287254
29	45	63.820060	63.820060	63.820060
29	46	88.814413	88.814413	88.814413
29	47	89.308454	89.308454	89.308454
29	48	91.241438	91.241438	91.241438
29	49	55.901699	55.901699	55.901699
29	50	53.141321	53.141321	53.141321
29	51	20.615528	20.615528	20.615528
29	52	38.327536	38.327536	38.327536

29	53	67.000000	67.000000	67.000000
29	54	74.726167	74.726167	74.726167
29	55	47.634021	47.634021	47.634021
29	56	68.876701	68.876701	68.876701
29	57	42.296572	42.296572	42.296572
29	58	62.201286	62.201286	62.201286
29	59	79.555012	79.555012	79.555012
29	60	82.607506	82.607506	82.607506
29	61	82.637764	82.637764	82.637764
29	62	58.600341	58.600341	58.600341
29	63	27.459060	27.459060	27.459060
29	64	28.792360	28.792360	28.792360
29	65	47.000000	47.000000	47.000000
29	66	57.870545	57.870545	57.870545
29	67	51.478151	51.478151	51.478151
29	68	30.463092	30.463092	30.463092
29	69	60.033324	60.033324	60.033324
29	70	64.845971	64.845971	64.845971
29	71	69.065187	69.065187	69.065187
29	72	36.796739	36.796739	36.796739
29	73	45.453273	45.453273	45.453273
29	74	94.868330	94.868330	94.868330
29	75	72.691127	72.691127	72.691127
29	76	90.520716	90.520716	90.520716
29	77	36.715120	36.715120	36.715120
29	78	74.094534	74.094534	74.094534
29	79	87.931792	87.931792	87.931792
29	80	94.021274	94.021274	94.021274
29	81	48.104054	48.104054	48.104054
29	82	51.312766	51.312766	51.312766
29	83	66.287254	66.287254	66.287254
29	84	55.009090	55.009090	55.009090
29	85	35.014283	35.014283	35.014283
29	86	29.832868	29.832868	29.832868
29	87	71.253070	71.253070	71.253070
29	88	80.224684	80.224684	80.224684
29	89	73.539105	73.539105	73.539105
29	90	35.355339	35.355339	35.355339
29	91	57.567352	57.567352	57.567352
29	92	44.643029	44.643029	44.643029
29	93	41.109610	41.109610	41.109610
29	94	38.013156	38.013156	38.013156
29	95	39.357337	39.357337	39.357337
29	96	36.674242	36.674242	36.674242
29	97	44.102154	44.102154	44.102154
29	98	88.814413	88.814413	88.814413
29	99	69.570109	69.570109	69.570109
29	100	66.189123	66.189123	66.189123
29	101	71.344236	71.344236	71.344236
30	1	52.201533	52.201533	52.201533
30	2	82.006097	82.006097	82.006097
30	3	78.892332	78.892332	78.892332
30	4	84.403791	84.403791	84.403791
30	5	83.216585	83.216585	83.216585
30	6	86.023253	86.023253	86.023253
30	7	82.365041	82.365041	82.365041
30	8	85.000000	85.000000	85.000000
30	9	87.464278	87.464278	87.464278
30	10	80.000000	80.000000	80.000000
30	11	80.156098	80.156098	80.156098
30	12	82.152298	82.152298	82.152298
30	13	82.607506	82.607506	82.607506
30	14	85.000000	85.000000	85.000000

30	15	85.586214	85.586214	85.586214
30	16	88.141931	88.141931	88.141931
30	17	90.138782	90.138782	90.138782
30	18	90.553851	90.553851	90.553851
30	19	54.918121	54.918121	54.918121
30	20	54.120237	54.120237	54.120237
30	21	52.000000	52.000000	52.000000
30	22	58.309519	58.309519	58.309519
30	23	53.851648	53.851648	53.851648
30	24	60.033324	60.033324	60.033324
30	25	55.713553	55.713553	55.713553
30	26	62.649820	62.649820	62.649820
30	27	7.071068	7.071068	7.071068
30	28	5.000000	5.000000	5.000000
30	29	5.385165	5.385165	5.385165
30	31	5.385165	5.385165	5.385165
30	32	2.000000	2.000000	2.000000
30	33	5.830952	5.830952	5.830952
30	34	11.180340	11.180340	11.180340
30	35	5.000000	5.000000	5.000000
30	36	55.036352	55.036352	55.036352
30	37	55.901699	55.901699	55.901699
30	38	53.235327	53.235327	53.235327
30	39	53.000000	53.000000	53.000000
30	40	54.083269	54.083269	54.083269
30	41	58.309519	58.309519	58.309519
30	42	51.224994	51.224994	51.224994
30	43	57.008771	57.008771	57.008771
30	44	61.032778	61.032778	61.032778
30	45	58.600341	58.600341	58.600341
30	46	84.314886	84.314886	84.314886
30	47	84.905830	84.905830	84.905830
30	48	88.566359	88.566359	88.566359
30	49	56.603887	56.603887	56.603887
30	50	53.225934	53.225934	53.225934
30	51	18.000000	18.000000	18.000000
30	52	38.078866	38.078866	38.078866
30	53	65.192024	65.192024	65.192024
30	54	71.589105	71.589105	71.589105
30	55	43.011626	43.011626	43.011626
30	56	65.000000	65.000000	65.000000
30	57	40.000000	40.000000	40.000000
30	58	60.827625	60.827625	60.827625
30	59	79.056942	79.056942	79.056942
30	60	81.394103	81.394103	81.394103
30	61	79.056942	79.056942	79.056942
30	62	54.083269	54.083269	54.083269
30	63	25.000000	25.000000	25.000000
30	64	29.154759	29.154759	29.154759
30	65	45.276926	45.276926	45.276926
30	66	55.226805	55.226805	55.226805
30	67	49.040799	49.040799	49.040799
30	68	26.925824	26.925824	26.925824
30	69	55.901699	55.901699	55.901699
30	70	61.400326	61.400326	61.400326
30	71	64.660653	64.660653	64.660653
30	72	32.015621	32.015621	32.015621
30	73	40.360872	40.360872	40.360872
30	74	91.482239	91.482239	91.482239
30	75	71.589105	71.589105	71.589105
30	76	90.138782	90.138782	90.138782
30	77	37.802116	37.802116	37.802116
30	78	74.249579	74.249579	74.249579

30	79	84.646323	84.646323	84.646323
30	80	90.249654	90.249654	90.249654
30	81	44.643029	44.643029	44.643029
30	82	47.010637	47.010637	47.010637
30	83	63.505905	63.505905	63.505905
30	84	53.150729	53.150729	53.150729
30	85	33.541020	33.541020	33.541020
30	86	29.546573	29.546573	29.546573
30	87	69.871310	69.871310	69.871310
30	88	78.771822	78.771822	78.771822
30	89	69.892775	69.892775	69.892775
30	90	37.802116	37.802116	37.802116
30	91	54.341513	54.341513	54.341513
30	92	41.593269	41.593269	41.593269
30	93	37.854986	37.854986	37.854986
30	94	33.615473	33.615473	33.615473
30	95	35.468296	35.468296	35.468296
30	96	34.058773	34.058773	34.058773
30	97	39.824616	39.824616	39.824616
30	98	87.664132	87.664132	87.664132
30	99	66.219333	66.219333	66.219333
30	100	64.000000	64.000000	64.000000
30	101	67.119297	67.119297	67.119297
31	1	52.000000	52.000000	52.000000
31	2	83.630138	83.630138	83.630138
31	3	79.881162	79.881162	79.881162
31	4	85.912746	85.912746	85.912746
31	5	84.403791	84.403791	84.403791
31	6	87.458562	87.458562	87.458562
31	7	83.216585	83.216585	83.216585
31	8	85.755466	85.755466	85.755466
31	9	88.481637	88.481637	88.481637
31	10	78.160092	78.160092	78.160092
31	11	78.638413	78.638413	78.638413
31	12	80.622577	80.622577	80.622577
31	13	81.394103	81.394103	81.394103
31	14	83.150466	83.150466	83.150466
31	15	84.344532	84.344532	84.344532
31	16	86.579443	86.579443	86.579443
31	17	88.566359	88.566359	88.566359
31	18	89.269256	89.269256	89.269256
31	19	50.606324	50.606324	50.606324
31	20	50.159745	50.159745	50.159745
31	21	48.383882	48.383882	48.383882
31	22	54.120237	54.120237	54.120237
31	23	50.289164	50.289164	50.289164
31	24	55.901699	55.901699	55.901699
31	25	52.201533	52.201533	52.201533
31	26	58.600341	58.600341	58.600341
31	27	7.000000	7.000000	7.000000
31	28	8.602325	8.602325	8.602325
31	29	4.000000	4.000000	4.000000
31	30	5.385165	5.385165	5.385165
31	32	5.000000	5.000000	5.000000
31	33	1.000000	1.000000	1.000000
31	34	5.830952	5.830952	5.830952
31	35	5.830952	5.830952	5.830952
31	36	58.872744	58.872744	58.872744
31	37	59.615434	59.615434	59.615434
31	38	56.859476	56.859476	56.859476
31	39	56.356011	56.356011	56.356011
31	40	57.306195	57.306195	57.306195
31	41	61.717096	61.717096	61.717096

31	42	54.083269	54.083269	54.083269
31	43	59.908263	59.908263	59.908263
31	44	64.140471	64.140471	64.140471
31	45	61.587336	61.587336	61.587336
31	46	85.603738	85.603738	85.603738
31	47	86.023253	86.023253	86.023253
31	48	87.298339	87.298339	87.298339
31	49	52.354560	52.354560	52.354560
31	50	49.396356	49.396356	49.396356
31	51	16.763055	16.763055	16.763055
31	52	34.481879	34.481879	34.481879
31	53	63.000000	63.000000	63.000000
31	54	70.880181	70.880181	70.880181
31	55	44.598206	44.598206	44.598206
31	56	65.299311	65.299311	65.299311
31	57	38.327536	38.327536	38.327536
31	58	58.215118	58.215118	58.215118
31	59	75.690158	75.690158	75.690158
31	60	78.638413	78.638413	78.638413
31	61	78.924014	78.924014	78.924014
31	62	55.443665	55.443665	55.443665
31	63	23.537205	23.537205	23.537205
31	64	25.079872	25.079872	25.079872
31	65	43.000000	43.000000	43.000000
31	66	53.935146	53.935146	53.935146
31	67	47.518417	47.518417	47.518417
31	68	26.832816	26.832816	26.832816
31	69	56.603887	56.603887	56.603887
31	70	61.098281	61.098281	61.098281
31	71	65.802736	65.802736	65.802736
31	72	33.970576	33.970576	33.970576
31	73	43.011626	43.011626	43.011626
31	74	91.082380	91.082380	91.082380
31	75	68.731361	68.731361	68.731361
31	76	86.683332	86.683332	86.683332
31	77	33.286634	33.286634	33.286634
31	78	70.384657	70.384657	70.384657
31	79	84.118963	84.118963	84.118963
31	80	90.376988	90.376988	90.376988
31	81	44.384682	44.384682	44.384682
31	82	48.010416	48.010416	48.010416
31	83	62.369865	62.369865	62.369865
31	84	51.009803	51.009803	51.009803
31	85	31.016125	31.016125	31.016125
31	86	25.961510	25.961510	25.961510
31	87	67.268120	67.268120	67.268120
31	88	76.236474	76.236474	76.236474
31	89	69.856997	69.856997	69.856997
31	90	32.649655	32.649655	32.649655
31	91	53.758720	53.758720	53.758720
31	92	40.804412	40.804412	40.804412
31	93	37.336309	37.336309	37.336309
31	94	34.828150	34.828150	34.828150
31	95	35.846897	35.846897	35.846897
31	96	32.756679	32.756679	32.756679
31	97	40.804412	40.804412	40.804412
31	98	84.852814	84.852814	84.852814
31	99	65.787537	65.787537	65.787537
31	100	62.201286	62.201286	62.201286
31	101	67.955868	67.955868	67.955868
32	1	50.289164	50.289164	50.289164
32	2	80.430094	80.430094	80.430094
32	3	77.175126	77.175126	77.175126

32	4	82.800966	82.800966	82.800966
32	5	81.541401	81.541401	81.541401
32	6	84.403791	84.403791	84.403791
32	7	80.622577	80.622577	80.622577
32	8	83.240615	83.240615	83.240615
32	9	85.755466	85.755466	85.755466
32	10	78.000000	78.000000	78.000000
32	11	78.160092	78.160092	78.160092
32	12	80.156098	80.156098	80.156098
32	13	80.622577	80.622577	80.622577
32	14	83.000000	83.000000	83.000000
32	15	83.600239	83.600239	83.600239
32	16	86.145226	86.145226	86.145226
32	17	88.141931	88.141931	88.141931
32	18	88.566359	88.566359	88.566359
32	19	53.254108	53.254108	53.254108
32	20	52.354560	52.354560	52.354560
32	21	50.159745	50.159745	50.159745
32	22	56.603887	56.603887	56.603887
32	23	52.000000	52.000000	52.000000
32	24	58.309519	58.309519	58.309519
32	25	53.851648	53.851648	53.851648
32	26	60.901560	60.901560	60.901560
32	27	8.602325	8.602325	8.602325
32	28	7.000000	7.000000	7.000000
32	29	6.403124	6.403124	6.403124
32	30	2.000000	2.000000	2.000000
32	31	5.000000	5.000000	5.000000
32	33	5.099020	5.099020	5.099020
32	34	10.440307	10.440307	10.440307
32	35	3.000000	3.000000	3.000000
32	36	54.230987	54.230987	54.230987
32	37	55.036352	55.036352	55.036352
32	38	52.325902	52.325902	52.325902
32	39	51.971146	51.971146	51.971146
32	40	53.000000	53.000000	53.000000
32	41	57.306195	57.306195	57.306195
32	42	50.000000	50.000000	50.000000
32	43	55.803226	55.803226	55.803226
32	44	59.908263	59.908263	59.908263
32	45	57.428216	57.428216	57.428216
32	46	82.661962	82.661962	82.661962
32	47	83.216585	83.216585	83.216585
32	48	86.579443	86.579443	86.579443
32	49	54.918121	54.918121	54.918121
32	50	51.429563	51.429563	51.429563
32	51	16.000000	16.000000	16.000000
32	52	36.249138	36.249138	36.249138
32	53	63.198101	63.198101	63.198101
32	54	69.634761	69.634761	69.634761
32	55	41.400483	41.400483	41.400483
32	56	63.158531	63.158531	63.158531
32	57	38.000000	38.000000	38.000000
32	58	58.855756	58.855756	58.855756
32	59	77.162167	77.162167	77.162167
32	60	79.429214	79.429214	79.429214
32	61	77.162167	77.162167	77.162167
32	62	52.430907	52.430907	52.430907
32	63	23.000000	23.000000	23.000000
32	64	27.459060	27.459060	27.459060
32	65	43.289722	43.289722	43.289722
32	66	53.235327	53.235327	53.235327
32	67	47.042534	47.042534	47.042534

32	68	25.000000	25.000000	25.000000
32	69	54.120237	54.120237	54.120237
32	70	59.481089	59.481089	59.481089
32	71	62.968246	62.968246	62.968246
32	72	30.479501	30.479501	30.479501
32	73	39.051248	39.051248	39.051248
32	74	89.560036	89.560036	89.560036
32	75	69.634761	69.634761	69.634761
32	76	88.255311	88.255311	88.255311
32	77	36.235342	36.235342	36.235342
32	78	72.449983	72.449983	72.449983
32	79	82.710338	82.710338	82.710338
32	80	88.391176	88.391176	88.391176
32	81	42.720019	42.720019	42.720019
32	82	45.276926	45.276926	45.276926
32	83	61.522354	61.522354	61.522354
32	84	51.156622	51.156622	51.156622
32	85	31.575307	31.575307	31.575307
32	86	27.730849	27.730849	27.730849
32	87	67.896981	67.896981	67.896981
32	88	76.791927	76.791927	76.791927
32	89	68.007353	68.007353	68.007353
32	90	36.619667	36.619667	36.619667
32	91	52.392748	52.392748	52.392748
32	92	39.623226	39.623226	39.623226
32	93	35.902646	35.902646	35.902646
32	94	31.906112	31.906112	31.906112
32	95	33.615473	33.615473	33.615473
32	96	32.062439	32.062439	32.062439
32	97	38.078866	38.078866	38.078866
32	98	85.702975	85.702975	85.702975
32	99	64.288413	64.288413	64.288413
32	100	62.000000	62.000000	62.000000
32	101	65.368188	65.368188	65.368188
33	1	51.078371	51.078371	51.078371
33	2	82.879430	82.879430	82.879430
33	3	79.056942	79.056942	79.056942
33	4	85.146932	85.146932	85.146932
33	5	83.600239	83.600239	83.600239
33	6	86.683332	86.683332	86.683332
33	7	82.377181	82.377181	82.377181
33	8	84.905830	84.905830	84.905830
33	9	87.658428	87.658428	87.658428
33	10	77.162167	77.162167	77.162167
33	11	77.646635	77.646635	77.646635
33	12	79.630396	79.630396	79.630396
33	13	80.411442	80.411442	80.411442
33	14	82.152298	82.152298	82.152298
33	15	83.360662	83.360662	83.360662
33	16	85.586214	85.586214	85.586214
33	17	87.572827	87.572827	87.572827
33	18	88.283634	88.283634	88.283634
33	19	49.739320	49.739320	49.739320
33	20	49.244289	49.244289	49.244289
33	21	47.434165	47.434165	47.434165
33	22	53.235327	53.235327	53.235327
33	23	49.335586	49.335586	49.335586
33	24	55.009090	55.009090	55.009090
33	25	51.244512	51.244512	51.244512
33	26	57.697487	57.697487	57.697487
33	27	8.000000	8.000000	8.000000
33	28	9.433981	9.433981	9.433981
33	29	5.000000	5.000000	5.000000

33	30	5.830952	5.830952	5.830952
33	31	1.000000	1.000000	1.000000
33	32	5.099020	5.099020	5.099020
33	34	5.385165	5.385165	5.385165
33	35	5.385165	5.385165	5.385165
33	36	58.523500	58.523500	58.523500
33	37	59.236813	59.236813	59.236813
33	38	56.462377	56.462377	56.462377
33	39	55.901699	55.901699	55.901699
33	40	56.824291	56.824291	56.824291
33	41	61.269895	61.269895	61.269895
33	42	53.535035	53.535035	53.535035
33	43	59.363288	59.363288	59.363288
33	44	63.631753	63.631753	63.631753
33	45	61.057350	61.057350	61.057350
33	46	84.811556	84.811556	84.811556
33	47	85.211502	85.211502	85.211502
33	48	86.313383	86.313383	86.313383
33	49	51.478151	51.478151	51.478151
33	50	48.466483	48.466483	48.466483
33	51	15.811388	15.811388	15.811388
33	52	33.526109	33.526109	33.526109
33	53	62.000000	62.000000	62.000000
33	54	69.921384	69.921384	69.921384
33	55	43.863424	43.863424	43.863424
33	56	64.412732	64.412732	64.412732
33	57	37.336309	37.336309	37.336309
33	58	57.218878	57.218878	57.218878
33	59	74.726167	74.726167	74.726167
33	60	77.646635	77.646635	77.646635
33	61	78.000000	78.000000	78.000000
33	62	54.671748	54.671748	54.671748
33	63	22.561028	22.561028	22.561028
33	64	24.166092	24.166092	24.166092
33	65	42.000000	42.000000	42.000000
33	66	52.952809	52.952809	52.952809
33	67	46.529560	46.529560	46.529560
33	68	25.942244	25.942244	25.942244
33	69	55.758407	55.758407	55.758407
33	70	60.166436	60.166436	60.166436
33	71	65.000000	65.000000	65.000000
33	72	33.301652	33.301652	33.301652
33	73	42.438190	42.438190	42.438190
33	74	90.138782	90.138782	90.138782
33	75	67.742158	67.742158	67.742158
33	76	85.726309	85.726309	85.726309
33	77	32.449961	32.449961	32.449961
33	78	69.462220	69.462220	69.462220
33	79	83.168504	83.168504	83.168504
33	80	89.470666	89.470666	89.470666
33	81	43.462628	43.462628	43.462628
33	82	47.201695	47.201695	47.201695
33	83	61.392182	61.392182	61.392182
33	84	50.009999	50.009999	50.009999
33	85	30.016662	30.016662	30.016662
33	86	25.000000	25.000000	25.000000
33	87	66.272166	66.272166	66.272166
33	88	75.239617	75.239617	75.239617
33	89	68.942005	68.942005	68.942005
33	90	32.015621	32.015621	32.015621
33	91	52.810984	52.810984	52.810984
33	92	39.849718	39.849718	39.849718
33	93	36.400549	36.400549	36.400549

33	94	34.058773	34.058773	34.058773
33	95	34.985711	34.985711	34.985711
33	96	31.780497	31.780497	31.780497
33	97	40.000000	40.000000	40.000000
33	98	83.862983	83.862983	83.862983
33	99	64.845971	64.845971	64.845971
33	100	61.204575	61.204575	61.204575
33	101	67.119297	67.119297	67.119297
34	1	51.478151	51.478151	51.478151
34	2	84.852814	84.852814	84.852814
34	3	80.430094	80.430094	80.430094
34	4	87.000000	87.000000	87.000000
34	5	85.146932	85.146932	85.146932
34	6	88.459030	88.459030	88.459030
34	7	83.600239	83.600239	83.600239
34	8	86.023253	86.023253	86.023253
34	9	89.022469	89.022469	89.022469
34	10	75.663730	75.663730	75.663730
34	11	76.485293	76.485293	76.485293
34	12	78.447435	78.447435	78.447435
34	13	79.555012	79.555012	79.555012
34	14	80.622577	80.622577	80.622577
34	15	82.462113	82.462113	82.462113
34	16	84.344532	84.344532	84.344532
34	17	86.313383	86.313383	86.313383
34	18	87.321246	87.321246	87.321246
34	19	45.617979	45.617979	45.617979
34	20	45.541190	45.541190	45.541190
34	21	44.147480	44.147480	44.147480
34	22	49.244289	49.244289	49.244289
34	23	46.097722	46.097722	46.097722
34	24	51.078371	51.078371	51.078371
34	25	48.052055	48.052055	48.052055
34	26	53.851648	53.851648	53.851648
34	27	11.180340	11.180340	11.180340
34	28	14.142136	14.142136	14.142136
34	29	8.602325	8.602325	8.602325
34	30	11.180340	11.180340	11.180340
34	31	5.830952	5.830952	5.830952
34	32	10.440307	10.440307	10.440307
34	33	5.385165	5.385165	5.385165
34	35	10.000000	10.000000	10.000000
34	36	62.641839	62.641839	62.641839
34	37	63.245553	63.245553	63.245553
34	38	60.406953	60.406953	60.406953
34	39	59.615434	59.615434	59.615434
34	40	60.415230	60.415230	60.415230
34	41	65.000000	65.000000	65.000000
34	42	56.824291	56.824291	56.824291
34	43	62.649820	62.649820	62.649820
34	44	67.082039	67.082039	67.082039
34	45	64.412732	64.412732	64.412732
34	46	86.452299	86.452299	86.452299
34	47	86.683332	86.683332	86.683332
34	48	85.375641	85.375641	85.375641
34	49	47.423623	47.423623	47.423623
34	50	44.922155	44.922155	44.922155
34	51	16.401219	16.401219	16.401219
34	52	30.413813	30.413813	30.413813
34	53	60.207973	60.207973	60.207973
34	54	69.641941	69.641941	69.641941
34	55	46.097722	46.097722	46.097722
34	56	65.192024	65.192024	65.192024

34	57	36.400549	36.400549	36.400549
34	58	55.000000	55.000000	55.000000
34	59	71.589105	71.589105	71.589105
34	60	75.166482	75.166482	75.166482
34	61	78.262379	78.262379	78.262379
34	62	56.568542	56.568542	56.568542
34	63	22.360680	22.360680	22.360680
34	64	20.615528	20.615528	20.615528
34	65	40.311289	40.311289	40.311289
34	66	52.201533	52.201533	52.201533
34	67	45.607017	45.607017	45.607017
34	68	27.018512	27.018512	27.018512
34	69	57.008771	57.008771	57.008771
34	70	60.373835	60.373835	60.373835
34	71	66.603303	66.603303	66.603303
34	72	36.055513	36.055513	36.055513
34	73	45.650849	45.650849	45.650849
34	74	90.077744	90.077744	90.077744
34	75	65.192024	65.192024	65.192024
34	76	82.462113	82.462113	82.462113
34	77	28.178006	28.178006	28.178006
34	78	65.787537	65.787537	65.787537
34	79	83.006024	83.006024	83.006024
34	80	89.944427	89.944427	89.944427
34	81	43.908997	43.908997	43.908997
34	82	48.836462	48.836462	48.836462
34	83	60.728906	60.728906	60.728906
34	84	48.373546	48.373546	48.373546
34	85	28.284271	28.284271	28.284271
34	86	22.090722	22.090722	22.090722
34	87	64.007812	64.007812	64.007812
34	88	73.006849	73.006849	73.006849
34	89	69.354164	69.354164	69.354164
34	90	26.907248	26.907248	26.907248
34	91	52.801515	52.801515	52.801515
34	92	39.812058	39.812058	39.812058
34	93	36.715120	36.715120	36.715120
34	94	36.124784	36.124784	36.124784
34	95	36.235342	36.235342	36.235342
34	96	31.384710	31.384710	31.384710
34	97	41.725292	41.725292	41.725292
34	98	81.301906	81.301906	81.301906
34	99	64.884513	64.884513	64.884513
34	100	59.841457	59.841457	59.841457
34	101	68.410526	68.410526	68.410526
35	1	47.434165	47.434165	47.434165
35	2	78.102497	78.102497	78.102497
35	3	74.625733	74.625733	74.625733
35	4	80.430094	80.430094	80.430094
35	5	79.056942	79.056942	79.056942
35	6	82.006097	82.006097	82.006097
35	7	78.032045	78.032045	78.032045
35	8	80.622577	80.622577	80.622577
35	9	83.216585	83.216585	83.216585
35	10	75.000000	75.000000	75.000000
35	11	75.166482	75.166482	75.166482
35	12	77.162167	77.162167	77.162167
35	13	77.646635	77.646635	77.646635
35	14	80.000000	80.000000	80.000000
35	15	80.622577	80.622577	80.622577
35	16	83.150466	83.150466	83.150466
35	17	85.146932	85.146932	85.146932
35	18	85.586214	85.586214	85.586214

35	19	50.803543	50.803543	50.803543
35	20	49.739320	49.739320	49.739320
35	21	47.423623	47.423623	47.423623
35	22	54.083269	54.083269	54.083269
35	23	49.244289	49.244289	49.244289
35	24	55.758407	55.758407	55.758407
35	25	51.078371	51.078371	51.078371
35	26	58.309519	58.309519	58.309519
35	27	11.180340	11.180340	11.180340
35	28	10.000000	10.000000	10.000000
35	29	8.602325	8.602325	8.602325
35	30	5.000000	5.000000	5.000000
35	31	5.830952	5.830952	5.830952
35	32	3.000000	3.000000	3.000000
35	33	5.385165	5.385165	5.385165
35	34	10.000000	10.000000	10.000000
35	36	53.141321	53.141321	53.141321
35	37	53.851648	53.851648	53.851648
35	38	51.078371	51.078371	51.078371
35	39	50.537115	50.537115	50.537115
35	40	51.478151	51.478151	51.478151
35	41	55.901699	55.901699	55.901699
35	42	48.259714	48.259714	48.259714
35	43	54.083269	54.083269	54.083269
35	44	58.309519	58.309519	58.309519
35	45	55.758407	55.758407	55.758407
35	46	80.212219	80.212219	80.212219
35	47	80.709355	80.709355	80.709355
35	48	83.600239	83.600239	83.600239
35	49	52.430907	52.430907	52.430907
35	50	48.764741	48.764741	48.764741
35	51	13.000000	13.000000	13.000000
35	52	33.541020	33.541020	33.541020
35	53	60.207973	60.207973	60.207973
35	54	66.708320	66.708320	66.708320
35	55	39.051248	39.051248	39.051248
35	56	60.415230	60.415230	60.415230
35	57	35.000000	35.000000	35.000000
35	58	55.901699	55.901699	55.901699
35	59	74.330344	74.330344	74.330344
35	60	76.485293	76.485293	76.485293
35	61	74.330344	74.330344	74.330344
35	62	50.000000	50.000000	50.000000
35	63	20.000000	20.000000	20.000000
35	64	25.000000	25.000000	25.000000
35	65	40.311289	40.311289	40.311289
35	66	50.249378	50.249378	50.249378
35	67	44.045431	44.045431	44.045431
35	68	22.135944	22.135944	22.135944
35	69	51.478151	51.478151	51.478151
35	70	56.612719	56.612719	56.612719
35	71	60.464866	60.464866	60.464866
35	72	28.284271	28.284271	28.284271
35	73	37.202150	37.202150	37.202150
35	74	86.683332	86.683332	86.683332
35	75	66.708320	66.708320	66.708320
35	76	85.440037	85.440037	85.440037
35	77	33.970576	33.970576	33.970576
35	78	69.771054	69.771054	69.771054
35	79	79.812280	79.812280	79.812280
35	80	85.615419	85.615419	85.615419
35	81	39.849718	39.849718	39.849718
35	82	42.720019	42.720019	42.720019

35	83	58.549125	58.549125	58.549125
35	84	48.166378	48.166378	48.166378
35	85	28.635642	28.635642	28.635642
35	86	25.059928	25.059928	25.059928
35	87	64.938432	64.938432	64.938432
35	88	73.824115	73.824115	73.824115
35	89	65.192024	65.192024	65.192024
35	90	34.985711	34.985711	34.985711
35	91	49.477268	49.477268	49.477268
35	92	36.674242	36.674242	36.674242
35	93	32.984845	32.984845	32.984845
35	94	29.410882	29.410882	29.410882
35	95	30.870698	30.870698	30.870698
35	96	29.068884	29.068884	29.068884
35	97	35.510562	35.510562	35.510562
35	98	82.764727	82.764727	82.764727
35	99	61.400326	61.400326	61.400326
35	100	59.000000	59.000000	59.000000
35	101	62.769419	62.769419	62.769419
36	1	44.204072	44.204072	44.204072
36	2	42.000000	42.000000	42.000000
36	3	46.097722	46.097722	46.097722
36	4	45.000000	45.000000	45.000000
36	5	47.265209	47.265209	47.265209
36	6	47.000000	47.000000	47.000000
36	7	50.009999	50.009999	50.009999
36	8	52.952809	52.952809	52.952809
36	9	52.239832	52.239832	52.239832
36	10	75.822160	75.822160	75.822160
36	11	72.622311	72.622311	72.622311
36	12	74.202426	74.202426	74.202426
36	13	71.281134	71.281134	71.281134
36	14	79.649231	79.649231	79.649231
36	15	73.783467	73.783467	73.783467
36	16	79.056942	79.056942	79.056942
36	17	80.709355	80.709355	80.709355
36	18	78.032045	78.032045	78.032045
36	19	83.240615	83.240615	83.240615
36	20	79.056942	79.056942	79.056942
36	21	74.330344	74.330344	74.330344
36	22	84.433406	84.433406	84.433406
36	23	75.026662	75.026662	75.026662
36	24	85.094066	85.094066	85.094066
36	25	75.769387	75.769387	75.769387
36	26	86.162637	86.162637	86.162637
36	27	61.717096	61.717096	61.717096
36	28	57.306195	57.306195	57.306195
36	29	60.415230	60.415230	60.415230
36	30	55.036352	55.036352	55.036352
36	31	58.872744	58.872744	58.872744
36	32	54.230987	54.230987	54.230987
36	33	58.523500	58.523500	58.523500
36	34	62.641839	62.641839	62.641839
36	35	53.141321	53.141321	53.141321
36	37	2.000000	2.000000	2.000000
36	38	3.605551	3.605551	3.605551
36	39	7.071068	7.071068	7.071068
36	40	8.602325	8.602325	8.602325
36	41	7.000000	7.000000	7.000000
36	42	13.453624	13.453624	13.453624
36	43	13.000000	13.000000	13.000000
36	44	12.000000	12.000000	12.000000
36	45	12.369317	12.369317	12.369317

36	46	47.095647	47.095647	47.095647
36	47	49.254441	49.254441	49.254441
36	48	76.321688	76.321688	76.321688
36	49	83.815273	83.815273	83.815273
36	50	77.162167	77.162167	77.162167
36	51	50.249378	50.249378	50.249378
36	52	66.098411	66.098411	66.098411
36	53	69.202601	69.202601	69.202601
36	54	58.600341	58.600341	58.600341
36	55	27.730849	27.730849	27.730849
36	56	44.654227	44.654227	44.654227
36	57	52.810984	52.810984	52.810984
36	58	70.491134	70.491134	70.491134
36	59	91.263355	91.263355	91.263355
36	60	86.452299	86.452299	86.452299
36	61	57.697487	57.697487	57.697487
36	62	29.732137	29.732137	29.732137
36	63	50.039984	50.039984	50.039984
36	64	65.030762	65.030762	65.030762
36	65	59.236813	59.236813	59.236813
36	66	55.217751	55.217751	55.217751
36	67	54.589376	54.589376	54.589376
36	68	43.104524	43.104524	43.104524
36	69	36.796739	36.796739	36.796739
36	70	48.836462	48.836462	48.836462
36	71	35.777088	35.777088	35.777088
36	72	30.066593	30.066593	30.066593
36	73	20.396078	20.396078	20.396078
36	74	69.641941	69.641941	69.641941
36	75	80.212219	80.212219	80.212219
36	76	101.212647	101.212647	101.212647
36	77	73.334848	73.334848	73.334848
36	78	93.059121	93.059121	93.059121
36	79	65.741920	65.741920	65.741920
36	80	63.324561	63.324561	63.324561
36	81	42.941821	42.941821	42.941821
36	82	32.449961	32.449961	32.449961
36	83	58.000000	58.000000	58.000000
36	84	61.773781	61.773781	61.773781
36	85	56.885851	56.885851	56.885851
36	86	62.128898	62.128898	62.128898
36	87	76.400262	76.400262	76.400262
36	88	82.134037	82.134037	82.134037
36	89	50.774009	50.774009	50.774009
36	90	80.000000	80.000000	80.000000
36	91	48.414874	48.414874	48.414874
36	92	46.615448	46.615448	46.615448
36	93	44.271887	44.271887	44.271887
36	94	33.541020	33.541020	33.541020
36	95	38.327536	38.327536	38.327536
36	96	49.244289	49.244289	49.244289
36	97	33.241540	33.241540	33.241540
36	98	91.967386	91.967386	91.967386
36	99	52.630789	52.630789	52.630789
36	100	64.660653	64.660653	64.660653
36	101	40.249224	40.249224	40.249224
37	1	43.011626	43.011626	43.011626
37	2	40.000000	40.000000	40.000000
37	3	44.147480	44.147480	44.147480
37	4	43.000000	43.000000	43.000000
37	5	45.276926	45.276926	45.276926
37	6	45.000000	45.000000	45.000000
37	7	48.052055	48.052055	48.052055

37	8	50.990195	50.990195	50.990195
37	9	50.249378	50.249378	50.249378
37	10	74.330344	74.330344	74.330344
37	11	71.063352	71.063352	71.063352
37	12	72.622311	72.622311	72.622311
37	13	69.634761	69.634761	69.634761
37	14	78.102497	78.102497	78.102497
37	15	72.111026	72.111026	72.111026
37	16	77.420927	77.420927	77.420927
37	17	79.056942	79.056942	79.056942
37	18	76.321688	76.321688	76.321688
37	19	82.710338	82.710338	82.710338
37	20	78.447435	78.447435	78.447435
37	21	73.681748	73.681748	73.681748
37	22	83.815273	83.815273	83.815273
37	23	74.330344	74.330344	74.330344
37	24	84.433406	84.433406	84.433406
37	25	75.026662	75.026662	75.026662
37	26	85.440037	85.440037	85.440037
37	27	62.649820	62.649820	62.649820
37	28	58.309519	58.309519	58.309519
37	29	61.269895	61.269895	61.269895
37	30	55.901699	55.901699	55.901699
37	31	59.615434	59.615434	59.615434
37	32	55.036352	55.036352	55.036352
37	33	59.236813	59.236813	59.236813
37	34	63.245553	63.245553	63.245553
37	35	53.851648	53.851648	53.851648
37	36	2.000000	2.000000	2.000000
37	38	3.000000	3.000000	3.000000
37	39	5.830952	5.830952	5.830952
37	40	7.071068	7.071068	7.071068
37	41	5.000000	5.000000	5.000000
37	42	12.206556	12.206556	12.206556
37	43	11.180340	11.180340	11.180340
37	44	10.000000	10.000000	10.000000
37	45	10.440307	10.440307	10.440307
37	46	45.099889	45.099889	45.099889
37	47	47.265209	47.265209	47.265209
37	48	74.625733	74.625733	74.625733
37	49	83.240615	83.240615	83.240615
37	50	76.537572	76.537572	76.537572
37	51	50.487622	50.487622	50.487622
37	52	65.764732	65.764732	65.764732
37	53	68.007353	68.007353	68.007353
37	54	57.008771	57.008771	57.008771
37	55	26.925824	26.925824	26.925824
37	56	43.011626	43.011626	43.011626
37	57	52.201533	52.201533	52.201533
37	58	69.462220	69.462220	69.462220
37	59	90.138782	90.138782	90.138782
37	60	85.146932	85.146932	85.146932
37	61	55.901699	55.901699	55.901699
37	62	28.284271	28.284271	28.284271
37	63	50.000000	50.000000	50.000000
37	64	65.000000	65.000000	65.000000
37	65	58.523500	58.523500	58.523500
37	66	54.083269	54.083269	54.083269
37	67	53.665631	53.665631	53.665631
37	68	43.011626	43.011626	43.011626
37	69	35.355339	35.355339	35.355339
37	70	47.381431	47.381431	47.381431
37	71	34.000000	34.000000	34.000000

37	72	30.000000	30.000000	30.000000
37	73	20.099751	20.099751	20.099751
37	74	67.779053	67.779053	67.779053
37	75	79.056942	79.056942	79.056942
37	76	100.000000	100.000000	100.000000
37	77	73.171033	73.171033	73.171033
37	78	92.130342	92.130342	92.130342
37	79	63.953108	63.953108	63.953108
37	80	61.400326	61.400326	61.400326
37	81	42.047592	42.047592	42.047592
37	82	31.384710	31.384710	31.384710
37	83	56.639209	56.639209	56.639209
37	84	60.827625	60.827625	60.827625
37	85	56.568542	56.568542	56.568542
37	86	62.032250	62.032250	62.032250
37	87	75.213031	75.213031	75.213031
37	88	80.808415	80.808415	80.808415
37	89	49.091751	49.091751	49.091751
37	90	80.024996	80.024996	80.024996
37	91	47.201695	47.201695	47.201695
37	92	45.880279	45.880279	45.880279
37	93	43.680659	43.680659	43.680659
37	94	33.241540	33.241540	33.241540
37	95	37.854986	37.854986	37.854986
37	96	48.836462	48.836462	48.836462
37	97	32.572995	32.572995	32.572995
37	98	90.609050	90.609050	90.609050
37	99	51.088159	51.088159	51.088159
37	100	63.411355	63.411355	63.411355
37	101	38.470768	38.470768	38.470768
38	1	40.607881	40.607881	40.607881
38	2	40.112342	40.112342	40.112342
38	3	43.566042	43.566042	43.566042
38	4	43.104524	43.104524	43.104524
38	5	45.044423	45.044423	45.044423
38	6	45.099889	45.099889	45.099889
38	7	47.518417	47.518417	47.518417
38	8	50.487622	50.487622	50.487622
38	9	50.039984	50.039984	50.039984
38	10	72.346389	72.346389	72.346389
38	11	69.202601	69.202601	69.202601
38	12	70.802542	70.802542	70.802542
38	13	67.955868	67.955868	67.955868
38	14	76.216796	76.216796	76.216796
38	15	70.491134	70.491134	70.491134
38	16	75.716577	75.716577	75.716577
38	17	77.388630	77.388630	77.388630
38	18	74.793048	74.793048	74.793048
38	19	79.812280	79.812280	79.812280
38	20	75.584390	75.584390	75.584390
38	21	70.837843	70.837843	70.837843
38	22	80.956779	80.956779	80.956779
38	23	71.512237	71.512237	71.512237
38	24	81.596569	81.596569	81.596569
38	25	72.235725	72.235725	72.235725
38	26	82.637764	82.637764	82.637764
38	27	60.033324	60.033324	60.033324
38	28	55.758407	55.758407	55.758407
38	29	58.591808	58.591808	58.591808
38	30	53.235327	53.235327	53.235327
38	31	56.859476	56.859476	56.859476
38	32	52.325902	52.325902	52.325902
38	33	56.462377	56.462377	56.462377

38	34	60.406953	60.406953	60.406953
38	35	51.078371	51.078371	51.078371
38	36	3.605551	3.605551	3.605551
38	37	3.000000	3.000000	3.000000
38	39	3.605551	3.605551	3.605551
38	40	5.385165	5.385165	5.385165
38	41	5.830952	5.830952	5.830952
38	42	9.899495	9.899495	9.899495
38	43	10.198039	10.198039	10.198039
38	44	10.440307	10.440307	10.440307
38	45	10.000000	10.000000	10.000000
38	46	45.000000	45.000000	45.000000
38	47	47.042534	47.042534	47.042534
38	48	73.061618	73.061618	73.061618
38	49	80.361682	80.361682	80.361682
38	50	73.681748	73.681748	73.681748
38	51	47.518417	47.518417	47.518417
38	52	62.801274	62.801274	62.801274
38	53	65.604878	65.604878	65.604878
38	54	55.217751	55.217751	55.217751
38	55	24.166092	24.166092	24.166092
38	56	41.340053	41.340053	41.340053
38	57	49.335586	49.335586	49.335586
38	58	66.887966	66.887966	66.887966
38	59	87.658428	87.658428	87.658428
38	60	82.879430	82.879430	82.879430
38	61	54.626001	54.626001	54.626001
38	62	26.248809	26.248809	26.248809
38	63	47.000000	47.000000	47.000000
38	64	62.000000	62.000000	62.000000
38	65	55.713553	55.713553	55.713553
38	66	51.613952	51.613952	51.613952
38	67	51.000000	51.000000	51.000000
38	68	40.012498	40.012498	40.012498
38	69	33.301652	33.301652	33.301652
38	70	45.343136	45.343136	45.343136
38	71	32.695565	32.695565	32.695565
38	72	27.000000	27.000000	27.000000
38	73	17.117243	17.117243	17.117243
38	74	66.730802	66.730802	66.730802
38	75	76.609399	76.609399	76.609399
38	76	97.616597	97.616597	97.616597
38	77	70.178344	70.178344	70.178344
38	78	89.470666	89.470666	89.470666
38	79	62.649820	62.649820	62.649820
38	80	60.638272	60.638272	60.638272
38	81	39.357337	39.357337	39.357337
38	82	28.844410	28.844410	28.844410
38	83	54.451814	54.451814	54.451814
38	84	58.180753	58.180753	58.180753
38	85	53.600373	53.600373	53.600373
38	86	59.033889	59.033889	59.033889
38	87	72.801099	72.801099	72.801099
38	88	78.568442	78.568442	78.568442
38	89	47.507894	47.507894	47.507894
38	90	77.025970	77.025970	77.025970
38	91	44.821870	44.821870	44.821870
38	92	43.081318	43.081318	43.081318
38	93	40.804412	40.804412	40.804412
38	94	30.265492	30.265492	30.265492
38	95	34.928498	34.928498	34.928498
38	96	45.891176	45.891176	45.891176
38	97	29.732137	29.732137	29.732137

38	98	88.413800	88.413800	88.413800
38	99	49.203658	49.203658	49.203658
38	100	61.073726	61.073726	61.073726
38	101	37.161808	37.161808	37.161808
39	1	37.202150	37.202150	37.202150
39	2	37.336309	37.336309	37.336309
39	3	40.311289	40.311289	40.311289
39	4	40.311289	40.311289	40.311289
39	5	42.000000	42.000000	42.000000
39	6	42.296572	42.296572	42.296572
39	7	44.283180	44.283180	44.283180
39	8	47.265209	47.265209	47.265209
39	9	47.000000	47.000000	47.000000
39	10	68.767725	68.767725	68.767725
39	11	65.604878	65.604878	65.604878
39	12	67.201190	67.201190	67.201190
39	13	64.350602	64.350602	64.350602
39	14	72.622311	72.622311	72.622311
39	15	66.887966	66.887966	66.887966
39	16	72.111026	72.111026	72.111026
39	17	73.783467	73.783467	73.783467
39	18	71.196910	71.196910	71.196910
39	19	77.129761	77.129761	77.129761
39	20	72.801099	72.801099	72.801099
39	21	68.007353	68.007353	68.007353
39	22	78.160092	78.160092	78.160092
39	23	68.622154	68.622154	68.622154
39	24	78.746428	78.746428	78.746428
39	25	69.289249	69.289249	69.289249
39	26	79.711982	79.711982	79.711982
39	27	59.908263	59.908263	59.908263
39	28	55.803226	55.803226	55.803226
39	29	58.309519	58.309519	58.309519
39	30	53.000000	53.000000	53.000000
39	31	56.356011	56.356011	56.356011
39	32	51.971146	51.971146	51.971146
39	33	55.901699	55.901699	55.901699
39	34	59.615434	59.615434	59.615434
39	35	50.537115	50.537115	50.537115
39	36	7.071068	7.071068	7.071068
39	37	5.830952	5.830952	5.830952
39	38	3.605551	3.605551	3.605551
39	40	2.000000	2.000000	2.000000
39	41	5.385165	5.385165	5.385165
39	42	6.403124	6.403124	6.403124
39	43	7.000000	7.000000	7.000000
39	44	8.602325	8.602325	8.602325
39	45	7.280110	7.280110	7.280110
39	46	42.047592	42.047592	42.047592
39	47	44.000000	44.000000	44.000000
39	48	69.462220	69.462220	69.462220
39	49	77.620873	77.620873	77.620873
39	50	70.880181	70.880181	70.880181
39	51	46.097722	46.097722	46.097722
39	52	60.406953	60.406953	60.406953
39	53	62.201286	62.201286	62.201286
39	54	51.613952	51.613952	51.613952
39	55	21.189620	21.189620	21.189620
39	56	37.735925	37.735925	37.735925
39	57	46.572524	46.572524	46.572524
39	58	63.631753	63.631753	63.631753
39	59	84.314886	84.314886	84.314886
39	60	79.397733	79.397733	79.397733

39	61	51.078371	51.078371	51.078371
39	62	22.671568	22.671568	22.671568
39	63	45.099889	45.099889	45.099889
39	64	60.074953	60.074953	60.074953
39	65	52.810984	52.810984	52.810984
39	66	48.259714	48.259714	48.259714
39	67	47.853944	47.853944	47.853944
39	68	38.052595	38.052595	38.052595
39	69	29.732137	29.732137	29.732137
39	70	41.773197	41.773197	41.773197
39	71	29.154759	29.154759	29.154759
39	72	25.179357	25.179357	25.179357
39	73	15.033296	15.033296	15.033296
39	74	63.245553	63.245553	63.245553
39	75	73.239334	73.239334	73.239334
39	76	94.201911	94.201911	94.201911
39	77	68.029405	68.029405	68.029405
39	78	86.313383	86.313383	86.313383
39	79	59.093147	59.093147	59.093147
39	80	57.271284	57.271284	57.271284
39	81	36.249138	36.249138	36.249138
39	82	25.553865	25.553865	25.553865
39	83	50.931326	50.931326	50.931326
39	84	55.009090	55.009090	55.009090
39	85	51.244512	51.244512	51.244512
39	86	57.008771	57.008771	57.008771
39	87	69.404611	69.404611	69.404611
39	88	75.073298	75.073298	75.073298
39	89	43.908997	43.908997	43.908997
39	90	75.166482	75.166482	75.166482
39	91	41.400483	41.400483	41.400483
39	92	40.162171	40.162171	40.162171
39	93	38.078866	38.078866	38.078866
39	94	28.017851	28.017851	28.017851
39	95	32.388269	32.388269	32.388269
39	96	43.416587	43.416587	43.416587
39	97	26.925824	26.925824	26.925824
39	98	84.899941	84.899941	84.899941
39	99	45.607017	45.607017	45.607017
39	100	57.628118	57.628118	57.628118
39	101	33.615473	33.615473	33.615473
40	1	36.055513	36.055513	36.055513
40	2	35.355339	35.355339	35.355339
40	3	38.327536	38.327536	38.327536
40	4	38.327536	38.327536	38.327536
40	5	40.000000	40.000000	40.000000
40	6	40.311289	40.311289	40.311289
40	7	42.296572	42.296572	42.296572
40	8	45.276926	45.276926	45.276926
40	9	45.000000	45.000000	45.000000
40	10	67.268120	67.268120	67.268120
40	11	64.031242	64.031242	64.031242
40	12	65.604878	65.604878	65.604878
40	13	62.681736	62.681736	62.681736
40	14	71.063352	71.063352	71.063352
40	15	65.192024	65.192024	65.192024
40	16	70.455660	70.455660	70.455660
40	17	72.111026	72.111026	72.111026
40	18	69.462220	69.462220	69.462220
40	19	76.687678	76.687678	76.687678
40	20	72.277244	72.277244	72.277244
40	21	67.446275	67.446275	67.446275
40	22	77.620873	77.620873	77.620873

40	23	68.007353	68.007353	68.007353
40	24	78.160092	78.160092	78.160092
40	25	68.622154	68.622154	68.622154
40	26	79.056942	79.056942	79.056942
40	27	61.032778	61.032778	61.032778
40	28	57.008771	57.008771	57.008771
40	29	59.363288	59.363288	59.363288
40	30	54.083269	54.083269	54.083269
40	31	57.306195	57.306195	57.306195
40	32	53.000000	53.000000	53.000000
40	33	56.824291	56.824291	56.824291
40	34	60.415230	60.415230	60.415230
40	35	51.478151	51.478151	51.478151
40	36	8.602325	8.602325	8.602325
40	37	7.071068	7.071068	7.071068
40	38	5.385165	5.385165	5.385165
40	39	2.000000	2.000000	2.000000
40	41	5.000000	5.000000	5.000000
40	42	5.385165	5.385165	5.385165
40	43	5.000000	5.000000	5.000000
40	44	7.071068	7.071068	7.071068
40	45	5.385165	5.385165	5.385165
40	46	40.049969	40.049969	40.049969
40	47	42.000000	42.000000	42.000000
40	48	67.742158	67.742158	67.742158
40	49	77.129761	77.129761	77.129761
40	50	70.342022	70.342022	70.342022
40	51	46.572524	46.572524	46.572524
40	52	60.207973	60.207973	60.207973
40	53	61.032778	61.032778	61.032778
40	54	50.000000	50.000000	50.000000
40	55	20.615528	20.615528	20.615528
40	56	36.055513	36.055513	36.055513
40	57	46.097722	46.097722	46.097722
40	58	62.649820	62.649820	62.649820
40	59	83.216585	83.216585	83.216585
40	60	78.102497	78.102497	78.102497
40	61	49.244289	49.244289	49.244289
40	62	21.213203	21.213203	21.213203
40	63	45.276926	45.276926	45.276926
40	64	60.207973	60.207973	60.207973
40	65	52.201533	52.201533	52.201533
40	66	47.169906	47.169906	47.169906
40	67	47.010637	47.010637	47.010637
40	68	38.209946	38.209946	38.209946
40	69	28.284271	28.284271	28.284271
40	70	40.311289	40.311289	40.311289
40	71	27.313001	27.313001	27.313001
40	72	25.495098	25.495098	25.495098
40	73	15.297059	15.297059	15.297059
40	74	61.351447	61.351447	61.351447
40	75	72.111026	72.111026	72.111026
40	76	93.005376	93.005376	93.005376
40	77	68.000000	68.000000	68.000000
40	78	85.428333	85.428333	85.428333
40	79	57.271284	57.271284	57.271284
40	80	55.317267	55.317267	55.317267
40	81	35.468296	35.468296	35.468296
40	82	24.596748	24.596748	24.596748
40	83	49.578221	49.578221	49.578221
40	84	54.129474	54.129474	54.129474
40	85	51.088159	51.088159	51.088159
40	86	57.078893	57.078893	57.078893

40	87	68.242216	68.242216	68.242216
40	88	73.756356	73.756356	73.756356
40	89	42.190046	42.190046	42.190046
40	90	75.325958	75.325958	75.325958
40	91	40.224371	40.224371	40.224371
40	92	39.560081	39.560081	39.560081
40	93	37.656341	37.656341	37.656341
40	94	28.017851	28.017851	28.017851
40	95	32.140317	32.140317	32.140317
40	96	43.185646	43.185646	43.185646
40	97	26.476405	26.476405	26.476405
40	98	83.546394	83.546394	83.546394
40	99	44.045431	44.045431	44.045431
40	100	56.400355	56.400355	56.400355
40	101	31.780497	31.780497	31.780497
41	1	40.311289	40.311289	40.311289
41	2	35.000000	35.000000	35.000000
41	3	39.293765	39.293765	39.293765
41	4	38.000000	38.000000	38.000000
41	5	40.311289	40.311289	40.311289
41	6	40.000000	40.000000	40.000000
41	7	43.174066	43.174066	43.174066
41	8	46.097722	46.097722	46.097722
41	9	45.276926	45.276926	45.276926
41	10	70.710678	70.710678	70.710678
41	11	67.268120	67.268120	67.268120
41	12	68.767725	68.767725	68.767725
41	13	65.604878	65.604878	65.604878
41	14	74.330344	74.330344	74.330344
41	15	68.007353	68.007353	68.007353
41	16	73.409809	73.409809	73.409809
41	17	75.000000	75.000000	75.000000
41	18	72.111026	72.111026	72.111026
41	19	81.584312	81.584312	81.584312
41	20	77.129761	77.129761	77.129761
41	21	72.277244	72.277244	72.277244
41	22	82.462113	82.462113	82.462113
41	23	72.801099	72.801099	72.801099
41	24	82.969874	82.969874	82.969874
41	25	73.375745	73.375745	73.375745
41	26	83.815273	83.815273	83.815273
41	27	65.192024	65.192024	65.192024
41	28	61.032778	61.032778	61.032778
41	29	63.631753	63.631753	63.631753
41	30	58.309519	58.309519	58.309519
41	31	61.717096	61.717096	61.717096
41	32	57.306195	57.306195	57.306195
41	33	61.269895	61.269895	61.269895
41	34	65.000000	65.000000	65.000000
41	35	55.901699	55.901699	55.901699
41	36	7.000000	7.000000	7.000000
41	37	5.000000	5.000000	5.000000
41	38	5.830952	5.830952	5.830952
41	39	5.385165	5.385165	5.385165
41	40	5.000000	5.000000	5.000000
41	42	10.198039	10.198039	10.198039
41	43	7.071068	7.071068	7.071068
41	44	5.000000	5.000000	5.000000
41	45	5.830952	5.830952	5.830952
41	46	40.112342	40.112342	40.112342
41	47	42.296572	42.296572	42.296572
41	48	70.455660	70.455660	70.455660
41	49	82.000000	82.000000	82.000000

41	50	75.186435	75.186435	75.186435
41	51	51.419841	51.419841	51.419841
41	52	65.192024	65.192024	65.192024
41	53	65.192024	65.192024	65.192024
41	54	53.150729	53.150729	53.150729
41	55	25.495098	25.495098	25.495098
41	56	39.051248	39.051248	39.051248
41	57	50.990195	50.990195	50.990195
41	58	67.082039	67.082039	67.082039
41	59	87.464278	87.464278	87.464278
41	60	82.006097	82.006097	82.006097
41	61	51.478151	51.478151	51.478151
41	62	25.000000	25.000000	25.000000
41	63	50.249378	50.249378	50.249378
41	64	65.192024	65.192024	65.192024
41	65	57.008771	57.008771	57.008771
41	66	51.478151	51.478151	51.478151
41	67	51.623638	51.623638	51.623638
41	68	43.185646	43.185646	43.185646
41	69	32.015621	32.015621	32.015621
41	70	43.931765	43.931765	43.931765
41	71	29.681644	29.681644	29.681644
41	72	30.413813	30.413813	30.413813
41	73	20.223748	20.223748	20.223748
41	74	63.158531	63.158531	63.158531
41	75	76.321688	76.321688	76.321688
41	76	97.082439	97.082439	97.082439
41	77	73.000000	73.000000	73.000000
41	78	89.961103	89.961103	89.961103
41	79	59.539903	59.539903	59.539903
41	80	56.612719	56.612719	56.612719
41	81	40.162171	40.162171	40.162171
41	82	29.154759	29.154759	29.154759
41	83	53.413481	53.413481	53.413481
41	84	58.694122	58.694122	58.694122
41	85	56.080300	56.080300	56.080300
41	86	62.072538	62.072538	62.072538
41	87	72.401657	72.401657	72.401657
41	88	77.620873	77.620873	77.620873
41	89	45.000000	45.000000	45.000000
41	90	80.305666	80.305666	80.305666
41	91	44.418465	44.418465	44.418465
41	92	44.384682	44.384682	44.384682
41	93	42.579338	42.579338	42.579338
41	94	33.015148	33.015148	33.015148
41	95	37.121422	37.121422	37.121422
41	96	48.166378	48.166378	48.166378
41	97	31.400637	31.400637	31.400637
41	98	87.321246	87.321246	87.321246
41	99	47.381431	47.381431	47.381431
41	100	60.464866	60.464866	60.464866
41	101	34.132096	34.132096	34.132096
42	1	30.805844	30.805844	30.805844
42	2	34.481879	34.481879	34.481879
42	3	36.000000	36.000000	36.000000
42	4	37.363083	37.363083	37.363083
42	5	38.327536	38.327536	38.327536
42	6	39.293765	39.293765	39.293765
42	7	40.000000	40.000000	40.000000
42	8	43.000000	43.000000	43.000000
42	9	43.289722	43.289722	43.289722
42	10	62.481997	62.481997	62.481997
42	11	59.405387	59.405387	59.405387

42	12	61.032778	61.032778	61.032778
42	13	58.309519	58.309519	58.309519
42	14	66.400301	66.400301	66.400301
42	15	60.901560	60.901560	60.901560
42	16	66.037868	66.037868	66.037868
42	17	67.742158	67.742158	67.742158
42	18	65.299311	65.299311	65.299311
42	19	71.386273	71.386273	71.386273
42	20	66.940272	66.940272	66.940272
42	21	62.096699	62.096699	62.096699
42	22	72.277244	72.277244	72.277244
42	23	62.641839	62.641839	62.641839
42	24	72.801099	72.801099	72.801099
42	25	63.245553	63.245553	63.245553
42	26	73.681748	73.681748	73.681748
42	27	58.258047	58.258047	58.258047
42	28	54.488531	54.488531	54.488531
42	29	56.400355	56.400355	56.400355
42	30	51.224994	51.224994	51.224994
42	31	54.083269	54.083269	54.083269
42	32	50.000000	50.000000	50.000000
42	33	53.535035	53.535035	53.535035
42	34	56.824291	56.824291	56.824291
42	35	48.259714	48.259714	48.259714
42	36	13.453624	13.453624	13.453624
42	37	12.206556	12.206556	12.206556
42	38	9.899495	9.899495	9.899495
42	39	6.403124	6.403124	6.403124
42	40	5.385165	5.385165	5.385165
42	41	10.198039	10.198039	10.198039
42	43	5.830952	5.830952	5.830952
42	44	10.440307	10.440307	10.440307
42	45	7.615773	7.615773	7.615773
42	46	38.639358	38.639358	38.639358
42	47	40.311289	40.311289	40.311289
42	48	63.529521	63.529521	63.529521
42	49	71.805292	71.805292	71.805292
42	50	65.000000	65.000000	65.000000
42	51	42.379240	42.379240	42.379240
42	52	55.081757	55.081757	55.081757
42	53	55.803226	55.803226	55.803226
42	54	45.486262	45.486262	45.486262
42	55	15.297059	15.297059	15.297059
42	56	31.764760	31.764760	31.764760
42	57	40.792156	40.792156	40.792156
42	58	57.306195	57.306195	57.306195
42	59	77.935871	77.935871	77.935871
42	60	73.000000	73.000000	73.000000
42	61	45.541190	45.541190	45.541190
42	62	16.401219	16.401219	16.401219
42	63	40.607881	40.607881	40.607881
42	64	55.443665	55.443665	55.443665
42	65	46.840154	46.840154	46.840154
42	66	41.880783	41.880783	41.880783
42	67	41.629317	41.629317	41.629317
42	68	33.541020	33.541020	33.541020
42	69	23.430749	23.430749	23.430749
42	70	35.468296	35.468296	35.468296
42	71	23.769729	23.769729	23.769729
42	72	21.189620	21.189620	21.189620
42	73	11.180340	11.180340	11.180340
42	74	57.974132	57.974132	57.974132
42	75	66.850580	66.850580	66.850580
42	76	87.800911	87.800911	87.800911
42	77	63.031738	63.031738	63.031738
42	78	80.056230	80.056230	80.056230
42	79	53.488316	53.488316	53.488316
42	80	52.469038	52.469038	52.469038
42	81	30.083218	30.083218	30.083218
42	82	19.235384	19.235384	19.235384

See Also

- http://en.wikipedia.org/wiki/Vehicle_routing_problem

Indices and tables

- [genindex](#)
- [search](#)

Graph Operations

- [Transformation - Family of functions](#) - Maps a given graph to a new form
- [pgr_lineGraph - Experimental](#) - Transformation algorithm for generating a Line Graph.
- [pgr_lineGraphFull - Experimental](#) - Transformation algorithm for generating a Line Graph out of each vertex in the input graph.

6.2.7 pgr_lineGraph - Experimental

pgr_lineGraph — Transforms a given graph into its corresponding edge-based graph.



Fig. 6.25: Boost Graph Inside

Warning: Experimental functions

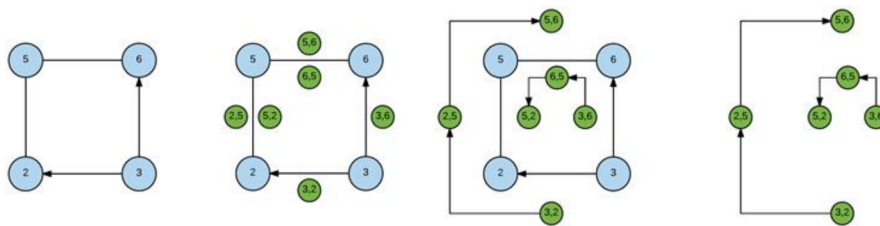
- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

Given a graph G , its line graph $L(G)$ is a graph such that:-

- each vertex of $L(G)$ represents an edge of G
- two vertices of $L(G)$ are adjacent if and only if their corresponding edges share a common endpoint in G .

The following figures show a graph (left, with blue vertices) and its Line Graph (right, with green vertices).

**Signature Summary**

```
pgr_lineGraph(edges_sql, directed)
RETURNS SET OF (seq, source, target, cost, reverse_cost)
OR EMPTY SET
```

Signatures

Minimal signature

```
pgr_lineGraph(edges_sql)
RETURNS SET OF (seq, source, target, cost, reverse_cost) or EMPTY SET
```

The minimal signature is for a **directed** graph:

Example

```
SELECT * FROM pgr_lineGraph(
  'SELECT id, source, target, cost, reverse_cost FROM edge_table'
);
```

seq	source	target	cost	reverse_cost
1	-18	18	1	1
2	-17	17	1	1
3	-16	-3	1	-1
4	-16	16	1	1
5	-15	-9	1	1
6	-15	15	1	1
7	-14	-10	1	1
8	-14	12	1	-1
9	-14	14	1	1
10	-10	-7	1	1
11	-10	-4	1	1
12	-10	8	1	1
13	-10	10	1	1
14	-9	-8	1	1
15	-9	9	1	1
16	-9	11	1	-1
17	-8	-7	1	1
18	-8	-4	1	1
19	-8	8	1	1
20	-7	-6	1	1
21	-6	6	1	1
22	-4	-1	1	1
23	-4	4	1	1
24	-3	-2	1	-1
25	-3	5	1	-1
26	-2	-1	1	-1
27	-2	4	1	-1
28	-1	1	1	1
29	5	-8	1	-1
30	5	9	1	-1
31	5	11	1	-1
32	7	-7	1	1
33	7	-4	1	1
34	8	11	1	-1
35	10	12	1	-1
36	11	13	1	-1
37	12	13	1	-1
38	13	-15	1	-1
39	16	-9	1	1
40	16	15	1	1

(40 rows)

Complete Signature

```
pgr_lineGraph(edges_sql, directed);
RETURNS SET OF (seq, source, target, cost, reverse_cost) or EMPTY SET
```

This signature returns the Line Graph of the current graph:

- on a **directed** graph when `directed` flag is missing or is set to `true`.
- on an **undirected** graph when `directed` flag is set to `false`.

Example

```
SELECT * FROM pgr_lineGraph(  
  'SELECT id, source, target, cost, reverse_cost FROM edge_table',  
  FALSE  
);
```

seq	source	target	cost	reverse_cost
1	-3	-2	1	-1
2	-3	5	1	-1
3	-2	4	1	-1
4	1	4	1	-1
5	4	8	1	-1
6	4	10	1	-1
7	5	9	1	-1
8	5	11	1	-1
9	6	7	1	-1
10	7	8	1	-1
11	7	10	1	-1
12	8	9	1	-1
13	8	11	1	-1
14	9	15	1	-1
15	10	12	1	-1
16	10	14	1	-1
17	11	13	1	-1
18	12	13	1	-1
19	16	15	1	-1

(19 rows)

Description of the Signatures

Description of the `edges_sql` query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Column	Type	Description
edges_sql	TEXT	SQL query as described above.
directed	BOOLEAN	<ul style="list-style-type: none"> When <code>true</code> the graph is considered as <i>Directed</i>. When <code>false</code> the graph is considered as <i>Undirected</i>.

Description of the return values

RETURNS SETOF (seq, source, target, cost, reverse_cost)

Column	Type	Description
seq	INTEGER	Sequential value starting from 1 .
source	BIGINT	Identifier of the source vertex of the current edge <i>id</i> . <ul style="list-style-type: none">When <i>negative</i>: the source is the reverse edge in the original graph.
target	BIGINT	Identifier of the target vertex of the current edge <i>id</i> . <ul style="list-style-type: none">When <i>negative</i>: the target is the reverse edge in the original graph.
cost	FLOAT	Weight of the edge (<i>source</i> , <i>target</i>). <ul style="list-style-type: none">When <i>negative</i>: edge (<i>source</i>, <i>target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	FLOAT	Weight of the edge (<i>target</i> , <i>source</i>). <ul style="list-style-type: none">When <i>negative</i>: edge (<i>target</i>, <i>source</i>) does not exist, therefore it's not part of the graph.

See Also

- https://en.wikipedia.org/wiki/Line_graph
- The queries use the [Sample Data](#) network.

Indices and tables

- genindex
- search

6.2.8 pgr_lineGraphFull - Experimental

`pgr_lineGraphFull` — Transforms a given graph into a new graph where all of the vertices from the original graph are converted to line graphs.

Warning: Experimental functions

- They are not officially of the current release.
- They likely will not be officially be part of the next release:
 - The functions might not make use of ANY-INTEGER and ANY-NUMERICAL
 - Name might change.
 - Signature might change.
 - Functionality might change.
 - pgTap tests might be missing.
 - Might need c/c++ coding.
 - May lack documentation.
 - Documentation if any might need to be rewritten.
 - Documentation examples might need to be automatically generated.
 - Might need a lot of feedback from the community.
 - Might depend on a proposed function of pgRouting
 - Might depend on a deprecated function of pgRouting

Synopsis

`pgr_lineGraphFull`, converts original directed graph to a directed line graph by converting each vertex to a complete graph and keeping all the original edges. The new connecting edges have a cost 0 and go between the adjacent original edges, respecting the directionality.

A possible application of the resulting graph is “routing with two edge restrictions”:

- Setting a cost of using the vertex when routing between edges on the connecting edge
- Forbid the routing between two edges by removing the connecting edge

This is possible because each of the intersections (vertices) in the original graph are now complete graphs that have a new edge for each possible turn across that intersection.

Characteristics

The main characteristics are:

- This function is for directed graphs.
- Results are undefined when a negative vertex id is used in the input graph.
- Results are undefined when a duplicated edge id is used in the input graph.
- Running time: TBD

Signature Summary

```
pgr_lineGraphFull(edges_sql)
RETURNS SET OF (seq, source, target, cost, edge)
OR EMPTY SET
```

Signatures

Minimal signature

```
pgr_lineGraphFull(TEXT edges_sql)
RETURNS SET OF (seq, source, target, cost, edge) OR EMPTY SET
```

Example

```
SELECT * FROM pgr_lineGraphFull(  
  'SELECT id, source, target, cost, reverse_cost  
    FROM edge_table  
    WHERE id IN (4,7,8,10) '  
);
```

seq	source	target	cost	edge
1	-1	5	1	4
2	2	-1	0	0
3	-2	2	1	-4
4	-3	8	1	-7
5	-4	6	1	8
6	-5	10	1	10
7	5	-2	0	0
8	5	-3	0	0
9	5	-4	0	0
10	5	-5	0	0
11	-6	-2	0	0
12	-6	-3	0	0
13	-6	-4	0	0
14	-6	-5	0	0
15	-7	-2	0	0
16	-7	-3	0	0
17	-7	-4	0	0
18	-7	-5	0	0
19	-8	-2	0	0
20	-8	-3	0	0
21	-8	-4	0	0
22	-8	-5	0	0
23	-9	-6	1	7
24	8	-9	0	0
25	-10	-7	1	-8
26	6	-10	0	0
27	-11	-8	1	-10
28	10	-11	0	0

(28 rows)

Description of the Signatures

Description of the edges_sql query for dijkstra like functions

edges_sql an SQL query, which should return a set of rows with the following columns:

Column	Type	Default	Description
id	ANY-INTEGER		Identifier of the edge.
source	ANY-INTEGER		Identifier of the first end point vertex of the edge.
target	ANY-INTEGER		Identifier of the second end point vertex of the edge.
cost	ANY-NUMERICAL		Weight of the edge (<i>source, target</i>) <ul style="list-style-type: none"> When negative: edge (<i>source, target</i>) does not exist, therefore it's not part of the graph.
reverse_cost	ANY-NUMERICAL	-1	Weight of the edge (<i>target, source</i>), <ul style="list-style-type: none"> When negative: edge (<i>target, source</i>) does not exist, therefore it's not part of the graph.

Where:

ANY-INTEGER SMALLINT, INTEGER, BIGINT

ANY-NUMERICAL SMALLINT, INTEGER, BIGINT, REAL, FLOAT

Description of the parameters of the signatures

Column	Type	Default	Description
sql	TEXT		SQL query as described above.

Additional Examples

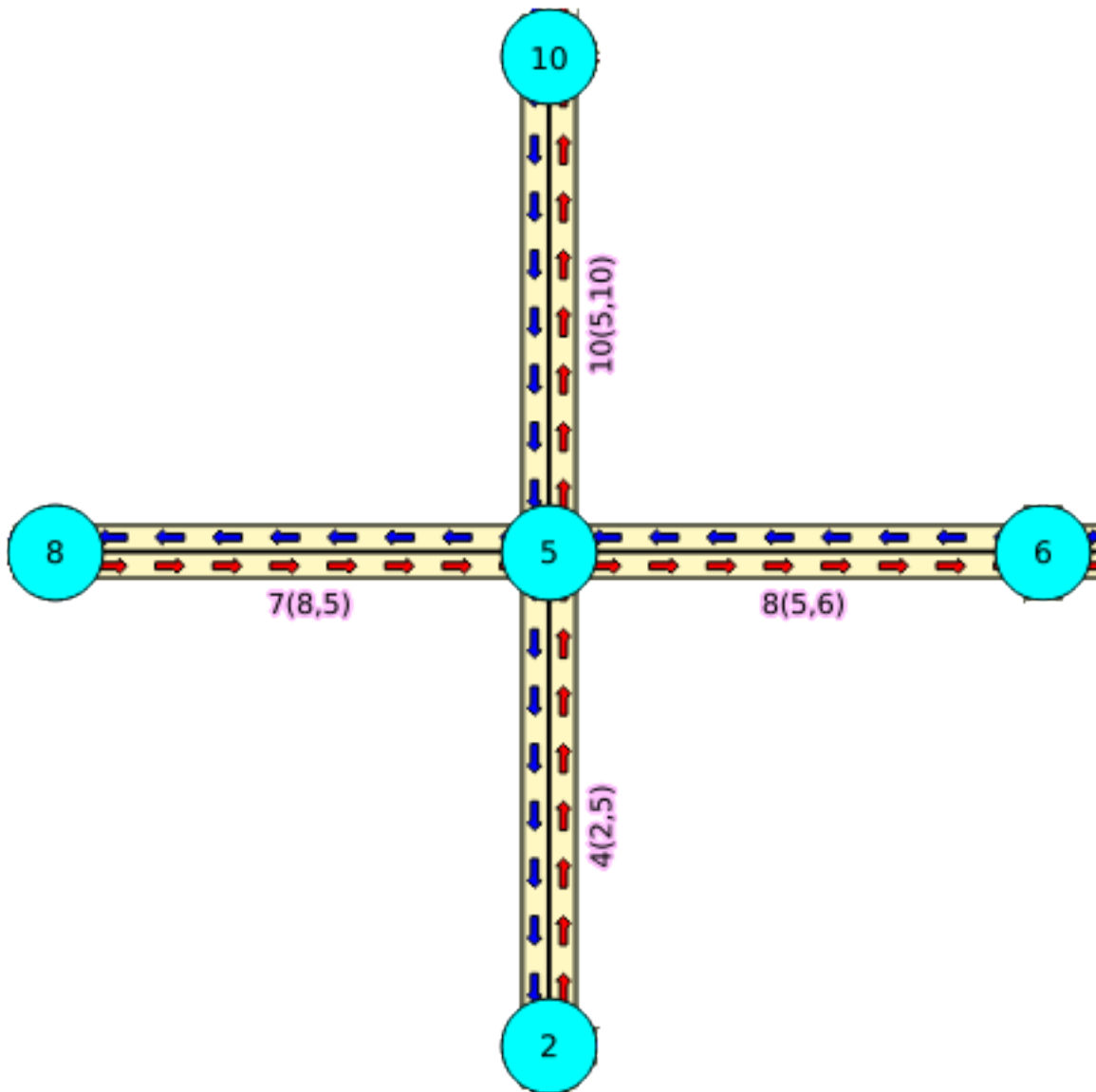
The examples of this section are based on the [Sample Data](#) network.

The examples include the subgraph including edges 4, 7, 8, and 10 with reverse_cost.

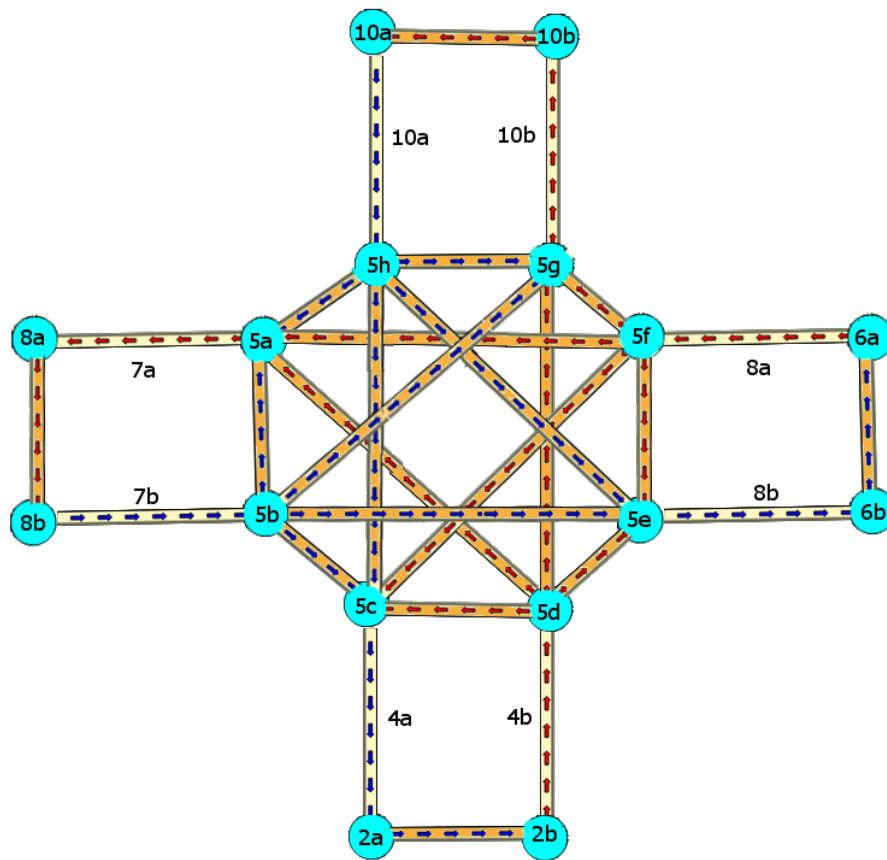
Example for generating the LineGraphFull

This example displays how this graph transformation works to create additional edges for each possible turn in a graph.

```
SELECT id, source, target, cost, reverse_cost
FROM edge_table
WHERE id IN (4,7,8,10);
```



```
SELECT * FROM pgr_lineGraphFull('SELECT id,
                                source,
                                target,
                                cost,
                                reverse_cost
                                FROM edge_table
                                WHERE id IN (4,7,8,10)');
```



In the transformed graph, all of the edges from the original graph are still present (yellow), but we now have additional edges for every turn that could be made across vertex 6 (orange).

Example for creating table that identifies transformed vertices

The vertices in the transformed graph are each created by splitting up the vertices in the original graph. Unless a vertex in the original graph is a leaf vertex, it will generate more than one vertex in the transformed graph. One of the newly created vertices in the transformed graph will be given the same vertex-id as the vertex that it was created from in the original graph, but the rest of the newly created vertices will have negative vertex ids. Following is an example of how to generate a table that maps the ids of the newly created vertices with the original vertex that they were created from

The first step is to store your results graph into a table and then create the vertex mapping table with one row for each distinct vertex id in the results graph.

```
CREATE TABLE lineGraph_edges AS SELECT * FROM pgr_lineGraphFull(
  $$SELECT id, source, target, cost, reverse_cost
  FROM edge_table WHERE id IN (4,7,8,10)$$
);
```

```
SELECT 28
CREATE TABLE lineGraph_vertices AS
SELECT *, NULL::BIGINT AS original_id
FROM (SELECT source AS id FROM lineGraph_edges
      UNION
      SELECT target FROM lineGraph_edges) as foo
ORDER BY id;
SELECT 16
```

Next, we set the `original_id` of all of the vertices in the results graph that were given the same vertex id as the vertex that it was created from in the original graph.

```
UPDATE lineGraph_vertices AS r
  SET original_id = v.id
  FROM edge_table_vertices_pgr AS v
 WHERE v.id = r.id;
UPDATE 5
```

Then, we cross reference all of the other newly created vertices that do not have the same `original_id` and set their `original_id` values.

```
WITH
unassignedVertices
  AS (SELECT e.id, e.original_id
      FROM lineGraph_vertices AS e
      WHERE original_id IS NOT NULL),
edgesWithUnassignedSource
  AS (SELECT *
      FROM lineGraph_edges
      WHERE cost = 0 and source IN (SELECT id FROM unassignedVertices)),
edgesWithUnassignedSourcePlusVertices
  AS (SELECT *
      FROM edgesWithUnassignedSource
      JOIN lineGraph_vertices
      ON(source = id)),
verticesFromEdgesWithUnassignedSource
  AS (SELECT DISTINCT edgesWithUnassignedSourcePlusVertices.target,
                     edgesWithUnassignedSourcePlusVertices.original_id
      FROM edgesWithUnassignedSourcePlusVertices
      JOIN lineGraph_vertices AS r
      ON(target = r.id AND r.original_id IS NULL))
UPDATE lineGraph_vertices
  SET original_id = verticesFromEdgesWithUnassignedSource.original_id
  FROM verticesFromEdgesWithUnassignedSource
  WHERE verticesFromEdgesWithUnassignedSource.target = id;
UPDATE 8
WITH
unassignedVertices
  AS (SELECT e.id, e.original_id
      FROM lineGraph_vertices AS e
      WHERE original_id IS NOT NULL),
edgesWithUnassignedTarget
  AS (SELECT *
      FROM lineGraph_edges
      WHERE cost = 0 and target IN (SELECT id FROM unassignedVertices)),
edgesWithUnassignedTargetPlusVertices
  AS (SELECT *
      FROM edgesWithUnassignedTarget
      JOIN lineGraph_vertices
      ON(target = id)),
verticesFromEdgesWithUnassignedTarget
  AS (SELECT DISTINCT edgesWithUnassignedTargetPlusVertices.source,
                     edgesWithUnassignedTargetPlusVertices.original_id
```



```

        FROM edgesWithUnassignedTargetPlusVertices
        JOIN lineGraph_vertices AS r
        ON(source = r.id AND r.original_id IS NULL))
UPDATE lineGraph_vertices
  SET original_id = verticesFromEdgesWithUnassignedTarget.original_id
  FROM verticesFromEdgesWithUnassignedTarget
  WHERE verticesFromEdgesWithUnassignedTarget.source = id;
UPDATE 3

```

The only vertices left that have not been mapped are a few of the leaf vertices from the original graph. The following sql completes the mapping for these leaf vertices (in the case of this example graph there are no leaf vertices but this is necessary for larger graphs).

```

WITH
unassignedVertexIds
  AS (SELECT id
      FROM lineGraph_vertices
      WHERE original_id IS NULL),
edgesWithUnassignedSource
  AS (SELECT source,edge
      FROM lineGraph_edges
      WHERE source IN (SELECT id FROM unassignedVertexIds)),
originalEdgesWithUnassignedSource
  AS (SELECT id,source
      FROM edge_table
      WHERE id IN (SELECT edge FROM edgesWithUnassignedSource))
UPDATE lineGraph_vertices AS d
  SET original_id = (SELECT source
                    FROM originalEdgesWithUnassignedSource
                    WHERE originalEdgesWithUnassignedSource.id =
                      (SELECT edge
                      FROM edgesWithUnassignedSource
                      WHERE edgesWithUnassignedSource.source = d.id))
  WHERE id IN (SELECT id FROM unassignedVertexIds);
UPDATE 0
WITH
unassignedVertexIds
  AS (SELECT id
      FROM lineGraph_vertices
      WHERE original_id IS NULL),
edgesWithUnassignedTarget
  AS (SELECT target,edge
      FROM lineGraph_edges
      WHERE target IN (SELECT id FROM unassignedVertexIds)),
originalEdgesWithUnassignedTarget
  AS (SELECT id,target
      FROM edge_table
      WHERE id IN (SELECT edge FROM edgesWithUnassignedTarget))
UPDATE lineGraph_vertices AS d
  SET original_id = (SELECT target
                    FROM originalEdgesWithUnassignedTarget
                    WHERE originalEdgesWithUnassignedTarget.id =
                      (SELECT edge
                      FROM edgesWithUnassignedTarget
                      WHERE edgesWithUnassignedTarget.target = d.id))
  WHERE id IN (SELECT id FROM unassignedVertexIds);
UPDATE 0

```

Now our vertex mapping table is complete:

```

SELECT * FROM lineGraph_vertices;
 id | original_id
-----+-----

```

```

 2 |          2
 5 |          5
 6 |          6
 8 |          8
10 |         10
-11 |         10
-10 |          6
 -9 |          8
 -5 |          5
 -4 |          5
 -3 |          5
 -2 |          5
 -1 |          2
 -8 |          5
 -7 |          5
 -6 |          5
(16 rows)

```

Example for running a dijkstra's shortest path with turn penalties

One use case for this graph transformation is to be able to run a shortest path search that takes into account the cost or limitation of turning. Below is an example of running a dijkstra's shortest path from vertex 2 to vertex 8 in the original graph, while adding a turn penalty cost of 100 to the turn from edge 4 to edge -7.

First we must increase set the cost of making the turn to 100:

```

UPDATE lineGraph_edges
SET cost = 100
WHERE source IN (SELECT target
                  FROM lineGraph_edges
                  WHERE edge = 4) AND target IN (SELECT source
                                                  FROM lineGraph_edges
                                                  WHERE edge = -7);

UPDATE 1

```

Then we must run a dijkstra's shortest path search using all of the vertices in the new graph that were created from vertex 2 as the starting point, and all of the vertices in the new graph that were created from vertex 8 as the ending point.

```

SELECT * FROM
(
  (SELECT * FROM
    (SELECT * FROM pgr_dijkstra($$SELECT seq AS id, * FROM lineGraph_edges$$,
      (SELECT array_agg(id) FROM lineGraph_vertices where original_id = 2),
      (SELECT array_agg(id) FROM lineGraph_vertices where original_id = 8)
    )) as shortestPaths
    WHERE start_vid = 2 AND end_vid = 8 AND (cost != 0 OR edge = -1)) as b;
seq | path_seq | start_vid | end_vid | node | edge | cost | agg_cost
-----+-----+-----+-----+-----+-----+-----+-----
29 | 2 | 2 | 8 | -1 | 1 | 1 | 0
31 | 4 | 2 | 8 | -4 | 5 | 1 | 1
33 | 6 | 2 | 8 | -10 | 25 | 1 | 2
35 | 8 | 2 | 8 | -3 | 4 | 1 | 3
36 | 9 | 2 | 8 | 8 | -1 | 0 | 4
(5 rows)

```

Normally the shortest path from vertex 2 to vertex 8 would have an aggregate cost of 2, but since there is a large penalty for making the turn needed to get this cost, the route goes through vertex 6 to avoid this turn.

If you cross reference the node column in the dijkstra results with the vertex id mapping table, this will show you that the path goes from v2 -> v5 -> v6 -> v5 -> v8 in the original graph.

See Also

- http://en.wikipedia.org/wiki/Line_graph
- http://en.wikipedia.org/wiki/Complete_graph

Indices and tables

- [genindex](#)
- [search](#)

6.2.9 Transformation - Family of functions

- *pgr_lineGraph - Experimental* - Transformation algorithm for generating a Line Graph.
- *pgr_lineGraphFull - Experimental* - Transformation algorithm for generating a Line Graph out of each vertex in the input graph.

Introduction

This family of functions is used for transforming a given input graph $G(V, E)$ into a new graph $G'(V', E')$.

See Also

Indices and tables

- [genindex](#)
- [search](#)

6.2.10 See Also

Indices and tables

- [genindex](#)
- [search](#)

Change Log

- *pgRouting 2.6.0 Release Notes*
- *pgRouting 2.5.3 Release Notes*
- *pgRouting 2.5.2 Release Notes*
- *pgRouting 2.5.1 Release Notes*
- *pgRouting 2.5.0 Release Notes*
- *pgRouting 2.4.2 Release Notes*
- *pgRouting 2.4.1 Release Notes*
- *pgRouting 2.4.0 Release Notes*
- *pgRouting 2.3.2 Release Notes*
- *pgRouting 2.3.1 Release Notes*
- *pgRouting 2.3.0 Release Notes*
- *pgRouting 2.2.4 Release Notes*
- *pgRouting 2.2.3 Release Notes*
- *pgRouting 2.2.2 Release Notes*
- *pgRouting 2.2.1 Release Notes*
- *pgRouting 2.2.0 Release Notes*
- *pgRouting 2.1.0 Release Notes*
- *pgRouting 2.0.1 Release Notes*
- *pgRouting 2.0.0 Release Notes*
- *pgRouting 1.x Release Notes*

7.1 Release Notes

To see the full list of changes check the list of [Git commits](https://github.com/pgRouting/pgrouting/commits)¹ on Github.

Table of contents

- *pgRouting 2.6.0 Release Notes*
- *pgRouting 2.5.3 Release Notes*

¹<https://github.com/pgRouting/pgrouting/commits>

- [*pgRouting 2.5.2 Release Notes*](#)
- [*pgRouting 2.5.1 Release Notes*](#)
- [*pgRouting 2.5.0 Release Notes*](#)
- [*pgRouting 2.4.2 Release Notes*](#)
- [*pgRouting 2.4.1 Release Notes*](#)
- [*pgRouting 2.4.0 Release Notes*](#)
- [*pgRouting 2.3.2 Release Notes*](#)
- [*pgRouting 2.3.1 Release Notes*](#)
- [*pgRouting 2.3.0 Release Notes*](#)
- [*pgRouting 2.2.4 Release Notes*](#)
- [*pgRouting 2.2.3 Release Notes*](#)
- [*pgRouting 2.2.2 Release Notes*](#)
- [*pgRouting 2.2.1 Release Notes*](#)
- [*pgRouting 2.2.0 Release Notes*](#)
- [*pgRouting 2.1.0 Release Notes*](#)
- [*pgRouting 2.0.1 Release Notes*](#)
- [*pgRouting 2.0.0 Release Notes*](#)
- [*pgRouting 1.x Release Notes*](#)

7.1.1 pgRouting 2.6.0 Release Notes

To see the issues closed by this release see the [Git closed milestone for 2.6.0²](#) on Github.

New fexperimental functions

- `pgr_lineGraphFull`

Bug fixes

- Fix `pgr_trsp(text, integer, double precision, integer, double precision, boolean, boolean[, text])`
 - without restrictions
 - * calls `pgr_dijkstra` when both end points have a fraction IN (0,1)
 - * calls `pgr_withPoints` when at least one fraction NOT IN (0,1)
 - with restrictions
 - * calls original `trsp` code

²<https://github.com/pgRouting/pgrouting/issues?utf8=%E2%9C%93&q=milestone%3A%22Release%202.6.0%22%20>

Internal code

- Cleaned the internal code of `trsp(text,integer,integer,boolean,boolean [, text])`
 - Removed the use of pointers
 - Internal code can accept BIGINT
- Cleaned the internal code of `withPoints`

7.1.2 pgRouting 2.5.3 Release Notes

To see the issues closed by this release see the [Git closed milestone for 2.5.3³](#) on Github.

Bug fixes

- Fix for postgresql 11: Removed a compilation error when compiling with postgresSQL

7.1.3 pgRouting 2.5.2 Release Notes

To see the issues closed by this release see the [Git closed milestone for 2.5.2⁴](#) on Github.

Bug fixes

- Fix for postgresql 10.1: Removed a compiler condition

7.1.4 pgRouting 2.5.1 Release Notes

To see the issues closed by this release see the [Git closed milestone for 2.5.1⁵](#) on Github.

Bug fixes

- Fixed prerequisite minimum version of: cmake

7.1.5 pgRouting 2.5.0 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.5.0⁶](#) on Github.

enhancement:

- `pgr_version` is now on SQL language

³<https://github.com/pgRouting/pgrouting/issues?utf8=%E2%9C%93&q=milestone%3A%22Release%202.5.3%22%20>

⁴<https://github.com/pgRouting/pgrouting/issues?utf8=%E2%9C%93&q=milestone%3A%22Release%202.5.2%22%20>

⁵<https://github.com/pgRouting/pgrouting/issues?utf8=%E2%9C%93&q=milestone%3A%22Release%202.5.1%22%20>

⁶<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A%22Release+2.5.0%22+is%3Aclosed>

Breaking change on:

- `pgr_edgeDisjointPaths`:
 - Added `path_id`, `cost` and `agg_cost` columns on the result
 - Parameter names changed
 - The many version results are the union of the one to one version

New Signatures:

- `pgr_bdAstar(one to one)`

New Proposed functions

- `pgr_bdAstar(one to many)`
- `pgr_bdAstar(many to one)`
- `pgr_bdAstar(many to many)`
- `pgr_bdAstarCost(one to one)`
- `pgr_bdAstarCost(one to many)`
- `pgr_bdAstarCost(many to one)`
- `pgr_bdAstarCost(many to many)`
- `pgr_bdAstarCostMatrix`
- `pgr_bdDijkstra(one to many)`
- `pgr_bdDijkstra(many to one)`
- `pgr_bdDijkstra(many to many)`
- `pgr_bdDijkstraCost(one to one)`
- `pgr_bdDijkstraCost(one to many)`
- `pgr_bdDijkstraCost(many to one)`
- `pgr_bdDijkstraCost(many to many)`
- `pgr_bdDijkstraCostMatrix`
- `pgr_lineGraph`
- `pgr_lineGraphFull`
- `pgr_connectedComponents`
- `pgr_strongComponents`
- `pgr_biconnectedComponents`
- `pgr_articulationPoints`
- `pgr_bridges`

Deprecated Signatures

- `pgr_bdastar` - use `pgr_bdAstar` instead

Renamed Functions

- `pgr_maxFlowPushRelabel` - use `pgr_pushRelabel` instead
- `pgr_maxFlowEdmondsKarp` -use `pgr_edmondsKarp` instead
- `pgr_maxFlowBoykovKolmogorov` - use `pgr_boykovKolmogorov` instead
- `pgr_maximumCardinalityMatching` - use `pgr_maxCardinalityMatch` instead

Deprecated function

- `pgr_pointToEdgeNode`

7.1.6 pgRouting 2.4.2 Release Notes

To see the issues closed by this release see the [Git closed milestone for 2.4.2⁷](#) on Github.

Improvement

- Works for postgresSQL 10

Bug fixes

- Fixed: Unexpected error column “cname”
- Replace `__linux__` with `__GLIBC__` for glibc-specific headers and functions

7.1.7 pgRouting 2.4.1 Release Notes

To see the issues closed by this release see the [Git closed milestone for 2.4.1⁸](#) on Github.

Bug fixes

- Fixed compiling error on macOS
- Condition error on `pgr_withPoints`

7.1.8 pgRouting 2.4.0 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.4.0⁹](#) on Github.

New Signatures

- `pgr_bdDijkstra`

⁷<https://github.com/pgRouting/pgrouting/issues?utf8=%E2%9C%93&q=milestone%3A%22Release%202.4.2%22%20>

⁸<https://github.com/pgRouting/pgrouting/issues?utf8=%E2%9C%93&q=milestone%3A%22Release%202.4.1%22%20>

⁹<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A%22Release+2.4.0%22+is%3Aclosed>

New Proposed Signatures

- `pgr_maxFlow`
- `pgr_astar(one to many)`
- `pgr_astar(many to one)`
- `pgr_astar(many to many)`
- `pgr_astarCost(one to one)`
- `pgr_astarCost(one to many)`
- `pgr_astarCost(many to one)`
- `pgr_astarCost(many to many)`
- `pgr_astarCostMatrix`

Deprecated Signatures

- `pgr_bddijkstra` - use `pgr_bdDijkstra` instead

Deprecated Functions

- `pgr_pointsToVids`

Bug fixes

- Bug fixes on proposed functions
 - `pgr_withPointsKSP`: fixed ordering
- TRSP original code is used with no changes on the compilation warnings

7.1.9 pgRouting 2.3.2 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.3.2](#)¹⁰ on Github.

Bug Fixes

- Fixed `pgr_gsoc_vrppdtw` crash when all orders fit on one truck.
- Fixed `pgr_trsp`:
 - Alternate code is not executed when the point is in reality a vertex
 - Fixed ambiguity on `seq`

7.1.10 pgRouting 2.3.1 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.3.1](#)¹¹ on Github.

¹⁰<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A%22Release+2.3.2%22+is%3Aclosed>

¹¹<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A%22Release+2.3.1%22+is%3Aclosed>

Bug Fixes

- Leaks on proposed max_flow functions
- Regression error on pgr_trsp
- Types discrepancy on pgr_createVerticesTable

7.1.11 pgRouting 2.3.0 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.3.0¹²](#) on Github.

New Signatures

- pgr_TSP
- pgr_aStar

New Functions

- pgr_eucledianTSP

New Proposed functions

- pgr_dijkstraCostMatrix
- pgr_withPointsCostMatrix
- pgr_maxFlowPushRelabel(one to one)
- pgr_maxFlowPushRelabel(one to many)
- pgr_maxFlowPushRelabel(many to one)
- pgr_maxFlowPushRelabel(many to many)
- pgr_maxFlowEdmondsKarp(one to one)
- pgr_maxFlowEdmondsKarp(one to many)
- pgr_maxFlowEdmondsKarp(many to one)
- pgr_maxFlowEdmondsKarp(many to many)
- pgr_maxFlowBoykovKolmogorov (one to one)
- pgr_maxFlowBoykovKolmogorov (one to many)
- pgr_maxFlowBoykovKolmogorov (many to one)
- pgr_maxFlowBoykovKolmogorov (many to many)
- pgr_maximumCardinalityMatching
- pgr_edgeDisjointPaths(one to one)
- pgr_edgeDisjointPaths(one to many)
- pgr_edgeDisjointPaths(many to one)
- pgr_edgeDisjointPaths(many to many)
- pgr_contractGraph

¹²<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A%22Release+2.3.0%22+is%3Aclosed>

Deprecated Signatures

- `pgr_tsp` - use `pgr_TSP` or `pgr_eucledianTSP` instead
- `pgr_astar` - use `pgr_aStar` instead

Deprecated Functions

- `pgr_flip_edges`
- `pgr_vidsToDmatrix`
- `pgr_pointsToDMatrix`
- `pgr_textToPoints`

7.1.12 pgRouting 2.2.4 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.2.4¹³](#) on Github.

Bug Fixes

- Bogus uses of extern “C”
- Build error on Fedora 24 + GCC 6.0
- Regression error `pgr_nodeNetwork`

7.1.13 pgRouting 2.2.3 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.2.3¹⁴](#) on Github.

Bug Fixes

- Fixed compatibility issues with PostgreSQL 9.6.

7.1.14 pgRouting 2.2.2 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.2.2¹⁵](#) on Github.

Bug Fixes

- Fixed regression error on `pgr_drivingDistance`

7.1.15 pgRouting 2.2.1 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.2.1¹⁶](#) on Github.

¹³<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A%22Release+2.2.4%22+is%3Aclosed>

¹⁴<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A%22Release+2.2.3%22+is%3Aclosed>

¹⁵<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A%22Release+2.2.2%22+is%3Aclosed>

¹⁶<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A2.2.1+is%3Aclosed>

Bug Fixes

- Server crash fix on pgr_alphaShape
- Bug fix on With Points family of functions

7.1.16 pgRouting 2.2.0 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.2.0¹⁷](#) on Github.

Improvements

- pgr_nodeNetwork
 - Adding a row_where and outall optional parameters
- Signature fix
 - pgr_dijkstra – to match what is documented

New Functions

- pgr_floydWarshall
- pgr_Johnson
- pgr_dijkstraCost(one to one)
- pgr_dijkstraCost(one to many)
- pgr_dijkstraCost(many to one)
- pgr_dijkstraCost(many to many)

Proposed functionality

- pgr_withPoints(one to one)
- pgr_withPoints(one to many)
- pgr_withPoints(many to one)
- pgr_withPoints(many to many)
- pgr_withPointsCost(one to one)
- pgr_withPointsCost(one to many)
- pgr_withPointsCost(many to one)
- pgr_withPointsCost(many to many)
- pgr_withPointsDD(single vertex)
- pgr_withPointsDD(multiple vertices)
- pgr_withPointsKSP
- pgr_dijkstraVia

¹⁷<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A%22Release+2.2.0%22+is%3Aclosed>

Deprecated functions:

- pgr_apspWarshall use pgr_floydWarshall instead
- pgr_apspJohnson use pgr_Johnson instead
- pgr_kDijkstraCost use pgr_dijkstraCost instead
- pgr_kDijkstraPath use pgr_dijkstra instead

Renamed and deprecated function

- pgr_makeDistanceMatrix renamed to _pgr_makeDistanceMatrix

7.1.17 pgRouting 2.1.0 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.1.0¹⁸](https://github.com/pgRouting/pgrouting/issues?q=is%3Aissue+milestone%3A%22Release+2.1.0%22+is%3Aclosed) on Github.

New Signatures

- pgr_dijkstra(one to many)
- pgr_dijkstra(many to one)
- pgr_dijkstra(many to many)
- pgr_drivingDistance(multiple vertices)

Refactored

- pgr_dijkstra(one to one)
- pgr_ksp
- pgr_drivingDistance(single vertex)

Improvements

- pgr_alphaShape function now can generate better (multi)polygon with holes and alpha parameter.

Proposed functionality

- Proposed functions from Steve Woodbridge, (Classified as Convenience by the author.)
 - pgr_pointToEdgeNode - convert a point geometry to a vertex_id based on closest edge.
 - pgr_flipEdges - flip the edges in an array of geometries so the connect end to end.
 - pgr_textToPoints - convert a string of x,y;x,y;... locations into point geometries.
 - pgr_pointsToVids - convert an array of point geometries into vertex ids.
 - pgr_pointsToDMatrix - Create a distance matrix from an array of points.
 - pgr_vidsToDMatrix - Create a distance matrix from an array of vertex_id.
 - pgr_vidsToDMatrix - Create a distance matrix from an array of vertex_id.
- Added proposed functions from GSoc Projects:

¹⁸<https://github.com/pgRouting/pgrouting/issues?q=is%3Aissue+milestone%3A%22Release+2.1.0%22+is%3Aclosed>

- pgr_vrppdtw
- pgr_vrponedepot

Deprecated functions

- pgr_getColumnName
- pgr_getTableName
- pgr_isColumnCndexed
- pgr_isColumnInTable
- pgr_quote_ident
- pgr_versionless
- pgr_startPoint
- pgr_endPoint
- pgr_pointToId

No longer supported

- Removed the 1.x legacy functions

Bug Fixes

- Some bug fixes in other functions

Refactoring Internal Code

- A C and C++ library for developer was created
 - encapsulates postgreSQL related functions
 - encapsulates Boost.Graph graphs
 - * Directed Boost.Graph
 - * Undirected Boost.graph.
 - allow any-integer in the id's
 - allow any-numerical on the cost/reverse_cost columns
- Instead of generating many libraries: - All functions are encapsulated in one library - The library has the prefix 2-1-0

7.1.18 pgRouting 2.0.1 Release Notes

Minor bug fixes.

Bug Fixes

- No track of the bug fixes were kept.

7.1.19 pgRouting 2.0.0 Release Notes

To see the issues closed by this release see the [Git closed issues for 2.0.0¹⁹](#) on Github.

With the release of pgRouting 2.0.0 the library has abandoned backwards compatibility to *pgRouting 1.x* releases. The main Goals for this release are:

- Major restructuring of pgRouting.
- Standardization of the function naming
- Preparation of the project for future development.

As a result of this effort:

- pgRouting has a simplified structure
- Significant new functionality has being added
- Documentation has being integrated
- Testing has being integrated
- And made it easier for multiple developers to make contributions.

Important Changes

- Graph Analytics - tools for detecting and fixing connection some problems in a graph
- A collection of useful utility functions
- Two new All Pairs Short Path algorithms (`pgr_apspJohnson`, `pgr_apspWarshall`)
- Bi-directional Dijkstra and A-star search algorithms (`pgr_bdAstar`, `pgr_bdDijkstra`)
- One to many nodes search (`pgr_kDijkstra`)
- K alternate paths shortest path (`pgr_ksp`)
- New TSP solver that simplifies the code and the build process (`pgr_tsp`), dropped “Gaul Library” dependency
- Turn Restricted shortest path (`pgr_trsp`) that replaces Shooting Star
- Dropped support for Shooting Star
- Built a test infrastructure that is run before major code changes are checked in
- Tested and fixed most all of the outstanding bugs reported against 1.x that existing in the 2.0-dev code base.
- Improved build process for Windows
- Automated testing on Linux and Windows platforms trigger by every commit
- Modular library design
- Compatibility with PostgreSQL 9.1 or newer
- Compatibility with PostGIS 2.0 or newer
- Installs as PostgreSQL EXTENSION
- Return types re factored and unified
- Support for table SCHEMA in function parameters
- Support for `st_` PostGIS function prefix
- Added `pgr_` prefix to functions and types
- Better documentation: <http://docs.pgrouting.org>

¹⁹<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A%22Release+2.0.0%22+is%3Aclosed>

- shooting_star is discontinued

7.1.20 pgRouting 1.x Release Notes

To see the issues closed by this release see the [Git closed issues for 1.x²⁰](#) on Github. The following release notes have been copied from the previous RELEASE_NOTES file and are kept as a reference.

Changes for release 1.05

- Bug fixes

Changes for release 1.03

- Much faster topology creation
- Bug fixes

Changes for release 1.02

- Shooting* bug fixes
- Compilation problems solved

Changes for release 1.01

- Shooting* bug fixes

Changes for release 1.0

- Core and extra functions are separated
- Cmake build process
- Bug fixes

Changes for release 1.0.0b

- Additional SQL file with more simple names for wrapper functions
- Bug fixes

Changes for release 1.0.0a

- Shooting* shortest path algorithm for real road networks
- Several SQL bugs were fixed

Changes for release 0.9.9

- PostgreSQL 8.2 support
- Shortest path functions return empty result if they could not find any path

²⁰<https://github.com/pgRouting/pgrouting/issues?q=milestone%3A%22Release+1.x%22+is%3Aclosed>

Changes for release 0.9.8

- Renumbering scheme was added to shortest path functions
- Directed shortest path functions were added
- routing_postgis.sql was modified to use dijkstra in TSP search

Indices and tables

- genindex
- search

[C001] Simulated annealing algorithm for beginners²¹

²¹<http://www.theprojectspot.com/tutorial-post/simulated-annealing-algorithm-for-beginners/6>