

$$\begin{aligned}
g(x, x') &= \left[1 + \theta |x - x'| + \frac{1}{3} \theta^2 |x - x'|^2 \right] \exp \{ -\theta |x - x'| \} \\
\frac{\partial}{\partial x} g(x, x') &= \left[\theta \operatorname{sign}(x - x') + \frac{2}{3} \theta^2 (x - x') \right] \exp \{ -\theta |x - x'| \} \\
&+ \left[1 + \theta |x - x'| + \frac{1}{3} \theta^2 (x - x')^2 \right] \exp \{ -\theta |x - x'| \} (-\theta \operatorname{sign}(x - x')) \\
&= \exp \{ -\theta |x - x'| \} \left[\theta \operatorname{sign}(x - x') + \frac{2}{3} \theta^2 (x - x') - \theta \operatorname{sign}(x - x') - \theta^2 |x - x'| \operatorname{sign}(x - x') - \frac{1}{3} \theta^3 (x - x')^2 \operatorname{sign}(x - x') \right] \\
&= \exp \{ -\theta |x - x'| \} \left[-\frac{1}{3} \theta^2 (x - x') - \frac{1}{3} \theta^3 (x - x')^2 \operatorname{sign}(x - x') \right] \\
&= \exp \{ -\theta |x - x'| \} \left(-\frac{1}{3} \theta^2 (x - x') \right) [1 + \theta (x - x') \operatorname{sign}(x - x')] \\
&= -\frac{1}{3} \theta^2 (x - x') [1 + \theta |x - x'|] \exp \{ -\theta |x - x'| \} \\
\frac{\partial^2}{\partial x' \partial x} g(x, x') &= \frac{\partial}{\partial x'} \left[-\frac{1}{3} \theta^2 (x - x') [1 + \theta |x - x'|] \exp \{ -\theta |x - x'| \} \right] \\
&= \frac{\partial}{\partial x'} \left[\left[-\frac{1}{3} \theta^2 (x - x') - \frac{1}{3} \theta^3 (x - x')^2 \operatorname{sign}(x - x') \right] \exp \{ -\theta |x - x'| \} \right] \\
&= \left[\frac{1}{3} \theta^2 - \frac{2}{3} \theta^3 (x - x') (-1) \operatorname{sign}(x - x') \right] \exp \{ -\theta |x - x'| \} \\
&+ \left[-\frac{1}{3} \theta^2 (x - x') - \frac{1}{3} \theta^3 (x - x')^2 \operatorname{sign}(x - x') \right] \exp \{ -\theta |x - x'| \} (\theta \operatorname{sign}(x - x')) \\
&= \exp \{ -\theta |x - x'| \} \left[\frac{1}{3} \theta^2 + \frac{2}{3} \theta^3 |x - x'| - \frac{1}{3} \theta^3 |x - x'| - \frac{1}{3} \theta^4 (x - x')^2 \right] \\
&= \exp \{ -\theta |x - x'| \} \left[\frac{1}{3} \theta^2 + \frac{1}{3} \theta^3 |x - x'| - \frac{1}{3} \theta^4 (x - x')^2 \right] \\
&= \frac{1}{3} \theta^2 [1 + \theta |x - x'| - \theta^2 (x - x')^2] \exp \{ -\theta |x - x'| \}
\end{aligned}$$