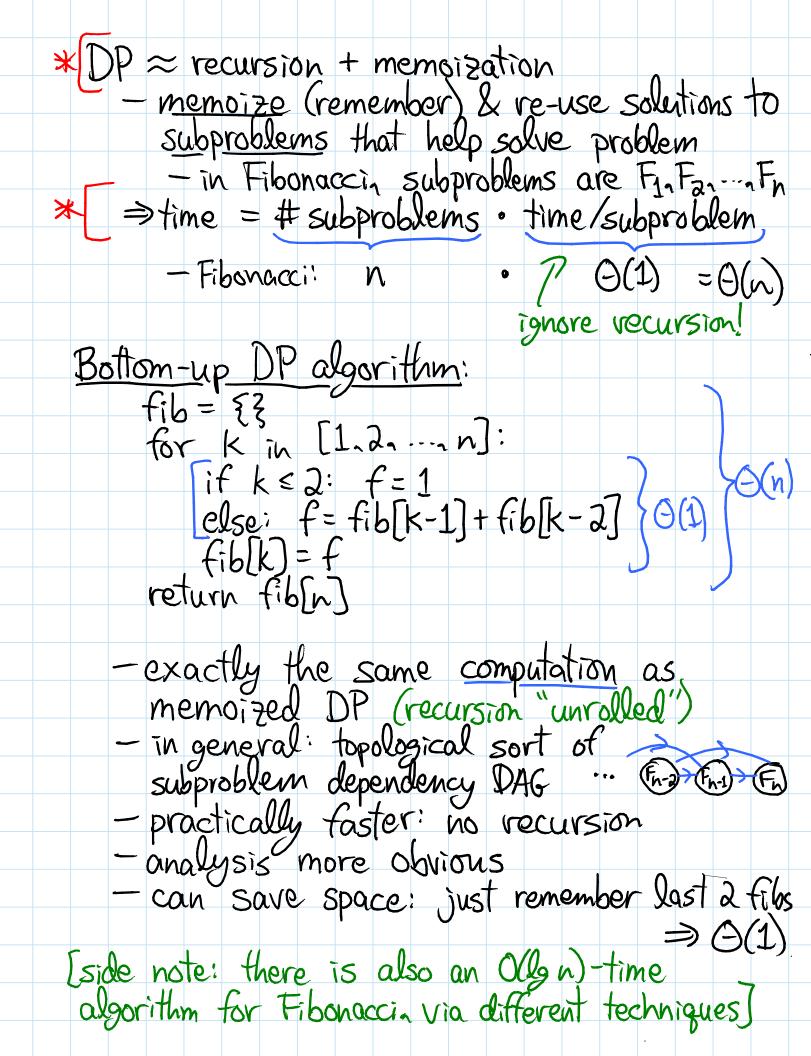
Nov. 22, 2011 Lecture 19 6.006TODAY: Dynamic Programming I (of 4)

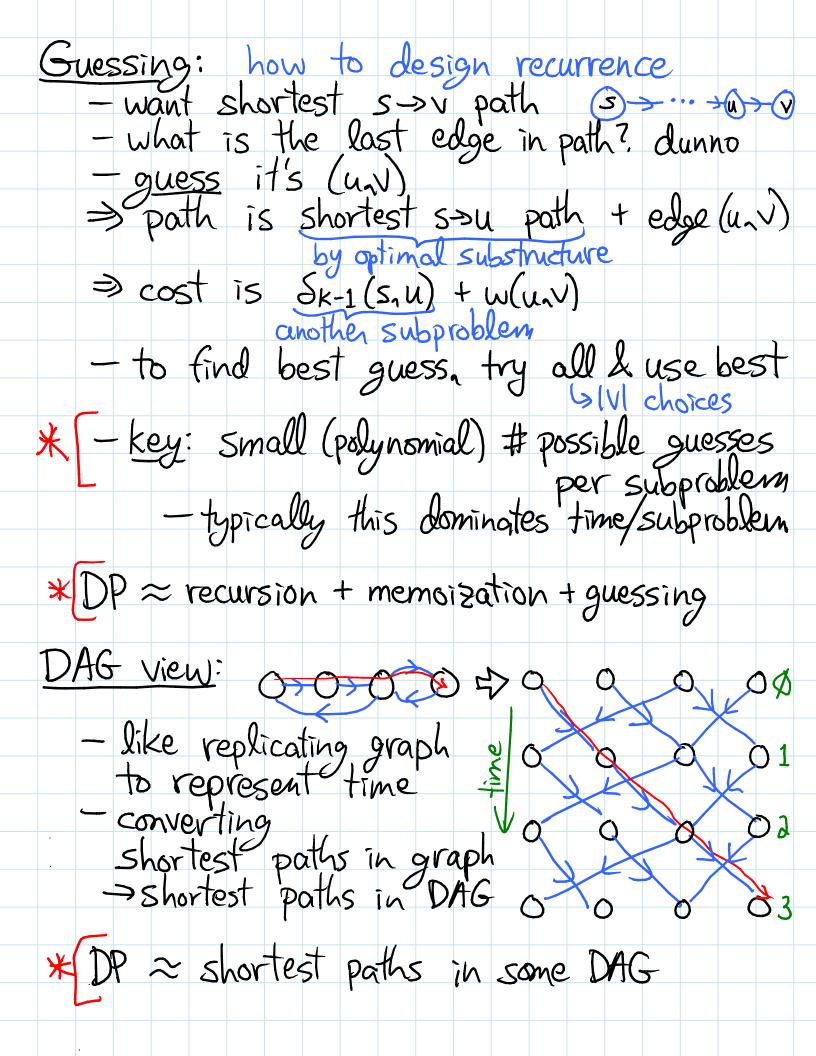
- memoization & subproblems: bottom up - Fibonacci
- shortest paths } examples - guessing & DAG view Dynamic programming: (DP) - big idea, hard yet simple powerful algorithmic design technique - large class of seemingly exponential problems have a polynomial solution ("only") via DP - particularly for optimization problems (min/max) (e.g. shortest paths) *DP ≈ careful brute force *DP ≈ recursion + 're-use'

> JEEE Medal of Honor, History: Richard E. Bellman (1920-1984) "Bellman ... explained that he invented the name dynamic programming to hide the fact that he was doing mathematical research at RAND under a Secretary of Defense who 'had a pathelogical fear and hatred of the term, research! He settled on the term dynamic programming because it would be difficult to give a 'pejorative meaning' and because 'It was something not even a Congressman could object to."
[John Rust 2006]

```
Fibonacci numbers: F1=F2=1: Fn=Fn-1+Fn-2
- goal: compute Fn
   Naïve algorithm: follow recursive definition
            Cif n \le 2: f=1
Lelse: f=fib(n-1)+fib(n-2)
return f
Fn-2Fn-3Fn-4
   \Rightarrow T(n) = T(n-1)+T(n-2)+O(1) \Rightarrow F<sub>n</sub> \approx \varphi<sup>n</sup> \Rightarrow 2T(n-2)+O(1) \Rightarrow 2<sup>N/2</sup> EXPONENTIAL - BAD!
   Memoized DP algorithm: remember remember
         fib(n):
              if n in memo: return memo[n]
            if n \le 2: f = 1
            else: f = fib(n-1) + fib(n-2)
            memo[n] = f
              return f
```



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