- 1) I am hoping that the variational expectation of the Cho et al paper for the beta parameter is wrong:
- 2) I cannot see much sparsity in the network I generate, it is actually quite well connected, but I am following the generative process. I was wondering how can we produce a sparser network using the same process. This is usually achieved when the hyperparameter α_k 's for the membership vector are set to small values.
- 3) I have to recheck the derivation of the lower bound. The increase in log likelihood is guaranteed. But I see from time to time very small glitches. I have two points of doubts, one in the first line about link probability, and the other one about the η, τ , in the derivations of the parameters especially.
- 4) I need to reconfirm the way I implement my sums regarding the derivations for the variational parameter updates. Especially the ones I go through links, and the ones I go through neighbors of each individual. The first has no double counts, but the second one has. The derivations don't imply any other ways. But I need to make sure about that.
- 5) If we are doing Variational EM, then this is all just the E-step, and we need to estimate the model parameters (hyperparameters) as well, so we need a way to estimate η_0, η_1 and also α . This requires the same maximization of the ELBO with respect to the model parameters, fixing the variational parameters. But the expressions are not analytical, I will need help with that. So in other places there are some suggestions for example for using Newton-Raphson method. Besides after updating the variational parameters, we should be able to reconstruct the actual parameters of the model in the mean field factorized distribution. I use some intuitive estimate for the parameters, such as θ and β . I also need to check this. For example we have to be able to reconstruct the Z from ϕ , or θ from γ , and β from τ . For $\theta_{a,k} = \frac{\gamma_{a,k}}{\sum_l \gamma_{a,l}}$, and for $\beta_{k,k} = \frac{\tau_{0,k}}{\tau_{0,k} + \tau_{1,k}}$. But I am not clear whether these are reasonable, plus I don't see much good output.

For now I am fixing the model parameters skip the M-step, and only doing the inference on the variational parameters, assuming I have the correct model parameters.

- 6) the problem of the smart/fast initializations of the global parameters still remains, for now I skipped it, because I expect the random initializations also should work. But it would be necessary to do this as it offers a good close enough number for K. But for now I use the correct number K of the ground truth.
- 7) Should I remove the parts in computing the ELBO, that are independent of the changes in the parameters, for example if I am updating the variational parameters where model parameters are untouched, can I skip those segments in the ELBO that are entirely a function of model parameters?
- 8) The ELBO behaves alright, but the values I am not sure if makes sense or not.
- 9)I do not exactly know how should I check the results. What should be the measure for evaluation? Should I use the estimated parameters to create links and memberships based on them to see how well I am doing?

- VISUALIZE HELP
 10) specify initializations
 11) The data given, is directed however, this will change the updates