

## Algebra Solution

**1. Answer: (C)**

$$x^4 + 1/x^4 = 1442$$

Add 2 from both side

$$x^4 + 1/x^4 + 2 = 1444$$

$$x^2 + 1/x^2 = 38$$

Subtract 2 from both side

$$x^2 + 1/x^2 - 2 = 36$$

$$x - 1/x = 6$$

**2. Answer: (B)**

$$\text{If } (3x - 7)^3 + (3x - 8)^3 + (3x + 6)^3 = 3(3x - 7)$$

$$(3x - 8)(3x + 6)$$

In these type of question go through option

$$x = 1$$

$$(3 - 7)^3 + (3 - 8)^3 + (3 + 6)^3 = 3(3 - 7)(3 - 8)(3 + 6)$$

$$540 = 540$$

Value for  $x = 1$  satisfied.

**3. Answer: (A)**

$$x + 1/x = 10$$

Cube both side

$$x^3 - 1/x^3 + 3(x - 1/x) = 1000$$

$$x^3 - 1/x^3 = 970$$

**4. Answer: (B)**

$$a^3 + b^3 = [a + b][a^2 + b^2 - ab] \quad \text{_____ (1)}$$

$$[a + b]^2 = a^2 + b^2 + 2ab$$

$$[a + b]^2 = 99 + 2 \times 11$$

$$a + b = 11$$

$$a^3 + b^3 = [a + b][a^2 + b^2 - ab]$$

$$a^3 + b^3 = [11][99 - 11]$$

$$a^3 + b^3 = 968$$

**5. Answer: (C)**

$$8[a + b]^3 + [a - b]^3 = [3a + b][Aa^2 + Bab + Cb^2]$$

$$[2(a + b)]^3 + [a - b]^3 = [3a + b][Aa^2 + Bab + Cb^2] = [3a + b][Aa^2 + Bab + Cb^2]$$

$$[2a + 2b + a - b][2(a + b)]^2 + [a - b] + (a + b) - (a - b)$$

$$= [3a + b][Aa^2 + Bab + Cb^2]$$

$$[3a + b][4a^2 + 4b^2 + 8ab + a^2 + b^2 - 2ab + 2a^2 - 2b^2] = [3a + b][Aa^2 + Bab + Cb^2]$$

$$[7a^2 + 3b^2 + 6ab] = [Aa^2 + Bab + Cb^2]$$

By comparing

$$A = 7, B = 6, C = 3$$

$$= A + B - C$$

$$= 7 + 6 - 3$$

$$= 10$$

**6. Answer: (B)**

$$x^2 - 6x + 1 = 0$$

Take x common

$$x + 1/x = 6 \quad \text{_____ (1)}$$

A.T.Q

$$= (x^4 + 1/x^2)/(x^2 + 1)$$

Multiply by x and divide is domination

$$(x^3 + 1/x^3)/(x + 1/x)$$

From (1)

$$x^3 + 1/x^3 = 198 \quad \text{_____ (2)}$$

From (2)

$$= 198/6 = 33$$

**7. Answer: (D)**

$$x + y + z = 3$$

S.B.S

$$x^2 + y^2 + z^2 + 2(xy + yz + zx) = 9$$

$$x^2 + y^2 + z^2 - 36 = 9$$

$$x^2 + y^2 + z^2 = 45 \quad \text{_____ (1)}$$

$$x^3 + y^3 + z^3 - 3xyz = (x + y + z)(x^2 + y^2 + z^2 - xy - yz - zx)$$

$$x^3 + y^3 + z^3 - 3xyz = 3(45 + 18)$$

$$x^3 + y^3 + z^3 - 3xyz = 189$$

**8. Answer: (D)**

$$[2x + 7]^3 + [2x + 8]^3 + [2x + 3]^3 = 3[2x + 7]$$

$$(2x + 8)[2x + 3]$$

In these types of questions go through option

$$\text{Let } x = -3$$

$$[2x - 3 + 7]^3 + [2x - 3 + 8]^3 + [2x - 3 + 3]^3$$

$$+ 3[2x - 3 + 7][2x - 3 + 8][2x - 3 + 3]$$

$$[1]^3 + [2]^3 + [-3]^3 = 3 \times 1 \times 2 \times (-3)$$

$$1 + 8 - 27 = -18$$

$$-18 = -18$$

the value of  $x = -3$  is satisfied

9. **Answer: (B)**

$$x = \sqrt{3} - \sqrt{2} \text{ --- (1)}$$

$$\frac{1}{x} = \sqrt{3} + \sqrt{2} \text{ --- (2)}$$

$$x - \frac{1}{x} = \sqrt{3} - \sqrt{2} - \sqrt{3} - \sqrt{2}$$

$$x - \frac{1}{x} = -2\sqrt{2}$$

Cube both side

$$x^3 - \frac{1}{x^3} - 3 \times x \times \frac{1}{x} \left[ x - \frac{1}{x} \right] = -16\sqrt{2}$$

$$x^3 - \frac{1}{x^3} = -22\sqrt{2}$$

10. **Answer: (A)**

We know that

$$\text{If } a^3 + b^3 + c^3 = 3abc$$

$$\Rightarrow a + b + c = 0$$

$$\text{So here, } (x+7)^3 + (2x+8)^3 + (2x+3)^3 = 3(x+7)(2x+8)(2x+3)$$

$$\Rightarrow (x+7) + (2x+8) + (2x+3) = 0$$

$$\Rightarrow 5x + 18 = 0$$

$$\Rightarrow x = -18/5 = -3.6$$

11. **Answer: (A)**

$$x = 2 - \sqrt{3}$$

$$\text{Now, } x - \frac{1}{x} = -2\sqrt{3}$$

$$\text{Also, } x + \frac{1}{x} = 4 \Rightarrow x^2 + \frac{1}{x^2} = 16 - 2 = 14$$

$$\text{So, } x^3 - \frac{1}{x^3} = x^3 - \frac{1}{x^3} = \left(x - \frac{1}{x}\right) \left(x^2 + \frac{1}{x^2} + 1\right)$$

$$= (-2\sqrt{3})(14+1)$$

$$= -30\sqrt{3}$$

12. **Answer: (D)**

$$(2x-7)^3 + (2x-8)^3 + (2x-3)^3 = 3(2x-7)(2x-8)(2x-3)$$

In these type of question it is better to go through option.

Let  $x = 3$

$$(2 \times 3 - 7)^3 + (2 \times 3 - 8)^3 + (2 \times 3 - 3)^3 = 3(2 \times 3 - 7)(2 \times 3 - 8)(2 \times 3 - 3)$$

$$(-1)^3 + (-2)^3 + (3)^3 = 3(-1)(-2)(3)$$

$$18 = 18$$

So, the value of  $x = 3$

13. **Answer: (A)**

$$x^4 + 1/x^4 = 1442$$

add 2 both side

$$x^4 + 1/x^4 + 2 = 1442$$

$$x^2 + 1/x^2 = 38$$

add 2 both side

$$x^2 + 1/x^2 + 2 = 40$$

$$\left[x + \frac{1}{x}\right]^2 = 40$$

$$x + 1/x = 2\sqrt{10}$$

14.

**Answer: (A)**

$$a^3 - b^3 = [a - b][a^2 + b^2 + ab] \text{ --- (1)}$$

A.T.Q

$$a^2 + b^2 = 135$$

subtract  $2ab$  from both side.

$$a^2 + b^2 - 2ab = 135 - 2 \times 7$$

$$[a - b]^2 = 121$$

$$a - b = 11$$

from (1)

$$a^3 - b^3 = [a - b][a^2 + b^2 + ab]$$

$$= 11[135 + 7]$$

$$= 11 \times 142$$

$$= 1562$$

15.

**Answer: (C)**

$$x = 2 + \sqrt{3}$$

$$1/x = 2 - \sqrt{3}$$

Then

$$x - \frac{1}{x} = 2\sqrt{3}$$

Cube both side

$$x^3 - \frac{1}{x^3} - 3 \times x \times \frac{1}{x} \left[ x - \frac{1}{x} \right] = 24\sqrt{3}$$

$$x^3 - \frac{1}{x^3} = 24\sqrt{3} + 3 \times 2\sqrt{3}$$

$$x^3 - \frac{1}{x^3} = 30\sqrt{3}$$

16.

**Answer: (D)**

$$(x-7)^3 + (2x+8)^3 + (2x-3)^3 = 3(x-7)(2x+8)(2x-3)$$

$$(x-7)^3 + (2x+8)^3 + (2x-3)^3 - 3(x-7)(2x+8)(2x-3) = 0$$

$$a + b + c = 0$$

$$a^3 + b^3 + c^3 - 3abc = 0$$

then

$$x - 7 + 2x + 8 + 2x - 3 = 0$$

$$5x = 2$$



$$x = 0.4$$

17. **Answer: (D)**

$$a^3 + b^3 = [a + b] [a^2 + b^2 - ab]$$

$$(a + b)^2 - 3ab = a^2 + b^2 + 2ab - 3ab$$

$$= a^2 + b^2 - ab$$

A.T.Q

$$1344 = 28[a^2 + b^2 - ab]$$

$$a^2 + b^2 - ab = 48$$

18. **Answer: (C)**

$$x^4 + \frac{1}{x^4} = 47$$

add 2 both side

$$x^4 + \frac{1}{x^4} + 2 = 49$$

Then

$$\left[ x^2 + \frac{1}{x^2} \right] = 7$$

Add 2 both side

$$x^2 + \frac{1}{x^2} + 2 = 9$$

$$x + \frac{1}{x} = 3$$

$$x^2 + 1 = 3x$$

multiply by 4 both side

$$4x^2 + 4 = 12x \quad (1)$$

A.T.Q

$$= [2x - 3]^2$$

$$= 4x^2 + 9 - 12x$$

Put the value of  $12x$  from (1)

$$= 4x^2 + 9 - 4x^2 - 4$$

$$= 5$$

19. **Answer: (C)**

$$x = 2 + \sqrt{5} \quad \text{--- (1)}$$

$$\frac{1}{x} = \sqrt{5} - 2 \quad \text{--- (2)}$$

From (1) and (2)

$$x - \frac{1}{x} = 2 + \sqrt{5} - \sqrt{5} + 2$$

$$x - \frac{1}{x} = 4$$

Cube both side

$$x^3 - \frac{1}{x^3} - 3 \times x \times \frac{1}{x} \left[ x - \frac{1}{x} \right] = 64$$

$$x^3 - \frac{1}{x^3} = 64 + 3 \times 4 = 76$$

20. **Answer: (C)**

$$(x - 8)^3 + (2x + 16)^3 + (2x - 13)^3 = 3(x - 8)(2x + 16)(2x - 13)$$

$$a^3 + b^3 + c^3 - 3abc = 0$$

$$a + b + c = 0$$

$$[x - 8]^3 + [2x + 16]^3 + [2x - 13]^3 - 3(x - 8)(2x + 16)(2x - 13) = 0$$

A.T.Q

$$x - 8 + 2x + 16 + 2x - 13 = 0$$

$$5x - 5 = 0$$

$$5x = 5$$

$$x = 1$$