# 模拟集成电路设计课程

# 第5章 电流镜与偏置技术

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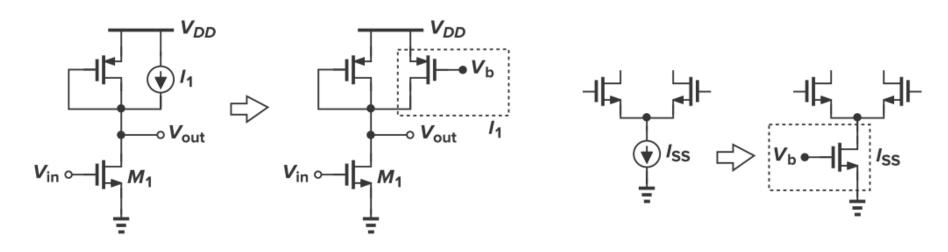
# 本章内容

- 5.1 基本电流镜
- 5.2 共源共栅电流镜
- 5.3 有源电流镜放大器
- 5.4 偏置技术 (自学)



### 5.1基本电流镜

- 工作在饱和区的MOS管可以当作电流源
- 电流源的要求:很大的输出电阻,且不消耗过多的电压余度



增大增益

尾电流源

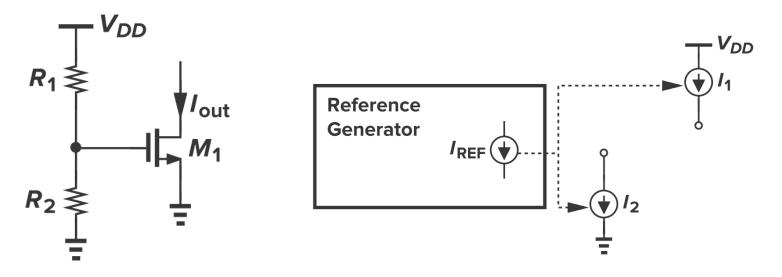


# 如何确定电流源的偏置?

• 电阻分压?

$$I_{out} \approx \frac{1}{2} \mu_n C_{ox} \frac{W}{L} \left( \frac{R_2}{R_1 + R_2} V_{DD} - V_{TH} \right)^2$$
 严重受PVT变化影响

• 即使给定了一个精确的栅源电压, 电流也无法准确确定

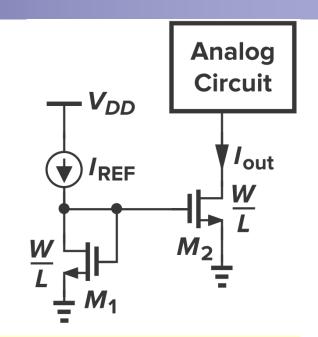


- 在模拟电路中, 电流源的设计是基于对基准电流的 "复制"
- 基准电流I<sub>REF</sub>由专门的基准产生电路提供



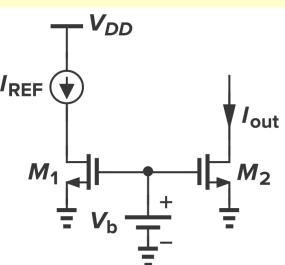
# 基本电流镜

• 忽略沟道长度调制效应



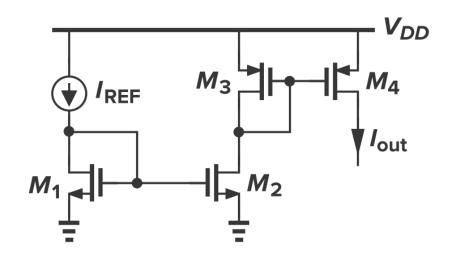
不受工艺和温度的影响, 仅与器件尺寸比率相关

• V<sub>GS</sub>必须由I<sub>REF</sub>产生,否则不能 /<sub>REF</sub> ◆ 完成电流复制





# 例5.1 $M_4$ 的漏电流?



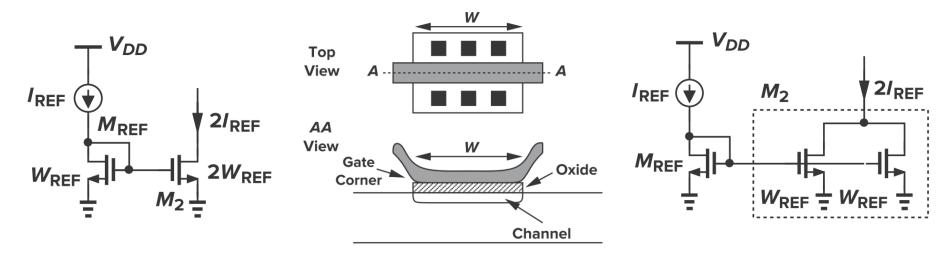
$$I_{D2} = I_{REF}[(W/L)_2/(W/L)_1]$$
 $|I_{D3}| = |I_{D2}|$ 
 $\Rightarrow |I_{D4}| = \alpha \beta I_{REF}$ 
 $I_{D4} = I_{D3} \times [(W/L)_4/(W/L)_3]$ 
 $\alpha = (W/L)_2/(W/L)_1$ 
 $\beta = (W/L)_4/(W/L)_3$ 

应避免长的电流镜链

可放大或缩小IREF



# 如何设计电流镜的尺寸?

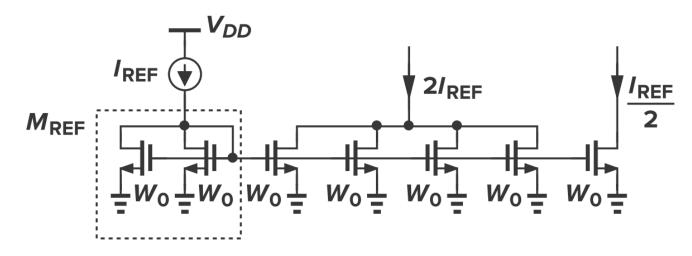


- 电流镜中的所有晶体管都采用相同的栅长
  - 保证相同的L<sub>eff</sub>
  - 短沟道器件的阈值电压对沟道长度有一定的依赖性
- 电流值之比只能通过调节晶体管的宽度来实现
- 采用"单元"晶体管,重复此器件实现电流复制

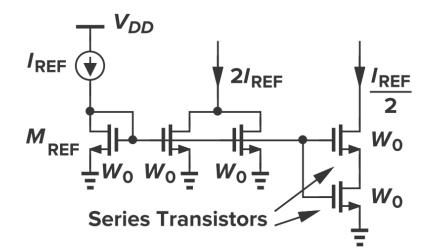


# 如何产生I<sub>REF</sub>/2的电流

• 二极管连接器件本身由两个"单元"器件构成



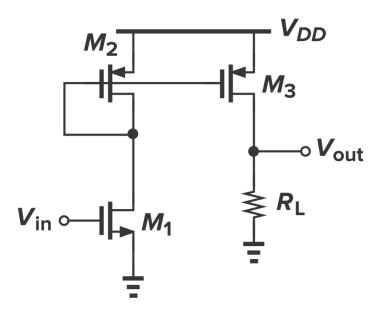
• 如果要生成多个电流,也可通过缩放沟道长度实现





# 例5.2 电流镜作为放大器

• 计算小信号增益

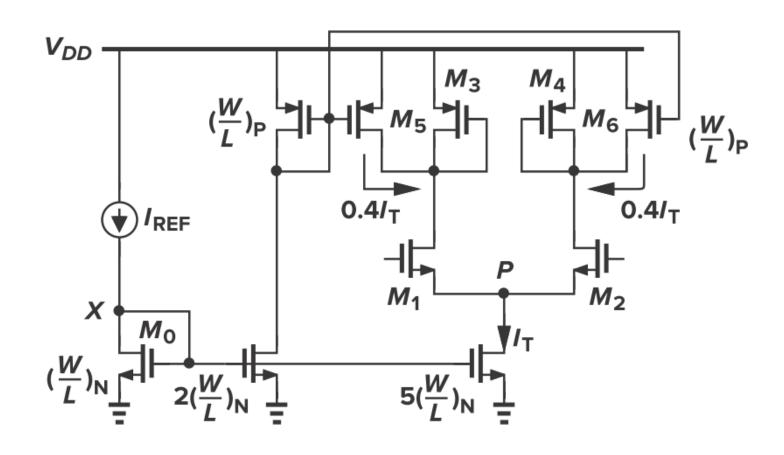


$$A_v = g_{m1}R_L(W/L)_3/(W/L)_2$$

以功耗为代价!



# 基本电流镜应用实例





# 基本电流镜的问题

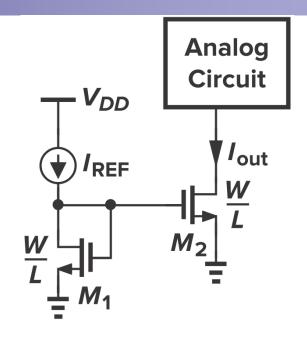
#### • 考虑沟道长度调制效应

$$I_{D1} = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L}\right)_1 (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS1})$$

$$I_{D2} = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L}\right)_2 (V_{GS} - V_{TH})^2 (1 + \lambda V_{DS2})$$

$$\implies \frac{I_{D2}}{I_{D1}} = \frac{(W/L)_2}{(W/L)_1} \cdot \frac{1 + \lambda V_{DS2}}{1 + \lambda V_{DS1}}$$

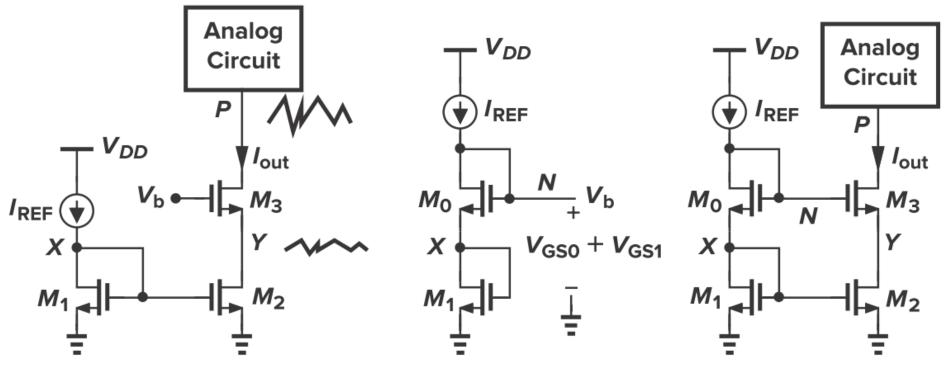
$$V_{DS1} = V_{GS1} = V_{GS2} \neq V_{DS2}$$



- 设计电路使得V<sub>DS1</sub>和V<sub>DS2</sub>相等
  - 迫使V<sub>DS2</sub>等于V<sub>DS1</sub>
  - 迫使V<sub>DS1</sub>等于V<sub>DS2</sub>



# 共源共栅电流镜



- 共源共栅器件可以起屏蔽作用,减小 $V_v$ 电压的变化
- $V_b V_{GS3} = V_{DS2} = V_{GS1} \implies V_b = V_{GS3} + V_{GS1}$
- 通过设计 $M_0$ 和 $M_3$ 的宽长比使得 $V_{GS0} = V_{GS3}$



# 例 5.3

• 画出 $V_X$ 和 $V_Y$ 与 $I_{REF}$ 的函数关系草图, 电流源两端需要的电压为 $0.5V_f$ ,求出 最大 $I_{REF}$ 

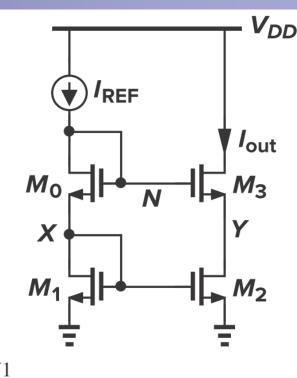
$$V_Y = V_X \approx \sqrt{2I_{REF}/[\mu_n C_{ox}(W/L)_1]} + V_{TH1}$$

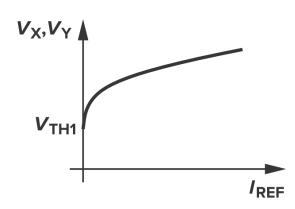
$$V_N = V_{GS0} + V_{GS1}$$

$$= \sqrt{\frac{2I_{REF}}{\mu_n C_{ox}}} \left[ \sqrt{\left(\frac{L}{W}\right)_0} + \sqrt{\left(\frac{L}{W}\right)_1} \right] + V_{TH0} + V_{TH1}$$

$$= \sqrt{\frac{2I_{REF}}{\mu_n C_{ox}}} \left[ \sqrt{\left(\frac{L}{W}\right)_0} + \sqrt{\left(\frac{L}{W}\right)_1} \right] + V_{TH0} + V_{TH1}$$

$$I_{REF,max} = \frac{\mu_n C_{ox}}{2} \frac{(V_{DD} - 0.5 \text{ V} - V_{TH0} - V_{TH1})^2}{(\sqrt{(L/W)_0} + \sqrt{(L/W)_1})^2}$$





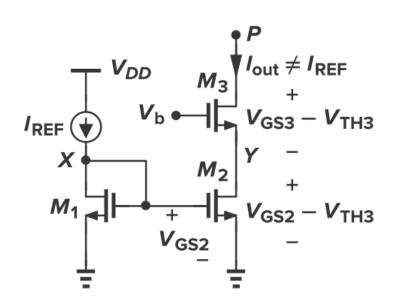


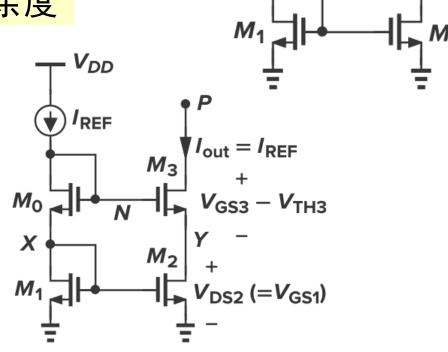
# 电压余度分析

• P点允许的最小电压为

$$V_N - V_{TH} = V_{GS0} + V_{GS1} - V_{TH}$$
  
=  $(V_{GS0} - V_{TH}) + (V_{GS1} - V_{TH}) + V_{TH}$ 

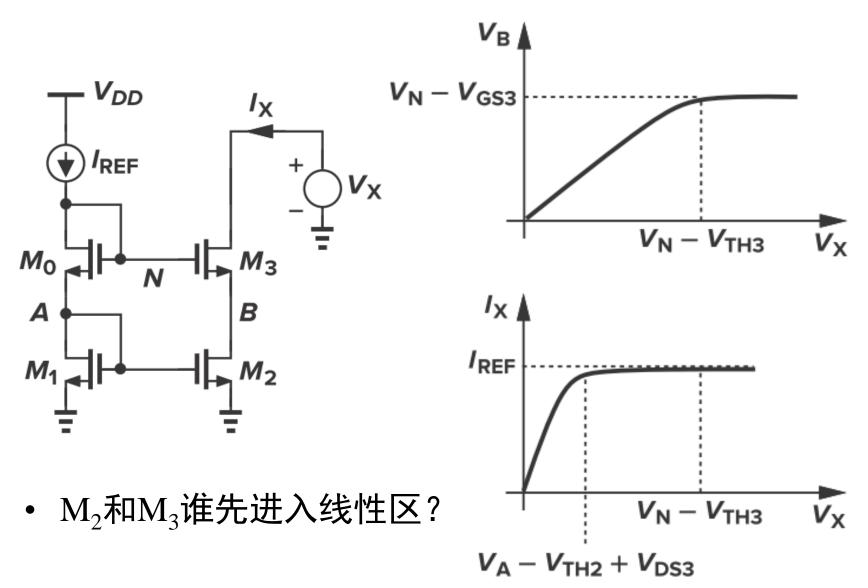
#### 浪费了一个阈值电压的余度







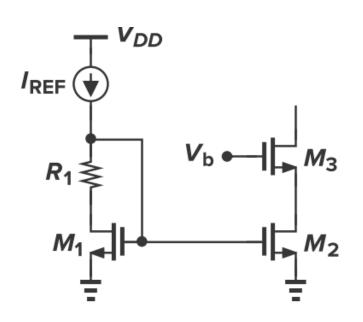
# 例5.4 大信号分析

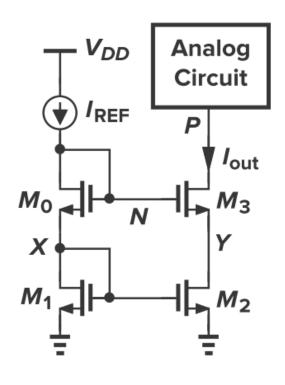




# 如何减小电压余度的损失?

- · 希望V<sub>DS2</sub>只消耗一个过驱动电压
- 如何使 $V_{DS1}$ 只消耗一个过驱动电压?





很难保证

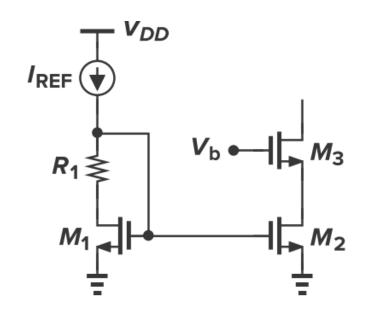
$$R_1I_{REF} \approx V_{TH1} \Longrightarrow V_{DS1} = V_{GS1} - R_1I_{REF} \approx V_{GS1} - V_{TH1}$$

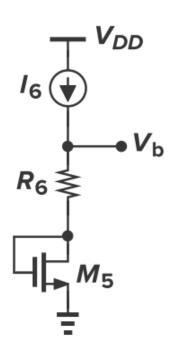
$$V_b = V_{GS3} + (V_{GS1} - V_{TH1}) \Longrightarrow V_{DS1} = V_{DS2}$$



# 如何产生Vb

$$V_b = V_{GS3} + (V_{GS1} - V_{TH1})$$





$$V_{b} = V_{GS5} + R_{6}I_{6}$$

$$V_{GS5} = V_{GS3}$$

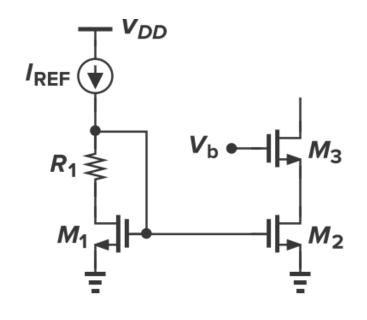
$$R_{6}I_{6} = V_{GS1} - V_{TH1} = V_{GS1} - R_{1}I_{REF}$$

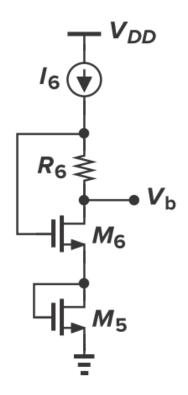
很难实现!



# 如何产生Vb

$$V_b = V_{GS3} + (V_{GS1} - V_{TH1})$$



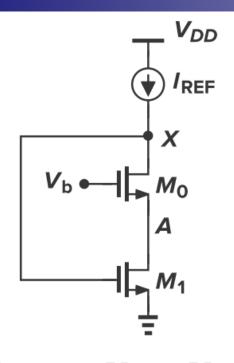


$$V_{GS5} = V_{GS3}$$

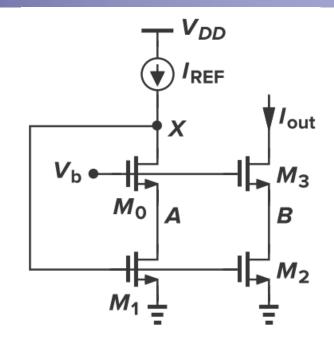
$$V_{GS6} - R_6 I_6 = V_{GS1} - V_{TH1} = V_{GS1} - R_1 I_{REF}$$



# 低压共源共栅电流镜



$$V_{DS1} = V_b - V_{GS0}$$



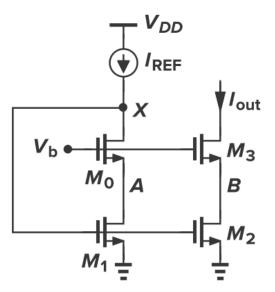
$$V_{GS0} = V_{GS3}$$

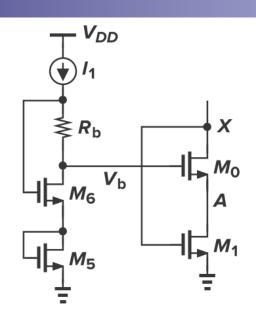
低压共源共栅结构

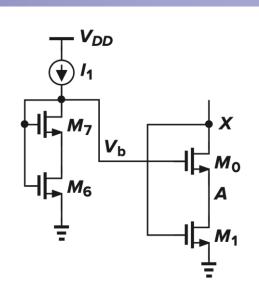
- 如何选择V<sub>b</sub>?
- 如何产生 $V_b$ ?



### 低压共源共栅电流镜







• 如何选择 $V_b$ ?

 $M_0$ 工作在饱和区  $\Longrightarrow V_b - V_{TH0} \leq V_X (= V_{GS1})$ 

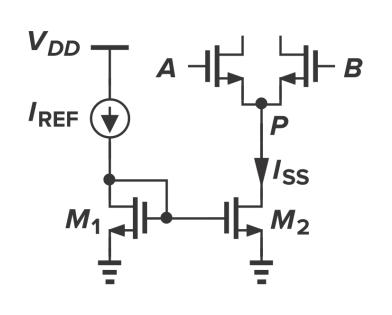
$$V_{GS0} + (V_{GS1} - V_{TH1}) \le V_b \le V_{GS1} + V_{TH0}$$

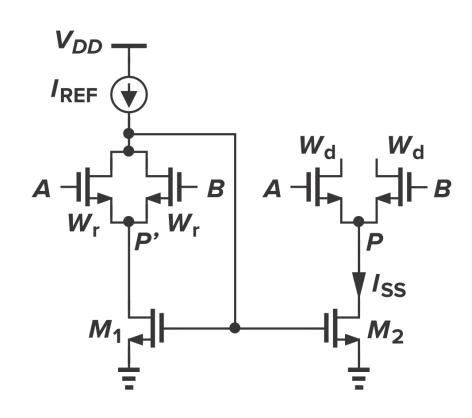
• 如何产生 $V_b$ ?



# 例 5.6 基本电流镜的改进

• 无法使用共源共栅电流镜

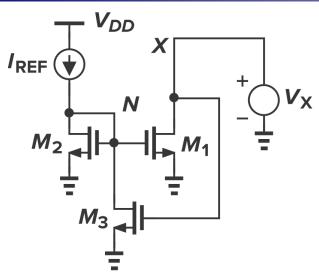


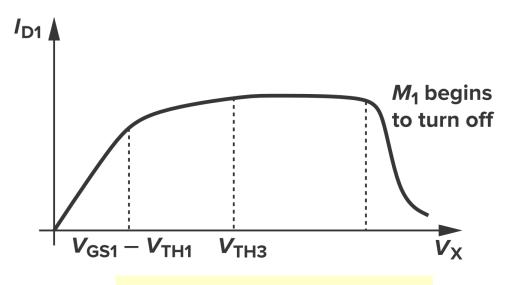


- 设法使V<sub>DS1</sub>等于V<sub>DS2</sub>
- A点和B点共模输入电平不可过大,否则复制的差动对进入线性区,引入误差



# 例 5.7 另一种高输出阻抗的电流镜





• 小信号特性?

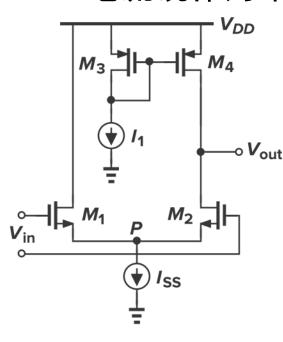
有电压余度限制, $V_X > V_{TH3}$ 

• 大信号特性?

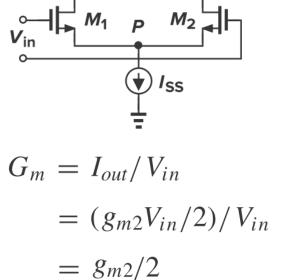


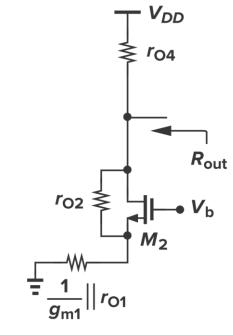
# 5.3 有源电流镜

电流镜作为单端输出差动放大器的电流源负载



 $|A_v| = G_m R_{out}$ 





$$= I_{out}/V_{in} R_{deg} = (1/g_{m1})||r_{O1}|$$

$$= (g_{m2}V_{in}/2)/V_{in} R_{out} = [(1 + g_{m2}r_{O2})\bar{R}_{deg} + r_{O2}]$$

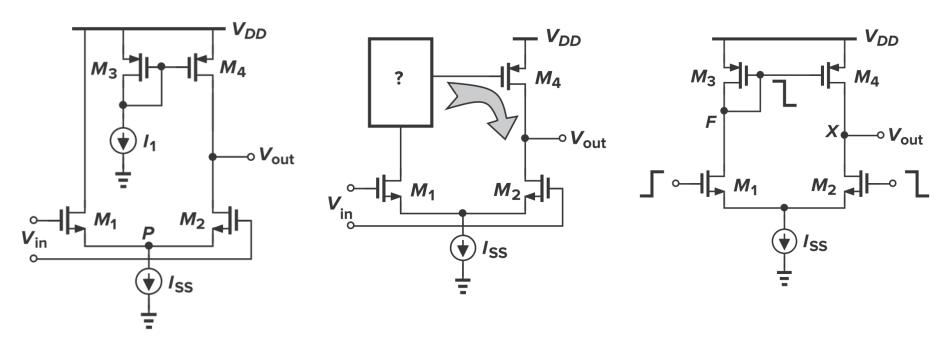
$$= g_{m2}/2 ||r_{O4}||$$

$$= (2r_{O2})||r_{O4}||$$

$$|A_v| = \frac{g_{m2}}{2}[(2r_{O2})||r_{O4}]$$



# 有源负载差动对

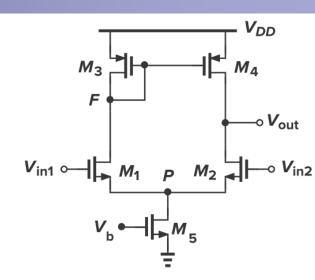


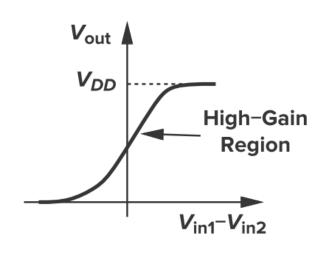
- M₁的小信号漏电流被浪费了
- 如何把这部分电流利用起来?
- 五管 $OTA: M_3$ 和 $M_4$ 相同且构成有源电流镜
- M<sub>3</sub>如何提高增益的?



### 大信号分析

- 当 $V_{in1}$ 比 $V_{in2}$ 小很多,  $M_1$ ,  $M_3$ 和 $M_4$ 均关断。没有电流能从 $V_{DD}$ 流出, $M_2$ 和 $M_5$ 都工作在深线性区, $V_{out}=0$ 。
- 当 $V_{in1}$ 接近 $V_{in2}$ ,  $M_1$ 导通,使 $I_{D5}$ 的一部分流过 $M_3$ ,使 $M_4$ 导通。 $V_{out}$ 开始依赖于 $I_{D4}$ 和 $I_{D2}$ 之间的差值。
- 当 $V_{in1}$ 和 $V_{in2}$ 非常接近时, $M_2$ 和 $M_4$ 都工作在饱和区,小信号增益很高。
- 当V<sub>in1</sub>大于V<sub>in2</sub>时, I<sub>D4</sub>增大而I<sub>D2</sub>减小,
   V<sub>out</sub>增大,最终使M<sub>4</sub>进入线性区。
- 当 $V_{in1}$ 比 $V_{in2}$ 大很多, $M_2$ 关断, $M_4$ 的 电流为0且工作的深线性区, $V_{out} = V_{DD}$

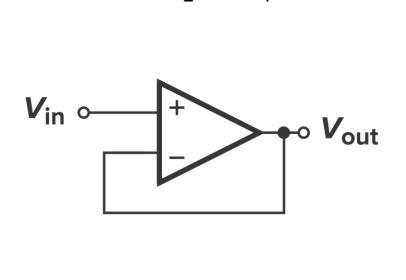


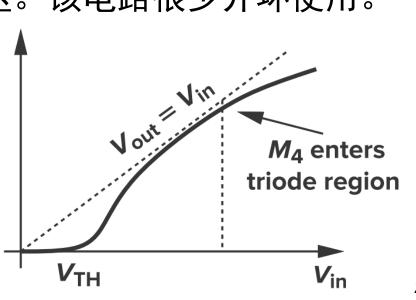




### 输入/输出共模电平

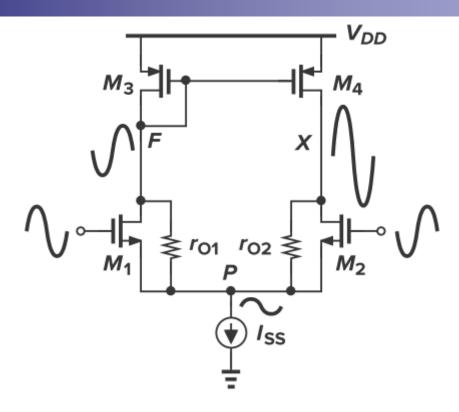
- 为了得到最大摆幅,输入共模电平 应该尽可能低,最低值为 $V_{GS1,2} + V_{DS5,min}$
- 输入共模电平对输出摆幅的限制是 此电路的一个严重缺点
- 如果电路完全对称, $V_{out} = V_F = V_{DD} |V_{GS3}|$
- 由于电路存在不对称,会导致 $V_{out}$ 产生一个大的偏差,容易使 $M_2$ 或 $M_4$ 进入线性区。该电路很少开环使用。







# 小信号分析

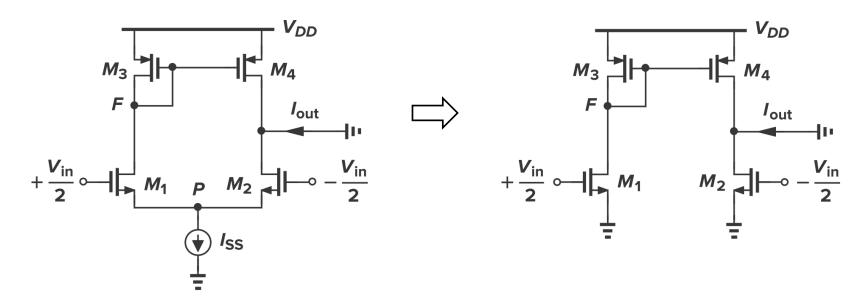


- 能否使用半边电路方法分析?
- Y点的电压变化幅度比F点大,左边是二极管连接负载, 右边类似电流源负载



# 近似分析

• 计算G<sub>m</sub>



节点F的摆幅很小,F点对P点的影响可以忽略不计, P点可近似看成虚地点

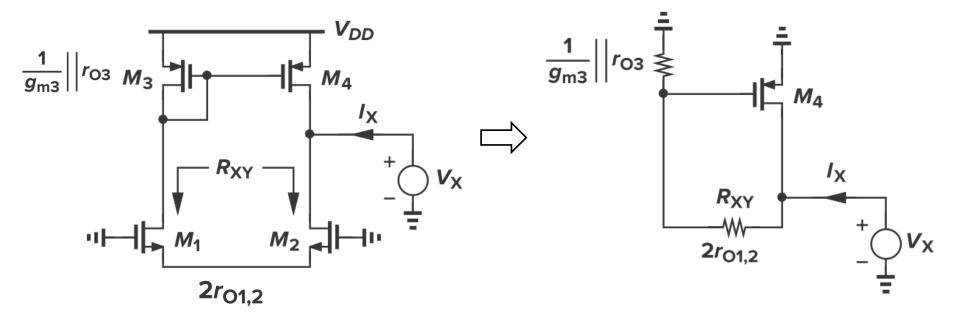
$$I_{D1} = |I_{D3}| = |I_{D4}| = g_{m1,2}V_{in}/2$$

$$I_{D2} = -g_{m1,2}V_{in}/2 \qquad \Longrightarrow I_{out} = -g_{m1,2}V_{in} \Longrightarrow |G_m| = g_{m1,2}$$



# 近似分析

#### • 计算R<sub>out</sub>



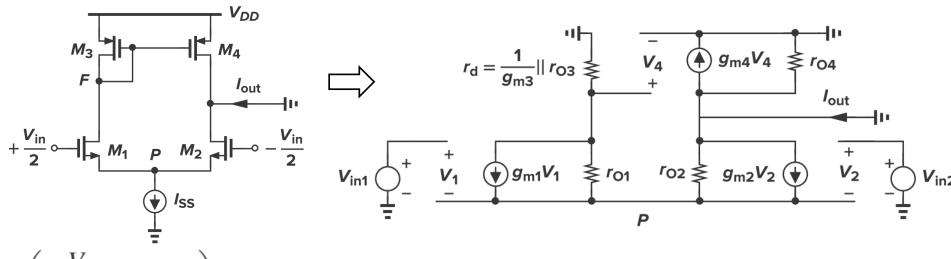
$$I_X = \frac{V_X}{2r_{O1,2} + \frac{1}{g_{m3}}||r_{O3}|} \left[ 1 + \left( \frac{1}{g_{m3}}||r_{O3} \right) g_{m4} \right] + \frac{V_X}{r_{O4}}$$

$$R_{out} \approx r_{O2} \| r_{O4} \qquad \Rightarrow |A_v| = G_m R_{out} = g_{m1,2} (r_{O2} \| r_{O4})$$



# 精确分析

#### • 计算G<sub>m</sub>



$$\left(-\frac{V_4}{r_d} - g_{m1}V_1\right)r_{O1} + V_{in1} - V_1 = V_4$$

$$g_{m2}V_2 - \frac{V_{in2} - V_2}{r_{O2}} = \frac{V_4}{r_d}$$

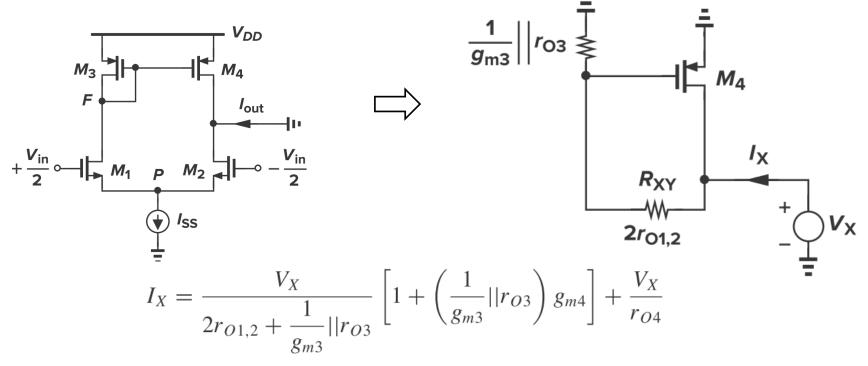
$$V_1 - V_2 = V_{in1} - V_{in2}$$

$$I_{out} = g_{m4}V_4 + V_4/r_d$$



# 精确分析

#### • 计算R<sub>out</sub>



$$G_m R_{out} = -g_{m1} r_{O1} \frac{(g_{m4} r_d + 1) r_{O4}}{(g_{m4} r_d + 1) r_{O4} + 2r_{O1} + r_d}$$



# 精确分析

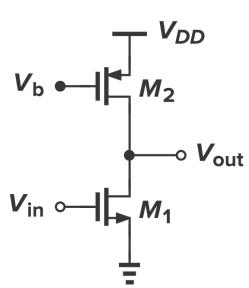
• 计算G<sub>m</sub>R<sub>out</sub>

$$G_m R_{out} = -g_{m1} r_{O1} \frac{(g_{m4} r_d + 1) r_{O4}}{(g_{m4} r_d + 1) r_{O4} + 2r_{O1} + r_d}$$

$$G_{m}R_{out} = -g_{m1}r_{O1}r_{O4} \frac{2g_{m3}r_{O3} + 1}{(2g_{m3}r_{O3} + 1)r_{O4} + 2r_{O1}(1 + g_{m3}r_{O3}) + r_{O3}}$$

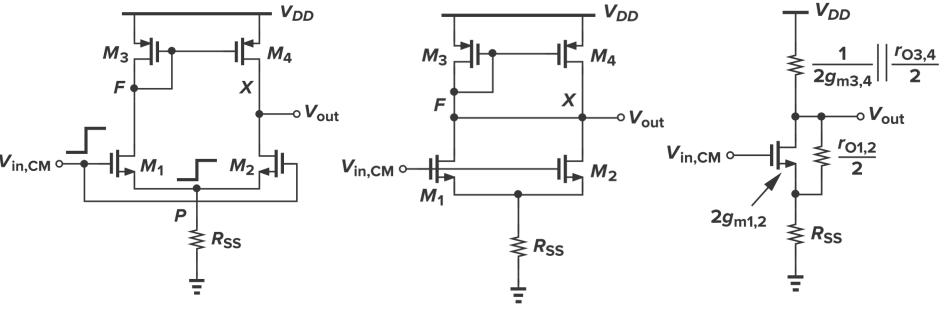
$$= -\frac{g_{m1}r_{O1}r_{O4}}{r_{O1} + r_{O3}} \cdot \frac{2g_{m3}r_{O3} + 1}{2(g_{m3}r_{O3} + 1)}$$

$$V_{b} \qquad V_{DD}$$





# 共模特性



• 共模增益: 输入共模电平的变化产生的单端输出的变化

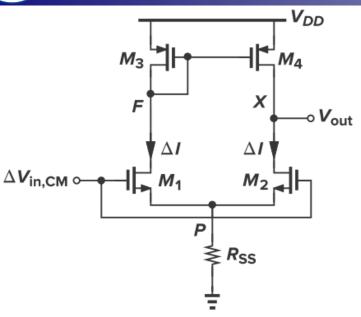
$$A_{CM} = \frac{\Delta V_{out}}{\Delta V_{in,CM}}$$

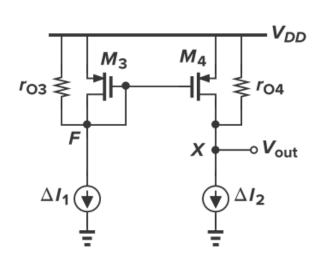
• 不考虑M<sub>1</sub>和M<sub>2</sub>的沟道长度调制效应

$$A_{CM} \approx \frac{-\frac{1}{2g_{m3,4}} \left\| \frac{r_{O3,4}}{2}}{\frac{1}{2g_{m1,2}} + R_{SS}} = \frac{-1}{1 + 2g_{m1,2}R_{SS}} \frac{g_{m1,2}}{g_{m3,4}}$$



### 共模特性



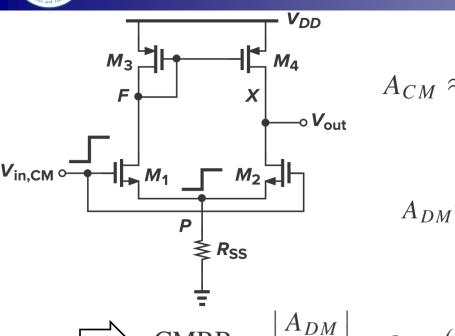


#### • 为什么共模增益不是0?

$$\Delta V_F = \Delta I_1 \left( \frac{1}{g_{m3}} \middle| r_{O3} \right) \Longrightarrow |\Delta I_{D4}| = g_{m4} \Delta V_F = g_{m4} \Delta I_1 \frac{r_{O3}}{1 + g_{m3} r_{O3}}$$



#### 共模特性



$$A_{CM} \approx \frac{-\frac{1}{2g_{m3,4}} \left\| \frac{r_{O3,4}}{2}}{\frac{1}{2g_{m1,2}} + R_{SS}} = \frac{-1}{1 + 2g_{m1,2}R_{SS}} \frac{g_{m1,2}}{g_{m3,4}}$$

$$A_{DM} = g_{m1}(r_{O1}||r_{O4})$$

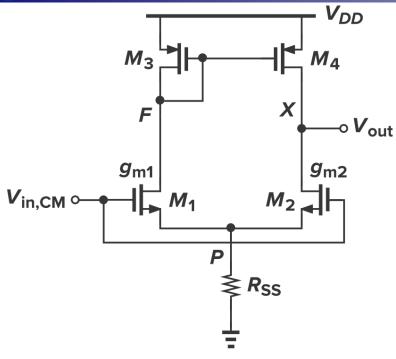
CMRR的数量级是 
$$(g_m r_o)^2$$

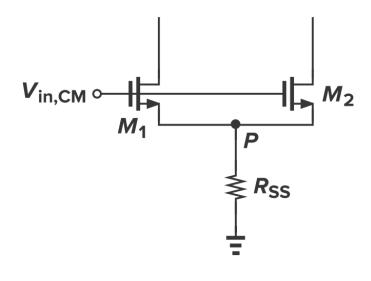
$$= (1 + 2g_{m1,2}R_{SS})g_{m3,4}(r_{O1,2}||r_{O3,4})$$

 即使完全匹配,输出信号也会因为输入信号共模变化 而变差,特别是在高频时。



#### 失配的影响





$$\Delta V_P = \Delta V_{in,CM} \frac{R_{SS}}{R_{SS} + \frac{1}{g_{m1} + g_{m2}}} \qquad \Longrightarrow$$

$$\Delta I_{D1} = g_{m1}(\Delta V_{in,CM} - \Delta V_P)$$

$$= \frac{\Delta V_{in,CM}}{R_{SS} + \frac{1}{g_{m1} + g_{m2}}} \frac{g_{m1}}{g_{m1} + g_{m2}}$$

$$\Delta I_{D2} = g_{m2}(\Delta V_{in,CM} - \Delta V_P)$$

$$= \frac{\Delta V_{in,CM}}{R_{SS} + \frac{1}{g_{m1} + g_{m2}}} \frac{g_{m2}}{g_{m1} + g_{m2}}$$



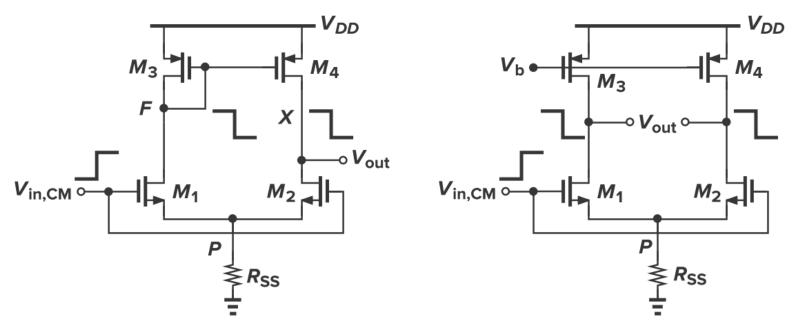
### 失配的影响

$$|\Delta I_{D4}| = g_{m4}[(1/g_{m3})||r_{O3}]\Delta I_{D1}$$

$$\stackrel{r_{O3} \gg 1/g_{m3}}{\Longrightarrow} \frac{\Delta V_{out}}{\Delta V_{in,CM}} \approx \frac{(g_{m1} - g_{m2})r_{O3} - g_{m2}/g_{m3}}{1 + (g_{m1} + g_{m2})R_{SS}}$$



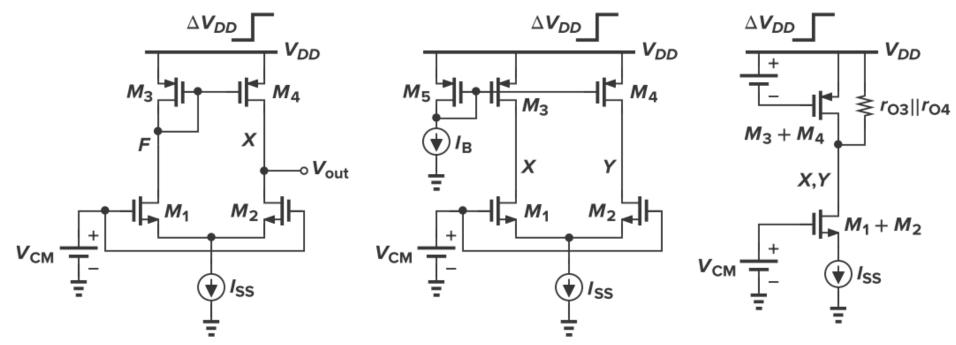
# 五管OTA与全差分结构的对比



- · 五管OTA的两个缺点:
  - 即使电路完全匹配, 电路的CMRR仍然有限



# 五管OTA与全差分结构的对比



- · 五管OTA的两个缺点:
  - 即使电路完全匹配, 电路的CMRR仍然有限
  - 电源抑制性能较差



# 本章总结

- 基本电流镜
  - 电流仅于晶体管宽长比的比率有关
  - 采用"单元"晶体管实现比例的缩放
  - 精度受到沟道长度调制效应影响
- 共源共栅电流镜
  - 电压余度问题
  - 低压共源共栅结构
- 有源电流镜(五管OTA)
  - 大信号分析
  - 小信号分析
  - 共模特性

# Thank you

程林

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