

# Lecture 8 (Informed Search)

## 1 Greedy Best-First Search

Best-first search but  $f(n) = h(n)$

## 2 $A^*$ Search

Combines UCS and Greedy Best-First Search by using  $f(n) = g(n) + h(n)$ , where  $g(n)$  is cost incurred until now. Surprisingly this algo is optimal for tree-search if heuristic is admissible.

### 2.1 Admissible Heuristic

Let  $h^*(n)$  be actual shortest path.  $h$  is admissible if  $h(n) \leq h^*(n) \forall n$ . Only those heuristics are optimal (in  $A^*$  search) which are admissible.

### 2.2 Consistent Heuristic

An admissible heuristic is consistent if for every state  $s$  and for every successor  $s'$ ,  $h(s) \leq c(s, s') + h(s')$  (inspired from triangle inequality). This implies that  $f(n)$  only increases along the path and the **graph-search** algo also gives optimal solution.

### 2.3 Properties

1. Optimal - graph search too for consistent heuristics
2. Solution will be found if:
  - i.  $b$  is finite
  - ii.  $c(step) \geq \delta$
  - iii. only finite nodes have cost  $\leq C^*$  (least cost)
3. Complexity:  $O(b^{ed})$  where  $b^e$  is effective branching factor,  $e$  is given as:  $\frac{h^* - h}{h^*}$
4.  $A^*$  search is optimally efficient, i.e., with a given heuristic, no other algorithm will be able to expand a fewer nodes.
5. Space is still exponential in length of the solution