

2. COL703: Major-Q2 09:50-10:10, late submission accepted till 10:15, 5+(1+4) = 10 marks

Let Σ be a non-empty signature containing two or more function symbols.

- (a) Prove that two terms s and t are unifiable iff for every position $p \in \text{pos}(s) \cap \text{pos}(t)$, $\text{rootsym}(s|_p) \neq \text{rootsym}(t|_p)$ implies at least one of the symbols $\text{rootsym}(s|_p)$ or $\text{rootsym}(t|_p)$ is a variable.
- (b) Let $S = \{s_1, \dots, s_n\}$ be a set of terms with $n > 2$. Then
 - i. S is unifiable iff _____.
Complete this sentence.
 - ii. Prove your statement of the above part.