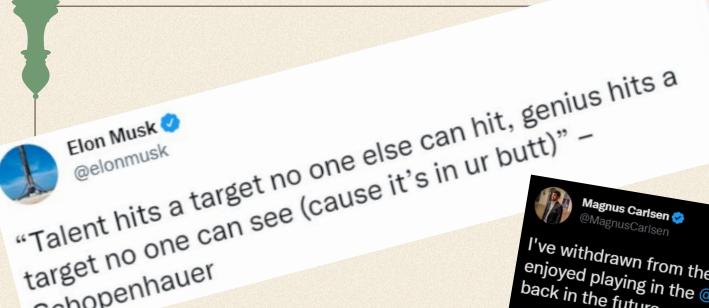


Predicting Performance in Chess via Regression and Statistical Inference Methodologies





Schopenhauer





I've withdrawn from the tournament. I've always enjoyed playing in the @STLChessClub, and hope to be back in the future

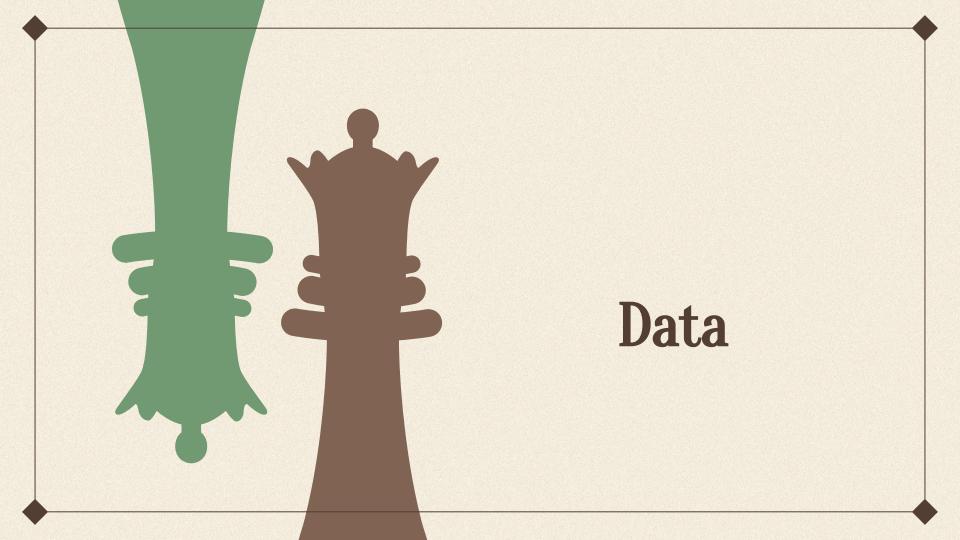


youtube.com

...

If I speak I am in big trouble-Mourinho Twitter-https://twitter.com/LFCBenji10

2:00 PM · Sep 5, 2022



Data Gathering



Tomashevsky, Evgeny

Xiong, Jeffery

USA

2692 0

2000



Players

<u>A-L</u>		<u>M-Z</u>	
Adams.pgn Download View	Michael Adams, 3380 games	MacKenzie.pgn Download View	George MacKenzie, 198 games
Akobian.pgn Download View	Varuzhan Akobian, 1429 games	Malakhov.pgn Download View	Vladimir Malakhov, 1973 games
Akopian.pgn Download View	Vladimir Akopian, 1957 games	Mamedyarov.pgn	Shakhriyar Mamedyarov, 4029 game

Resulting Dataset

Data

Contains information on over-the-board chess games played by 31 players

Key Variables

- <u>Elo</u> player's Elo (ranking) before the game
- Opponent Elo the Elo of the opponent the player is playing against
- Mean Centipawn Loss number of hundredths of a pawn by which a player deviated from the most accurate move calculated by a computer averaged over all moves in the game
- Standard Deviation in Centipawn Loss standard deviation in the number of hundredths of a pawn by which a player deviated from the most accurate move calculated by a computer for all moves in the game

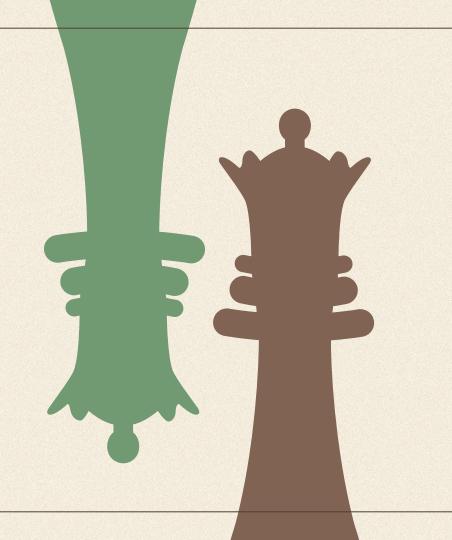


Standard Deviation in Centipawn Mean Centipawn Loss Standard Deviation in Centipawn Loss in a Game Mean Centipawn Loss

Exploring Centipawn Loss

- Mean Centipawn Loss ranges from 2 CP to 119 CP
 - Centered around CP of 14 to33
- Standard Deviation in Centipawn Loss ranges from 4.77 CP to 431.85 CP
 - Centered around CP of 19.52
 to 56.15





What are the best predictors for how well and consistently a chess player performs?

Linear Regression w/ Outliers

Normalizing response variables by applying a natural log transformation:

With the OLS step forward regression method (provided by the olsrr library), we can select the subset of variables to create the best linear regression models predicting Mean CP and SD CP from the following full models:

$$\begin{aligned} \text{MeanCP}_{\mathbf{i}} &= \boldsymbol{\beta}_0 + \boldsymbol{\beta}_1 \cdot \text{StdCP}_{\mathbf{i}} + \boldsymbol{\beta}_2 \cdot \text{Elo}_{\mathbf{i}} + \boldsymbol{\beta}_3 \cdot \text{OppElo}_{\mathbf{i}} + \boldsymbol{\beta}_4 \cdot \text{Age OR Time}_{\mathbf{i}} + \boldsymbol{\epsilon}_{\mathbf{i}} \\ & \text{where } \boldsymbol{\epsilon}_{\mathbf{i}} \in N(0, \, \sigma^2) \text{ iid} \end{aligned}$$

$$\begin{array}{l} \textbf{StdCP}_{i} = \boldsymbol{\beta}_{0} + \boldsymbol{\beta}_{1} \cdot \textbf{MeanCP}_{i} + \boldsymbol{\beta}_{2} \cdot \textbf{Elo}_{i} + \boldsymbol{\beta}_{3} \cdot \textbf{OppElo}_{i} + \boldsymbol{\beta}_{4} \cdot \textbf{Age OR Time}_{i} + \boldsymbol{\epsilon}_{i} \\ & \text{where } \boldsymbol{\epsilon}_{i} \subseteq \textbf{N}(0, \, \boldsymbol{\sigma}^{2}) \text{ iid} \\ \end{array}$$

Linear Regression w/ Outliers

Optimal regression equation with step forward variable selection (best model chosen based on R², Predicted R², Adjusted R², AIC, Mallow's Cp):





INTERPRETATION:

On average, given identical player Elos, with every 1% increase in Std CP, Mean CP increases by $(1.01^{0.745} - 1) * 100$, or 0.744%, and on average, given identical Std CPs, with every point increase in player Elo, Mean CP increases by $(e^{-0.0002} - 1) * 100$, or -0.016%.

Linear Regression w/o Outliers

Repeating the same model selection process after removing Mean CP and Std CP outliers from the dataset:



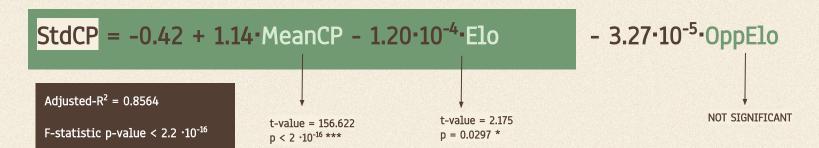


INTERPRETATION:

On average, given identical player Elos, with every 1% increase in Std CP, Mean CP increases by $(1.01^{0.74} - 1) * 100$, or 0.742%, and on average, given identical Std CPs, with every 1 point increase in player Elo, Mean CP increases by $(e^{-0.000159} - 1) * 100$, or -0.016%.

Linear Regression w/ Outliers

Optimal regression equation with step forward variable selection (best model chosen based on R², Predicted R², Adjusted R², AIC, Mallow's Cp):





INTERPRETATION:

On average, given identical player Elos, with every 1% increase in Mean CP, Std CP increases by $(1.01^{1.14} - 1) * 100$, or 1.141%, and on average, given identical Mean CPs, with every 1 point increase in player Elo, Std CP increases by $(e^{-0.0002} - 1) * 100$, or 0.012%.

Linear Regression w/o Outliers

Repeating the same model selection process after removing Mean CP and Std CP outliers from the dataset:

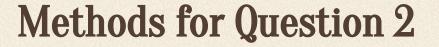




INTERPRETATION:

On average, with every 1% increase in Mean CP, Std CP increases by $(1.01^{1.146} - 1) * 100$, or 1.147%.

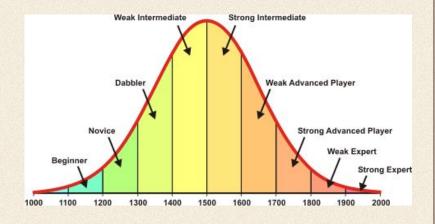




Question: How does Niemann's growth compare to other Grandmasters?

Methods

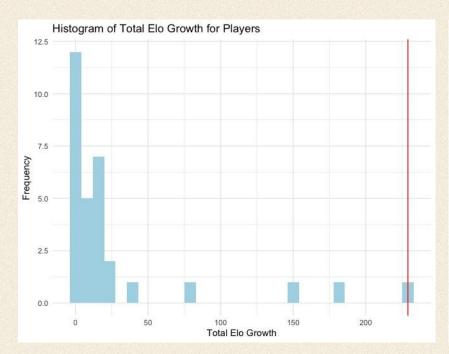
- Elo as a measure of performance
- Take Maximum Elo vs First Elo
- Compare Niemann's Elo Change to Other Players

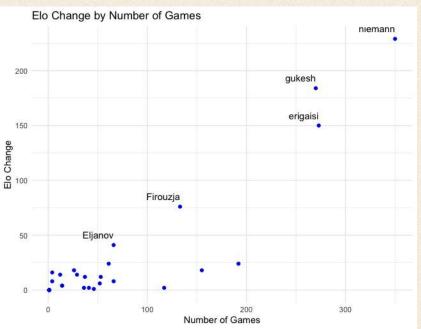




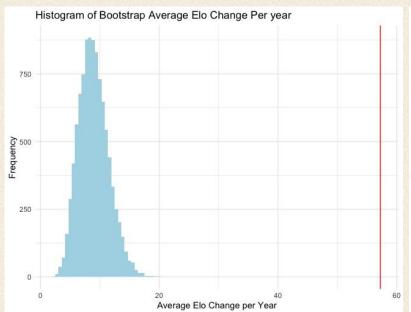


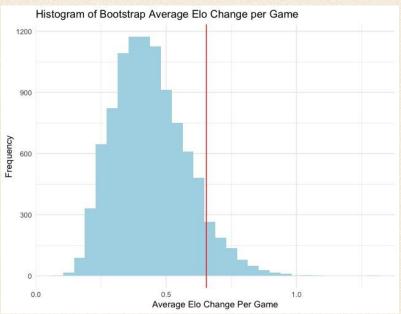
Visualization





Results





95% Confidence Interval: [4.55 : 14.24]

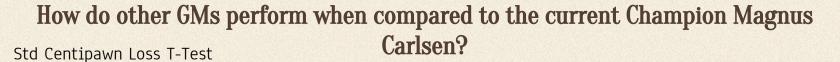
95% Confidence Interval: [0.211 : 0.745]



How do other GMs perform when compared to the current Champion Magnus Carlsen?

Mean Centipawn Loss T-Test

Bu Xiangzhi	Mean CP	0.0003076189		
Ding Liren	Mean CP	0.0001958873		
Ian Nepo	Mean CP	0.0001694836		
Wei Yi	Mean CP	0.0159982436		
Jennifer Yu	Mean CP	0.0371047003		



Dmitry Andreikin	Std CP	2.524653e-02
Bu Xiangzhi	Std CP	6.122359e-04
Ding Liren	Std CP	3.393064e-05
Ian Nepo	Std CP	5.687054e-06
Wei Yi	Std CP	6.322617e-03
Jennifer Yu	Std CP	7.677776e-03



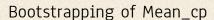
Kruskal-Wallis Test

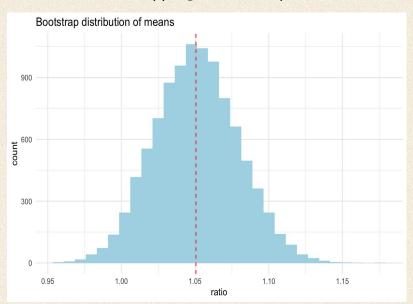
- Compared variance of players for both mean and std centipawn loss
- Done with and without Carlsen

	Test Statistic	P Value
Before	187.25	2.2e-16
After	182.02	2.2e-16



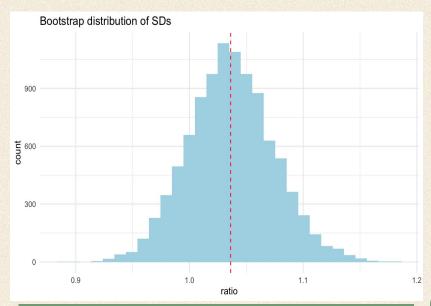
How do other GMs perform when compared to the rising chess prodigy Niemann?





95% Confidence Interval: [1.00 : 1.11]

Bootstrapping of Std_cp



95% Confidence Interval: [0.97 : 1.11]



How do other GMs perform when compared to the rising chess prodigy Niemann?

T-test of Mean_cp

t=1.8045,

p-value=0.03593

95% confidence interval:

0.1115292 ~ Inf

T-test of Std_cp

t=0.96464,

p-value=0.1676

95% confidence interval:

-1.106044 ~ Inf



INTERPRETATION:

Niemann shows a statistically significant higher mean centipawn loss in comparison with other players, thus we reject the theory of Niemann cheating by using a computer helper.

Conclusions

What are the best predictors for how well and consistent a player performs?

- As player's **accuracy** tends to **decrease** as their **consistency decreases** (and vice versa).
- A player's **accuracy** tends to **increase** as their **strength increases**.

How does Niemann's growth compare to other GMs?

- Niemann has a **statistically significant** higher **yearly ELO growth** than the average player, but there is no evidence to suggest that his ELO **growth per game** is different from the average player. Mixed results that call for more research but **no definitive proof** of cheating.

How do other GMs perform when compared to the current World Champion Magnus Carlsen?

- Out of the 31 grandmasters in our dataset, Magnus Carlsen performed with **overall less accuracy and consistency** than only 5-6 other grandmasters.

How do other GMs perform when compared to the rising chess prodigy Niemann?

- Niemann performed **less accurately** than other GMs but played with the **same consistency.** Mixed results that call for more research but **no definitive proof** of cheating.

Discussion and Limitations



- Consideration of **dependencies** within the data
 - Elo is inherently correlated w/ the player
 - Centipawn loss will be correlated w/ game time format
 - Centipawn calculations will differ based on the version of Stockfish used
- Our dataset only considers over-the-board games and 31 professional players
- When playing chess at grandmaster levels, there tends to be many outliers and influential points.
 - This could be because that at this level, the players tend to play variably (e.g. more risky / out-of-theory moves, time constraints).



Future Studies and Implications

- There may be other analyses like Time Series
 Analysis that can provide better insight into
 whether, players like Niemann are cheating by
 considering performance over time.
- Our dataset stops before the game when Niemann was accused of cheating against Carlsen. Future studies might try fitting the Mean CP and Std CP from that game into our regression models.