

Multiple Linear Regression. In-class Exercise 2

EL-GY 6143 Intro Machine Learning. Prof. Sundeep Rangan

Question

From the lecture slides.

□ **Linear Model:** $[\text{HR increase}] \approx \beta_0 + \beta_1[\text{mins exercise}] + \beta_2[\text{exercise intensity}]$

□ **Data**

Subject number	HR before	HR after	Mins on treadmill	Speed (min/km)	Days exercise / week
123	60	90	1	5.2	3
456	80	110	2	4.1	1
789	70	130	5	3.5	2
⋮	⋮	⋮	⋮	⋮	⋮
283	75	100	1	4.8	0

100 subjects

□ **Q1:** What is feature matrix A and target vector y for this problem

- Fill in only the values in the first three rows and last row

□ **Q2:** Suppose, after training, we find parameters $\beta = (0, 15, 3)$.

If the initial HR is 70 bpm, what is the predicted HR after 2 minutes of exercise at 5 km/hr?

Solution

Q1 $y = \begin{pmatrix} 30 \\ 30 \\ 60 \\ \vdots \\ 25 \end{pmatrix}$ } 100 $A = \begin{pmatrix} 1 & 1 & 5.2 \\ 1 & 2 & 4.1 \\ 1 & 5 & 3.5 \\ \vdots & \vdots & \vdots \\ 1 & 1 & 4.8 \end{pmatrix}$

100 x 3

Q2 $\beta = (0, 15, 3)$

$$\hat{y} = \beta_0 + \beta_1 x_1 + \beta_2 x_2$$
$$= 0 + (15)(2) + (3)(5) = 45$$

$$\text{HR after} = 70 + 45 = \boxed{115 \text{ bpm}}$$