

EEE 391
Basics of Signals and Systems
Spring 2015-2016
Computer Assignment 1

Due: 22 February 2016, Monday by 17:00 in the homework box

- 1) In this part, you will write a MATLAB program to determine the parameters of a given sampled sinusoidal signal.

The file “**data.mat**” contains a two-dimensional array **X**. The i th row of **X** contains a uniformly sampled sinusoid $x_i[n] = x_i(nT_s)$, $n = 0, 1, 2, \dots, N$, where

$$x_i(t) = C_i + A_i \cos(2\pi f_i t + \phi_i).$$

The sampling rate is $f_s = 1/T_s = 1000$ Hz. The parameters of the i th signal are the d.c. value C_i , the amplitude A_i , the frequency f_i (in Hz), and the phase ϕ_i (in degrees).

You will select and use three of the given 10 signals according to your student ID. Select the three signals which are indexed by the last three digits of your ID. If any of these digits is 0, use 10 instead. For example, if your ID is 21098760, you need to use $x_7(t)$, $x_6(t)$, and $x_{10}(t)$.

- (a) Plot the three signals separately. The sampling rate is sufficiently high, so use the `plot` command instead of `stem` in plotting. The horizontal axis must be t (time) in seconds. In each plot, indicate which signal is plotted in the plot title.
- (b) For each of the three signals, estimate the values of the parameters C_i , A_i , f_i (in Hz), and ϕ_i (in degrees) by hand from the plots you obtained in part (a). Briefly explain how you estimate each of the four parameters from the plot of a sinusoidal signal.
- (c) Now estimate the parameter values of the three signals automatically in MATLAB. That is, write a MATLAB function whose inputs are the sampling rate (in Hz) and a sampled sinusoidal signal **x** (such as a row of **X**) and outputs are the estimates of C , A , f (in Hz), and ϕ (in degrees). Call the function “[**C,A,f,phi**] = `parameters_of_sin(fs,x)`.” Assume that **x** contains at least two periods and the first sample of **x** corresponds to $t = 0$. Explain how you calculate the parameter values. You are *not* allowed to use advanced methods such as the Fourier transform (e.g., `fft` command) or curve fitting. You must *not* use any built-in function or any external toolbox for peak detection.

Write another MATLAB program that obtains the parameter values of the three signal by calling the function `parameters_of_sin` and displays the three signals in the Command Window in the form of “**x_1(t) = -1.30 +2.61 cos(87.01 t +0.80)**”. The d.c. value, amplitude, frequency, and phase should contain exactly two digits to the right of the decimal point. The phase value must be in radians. There should be “+” or “-” signs to the left of the d.c. value and the phase according to their signs.

Hint: To estimate C and A , you may simply use the minimum and maximum values of \mathbf{x} since it contains at least one period. The f and ϕ may be estimated from the first peak (i.e., the peak having the smallest t value) and the first negative peak of \mathbf{x} . These peaks correspond to the maximum and minimum values of the sinusoid in the first period. However, finding these peaks may not be trivial because in sampling the sinusoid, there may not be a sample exactly at the maximum and minimum value of the sinusoid (e.g., see Fig. 4-3 in the textbook), and this behavior may not be the same in all the periods. Therefore, the peak values in the sampled signal may change slightly from period to period, and the first exact maximum or minimum value of \mathbf{x} may reside in another period, which is not desired. To overcome this problem, instead of finding the first maximum value of \mathbf{x} , you may find the first value that exceeds $C + A - A/1000$, a value slightly lower than the maximum value of the continuous-time signal. Similarly, for the first negative peak, you may find the first value that is smaller than $C - A + A/1000$, a value slightly greater than the actual minimum value.

- (d) Compare the estimated values of the parameters you obtained in parts (b) and (c). Are they *exactly* the same? If not, what are the reasons? Explain and discuss.

Note: In this assignment, you are *not* allowed to use symbolic operations in MATLAB. To modify the styles of the plots, to add labels, and to scale the plots, use only MATLAB commands; do *not* use the GUI of the figure windows. When your program is executed, the figures must appear exactly the same as you provide in your solution.

Submit the results of your own work in the form of a well-documented report as hard copy. Borrowing full or partial code from your peers or elsewhere is strictly forbidden and will be punished. The report should include your own code, plots, and other results. Please include all evidence (plots, screen dumps, MATLAB codes, MATLAB command window print-outs, etc.) as needed in your report. The axes of all plots should be scaled and labeled. Please do not submit any electronic files on CD or by e-mail.