

Using C++20's Three-way Comparison $\lt{=}>$

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Guideline 0

Every type should either

- 1 overload `==`, `!=`, `<`, `<=`, `>=`, and `>` (**ordering**);
- 2 overload only `==` and `!=` (**equality**);
- 3 overload none of those.

Guideline 0

Every type should either

- 1 overload `==`, `!=`, `<`, `<=`, `>=`, and `>` (**ordering**);
- 2 overload only `==` and `!=` (**equality**);
- 3 overload none of those.

In particular: don't overload only `<`, `<=`, `>=`, `>`.

Copying and Equality

Copying and Equality

```
struct A
{
    int i;

    A(const A&) = default;
};

bool operator==(const A& lhs, const A& rhs)
{
    return lhs.i == rhs.i;
}
```

What we copy	What we don't copy	What we compare	Good Type?
integer i	nothing	integer i	yes

Copying and Equality

```
struct B
{
    std::mutex m;
    int i;

    B(const B& other) : i(other.i) {}
};

bool operator==(const B& lhs, const B& rhs)
{
    return lhs.i == rhs.i;
}
```

What we copy	What we don't copy	What we compare	Good Type?
integer i	mutex m	integer i	yes

Copying and Equality

```
struct C
{
    std::vector<int> v;

    C(const C&) = default;
};

bool operator==(const C& lhs, const C& rhs)
{
    return lhs.v == rhs.v;
}
```

What we copy	What we don't copy	What we compare	Good Type?
elements of v	capacity of v	elements of v	yes

Copying and Equality

```
struct D
{
    int a, b;

    D(const D&) = default;
};

bool operator==(const D& lhs, const D& rhs)
{
    return lhs.a == rhs.a;
}
```

What we copy	What we don't copy	What we compare	Good Type?
integer a, b	nothing	integer a	maybe

Copying and Equality

```
struct E
{
    int a, b;

    E(const E& other) : a(other.a), b(42) {}
};

bool operator==(const E& lhs, const E& rhs)
{
    return lhs.a == rhs.a && lhs.b == rhs.b;
}
```

What we copy	What we don't copy	What we compare	Good Type?
integer a	integer b	integer a, b	no

Guideline 1

What is compared should be a subset of what is copied.

- **Strong Equality:** everything that is copied is compared
- **Weak Equality:** a proper subset of what is copied is compared

Equality and Ordering

Two objects *a*, *b* of an ordered type:

- *a* and *b* are equal
- *a* is less than *b*
- *a* is greater than *b*

That's a relationship!

Sean Parent

Relationships between a , b in an ordered type:

- a and b are equal
- a is less than b
- a is greater than b

Relationships between a , b in an ordered type:

- a and b are equal
- a is less than b
- a is greater than b

But comparison operators give us only a `bool`!

< is all you need:

- a is less than b: $a < b$

< is all you need:

- a is less than b: $a < b$
- a is greater than b: $b < a$

< is all you need:

- a is less than b: `a < b`
- a is greater than b: `b < a`
- a and b are “equal”: `!(a < b) && !(b < a)`

Equivalence of a and b: `!(a < b) && !(b < a)`

Equality of a and b: `a == b`

Equivalence of a and b: $!(a < b) \ \&\& \ !(b < a)$

Equality of a and b: $a == b$

Guideline 2

Equivalence and equality of a type should be identical.

$a \leq b$ should mean $a < b \ || \ a == b$.

Equivalence of a and b: `!(a < b) && !(b < a)`

Equality of a and b: `a == b`

Guideline 2

Equivalence and equality of a type should be identical.

`a <= b` should mean `a < b || a == b`.

Corollary

The same things should be compared in `==` and `<`.

Taxonomy of Comparable Types

Taxonomy	<code>==, !=</code>	<code>==, !=, <, <=, >=, ></code>
compares all copied members	strong equality	strong ordering
compares some copied members	weak equality	weak ordering

Relationships between a , b in an ordered type:

- a and b are equal
- a is less than b
- a is greater than b

Three-Way Comparison

Relationships between a , b in an ordered type:

- a and b are equal
- a is less than b
- a is greater than b

Return relationship directly!

Three-Way Comparison

`std::strcmp(a, b):`

- a and b are equal: `== 0`
- a is less than b: `< 0`
- a is greater than b: `> 0`

C++20 Three-Way Comparison

Language:

- new operator `<=>` for a three-way comparison
- new operator rewrite rules for comparisons
- ability to `= default` comparison operators

Library (mostly in header `<compare>`):

- comparison categories: `std::strong_ordering`, `std::weak_ordering`
- concepts, utility functions
- completely transparent removal of many comparison operators

Language:

- new operator `<=>` for a three-way comparison
- new operator rewrite rules for comparisons
- ability to `= default` comparison operators

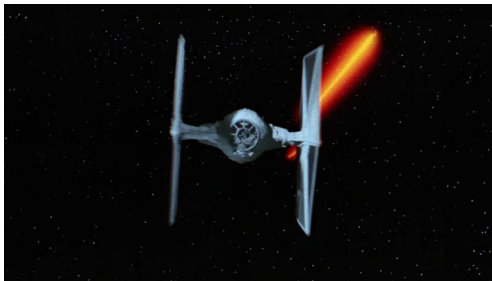
Library (mostly in header `<compare>`):

- comparison categories: `std::strong_ordering`, `std::weak_ordering`
- concepts, utility functions
- completely transparent removal of many comparison operators

Resources: jonathanmueller.dev/talk/cppcon2019

Spaceship?

C++20 Three-Way Comparison



| = |

TIE fighter.

<https://www.starwars.com/databank/tie-fighter>

C++20 Three-Way Comparison

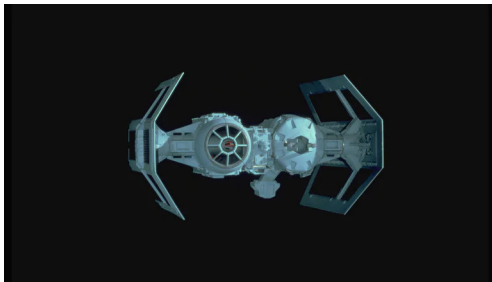


`<=>`

Darth Vader's TIE fighter.

<https://www.starwars.com/databank/darth-vader-s-tie-fighter>

C++20 Three-Way Comparison



`<==>`

TIE Bomber.

<https://www.starwars.com/databank/tie-bomber>

C++20 Three-Way Comparison



(=)

Inquisitor's TIE Advanced Prototype.

<https://www.starwars.com/databank/inquisitor-s-tie-advanced-prototype>

C++20 Three-Way Comparison



/o\

TIE Striker.

<https://www.starwars.com/databank/tie-striker>

`a <=> b:`

- `a` and `b` are equal: `== 0`
- `a` is less than `b`: `< 0`
- `a` is greater than `b`: `> 0`

`a <=> b`:

- `a` and `b` are equal: `== 0`
- `a` is less than `b`: `< 0`
- `a` is greater than `b`: `> 0`

But `<=>` does not return `int`.

Wrong, but useful:

```
enum class weak_ordering
{
    less = -1,
    equivalent = 0,
    greater = 1
};
```

// + comparison with 0

```
enum class strong_ordering
{
    less = -1,
    equal = 0,
    equivalent = 0,
    greater = 1
};
```

// + comparison with 0

Writing Comparison: Application Classes

```
struct Point  
{  
    int x, y;  
};
```

Goal: member-wise equality and inequality comparison.

```
struct Point
{
    int x, y;
};

bool operator==(const Point& lhs, const Point& rhs)
{
    return lhs.x == rhs.x && lhs.y == rhs.y;
}

bool operator!=(const Point& lhs, const Point& rhs)
{
    return !(lhs == rhs);
}
```



```
struct Point
{
    int x, y;

    bool operator==(const Point&) const = default;
};
```

Writing Comparison: Application Classes

```
Point a = {0, 0};  
Point b = {0, 1};
```

a == b →

Writing Comparison: Application Classes

```
Point a = {0, 0};  
Point b = {0, 1};
```

`a == b`

→

`a.operator==(b)`

Writing Comparison: Application Classes

```
Point a = {0, 0};
```

```
Point b = {0, 1};
```

<code>a == b</code>	<code>→</code>	<code>a.operator==(b)</code>
<code>a != b</code>	<code>→</code>	

Writing Comparison: Application Classes

```
Point a = {0, 0};  
Point b = {0, 1};
```

<code>a == b</code>	<code>→</code>	<code>a.operator==(b)</code>
<code>a != b</code>	<code>→</code>	<code>!(a.operator==(b))</code>

Writing Comparison: Application Classes

```
struct PointLike { operator Point(); };
```

```
Point p = {0, 0};
```

```
PointLike pl;
```

pl == p →

Writing Comparison: Application Classes

```
struct PointLike { operator Point(); };
```

```
Point p = {0, 0};
```

```
PointLike pl;
```

`pl == p` \rightarrow `p.operator==(pl)`

Guideline

Make comparison operator overloads free functions.

- required for conversions on the left-hand side

Guideline

Make comparison operator overloads member functions:

- it just works now
- no friend needed
- fewer overload resolution candidates:
 - potential for faster compilation
 - better error messages (!)

Technique

To get member-wise equality and inequality comparison:

```
class C
{
public:
    bool operator==(const C&) const = default;
};
```

```
struct Person
{
    PersonID id;
    std::string name;
    ...
};
```

Goal: equality and inequality comparison of `Person` forwarding to `id` member.

```
struct Person
```

```
{  
    PersonID id;  
    std::string name;  
    ...  
};
```

```
bool operator==(const Person& lhs, const Person& rhs)
```

```
{  
    return lhs.id == rhs.id;  
}
```

```
bool operator!=(const Person& lhs, const Person& rhs)
```

```
{  
    return lhs.id != rhs.id;  
}
```

```
struct Person
{
    PersonID id;
    std::string name;
    ...

    bool operator==(const Person& other) const
    {
        return other.id == id;
    }
};
```

```
struct Person
{
    PersonID id;
    std::string name;
    ...

    bool operator==(const Person& other) const
    {
        return other.id == id;
    }
};
```

Goal: equality and inequality comparison of Person with PersonID.

```
struct Person
```

```
{  
    PersonID id;  
    std::string name;  
    ...  
};
```

```
bool operator==(const Person& lhs, const Person& rhs);
```

```
bool operator!=(const Person& lhs, const Person& rhs);
```

```
bool operator==(const Person& lhs, PersonID rhs) { return lhs.id == rhs;
```

```
bool operator==(PersonID lhs, const Person& rhs) { return lhs == rhs.id;
```

```
bool operator!=(const Person& lhs, PersonID rhs) { return lhs.id != rhs;
```

```
bool operator!=(PersonID lhs, const Person& rhs) { return lhs != rhs.id;
```

Writing Comparison: Application Classes

C++20

```
struct Person
{
    PersonID id;
    std::string name;
    ...

    bool operator==(const Person& other) const
    {
        return id == other.id;
    }
    bool operator==(PersonID other) const
    {
        return id == other;
    }
};
```


Writing Comparison: Application Classes

```
Person p;  
PersonID id;
```

`p == id` \rightarrow

Writing Comparison: Application Classes

```
Person p;  
PersonID id;
```

`p == id`

→

`p.operator==(id)`

Writing Comparison: Application Classes

```
Person p;  
PersonID id;
```

<code>p == id</code>	<code>→</code>	<code>p.operator==(id)</code>
<code>id == p</code>	<code>→</code>	

Writing Comparison: Application Classes

```
Person p;  
PersonID id;
```

`p == id`

→

`p.operator==(id)`

`id == p`

→

`p.operator==(id)`

Writing Comparison: Application Classes

```
Person p;  
PersonID id;
```

<code>p == id</code>	<code>→</code>	<code>p.operator==(id)</code>
<code>id == p</code>	<code>→</code>	<code>p.operator==(id)</code>
<code>id != p</code>	<code>→</code>	

Writing Comparison: Application Classes

```
Person p;  
PersonID id;
```

<code>p == id</code>	→	<code>p.operator==(id)</code>
<code>id == p</code>	→	<code>p.operator==(id)</code>
<code>id != p</code>	→	<code>!(p.operator==(id))</code>

Technique

To get custom or mixed equality and inequality comparison:

```
class C
{
public:
    bool operator==(const T& other) const
    {
        // compare *this and other by calling == of members
    }
};
```

Writing Comparison: Application Classes

```
struct PersonID  
{  
    int impl;  
};
```

Goal: full member-wise ordering.


```
struct PersonID  
{  
    int impl;  
};
```

```
bool operator==(PersonID lhs, PersonID rhs) { return lhs.impl == rhs.impl;
```

```
bool operator<(PersonID lhs, PersonID rhs) { return lhs.impl < rhs.impl;
```

```
bool operator!=(PersonID lhs, PersonID rhs) { return !(lhs == rhs); }
```

```
bool operator>(PersonID lhs, PersonID rhs) { return rhs < lhs; }
```

```
bool operator<=(PersonID lhs, PersonID rhs) { return !(rhs < lhs); }
```

```
bool operator>=(PersonID lhs, PersonID rhs) { return !(lhs < rhs); }
```

```
struct PersonID
{
    int impl;

    std::strong_ordering operator<=>(const PersonID&) const = default;
};
```

Writing Comparison: Application Classes

```
struct PersonIDLike { operator PersonID(); };
```

```
PersonID a, b;
```

```
PersonIDLike c;
```

a < b →

Writing Comparison: Application Classes

```
struct PersonIDLike { operator PersonID(); };
```

```
PersonID a, b;
```

```
PersonIDLike c;
```

`a < b`

→

`a.operator<=>(b) < 0`

Writing Comparison: Application Classes

```
struct PersonIDLike { operator PersonID(); };
```

```
PersonID a, b;
```

```
PersonIDLike c;
```

a < b	→	a.operator<=>(b) < 0
a >= b	→	

Writing Comparison: Application Classes

```
struct PersonIDLike { operator PersonID(); };
```

```
PersonID a, b;
```

```
PersonIDLike c;
```

a < b	→	a.operator<=>(b) < 0
a >= b	→	a.operator<=>(b) >= 0

Writing Comparison: Application Classes

```
struct PersonIDLike { operator PersonID(); };
```

```
PersonID a, b;
```

```
PersonIDLike c;
```

a < b	→	a.operator<=>(b) < 0
a >= b	→	a.operator<=>(b) >= 0
c > b	→	

Writing Comparison: Application Classes

```
struct PersonIDLike { operator PersonID(); };
```

```
PersonID a, b;
```

```
PersonIDLike c;
```

a < b	→	a.operator<=>(b) < 0
a >= b	→	a.operator<=>(b) >= 0
c > b	→	0 > b.operator<=>(c)

Writing Comparison: Application Classes

```
struct PersonIDLike { operator PersonID(); };
```

```
PersonID a, b;
```

```
PersonIDLike c;
```

a < b	→	a.operator<=>(b) < 0
a >= b	→	a.operator<=>(b) >= 0
c > b	→	0 > b.operator<=>(c)
a == b	→	

Writing Comparison: Application Classes

```
struct PersonIDLike { operator PersonID(); };
```

```
PersonID a, b;  
PersonIDLike c;
```

a < b	→	a.operator<=>(b) < 0
a >= b	→	a.operator<=>(b) >= 0
c > b	→	0 > b.operator<=>(c)
a == b	→	a.operator==(b)

```
struct PersonID
{
    int impl;

    std::strong_ordering operator<=>(const PersonID&) const = default;

    // bool operator==(const PersonID&) const = default;
};
```

Technique

To get full member-wise ordering:

```
class C
{
public:
    std::strong_ordering operator<=>(const C&) const = default;
};
```

```
struct ID
{
    ByteString value;
    int domain;
};
```

Goal: member-wise comparison, but domain first then value (and member order can't be changed).

Writing Comparison: Application Classes

Pre C++20

```
bool operator==(const ID& lhs, const ID& rhs)
{
    return lhs.domain == rhs.domain && lhs.value == rhs.value;
}

bool operator<(const ID& lhs, const ID& rhs)
{
    if (lhs.domain != rhs.domain)
        return lhs.domain < rhs.domain;
    return lhs.value < rhs.value;
}

bool operator!=(ID lhs, ID rhs) { return !(lhs == rhs); }
bool operator>(ID lhs, ID rhs)  { return rhs < lhs; }
bool operator<=(ID lhs, ID rhs) { return !(rhs < lhs); }
bool operator>=(ID lhs, ID rhs) { return !(lhs < rhs); }
```

```
std::strong_ordering ID::operator<=>(const ID& other) const
{
    if (std::strong_ordering cmp = domain <=> other.domain;
        cmp != 0)
        return cmp;

    return value <=> other.value;
}
```

```
std::strong_ordering ID::operator<=>(const ID& other) const
{
    if (std::strong_ordering cmp = domain <=> other.domain;
        cmp != 0)
        return cmp;

    if (value == other.value)
        return std::strong_ordering::equal;
    else if (value < other.value)
        return std::strong_ordering::less;
    else
        return std::strong_ordering::greater;
}
```



```
template <typename T, std::totally_ordered_with<T> U>  
auto synth_three_way(const T& lhs, const U& rhs)  
{  
    ...  
}
```

```
template <typename T, std::totally_ordered_with<T> U>
auto synth_three_way(const T& lhs, const U& rhs)
{
    if constexpr (std::three_way_comparable_with<T, U>)
        return lhs <=> rhs;
    else
        ...
}
```

Writing Comparison: Application Classes

C++20

```
template <typename T, std::totally_ordered_with<T> U>
auto synth_three_way(const T& lhs, const U& rhs)
{
    if constexpr (std::three_way_comparable_with<T, U>)
        return lhs <=> rhs;
    else
    {
        if (lhs == rhs)
            return std::strong_ordering::equal;
        else if (lhs < rhs)
            return std::strong_ordering::less;
        else
            return std::strong_ordering::greater;
    }
}
```

```
std::strong_ordering ID::operator<=>(const ID& other) const
{
    if (auto cmp = domain <=> other.domain;
        cmp != 0)
        return cmp;

    return synth_three_way(value, other.value);
}
```

```
std::strong_ordering ID::operator<=>(const ID& other) const
{
    if (auto cmp = domain <=> other.domain;
        cmp != 0)
        return cmp;

    return synth_three_way(value, other.value);
}

bool ID::operator==(const ID& other) const
{
    return lhs.domain == rhs.domain && lhs.value == rhs.value;
}
```

Technique

To get custom or mixed ordering:

```
class C
{
public:
    std::strong_ordering operator<=>(const T& other) const
    {
        // compare with <=> or a synth_three_way helper
    }
};
```

And implement equality by providing operator==.

```
struct ID
{
    // swapped members!
    int domain;
    ByteString value;

    std::strong_ordering operator<=>(const ID&) const = default;
};
```

Using Comparison: Algorithms


```
template <typename Iter>  
Iter min_element(Iter begin, Iter end)  
{  
    // return minimum according to '<'  
}
```

```
template <typename Iter>
Iter min_element(Iter begin, Iter end)
{
    Iter min = begin;
    for (auto cur = begin; cur != end; ++cur)
    {
        if (*cur < *min)
            min = cur;
    }
    return min;
}
```

```
template <typename Iter>
Iter min_element(Iter begin, Iter end)
{
    Iter min = begin;
    for (auto cur = begin; cur != end; ++cur)
    {
        if (*cur < *min)
            min = cur;
    }
    return min;
}
```

Guideline

If you only need `==`, `<`, `>=` etc., just call it; don't call `<=>`.

```
template <typename Iter, typename T>
bool binary_search(Iter begin, Iter end, const T& value)
{
    // return true if value is in [begin, end)
    // range is sorted according to '<'
}
```

Assumption: we can use all comparison operators.

Using Comparison: Algorithms

Pre C++20

```
template <typename Iter, typename T>
bool binary_search(Iter begin, Iter end, const T& value)
{
    if (begin == end)
        return false; // empty range, value not there

    auto mid = begin + std::distance(begin, end) / 2;
    if (value == *mid)
        return true; // found it
    else if (value < *mid)
        return binary_search(begin, mid, value); // first half
    else
        return binary_search(mid + 1, end, value); // second half
}
```

(**Note:** not a great binary search implementation)

```
auto mid = begin + std::distance(begin, end) / 2;  
if (auto cmp = value <=> *mid;  
    cmp == 0)  
    return true; // found it  
else if (cmp < 0)  
    return binary_search(begin, mid, value); // first half  
else  
    return binary_search(mid + 1, end, value); // second half
```

```
auto mid = begin + std::distance(begin, end) / 2;
if (auto cmp = synth_three_way(value, *mid);
    cmp == 0)
    return true; // found it
else if (cmp < 0)
    return binary_search(begin, mid, value); // first half
else
    return binary_search(mid + 1, end, value); // second half
```


Guideline

Don't call `<=>` in generic code; use something like `synth_three_way`.

```
template <typename Iter, typename T, class Predicate>
bool binary_search(Iter begin, Iter end, const T& value, Predicate p)
{
    // return true if value is in [begin, end)
    // range is partitioned according to p
}
```

```
template <typename Iter, typename T, class Predicate>
bool binary_search(Iter begin, Iter end, const T& value, Predicate p)
{
    // return true if value is in [begin, end)
    // range is partitioned according to p
}
```

- $p(a, b)$ means a is “less than” b
- $!p(a, b) \ \&\& \ !p(b, a)$ means a is “equivalent to” b

```
auto mid = begin + std::distance(begin, end) / 2;
if (p(value, *mid))
    return binary_search(begin, mid, value); // first half
else if (p(*mid, value))
    return binary_search(mid + 1, end, value); // second half
else
    return true; // found it
```

```
template <typename Iter, typename T, class Ordering>
bool binary_search(Iter begin, Iter end, const T& value, Ordering o)
{
    // return true if value is in [begin, end)
    // range is partitioned according to o
}
```

```
template <typename Iter, typename T, class Ordering>
bool binary_search(Iter begin, Iter end, const T& value, Ordering o)
{
    // return true if value is in [begin, end)
    // range is partitioned according to o
}
```

- $o(a, b) == 0$ if a and b are “equivalent”
- $o(a, b) < 0$ if a is “less than” b
- $o(a, b) > 0$ if a is “greater than” b

```
auto mid = begin + std::distance(begin, end) / 2;
if (auto cmp = o(value, *mid);
    cmp == 0)
    return true; // found it
else if (cmp < 0)
    return binary_search(begin, mid, value); // first half
else
    return binary_search(mid + 1, end, value); // second half
```

```
template <typename T, typename U>  
std::strong_ordering my_order(const T& a, const U& b);
```

■ `my_order(a, b) == 0` means `a == b`

e.g. `<=>`


```
template <typename T, typename U>  
std::strong_ordering my_order(const T& a, const U& b);
```

- `my_order(a, b) == 0` means `a == b`

e.g. `<=>`

```
template <typename T, typename U>  
std::weak_ordering my_weaker_order(const T& a, const U& b);
```

- `my_weaker_order(a, b) == 0` does not necessarily mean `a == b`
- but: `a == b` means `my_weaker_order(a, b) == 0`!

e.g. `case_insensitive_compare`

Guideline

Consider a three-way ordering instead of a “less than” predicate if you need three-way comparison.

- `order(a, b) == 0`
- `order(a, b) < 0`
- `order(a, b) > 0`

Guideline

Use `std::weak_ordering` (only) as the return type of a three-way ordering with a weaker equality.

Writing Comparison: Library Classes

Assumptions:

- 1 Types provide equality or an ordering or none (Guideline 0)

Standard library assumptions:

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Standard library assumptions:

- 1 Types provide `==` or `<` or both. If a type provides `<` it does not necessarily have `==`.
- 2 `<` and `==` do not necessarily define the same equality.


```
template <typename T>
struct wrapper
{
    T value;
};
```

Goal: full member-wise ordering.

```
template <typename T>
bool wrapper<T>::operator==(const wrapper& other) const
{
    return value == other.value;
}
```

```
template <typename T>  
bool wrapper<T>::operator==(const wrapper&) const = default;
```

```
template <typename T>
auto wrapper<T>::operator<=>(const wrapper& other) const
{
    return value <=> other.value;
}
```

```
template <typename T>
auto wrapper<T>::operator<=>(const wrapper& other) const
{
    return synth_three_way(value, other.value);
}
```

```
template <typename T>
auto wrapper<T>::operator<=>(const wrapper& other) const
{
    return synth_three_way(value, other.value);
}
```

Note: implementing `<=>` with `<` and `==` requires assuming a comparison category.

```
template <typename T>
auto wrapper<T>::operator<=>(const wrapper& other) const
{
    return synth_three_way(value, other.value);
}
```

Note: implementing `<=>` with `<` and `==` requires assuming a comparison category.

- my recommendation: assume `std::strong_ordering`
- standard library recommendation: assume `std::weak_ordering`

```
template <typename T>  
auto wrapper<T>::operator<=>(const wrapper&) const = default;
```



```
template <typename T, std::totally_ordered_with<T> U>
auto synth_three_way(const T& lhs, const U& rhs)
{
    ...
}

template <typename T, typename U = T>
using synth_three_way_category
    = decltype(synth_three_way(std::declval<const T>(),
                               std::declval<const U>()));
```

```
template <typename T>
struct wrapper
{
    T value;

    synth_three_way_category<T> operator<=>(const wrapper&) const
        = default;
};
```

Writing Comparison: Library Classes

Technique

To get full member-wise ordering in generic code:

```
template <typename T>
class C
{
public:
    compute-category<T> operator<=>(const C&) const = default;
};
```

Note: keep in mind that this assumes the comparison category the type provides if it doesn't have a spaceship operator.

See also: `std::common_comparison_category`.

```
template <typename T>
class container
{
    T* ptr;
    std::size_t size;
};
```

Goal: full member-wise ordering of elements.

```
template <typename T>
bool container<T>::operator==(const container& other) const
{
    return std::equal(ptr, ptr + size,
                      other.ptr, other.ptr + other.size);
}
```

```
template <typename T>
auto container<T>::operator<=>(const container& other) const
{
    return std::lexicographical_compare_three_way(ptr, ptr + size,
        other.ptr, other.ptr + other.size);
}
```

```
template <typename T>
auto container<T>::operator<=>(const container& other) const
{
    return std::lexicographical_compare_three_way(ptr, ptr + size,
        other.ptr, other.ptr + other.size,
        synth_three_way);
}
```

Writing Comparison: Library Classes

C++20

```
template <typename T, std::totally_ordered_with<T> U>
auto synth_three_way(const T& lhs, const U& rhs)
{
    if constexpr (std::three_way_comparable_with<T, U>)
        return lhs <=> rhs;
    else
    {
        if (lhs == rhs)
            return std::strong_ordering::equal;
        else if (lhs < rhs)
            return std::strong_ordering::less;
        else
            return std::strong_ordering::greater;
    }
}
```



```
struct synth_three_way_t
{
    template <typename T, std::totally_ordered_with<T> U>
    auto operator()(const T& lhs, const U& rhs) const
    {
        ...
    }
};

inline constexpr synth_three_way_t synth_three_way;
```

Technique

- To get equality of a container: implement `operator==` using the `std::equal` algorithm.

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Technique

- To get equality of a container: implement `operator==` using the `std::equal` algorithm.
- To get ordering of a container: implement `operator<=>` the `std::lexicographical_compare_three_way` algorithm with a `synth_three_way` comparison function.
- Implement the `synth_three_way` comparison function as a function object.

Interlude: Why is == separate from <=>?

<=> of two ranges:

- 1 Iterate and compare elements until one range ended.
- 2 Return less/greater depending on the range that ended.

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<=> of two ranges:

- 1 Iterate and compare elements until one range ended.
- 2 Return less/greater depending on the range that ended.

== of two ranges:

- 1 Compare size (if possible). If not equal, range can't be equal.
- 2 Iterate and compare elements.

```
template <typename T>
class optional
{
public:
    bool has_value() const;
    const T& value() const;
};
```

Goal: full member-wise ordering, mixed comparisons with `T` and `std::nullopt`. Empty `optional` is less than all other values.

- `==, !=, <, <=, >=, >` for `optional<T>` and `optional<U>`

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- `==, !=, <, <=, >=, >` for `std::nullopt` and `optional<T>`

30 comparison operator overloads!

optional<T> and std::nullopt:

C++20

```
template <typename T>
bool optional<T>::operator==(std::nullopt_t) const
{
    return !has_value();
}

template <typename T>
std::strong_ordering optional<T>::operator<=>(std::nullopt_t) const
{
    if (has_value())
        return std::strong_ordering::greater;
    else
        return std::strong_ordering::equal;
}
```

optional<T> and U:

```
template <typename T, typename U>
bool optional<T>::operator==(const U& other) const
{
    if (has_value())
        return value() == other;
    else
        return false;
}
```


optional<T> and U:

```
template <typename T, typename U>
auto optional<T>::operator<=>(const U& other) const
{
    if (has_value())
        return synth_three_way(value(), other);
    else
        return std::strong_ordering::less;
}
```

`optional<T>` and `optional<U>`:

```
template <typename T, typename U>
bool optional<T>::operator==(const optional<U>& other) const
{
    if (has_value())
        return value() == other; // forward
    else
        return std::nullopt == other; // forward
}
```

`optional<T>` and `optional<U>`:

```
template <typename T, typename U>
auto optional<T>::operator<=>(const optional<U>& other) const
{
    if (has_value())
        return value() <=> other; // forward
    else
        return std::nullopt <=> other; // forward
}
```

Technique

- Formulating complex orderings using three-way comparison is easier than using `<`.
- Implement complex operators in terms of simpler ones.

Writing Comparison: Corner Cases

Writing Comparison: Corner Cases

```
struct Temperature
{
    double value;
};
```

Goal: full member-wise ordering.

```
struct Temperature
{
    double value;

    std::strong_ordering operator<=>(const Temperature&) = default;
};
```

I lied to you.

Relationships between two floats a , b :

- a and b are equal
- a is less than b
- a is greater than b

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- a and b are **unordered** (NaN!)

Relationships between two floats a , b :

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- a is less than b
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- a and b are **unordered** (NaN!)

This is called a **partial order**.

Wrong, but useful:

```
enum class partial_ordering
{
    less = -1,
    equivalent = 0,
    greater = 1,

    unordered = NaN
};

// + comparison with 0
```

Guideline

`<=>` should never return `std::partial_ordering!`

- it is surprising if `<`, `==` and `>` are all `false`
- no standard library algorithm works with partial ordering `<`
- `std::set/std::map` don't work with partial ordering `<`

```
struct Temperature
{
    double value;

    std::strong_ordering operator<=>(const Temperature&) = default;
};
```

```
std::partial_ordering operator<=>(double lhs, double rhs);
```

```
struct Temperature
{
    double value;

    std::strong_ordering operator<=>(const Temperature& other)
    {
        // just ignore NaNs...
        if (value == other.value)
            return std::strong_ordering::equal;
        else if (value < other.value)
            return std::strong_ordering::less;
        else
            return std::strong_ordering::greater;
    }
};
```

Floating Point Ordering:

- `a <=> b` gives a `std::partial_ordering`
 - normal numbers totally ordered
 - `+0/-0` is treated as equal
 - NaNs are unordered

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- `std::strong_order(a, b)` gives a `std::strong_ordering`
 - normal numbers totally ordered
 - `+0/-0` are treated as non-equal
 - NaNs are all totally ordered, different from each other
- `std::weak_order(a, b)` gives a `std::weak_ordering`
 - normal numbers totally ordered
 - `+0/-0` are treated as equal
 - NaNs all treated equal, totally ordered with others

Writing Comparison: Corner Cases

Guideline

Comparing floating points is hard.

```
struct Point
{
    int x, y;

    bool operator==(const Point&) const = default;
};

std::map<Point, T> spatial_grid;
```

```
struct Point
{
    int x, y;

    std::strong_ordering operator<=>(const Point&) const = default;
};

std::map<Point, T> spatial_grid;
```

Guideline

Don't implement `<=>` (or `<`) if you need to use it as key in map, only when it makes sense to provide it.

```
struct Point
{
    int x, y;

    bool operator==(const Point&) const = default;
};

std::strong_ordering strong_order(Point lhs, Point rhs)
{
    if (auto cmp = lhs.x <=> rhs.x; cmp != 0)
        return cmp;

    return lhs.y <=> rhs.y;
}
```

```
struct strong_order_cmp
{
    using is_transparent = void;

    template <typename T, typename U>
    bool operator()(const T& t, const U& u) const
    {
        return std::strong_order(t, u) < 0;
    }
};
```

```
std::map<point, T, strong_order_cmp> spatial_grid;
```


`std::strong_order:`

- 1 `strong_order(a, b)` if one available via ADL
- 2 special case for floats
- 3 `<=>`

(also `std::weak_order`, `std::partial_order`)

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`std::compare_strong_order_fallback:`

- 1 `strong_order(a, b)` if one available via ADL
- 2 special case for floats
- 3 `<=>`
- 4 `==` and `<`

(also `std::compare_weak_order_fallback`,
`std::compare_partial_order_fallback`)

Technique

Provide an ordering under the name `strong_order` (or `weak_order`, or `partial_order`) if:

- there is *some* ordering for the type, just not one that makes sense, or

Technique

Provide an ordering under the name `strong_order` (or `weak_order`, or `partial_order`) if:

- there is *some* ordering for the type, just not one that makes sense, or
- there is an alternative ordering that is faster than `<=>`.

Technique

Provide an ordering under the name `strong_order` (or `weak_order`, or `partial_order`) if:

- there is *some* ordering for the type, just not one that makes sense, or
- there is an alternative ordering that is faster than `<=>`.

Call `std::strong_order` (or `std::weak_order`, or `std::partial_order`) if you only need *some* ordering, not one that makes sense.

```
class C
{
public:
    bool operator==(const C&) const/* = default*/;
    std::strong_ordering operator<=>(const C&) const/* = default*/;
};
```

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