



SOLUTIONS

**Istanbul Medipol University**  
**School of Engineering and Natural Sciences**  
**General Physics 1**

**Midterm****17 November 2019****Duration: 120 min**

Name	
Student ID	
Department	
Signature	

- Closed book, closed notes, no calculators
- Write your student ID on every page in the spaces provided above.
- Show all your work. Your work and answers must be shown on the pages provided. You may write on the back side of the paper.
- Your grade will be based on the correctness of your solution and the clarity of your work leading up to the solution.
- Numerical answers must be given with correct SI units, and SI unit symbols must be used only.

**Grade:**

Question	Course Learning Outcome	Grade
1 (20 points)	1, 3	
2 (20 points)	1, 3	
3 (20 points)	1, 3	
4 (20 points)	1, 3	
5 (20 points)	1, 3	
Total		



Question 1 (from Young and Friedman)

An automobile and a truck start from rest at the same instant, with the automobile initially at some distance behind the truck. The truck has a constant acceleration of  $2 \text{ m/s}^2$ , and the automobile an acceleration of  $3 \text{ m/s}^2$ . The automobile overtakes the truck after the truck has moved  $40 \text{ m}$ .

- How much time does it take the automobile to overtake the truck?
- How far was the automobile behind the truck initially?
- What is the speed of each when the automobile catches the truck?

a.) Truck starts from rest with  $a_T = 2 \text{ m/s}^2$  and moves  $40 \text{ m}$ :

$$x = x_0 + v_0 t + \frac{1}{2} a_T t^2, \quad x_0 = 0, \quad v_0 = 0$$

$$x = \frac{1}{2} a_T t^2$$

$$40 \text{ m} = \frac{1}{2} (2 \text{ m/s}^2) t^2$$

10  $t = 2\sqrt{10} \text{ s}$

b.) The total distance that the automobile travels:

$$x_A = x_0 + v_0 t + \frac{1}{2} a_A t^2 \quad x_0 = 0, \quad v_0 = 0 \quad t = 2\sqrt{10} \text{ s} \quad a_A = 3 \text{ m/s}^2$$

$$x_A = \frac{1}{2} (3 \text{ m/s}^2) (40 \text{ s}^2)$$

$$3 = 60 \text{ m}$$

5  $2 \quad x_A - x_T = 60 \text{ m} - 40 \text{ m} = 20 \text{ m}$

$$c.) \quad v_A = v_{0A} + a_A t \quad v_0 = 0$$

$$= (3 \text{ m/s}^2) 2\sqrt{10} \text{ s}$$

2.5  $= 6\sqrt{10} \text{ m/s}$

$$v_T = v_{0T} + a_T t, \quad v_0 = 0$$

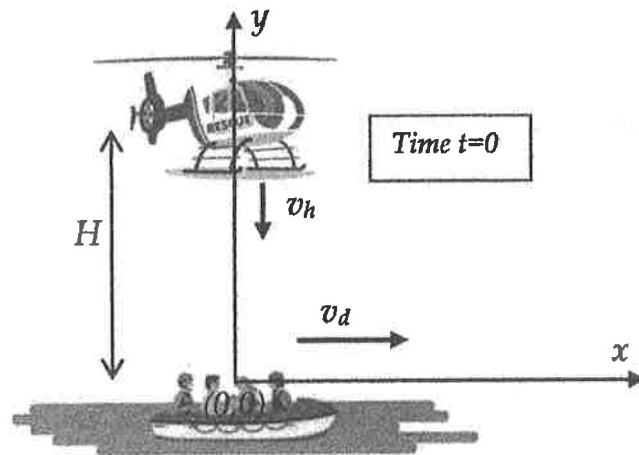
$$= (2 \text{ m/s}^2) 2\sqrt{10} \text{ s}$$

2.5  $= 4\sqrt{10} \text{ m/s}$



Question 2 (from Prof. Bordel)

A helicopter has constant vertical speed  $v_h$  downwards. When the helicopter is at a height  $H$ , right below it there is a boat that is moving horizontally with speed  $v_d$ . If at this instant, a package is thrown from the helicopter horizontally:



- 6 a. What should be the initial speed and direction (left or right) of the package with respect to the helicopter for it to land on the boat?
- 6 b. How long does it take for the package to reach the boat?
- 3 c. What is the trajectory  $y(x)$  of the package for an observer on the shore?
- 3 d. What is the horizontal distance traveled by the package?
- 2 e. When the package lands on the boat, which way does its velocity point? What is the angle between the velocity and the horizontal?

a) Its ~~horizontal~~ horizontal velocity should match the velocity of the boat. Since it's thrown horizontally, it should be thrown with  $\vec{v}_d$  to the right.

$$b) \quad y = y_0 + v_{y0}t - \frac{1}{2}gt^2$$

$$0 = (H) - (v_h)t - \frac{1}{2}gt^2$$

$$gt^2 + 2v_h t - 2H = 0$$

$$\text{solve for } t: \quad \frac{-2v_h \pm \sqrt{4v_h^2 + 8Hg}}{2g} = \frac{-v_h \pm \sqrt{v_h^2 + 2gH}}{g}$$

$$c) \quad x = v_d t \Rightarrow t = \frac{x}{v_d}$$

$$y = H - \frac{v_h}{v_d}x - \frac{g}{2v_d^2}x^2$$

$$d) x = v_d t$$

$$= \frac{v_d}{g} \left( -v_h + \sqrt{v_h^2 + 2gH} \right)$$

$$e) \tan \theta = \frac{v_{y \text{ final}}}{v_{x \text{ final}}}$$

$$v_{x \text{ final}} = v_d \hat{i}$$

$$v_{y \text{ final}} = v_{y_0} - gt$$

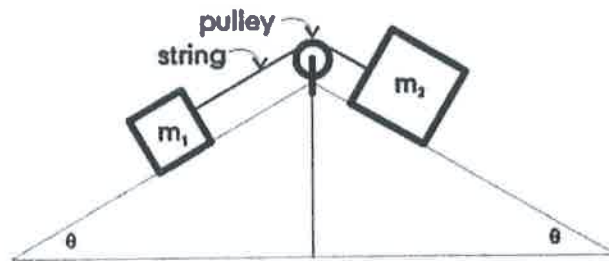
$$= -v_h - g \left( \frac{-v_h \pm \sqrt{v_h^2 + 2gH}}{g} \right)$$

$$= \sqrt{v_h^2 + 2gH} \hat{j}$$

$$\theta = \arctan \left( \frac{-\sqrt{v_h^2 + 2gH}}{v_d} \right)$$

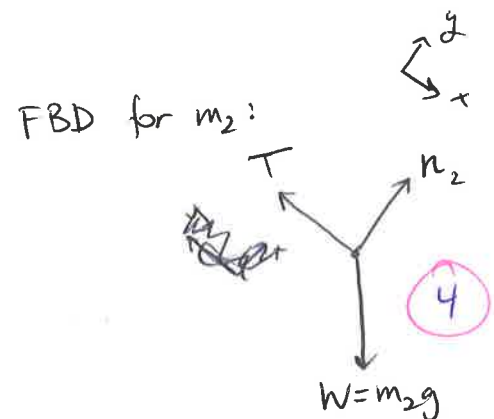
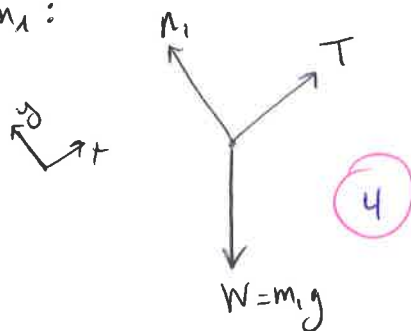
Question 3 (from Prof. Chiao)

Two masses  $m_1 = 5\text{ kg}$  and  $m_2 = 10\text{ kg}$  are on opposite sides of a double incline that has an angle of  $\theta = 30^\circ$  with respect to the ground on both sides. The masses are attached by a spring over a pulley that sits at the top of the incline. The spring and pulley are massless and the incline is frictionless. (You can take  $g = 10\text{ m/s}^2$ )



- Draw free body diagrams for both masses
- Find the acceleration of the two masses
- Find the tension in the string

a) FBD for  $m_1$ :



b)  $m_1$ :  $\sum F_y = 0 : -m_1 g \cos \theta + n_1 = 0$

$$\sum F_x = m_1 a = T - m_1 g \sin \theta \rightarrow T = m_1 (a + g \sin \theta)$$

$m_2$ :  $\sum F_y = 0 : -m_2 g \cos \theta + n_2 = 0$

$$\sum F_x = m_2 a = m_2 g \sin \theta - T$$

$$m_2 a = m_2 g \sin \theta - m_1 (a + g \sin \theta)$$

$$(m_1 + m_2) a = (m_2 - m_1) g \sin \theta$$

$$a = \frac{m_2 - m_1}{m_1 + m_2} g \sin \theta = \left( \frac{10\text{ kg} - 5\text{ kg}}{5\text{ kg} + 10\text{ kg}} \right) (10\text{ m/s}^2) \sin 30^\circ$$

$$= \frac{50}{30} \text{ m/s}^2 = \frac{5}{3} \text{ m/s}^2$$

$$c) T = m_1 (a + g \sin \theta)$$

$$= m_1 \left( \frac{m_2 - m_1}{m_1 + m_2} g \sin \theta + g \sin \theta \right)$$

$$= g \sin \theta \left[ m_1 + \frac{m_1 m_2 - m_1^2}{m_1 + m_2} \right]$$

$$= g \sin \theta \left[ \frac{m_1^2 + m_1 m_2 + m_1 m_2 - m_1^2}{m_1 + m_2} \right]$$

$$= g \sin \theta \left( \frac{2 m_1 m_2}{m_1 + m_2} \right)$$

$$= (10 \text{ m/s}^2) \frac{1}{2} \left( \frac{2 (5 \text{ kg})(10 \text{ kg})}{15 \text{ kg}} \right)$$

$$= \frac{100 \text{ N}}{3}$$

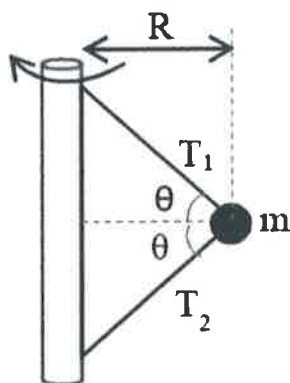
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Question 4 (from Prof. Tonguc)

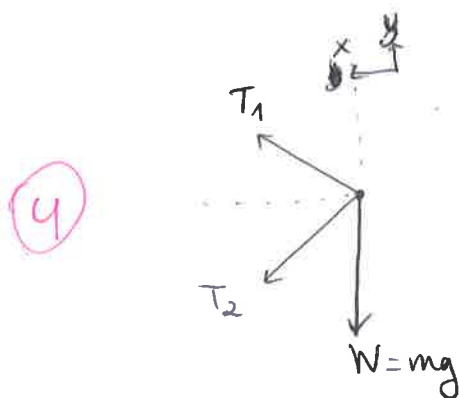
A point object with mass  $m$  is tied to a vertical rod with two massless ropes as shown in the figure. If  $m$  is uniformly turning in the horizontal plane around the rod;

- Draw the free body diagram for  $m$  and write the relevant equations.
- Given the values listed below, find the tension  $T_1$  and the linear velocity of  $m$ .



$$\begin{aligned} T_2 &= 50 \text{ N} \\ R &= 2 \text{ m} \\ m &= 8 \text{ kg} \\ g &= 10 \text{ m/s}^2 \\ \theta &= 53^\circ \\ \sin 53^\circ &= 0.8 \\ \cos 53^\circ &= 0.6 \end{aligned}$$

a) FBD for  $m$ :



$$y: T_1 \sin \theta - T_2 \sin \theta - mg = 0$$

$$x: T_1 \cos \theta + T_2 \cos \theta = m \frac{v^2}{R}$$

$$b) T_1 \sin 53^\circ - T_2 \sin 53^\circ - mg = 0$$

$$T_1 (0.8) - (50 \text{ N})(0.8) - (8 \text{ kg})(10 \text{ m/s}^2) = 0$$

$$T_1 = \frac{120 \text{ N}}{0.8} = 150 \text{ N}$$

$$(T_1 + T_2) \cos \theta = m \frac{v^2}{R}$$

$$(150 \text{ N} + 50 \text{ N}) 0.6 = (8 \text{ kg}) \frac{v^2}{2 \text{ m}}$$

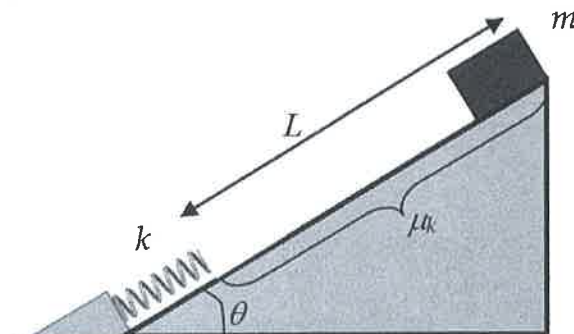
$$\frac{240}{8} = v^2$$

$$\rightarrow v = \sqrt{30} \text{ m/s}$$



Question 5 (from Prof. Bordel)

A block of mass  $m$  is released from rest at the top of an incline forming an angle  $\theta$  with the horizontal. After traveling a distance  $L$ , the block hits a spring of stiffness constant  $k$  which is initially in its equilibrium configuration. The surface of the incline is rough above the spring - with a coefficient of kinetic friction  $\mu_k$  between the block and the ramp - but smooth under the spring as seen in Figure.



- Without any calculation, explain whether or not the block reaches the top of the incline after being pushed by the spring.
- Determine the speed of the block when it reaches the spring
- Determine the length of the compression  $l$ .
- Determine the distance  $d$  traveled by the block on the way back, from the point where it loses contact with the spring to where it reaches its maximum height.
- Determine the kinetic friction coefficient that allows the block to get to a stop after traveling a distance  $L/2$  on the way back.

4 a) Because of energy dissipation due to friction, the block cannot reach the top again.

5 b)  $W_{\text{other}} + K_1 + U_{\text{grav},1} + U_{\text{el},1} = K_2 + U_{\text{grav},2} + U_{\text{el},2} \quad \left[ H = L \sin \theta \right]$

$$-\mu_k n L + mgH = \frac{1}{2} m v_2^2$$

$$-\mu_k mg \cos \theta L + mgH = \frac{1}{2} m v_2^2$$

$$-gL \mu_k \cos \theta + gL \sin \theta = \frac{1}{2} v_2^2$$

$$\left[ 2gL [\sin \theta - \mu_k \cos \theta] \right] = v_2^2$$

5 c)  $W_{\text{other}} + K_2 + U_{\text{grav},2} + U_{\text{el},2} = K_1 + U_{\text{grav},1} + U_{\text{el},1}$

$$\frac{1}{2} m v_2^2 + l \sin \theta mg = \frac{1}{2} k l^2$$

$$l^2 - \frac{2mg}{k} \sin \theta l - \frac{m}{k} v_2^2 = 0 : l =$$

$$\frac{2mg}{k} \sin \theta + \sqrt{\frac{4m^2 g^2 \sin^2 \theta}{k^2} + \frac{4mv_2^2}{k}}$$

$$\frac{1}{2} m v_2^2 + l mg \sin \theta = \frac{1}{2} k l^2$$

$$\frac{1}{2} m [2gL(\sin \theta - \mu_k \cos \theta)] + l mg \sin \theta = \frac{1}{2} k l^2$$

$$\cancel{\frac{1}{2}} m g L \sin \theta - m g L \mu_k \cos \theta + l m g \sin \theta - \frac{1}{2} k l^2 = 0$$

$$l = \frac{-m g \sin \theta \pm \sqrt{m^2 g^2 \sin^2 \theta + 2 k m g L (\sin \theta - \mu_k \cos \theta)}}{-k}$$

$\# d)$   $W_{other} + K_2 + U_{grav_2} + \cancel{U_{el_2}} = K_4 + U_{grav_2} + \cancel{U_{el_4}}$

$$-\mu_k m g \cos \theta \frac{L}{2} + \frac{1}{2} m v_2^2 = m g \frac{L}{2} \sin \theta$$

$$v_2^2 - g L \sin \theta = \mu_k g L \cos \theta$$

$$\frac{v_2^2}{g L \cos \theta} - \tan \theta = \mu_k$$

2

$$2 g L (\sin \theta - \mu_k \cos \theta) - g L \sin \theta = \mu_k g L \cos \theta$$

$$g L \sin \theta - 2 g L \mu_k \cos \theta = \mu_k g L \cos \theta$$

$$\sin \theta - 2 \mu_k \cos \theta = \mu_k \cos \theta$$

$$\mu_k = \frac{\tan \theta}{3}$$