

SortedArray

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CONTEXT
  SortedArray TASKING CONTEXT --undefined-- >
EXTENDS
  Array
AXIOMS
  axm1:  $\forall i, j. i \in 1..n \wedge j \in i..n \Rightarrow a(i) \leq a(j)$  not theorem TYPING --
undefined-- >
END
```

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MACHINE
  U00    >
REFINES
  U0
SEES
  SortedArray
VARIABLES
  result private >
  c private >
INVARIANTS
  inv4:  c ∈ 0..n-1 not theorem TYPING --undefined-- >
  inv5:  ∀ i · i ∈ 1..n ∧ a(i) ≥ x ⇒ i > c not theorem TYPING --undefined-- >
  inv6:  ∀ i · i ∈ 1..c ⇒ a(i) < x theorem TYPING --undefined-- >
  DLF:   (a(c+1) = x ∧ (c+1 = n ∨ a(c+2) > x)) ∨
         (c = n-1 ∧ a(n) ≠ x) ∨
         (c+2 ≤ n ∧ a(c+1) = x ∧ a(c+2) = x) ∨
         (c+1 < n ∧ a(c+1) < x) ∨
         (c < n ∧ a(c+1) > x) ∨
         (c = n-1 ∧ a(c+1) < x) theorem TYPING --undefined-- >
EVENTS
  INITIALISATION:  extended ordinary internal --undefined-- >
    THEN
      act1:  result := 0 >
      act2:  c := 0 >
    END

  Success:  not extended ordinary internal --undefined-- >
    REFINES
      Success
    WHERE
      grd2:  a(c+1) = x not theorem TYPING --undefined-- >
      grd3:  c+1 = n ∨ a(c+2) > x not theorem TYPING --undefined-- >
    WITH
      i:  i = c+1 >
    THEN
      act1:  result := c+1 >
    END

  Failure0:  not extended ordinary internal --undefined-- >
    REFINES
      Failure0
    WHERE
      grd1:  c = n-1 ∧ a(n) ≠ x not theorem TYPING --undefined-- >
    END

  Failure2:  not extended ordinary internal --undefined-- >
    REFINES
      Failure2
    WHERE
      grd6:  c+2 ≤ n not theorem TYPING --undefined-- >
      grd7:  a(c+1) = x not theorem TYPING --undefined-- >
      grd8:  a(c+2) = x not theorem TYPING --undefined-- >
    WITH
      i:  i = c+1 >

```

U00

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      j:  j = c+2  >
    END

Forward:    not extended ordinary internal --undefined-- >
    WHERE
      grd1:    c+1<n not theorem TYPING --undefined-- >
      grd3:    a(c+1)<x not theorem TYPING --undefined-- >
    THEN
      act1:    c:=c+1  >
    END

Failure00: not extended ordinary internal --undefined-- >
    REFINES
      Failure0
    WHERE
      grd1:    c<n not theorem TYPING --undefined-- >
      grd2:    a(c+1)>x not theorem TYPING --undefined-- >
    END

END
```