```
termvar, x
                                    term variable
index,\;i,\;j,\;k,\;n,\;m,\;p
            ::=
                     bool
                     int
                     \langle T1,..,Tn \rangle
                     T@\mathbf{r}
                     T@(r1,..,rn)
                     T@(r1,..,rk)
                     \mathbf{coloring}\,(\,\mathbf{r}\,)
                     \mathbf{coloring}(\mathbf{rp})
                     \exists r1,..,rn.(T1,..,Tn), Phi, Q \rightarrow \mathbf{Tr}
Om
            ::=
                     \{o1,..,on\}
             om
            ::=
                     r1 \leq r2
                     r1\times r2
Phi
              \{phi1,..,phin\}
phi
            ::=
                     \mathbf{reads}(\mathbf{r})
                     \mathbf{writes}(\mathbf{r})
                     \mathbf{reducesid}(\mathbf{r})
Q
            ::=
              \{q1,..,qn\}
            ::=
q
                     \mathbf{atomic}\,(\,\mathbf{r}\,)
                     \mathbf{simult}(\mathbf{r})
v
            ::=
                     bv
                     iv
                     \langle v_1, v_2 \rangle
                     null
                     1
                     \langle\langle rho1,..,rhon,v\rangle\rangle
bv
            ::=
                     true
                                                                                     constant true
                     false
                                                                                      constant false
iv
            ::=
                     0
```

```
\mathbf{S}\ iv
e
                       ::=
                                \boldsymbol{x}
                                iv
                                bv
                                \langle e1,..,en \rangle
                                e iv
                                id
                                \mathbf{new}\ T@\mathbf{r}
                                \mathbf{null}\ T@\ \mathbf{r}
                                \mathbf{isnull}(e)
                                upregion (e, r1, .., rn)
                                downregion (e, r1, .., rn)
                                \mathbf{read}(e)
                                write (e_1, e_2)
                                \mathbf{reduce}\,(\,\mathbf{id}\,,\mathit{e}_{1},\mathit{e}_{2})
                                newcolor r
                                color (e_1, e_2, e_3)
                                e_1 + e_2
                                e_1 < e_2
                               \mathbf{let}\,\mathbf{id}\,:\,T=e_1\,\in\,e_2
                                if b then c0 else c1
                                                                                                          conditional
                                id[r1,..,rn](e1,..,en)
                                partition rp using e_1 as r1, ..., rn \in e_2
                                pack e_1 as T[r1,..,rn]
                                \mathbf{unpack}\ e_1\,\mathbf{as}\,\mathbf{id}\ :\ T[r1,..,rn]\ \in\ e_2
logic
                       ::=
                                \forall i, phi \in Phi
                                \exists\: i.phi\:\in\: Phi
terminals
                                \exists
                                \forall
                                \in
                                \Omega
                                \omega
                                Φ
                                \phi
```

$$\Gamma, \Phi, \Omega \vdash e : T$$
 Typing

$$\frac{\Gamma, \Phi, \Omega \vdash e_1 : T@(r_1, .., r_n)}{\Gamma, \Phi, \Omega \vdash \mathbf{read}(e_1) : T} \quad T_READ$$

```
\Gamma, \Phi, \Omega \vdash e_1 : T@(r_1,...,r_n)
                                 \Gamma, \Phi, \Omega \vdash e_2 : T
                                                                             T_{-}W_{RITE}
                           \Gamma, \Phi, \Omega \vdash \mathbf{write}(e_1, e_2) \overline{: T@(r_1, ..., r_n)}
                                 \Gamma, \Phi, \Omega \vdash e_1 : T@(r_1,..,r_n)
                                 \Gamma, \Phi, \Omega \vdash e_2 : T
                                                                                 T_Reduce
                      \overline{\Gamma, \Phi, \Omega \vdash \mathbf{reduce}(\mathbf{id}, e_1, e_2) : T_1@(r_1, ..., r_n)}
                                                                        T_NEW
                                   \overline{\Gamma \cdot \Phi \cdot \Omega \vdash \mathbf{new} \ T@\mathbf{r} : T@\mathbf{r}}
                                 \Gamma, \Phi, \Omega \vdash e : T@(r1,..,rk)
                                                                                   T_UPRGN
                    \overline{\Gamma, \Phi, \Omega \vdash \mathbf{upregion}(e_1, r_1, .., r_n) : T@(r_1, .., r_n)}
                                 \Gamma, \Phi, \Omega \vdash e : T@(r1,..,rk)
                                                                                    T_DNRGN
                   \Gamma, \Phi, \Omega \vdash downregion (e, r1, ..., rn) : T@(r1, ..., rn)
                                                                    T_NewColor
                              \overline{\Gamma, \Phi, \Omega \vdash \mathbf{newcolor} \, \mathbf{r} : T@\, \mathbf{r}}
                                 \Gamma, \Phi, \Omega \vdash e_1 : T@(r_1,..,r_n)
                                 \Gamma, \Phi, \Omega \vdash e_2 : T@\mathbf{r}
                                 \Gamma, \Phi, \Omega \vdash e_3 : \mathbf{int}
                                                                               T_{-}Color
                         \Gamma, \Phi, \Omega \vdash \mathbf{color}(e_1, e_2, e_3) : \mathbf{coloring}(\mathbf{r})
                                        \Gamma, \Phi, \Omega \vdash e_1: coloring (rp)
                                        \Gamma, \Phi, \Omega \vdash e_2 : T
                                                                                                                       T_PARTITI
<<no parses (char 42): G,P,O |- partition rp using e1 as r1,..,rk*** in e2:</pre>
                                        \Gamma, \Phi, \Omega \vdash e_3: int
     <<no parses (char 31): G,P,O |- pack e1 as T1[r1,..,rk***]:T1 >>
                     \Gamma, \Phi, \Omega \vdash e_1 : T_1
                     <<no parses (char 2): G'***,P,O' |- e2 : T3 >>
                                                                                                                 T_UnPack
<<no parses (char 37): G,P,O |- unpack e1 as id: \overline{T1[r1,..,rk***]} in e2:T3 >>
            <<no parses (char 17): G,P,O |- ei : Ti[***r1/r1',..,rk/rk'] >>
                                                                                                                       T_CALL
<<no parses (char 20): G,P,O |- id[r1,..,rk***](e1,..,en):Tr[r1/r1',..,rk/rk'] >>
<<no parses (char 1): |***- {function id1[r11,..,rk11](a11:T11,..,a1n1), P1,Q1,T1r:e1,...</pre>
  p \longrightarrow p'
                Evaluation
     <<no parses (char 1): s***tate,T,E[x := a] --> state,T,E[skip] >>
     <<no parses (char 1): s***tate, T, E[skip;c] --> state,T,E[c] >>
                                                                                                                     E_IFTRUE
<<no parses (char 1): s***tate, T, E[if b then c0 else c1] --> state,T,E[c0] >>
                                                                                                                     E_{-}IfFalse
<<no parses (char 1): s***tate, T, E[if b then c0 else c1] --> state, T, E[c1] >>
<<no parses (char 1): s***tate, T, E[while b do c] --> state,T,E[if b then (c; while b do c)
                                                                                                       E_ASYNC
 <<no parses (char 1): s***tate, T, E[async c] --> state,T,E[skip] >>
                                                                                                      E_YIELD
   <<no parses (char 1): s***tate, T, E[yield] --> state,T,E[skip] >>
```