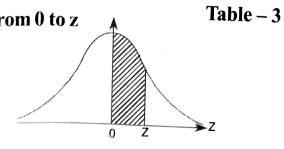
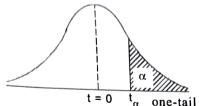
Areas under the Standard Normal Curve from 0 to z

$$Z = \frac{x - \mu}{\sigma}$$



								U	2		
=	0	1	2	3	4	5	6	7	8	9	
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	0 .0359	
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714		
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103		
0.3	.1179	.1217	.1256	.1293	.1331	.1368	.1406	.1443	.1480		
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808			
0.5	.1916	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	2224	
0.6	.2258	.2291	.2324	.2357	.2389	.2422	.2454	.2486			
0.7	.2580	.2612	.2642	.2673	.2704	.2734	.2764		.2518		
0.8	.2881	.2910	.2939	.2967				.2794	.2823	.2852	
0.9	.3159				.2996	.3023	.3051	.3078	.3106	.3133	
0.9	.5159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389	
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621	
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830	
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015	
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177	
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319	
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441	
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535		
1.7	.4654	.4564	.4573	.4582	.4591	.4599	.4608	.4616		.4545	
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4625	.4633	
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4699 .4761	.4706 .4767	
2.0	.4772	.4778	.4783	.4788	4793	.4798	4802	4000			
2.1	.4821	.4826	.4830	.4834	.4838	d c	.4803	.4808	.4812	.4817	
2.2	.4861	.4864	.4868	.4871	.4875	.4842	.4846	.4850	.4854	.4857	
2.3	.4893	, .4896	.4898	.4901	.4904	.4878	.4881	.4884	.4887	.4890	
2.4	.4918	.4920	.4922	.4925	.4904	.4906 .4929	.4909	.4911	.4913	.4916	
					.4727	.4929	.4931	.4932	.4934	.4936	
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952	
2.6	.4953	.4955	4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964	
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974	
2.8	.4974	.4975	.4976	.4977	.4979	.4978	.4979	.4979	.4980	.4981	
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986	
3.0	.4987	.4987	.4987	<b>7000</b>	4000	4000					.
3.1	.4990	.4991	.4991	.4988 .4991	.4988	.4989	.4989	.4989	.4990	.4990	
3.2	.4993	.4993	.4994	.4991	.4992	.4992	.4992	.4992	.4993	.4993	
3.3	.4995	.4995	.4995	.4994	.4994	.4994	.4994	.4995	,4995	.4995	
3.4	.4997	.4997	.4997	.4996 .4997	.4996 .4997	.4996 .4997	.4996	.4996	.4996	.4997	
2 6	4000	400"		· <b>4</b> 23/	.499/	.499/	.4997	.4997	.4997	.4998	
3.5 3.6	.4998 .4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	.4998	
3.7	.4998 .4999	.4998	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	1
3.8	.4999	.4999 .4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	
3.9	.5000	.5000	.4999	.4999	.4999	.4999	.4999	.4999	.4999	.4999	
		.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	.5000	

t<sub>α</sub> - Critical Values of the t-Distribution with ν Degrees of Freedom Table - 4



٧	0.40	0.30	α						
		0.30	0.20	0.15	0.10	0.05	0.025	0.01	0.005
1	0.325	0.725							0.002
2	0.289	0.727	1.376	1.963	2.0==				
3	0.277	0.617	1.061	1.386	3.078	6.314	12.706	31.821	63.65
4	0.271	0.584	0.978		1.886	2.920	4.303	6.965	9.925
5	0.267	0.569	0.941	1.250	1.638	2.353	3.182	4.541	5.841
		0.559	0.920	1.190	1.533	2.132	2.776	3.747	4.604
6	0.265			1.156	1.476	2.015	2.571	3.365	4.032
7		0.553	0.906					3.303	7.032
8	0.263	0.549	0.896	1.134	1.440	1.943	2.447	3.143	2 705
	0.262	0.546	0.889	1.119	1.415	1.895	2.365	2.998	3.707
9	0.261	0.543	0.883	1.108	1.397	1.860	2.306		3.499
10	0.260	0.542	0.883	1.100	1.383	1.833	2.262	2.896	3.355
- 1			0.879	1.093	1.372	1.812	2.228	2.821	3.250
11	0.260	0.540	0.055				2.220	2.764	3.169
12	0.259	0.539	0.876	1.088	1.363	1.796	2.201	2.210	
13	0.259	0.537	0.873	1.083	1.356	1.782	2.179	2.718	3.106
14	0.258		0.870	1.079	1.350	1.771	2.179	2.681	3.055
15	0.258	0.537	0.868	1.076	1.345	1.761	2.145	2.650	3.012
	0.238	0.536	0.866	1.074	1.341	1.753		2.624	2.97
16	0.250	- h-11				55	2.131	2.602	2.947
	0.258	0.535	0.865	1.071	1.337	1.746	2.120		
17	0.257	0.534	0.863	1.069	1.333	1.740	2.120	2.583	2.92
18	0.257	0.534	0.862	1.067	1.330	1.734	2.110	2.567	2.89
19	0.257	0.533	0.861	1.066	1.328	1.734	2.101	2.552	2.87
20	0.257	0.533	0.860	1.064	1.325	1.725	2.093	2.539	2.86
	1/2	M. Fr.			1.525	1.723	2.086	2.528	2.84
21	0.257	0.532	0.859	1.063	1.323	1 721	2 000		
22	0.256	0.532	0.858	1.061	1.321	1.721 1.717	2.080	2.518	2.83
23	0.256	0.532	0.858	1.060	1.319		2.074	2.508	2.81
24	0.256	0.531	0.857	1.059	1.319	1.714	2.069	2.500	2.80
25	0.256	0.531	0.856	1.058	1.316	1.711 1.708	2.064	2.492	2.79
		4.7	0.050	1.050	1.510	1.708	2.060	2.485	2.78
26	0.256	0.531	0.856	1.058	1 215	1.706	2.024		
27	1	0.531	0.855	1.057	1.315 1.314	1.706	2.056	2.479	2.77
28	1	0.531				1.703	2.052	2.473	2.77
29	1		0.855	1.056	1.313	1.701	2.048	2,467	2.76
		0.530	0.854	1.055	1.311	1.699	2.045	2.462	2.75
30	0.256	0.530	0.854	1.055	1.310	1.697	2.042	2.457	2,75
40	0.255	0.529	0.851	1.050	1.303	1.684	2.021	2.423	2.7
60	0.254	0.527	0.848	1.045	1.296	1.671	2.000	2.390	2.60
120	0.254	0.526	0.845	1.041	1.289	1.658	1.980	2.358	2.6
ox	0.253	0.524	0.842	1.036	1.282	1.645	1.960	2,326	2.5

Note: The above table gives the values of t for one-tail test (either left-tail or right-tail test). If we have to find the value of t for a two-tail test at a level, we take the value of  $\alpha/2$  for  $\alpha$ . For example, the value of t at 5% level with 9 d.f. is  $t_{0.025} = 2.262$  and the value of t at 1% level with 11 d.f. is  $t_{0.005} = 3.106$ 

Probability and Statistics

## Critical Values of the F-Distribution

Table – 5

ν <sub>2</sub>			Val	ues of F <sub>0.0</sub>	$_{05}(v_1, v_2)$									
ν <sub>2</sub>					1 2									
ν <sub>2</sub>														
	1	2	3	4	5	6	7	8	9					
1	161.4	199.5	215.7	224.6	230.2	234.0	236.8	238.9	240.5					
2	18.51	19.00	19.16	19.25	19.30	19.33	19.35	19.37	19.38					
3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81					
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00					
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77					
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10					
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68					
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39					
9	5.12	4.26	3.86`	3.63	3.48	3.37	3.29	3.23	3.18					
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02					
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90					
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80					
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71					
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65					
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59					
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54					
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49					
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46					
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42					
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39					
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37					
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34					
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32					
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30					
25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28					
26	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27					
27	4.23	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25					
28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24					
29	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.22 2.21					
30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21					
	1.00	2.22	2.84	2.61	2.45	2.34	2.25	2.18	2.12					
40	4.08	3.23 3.15	2.84	2.53	2.37	2.25	2.17	2.10	2.04					
60	4.00	3.15	2.68	2.45	2.29	2.17	2.09	2.02	1.96					
120 ∞	3.92	3.07	2.60	2.37	2.21	2.10	2.01	1.94	1.88					

<sub>Statistical</sub> Tables\_\_\_\_\_

## (Continued) Critical Values of the F-Distribution

				V	alues		$(v_1, v_2)$	2)				
						v <sub>1</sub>	24	30	40	60	120	, <b>x</b>
	1	0	12	15	20		24			252.2	253.3	254.3
	24	11.9	243.9	245.9	248	.0	249.1	250.1	251.1	19.48	19.49	19.50
	1	19.40	19.41	19.43	19	.45	19.45	19.46	19.47	8.57	8.55	8.52
,		8.79	8.74	8.70	8	.66	8.64	8.62	8.59	5.69	5.66	5.62
4		5.96	5.91	5.86	5	3.80	5.77	5.75	5.72	4.43	4.40	4.36
5		4.74	4.68	4.62		1.56	4.53	4.50	4.46	4.43	4.10	
		4.07	4.00	2.04		3.87	3.84	3.81	3.77	3.74	3.70	3.67
6		4.06	4.00	3.94			3.41	3.38	3.34	3.30	3.27	3.23
7	1	3.64	3.57 3.28	3.51 3.22		3.44 3.15	3.12	3.08	3.04	3.01	2.97	2.93
8	1	3.35 3.14	3.28	3.0		2.94	2.90	2.86	2.83	2.79	2.75	2.71
9	1		2.91	2.8		2.77	2.74	2.70	2.66	2.62	2.58	2.54
10	1	2.98	2.91	2.0	,	2.7,7	2.,,					
11		2.85	2.79	2.7	2	2.65	2.61	2.57	2.73	2.49	2.45	2.40
12		2.75	2.69	2.6		2.54	2.51	2.47	2.43	2.38	2.34	2.30
1		2.67	2.60	2.	53	2.46	2.42	2.38	2.34	2.30	2.25	2.21
1	4	2.60	2.53	2.	46	2.39	2.35	2.31	2.27	2.22	2.18	2.13
1	5	2.54	2.48	2.	40	2.33	2.29	2.25	2.20	2.16	2.11	2.07
	16	2.49	2.42	2	.35	2.28	2.24	2.19	2.15	2.11	2.06	2.01
	17	2.4	5 2.38	2	.31	2.23	2.19	2.17	2.10	2.06	2.01	1.96
	18	2.4	1 2.34		.27	2.19	2.15				1.97	1.92
	19	2.3			2.23	2.16	2.1				1.93	1.88
	20	2.	35 2.2	8 :	2.20	2.12	2.0	8 2.04	1.99	9 1.95	1.90	1.84
	21	2	.32 2.2	.5	2.18	2.10	2.0	5 2.0	1 1.9	6 1.92	1.87	1.81
1	22	1	.30 2.2		2.15	2.07	2.0				1.84	1.78
	23	1	2.27 2.3		2.13	2.05	2.0					1.76
	24	- 1	2.25 2. 2.24 2.		2.11	2.03 2.01						1.73
	2.	'	2.24 2.	16	2.09	2.01	1,	96 1.9	1.8	37 1.82	1.77	1.71
	2	6	2.22 2.	15	2,07	1.99	1.	95 1.	90 1.5	85 1.80	1.75	1.69
		1		.13	2.06	1.97				84 1.79	1,73	1.67
		1		.12	2.04	1,90				82 1.77		1.65
				.10	2.03	1.9	3			81 1.75		1.64
Carolina a	3	30	2.16	2.09	2.01	1.9	3	.89 1	.84 1.	79 1.75	1.68	1.62
		40	2.08	2.00	1.92	1.8	4 , 1	.79	.74	.69 1.64	1.58	1.51
	1	60	1.99	1.92	1.84	1.7	7			.59 1.53		_
	1	20	1.91 1.83	1.83	1.75	1.0				.50 1.43 .39 1.33		

## (Continued) Critical Values of the F-Distribution

	Values of $F_{0.01}(v_1, v_2)$											
	T .			$\nu_{_1}$								
ν <sub>2</sub>	1	2	3	4	5	6	7	8	9			
1	4052	4999.5	5403	5625	5764	5859	5928	5981	6022			
2	98.50	99.00	99.17	99.25	99.30	99.33	99.36	99.37	99.39			
3	34.12	30.82	29.46	28.71	28.24	27.91	27.67	27.49	27.35			
4	21.20	18.00	16.69	15.98	15.52	15.21	14.98	14.80	14.66			
5	16.26	13.27	12.06	11.39	10.97	10.67	10.46	10.29	10.16			
6	13.75	10.92	9.78	9.15	8.75	8.47	8.26	8.10	7.98			
7	12.25	9.55	8.45	7.85	7.46	7.19	6.99	6.84	6.72			
8	11.26	8.65	7.59	7.01	6.63	6.37	6.18	6.03	5.91			
9	10.56	8.02	6.99	6.42	6.06	5.80	5.61	5.47	5.35			
10	10.04	7.56	6.55	5.99	5.64	5.39	5.20	5.06	4.94			
11	9.65	7.21	6.22	5.67	5.32	5.07	4.89	4.74	4.63			
12	9.33	6.93	5.95	5.41	5.06	4.82	4.64	4.74	4.39			
13	9.07	6.70	5.74	5.21	4.86	4.62	4.44	4.30	4.19			
14	8.86	6.51	5.56	5.04	4.69	4.46	4.28	4.14	4.03			
15	8.68	6.36	5.42	4.89	4.56	4.32	4.14	4.00	3.89			
16	8.53	6.23	5.29	4.77	4.44	4.20	4.03	3.89	3.78			
17	8.40	6.11	5.18	4.67	4.34	4.10	3.93	3.79	3.68			
18	8.29	6.01	5.09	4.58	4.25	4.01	3.84	3.71	3.60			
19	8.18	5.93	5.01	4.50	4.17	3.94	3.77	3.63	3.52			
20	8.10	5.85	4.94	4.43	4.10	3.87	3.70	3.56	3.46			
21	8.02	5.78	4.87	4.37	4.04	3.81	3.64	3.51	3.40			
22	7.95	5.72	4.82	4.31	3.99	3.76	3.59	3.45	3.35			
23	7.88	5.66	4.76	4.26	3.94	3.71	3.54	3.41	3.30			
24	7.82	5.61	4.72	4.22	3.90	3.67	3.50	3.36	3.26			
25	7.77	5.57	4.68	4.18	3.85	3.63	3.46	3.32	3.22			
26	7.72	5.53	4.64	4.14	3.82	3.59	3.42	3.29	3.18			
27	7.68	5.49	4.60	4.11	3.78	3.56	3.39	3.26	3.15			
28	7.64	5.45	4.57	4.07	3.75	3.53	3.36	3.23	3.12			
29	7.60	5.42	4.54	4.04	3.73	3.50	3.33	3.20	3.09			
30	7.56	5.39	4.51	4.02	3.70	3.47	3.30	3.17	3.07			
40	7.31	5.18	4.31	3.83	3.51	3.29	3.12	2.99	2.89			
60	7.08	4.98	4.13	3.65	3.34	3.12	2.95	2.82	2.72			
120	6.85	4.79	3.95	3.48	3.17	2.96	3.79	2.66	2.56			
$\infty$	6.63	4.61	3.78	3.32	3.02	2.80	2.64	2.51	2.41			

## (Continued) Critical Values of the F-Distribution

		8.	1	Volume	of C		th 75y				
				Values		$v_1, v_2$	07				
$v_2^{}$	10	12	Pr -	$\mathbf{v}_{_{\mathrm{I}}}$							
		12	15	20	24	30	40	60	120	<b>∞</b>	
1	6056	6106	6157	6209	6225	(26)	(207	(212	(220	(266	
3	99.40	99.42	99.43	99.45	6235 99.46	6261	6287	6313	6339	6366	
4	27.23	27.05	26.87	26.69	26.60	99.47	99.47	99.48	99.49	99.50	
5	14.55	14.37	14.20	14.02	13.93	26.50	26.41	26.32	26.22	26.13	
3	10.05	9.89	9.72	9.55	9.47	9.38	13.75 9.29	13.65 9.20	13. <b>5</b> 6 9.11	13.46 9.02	
6	7.87	7.70				7.50	7.27	y,20	2.11	7.02	
7	6.62	7.72	7.56	7.40	7.31	7.23	7.14	7.06	6.97	6.88	
8	5.81	6.47	6.31	6.16	6.07	5.99	5.91	5.82	5.74	5.65	
9		5.67	5.52	5.36	5.28	5.20	5.12	5.03	4.95	4.86	
10	5.26	5.11	4.96	4.81	4.73	4.65	4.57	4.48	4.40	4.31	
10	4.85	4.71	4.56	4.41	4.33	4.25	4.17	4.08	4.00	3.91	
11	4.54	4.40	4.25	4.10	4.00	201					
12	4.30	4.16	4.01	3.86	4.02	3.94	3.86	3.78	3.69	3.60	
13	4.10	3.96	3.82	3.66	3.78	3.70	3.62	3.54	3.45	3.36	
14	3.94	3.80	3.66	3.51	3.59	3.51	3.43	3.34	3.25	3.17	
15	3.80	3.67	3.52	3.37	3.43 3.29	3.35	3.27	3.18	3.09	3.00	
			, , , , , , , , , , , , , , , , , , ,	5.57	3.29	3.21	3.13	3.05	2.96	2.87	
16	3.69	3.55	3.41	3.26	3.18	3.10	3.02	2.93	2.84	2.75	
17	3.59	3.46	3.31	3.16	3.08	3.00	2.92	2.83	2.75	2.65	
18	3.51	3.37	3.23	3.08	3.00	2.92	2.84	2.75	2.66	2.57	
19	3.43	3.30	3.15	3.00	2.92	2.84	2.76	2.67	2.58	2.49	
20	3.37	3.23	3.09	2.94	2.86	2.78	2.69	2.61	2.52	2.42	
21	2.21	2.17	2.02	2.00	2.00	0.70	2.5				
22	3.31 3.26	3.17 3.12	3.03	2.88 2.83	2.80 2.75	2.72	2.64	2.55	2.46	2.36	
23		3.12	2.93	2.78	2.73	2.67	2.58	`2.50	2.40	2.31	
24	3.21					2.62	2.54	2.45	2.35	2.26	
	3.17	3.03	2.89	2.74	2.66	2.58	2.49	2.40	2.31	2.21	
25	3.13	2.99	2.85	2.70	2.62	2.54	2.45	2.36	2.27	2.17	
26	3.09	2.96	2.81	2.66	2.58	2.50	2.42	2.33	2.23	2.13	
27	3.06	2.93	2.78	2.63	2.55	2.47	2.38	2,29	2.20	2.10	
28	3.03	2.90	2.75	2.60		2.44	2.35	2.26	2.17	2.06	
29	3.00	2.87	2.73	2.57	2.49	2.41	2,33	2,23	2.14		
30	2.98	2.84	2.70	2.55	247	ik.	2.30	2.21	2.11	2.01	
400			=:70 ;	3/		938-1	1-1	1	2.11	2.01	
40	2.80	2.66	2.52	2.37	2.29	2.20	2.11	2.02	1.92	1.80	
60	2.63	2.50	2.35	2.20	2.12	2.03	1.94	1.84	1.73		
20	2.47	2.34	2.19	2.03	1.95	1,86	1.76	1.66	1.53		
$\infty$	2.32	2.18	2.04	1.88	1.79	1.70	1.59	1.47	1.32		