survcomp: a package for performance assessment and comparison for survival analysis

Benjamin Haibe-Kains^{1,2,3}, Markus Schröder^{1,5}, John Quackenbush^{1,2}, Christos Sotiriou⁴, and Gianluca Bontempi³

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1 Introduction

The *survcomp* package is providing functions to assess and to compare the performance of risk prediction (survival) models. This package has been primarily used in gene

¹Computational Biology and Functional Genomics Laboratory, Dana-Farber Cancer Institute, Harvard School of Public Health

²Center for Cancer Computational Biology, Dana-Farber Cancer Institute ³Machine Learning Group, Université Libre de Bruxelles

⁴Breast Cancer Translational Research Laboratory, Institut Jules Bordet, Université Libre de Bruxelles

 $^{^5} Bioinformatics\ Resource\ Facility,\ Center\ for\ Biotechnology,\ Bielefeld\ University,\ Germany$

expression studies and the corresponding results have been published in high impact journals (Bioinformatics, Clinical Cancer Research, Journal of Clinical Oncology, ...). We plan to extend its use to other omics high-throughput data in a close future.

1.1 Installation

survcomp requires that survival, ipred, prodlim, survivalROC, SuppDists, bootstrap and R (>= 2.3.0) are installed. These should be installed automatically when you install survcomp. To install survcomp, source biocLite from bioconductor

```
> source("http://bioconductor.org/biocLite.R")
> biocLite("survcomp")
```

1.2 Further help

To view the *survcomp* description and a summary of all the functions within *survcomp*, type the following:

> library(help=survcomp)

1.3 Citing

We are delighted if you use this package. Please do email us if you find a bug or have a suggestion. We would be very grateful if you could cite:

B. Haibe-Kains, C. Desmedt, C. Sotiriou and G. Bontempi (2008) A comparative study of survival models for breast cancer prognostication based on microarray data: does a single gene beat them all? *Bioinformatics* **24(19)**:2200-2208.

2 Quickstart

We will very briefly demonstrate some of the functions in *survcomp*.

2.1 Overview

\$upper

2.1.1 The Concordance Index

The Concordance Index function computes the concordance index for a risk prediction, i.e. the probability that, for a pair of randomly chosen comparable samples, the sample with the higher risk prediction will experience an event before the other sample or belongs to a higher binary class. The usage is:

```
concordance.index(x, surv.time, surv.event, cl, weights, strat, alpha =
0.05, outx = TRUE, method = c("conservative", "noether", "nam"), na.rm = FALSE)
```

And a small example with random data could look like this:

```
> set.seed(12345)
> age <- rnorm(100, 50, 10)
> sex <- sample(0:1, 100, replace = TRUE)
> stime <- rexp(100)
> cens <- runif(100, 0.5, 2)
> sevent <- as.numeric(stime <= cens)
> stime <- pmin(stime, cens)</pre>
> strat <- sample(1:3, 100, replace = TRUE)
> cat("survival prediction:\n")
survival prediction:
> ci <- concordance.index(x = age, surv.time = stime, surv.event = sevent,
      strat = strat, method = "noether")
> ci[1:5]
$c.index
[1] 0.5500355
$se
[1] 0.03662212
$lower
[1] 0.4782575
```

```
[1] 0.6218135
```

\$p.value
[1] 0.08592802

[1] 1.518456

2.1.2 The D Index

The D Index function computes the D index for a risk prediction, i.e. an estimate of the log hazard ratio comparing two equal-sized prognostic groups. This is a natural measure of separation between two independent survival distributions under the proportional hazards assumption. The usage is:

```
D.index(x, surv.time, surv.event, weights, strat, alpha = 0.05, na.rm =
FALSE, ...)
```

And a small example with random data could look like this:

```
> set.seed(12345)
> age <- rnorm(100, 50, 10)
> stime <- rexp(100)
> cens <- runif(100, 0.5, 2)
> sevent <- as.numeric(stime <= cens)
> stime <- pmin(stime, cens)</pre>
> strat <- sample(1:3, 100, replace = TRUE)
> di <- D.index(x = age, surv.time = stime, surv.event = sevent,</pre>
      strat = strat)
> di[1:8]
$d.index
[1] 1.057789
$coef
[1] 0.05618072
$se
[1] 0.1844491
$lower
[1] 0.736878
$upper
```

```
$p.value
[1] 0.7606811
$n
[1] 100
$coxm
Call:
coxph(formula = Surv(stime, sevent) ~ strata(sstrat) + z, weights = sweights)
    coef exp(coef) se(coef) z
z 0.0562
              1.06
                    0.184 0.305 0.76
Likelihood ratio test=0.09 on 1 df, p=0.76 n= 100, number of events= 70
2.1.3
       The Hazard Ratio
The Hazard Ratio function computes the hazard ratio for a risk prediction. The usage is:
   hazard.ratio(x, surv.time, surv.event, weights, strat, alpha = 0.05, na.rm
= FALSE, ...)
And a small example with random data could look like this:
> set.seed(12345)
> age <- rnorm(100, 50, 10)
> stime <- rexp(100)
> cens <- runif(100, 0.5, 2)
> sevent <- as.numeric(stime <= cens)
> stime <- pmin(stime, cens)</pre>
> strat <- sample(1:3, 100, replace = TRUE)
> hr <- hazard.ratio(x = age, surv.time = stime, surv.event = sevent,
      strat = strat)
> hr[1:8]
$hazard.ratio
[1] 1.003961
$coef
[1] 0.003952968
```

\$se

```
[1] 0.01044472
$lower
[1] 0.9836174
$upper
[1] 1.024725
$p.value
[1] 0.7050847
$n
[1] 100
$coxm
Call:
coxph(formula = Surv(stime, sevent) ~ strata(sstrat) + sx, weights = sweights)
      coef exp(coef) se(coef)
sx 0.00395
                1.00
                       0.0104 0.378 0.71
```

2.1.4 The Brier Score

The Brier Score function computes all the Brier scores (BSC) and the corresponding integrated Briser score (IBSC) from a risk score, for all the times of event occurrence. The risk score is first transformed in survival probabilities using either a Cox model or the product-limit estimator. The usage is:

Likelihood ratio test=0.14 on 1 df, p=0.705 n= 100, number of events= 70

```
sbrier.score2proba(data.tr, data.ts, method = c("cox", "prodlim"))
```

And a small example with random data could look like this:

```
> set.seed(12345)
> age <- rnorm(30, 50, 10)
> stime <- rexp(30)
> cens <- runif(30, 0.5, 2)
> sevent <- as.numeric(stime <= cens)
> stime <- pmin(stime, cens)
> dd <- data.frame(time = stime, event = sevent, score = age)
> sb1 <- sbrier.score2proba(data.tr = dd, data.ts = dd, method = "cox")</pre>
```

```
> sb2 <- sbrier.score2proba(data.tr = dd, data.ts = dd, method = "prodlim")
> sb1$bsc.integrated
```

[1] 0.1921649

> sb2\$bsc.integrated

[1] 0.1986622

3 Functions in survcomp

FUNCTION DESCRIPTION

D.index Function to compute the D index

censor.time Function to artificially censor survival data cindex.comp Function to compare two concordance indices cindex.comp.meta Function to compare two concordance indices

combine.est Function to combine estimates combine.test Function to combine probabilities

concordance.index Function to compute the concordance index for survival or binary

class prediction

cvpl Function to compute the CVPL dindex.comp Function to compare two D indices

dindex.comp.meta Function to compare two concordance indices fisherz Function to compute Fisher z transformation

forestplot.surv Function to create a Forest Plot

getsurv2 Function to retrieve the survival probabilities at a specific point in

 $_{
m time}$

hazard.ratio Function to estimate the hazard ratio through Cox regression

hr.comp Function to statistically compare two hazard ratios hr.comp.meta Function to compare two concordance indices

hr.comp2 Function to statistically compare two hazard ratios (alternative in-

terface)

iauc.comp Function to compare two IAUCs through time-dependent ROC

curves

ibsc.comp Function to compare two IBSCs

km.coxph.plot Function to plot several Kaplan-Meier survival curves

logpl Function to compute the log partial likelihood of a Cox model

no.at.risk Function to compute the number of individuals at risk

sbrier.score2proba Function to compute the BSCs from a risk score, for all the times

of event occurrence

score2proba Function to compute the survival probabilities from a risk score survcomp-package Performance Assessment and Comparison for Survival Analysis td.sens.spec Function to compute sensitivity and specificity for a binary classi-

fication of survival data

tdrocc Function to compute time-dependent ROC curves

test.hetero.est Function to test the heterogeneity of set of probabilities test.hetero.test Function to test the heterogeneity of set of probabilities

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