

Introduction to Computer Midterm, HW2

Instructor: Chi-cheng Chiu (邱繼正)

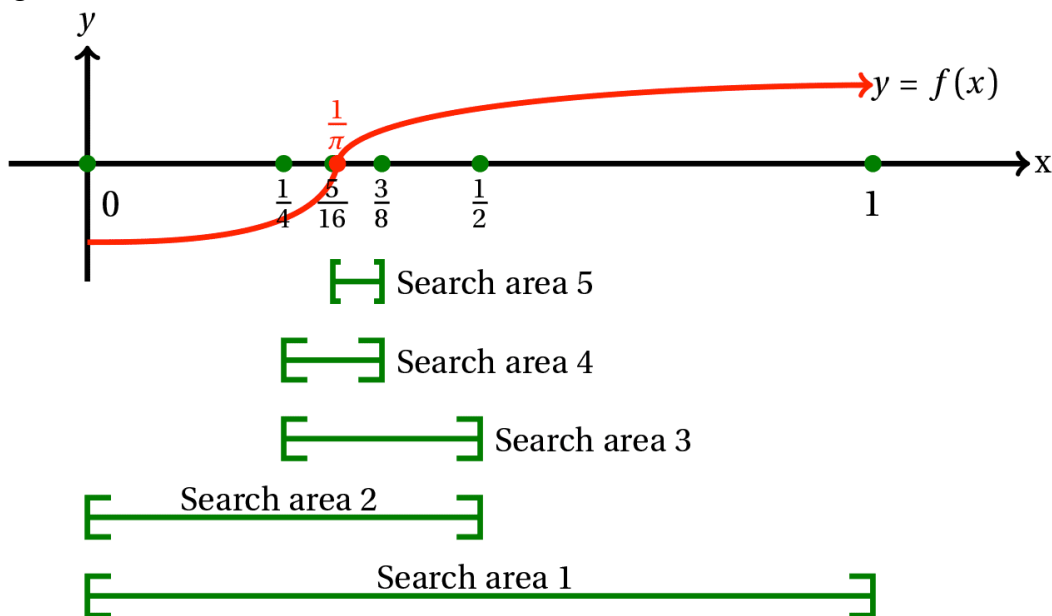
Course Num: E316200

檔名請千萬不要打錯，請大家留意！

Based on the Bolzano's Intermediate Value Theorem, if $f(x)$ is continuous in the range $[a, b]$ and $f(a) \cdot f(b) < 0$, then there exists a root value c in the range (a, b) such that $f(c) = 0$.

The bisection method is a root-finding method that applies to any continuous functions for which one knows two values with opposite signs. Consider a continuous function f , an interval $[a, b]$, and the function values are of opposite sign (there is at least one zero crossing within the interval). Each iteration performs these steps:

1. Calculate c , the midpoint of the interval, $c = (a + b)/2$.
2. Calculate the function value at the midpoint, $f(c)$.
3. If convergence is satisfactory (that is, $c - a$ is sufficiently small, or $|f(c)|$ is sufficiently small), return c and stop iterating.
4. Examine the sign of $f(c)$ and replace either $(a, f(a))$ or $(b, f(b))$ with $(c, f(c))$ so that there is a zero crossing within the new interval.



Considering the following function:

$$f(x) = 0.0021 \times x^5 + 0.00067 \times (x - 13)^4 + 46.7 \times x - 100$$

Write a C code to estimate the root value in the range of $[-15, 15]$ for the above $f(x)$ function with the accuracy of $<10^{-5}$.