MIT 6.1100 **Top-Down Parsing**

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Orientation

- Language specification
 - Lexical structure regular expressions
 Syntactic structure grammar
- This Lecture recursive descent parsers
 - Code parser as set of mutually recursive procedures
 Structure of program matches structure of grammar

Starting Point

- Assume lexical analysis has produced a sequence of tokens
 - Each token has a type and value

 - Types correspond to terminalsValues to contents of token read in
- Examples
 - Int 549 integer token with value 549 read in
 if if keyword, no need for a value
 AddOp + add operator, value +

```
Example
Boolean Term()
  if (token = Int n) token = NextToken(); return(TermPrime())
   else return(false)
Boolean TermPrime()
  if (token = *)
token = NextToken();
       if (token = Int n) token = NextToken(); return(TermPrime())
       else return(false)
  else if (token = /)
       token = NextToken();
       if (token = Int n) token = NextToken(); return(TermPrime())
       else return(false)
  else return(true)
                                    Term → Int Term'
                                    Term' → * Int Term'
                                    Term' → / Int Term'
                                   Term' \rightarrow \epsilon
```

Basic Approach

- Start with Start symbol
- Build a leftmost derivation
 - If leftmost symbol is nonterminal, choose a production and apply it
 - If leftmost symbol is terminal, match against input

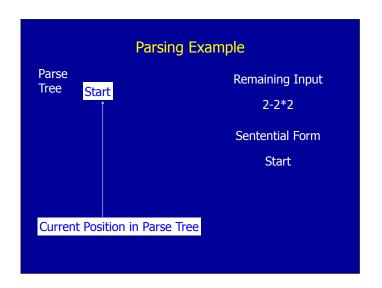
 - If all terminals match, have found a parse!
 Key: find correct productions for nonterminals

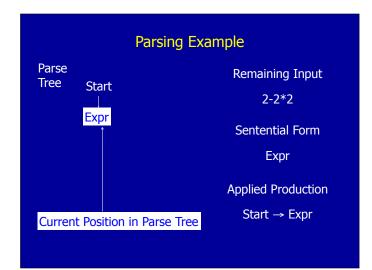
Graphical Illustration of Leftmost Derivation

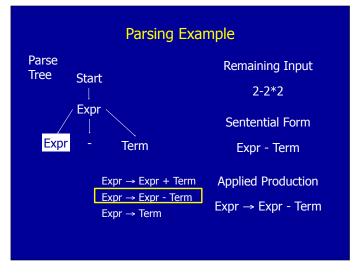
Sentential Form

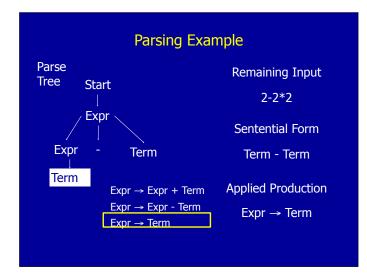


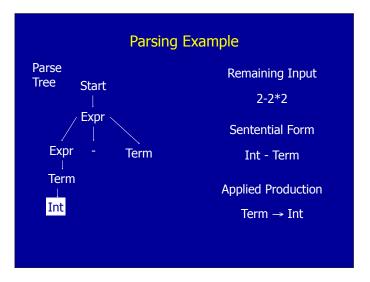
Grammar for Parsing Example Start → Expr Expr → Expr + Term Expr → Expr - Term Expr → Term Term → Term * Int Term → Term / Int Term → Int Set of tokens is { +, -, *, /, Int }, where Int = [0-9][0-9]* • For convenience, may represent each Int n token by n

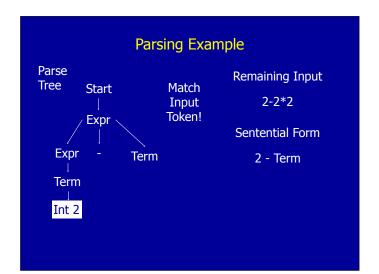


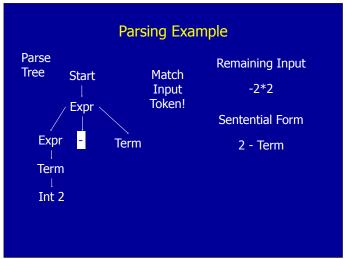


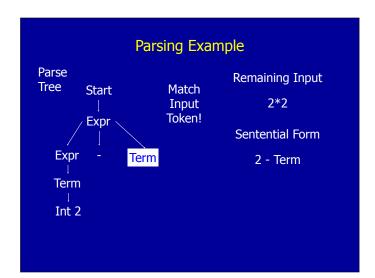


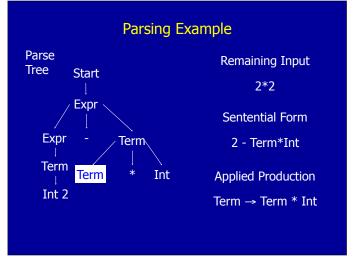


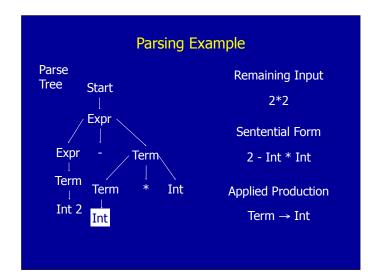


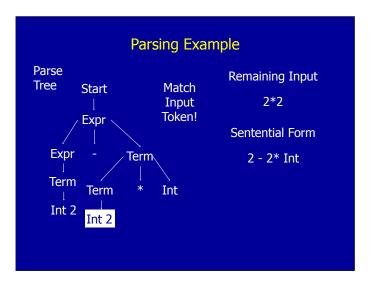


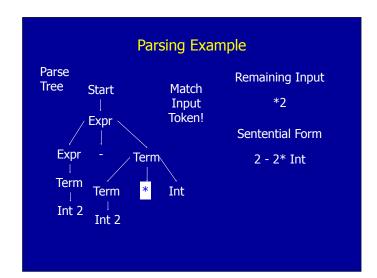


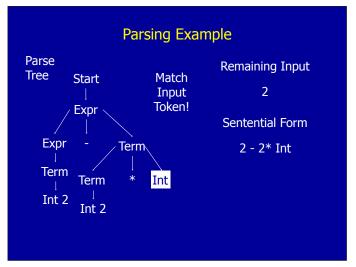


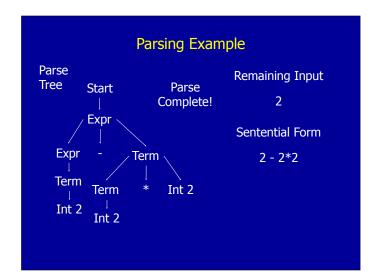












Summary Three Actions (Mechanisms) Apply production to expand current nonterminal in parse tree Match current terminal (consuming input) • Accept the parse as correct • Parser generates preorder traversal of parse tree visit parents before childrenvisit siblings from left to right

Policy Problem

- Which production to use for each nonterminal?
- Classical Separation of Policy and Mechanism
- One Approach: Backtracking
 Treat it as a search problem
 At each choice point, try next alternative
 If it is clear that current try fails, go back to previous choice and try something different
- General technique for searching
- Used a lot in classical AI and natural language processing (parsing, speech recognition)

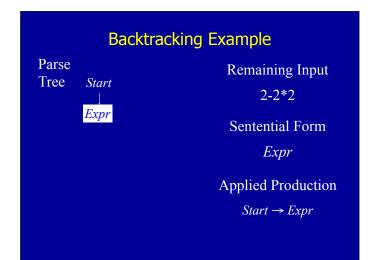
Backtracking Example

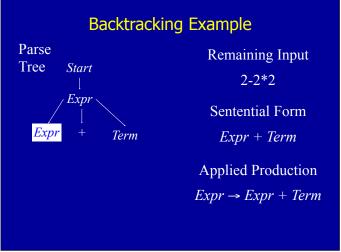
Parse Tree Start

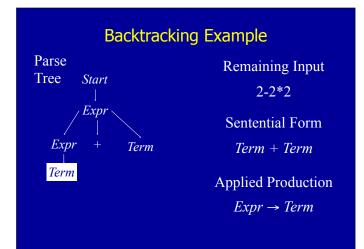
Remaining Input 2-2*2

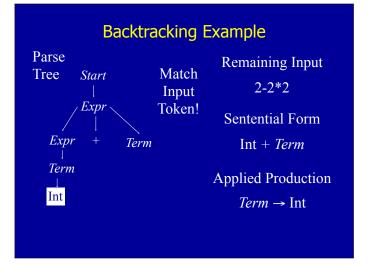
Sentential Form

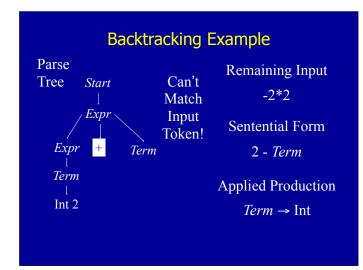
Start

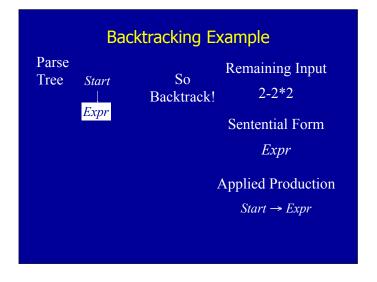


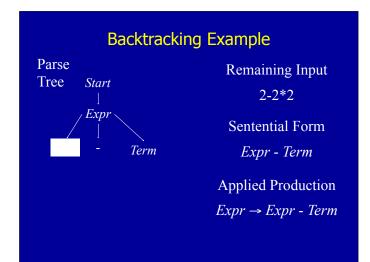


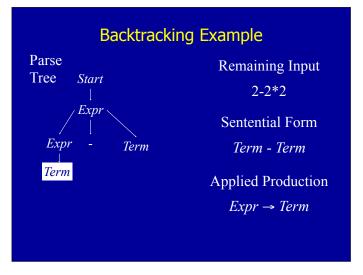


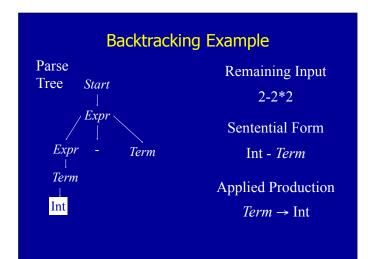


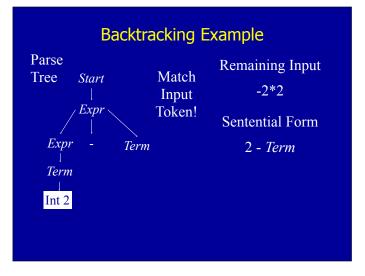


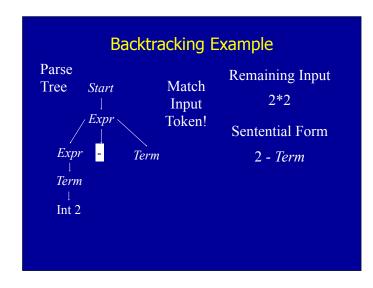


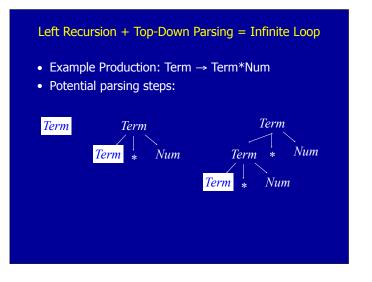












General Search Issues

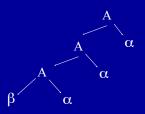
- Three components

 - Search space (parse trees)
 Search algorithm (parsing algorithm)
 - Goal to find (parse tree for input program)
- Would like to (but can't always) ensure that
 Find goal (hopefully quickly) if it exists
 Search terminates if it does not
- Handled in various ways in various contexts
 Finite search space makes it easy
 Exploration strategies for infinite search space
 - Sometimes one goal more important (model checking)
- For parsing, hack grammar to remove left recursion

Eliminating Left Recursion

- Start with productions of form

 - α , β sequences of terminals and nonterminals that do not start with A
- Repeated application of A \rightarrow A α builds parse tree like this:



Eliminating Left Recursion

• Replacement productions

$$- \stackrel{-}{A} \rightarrow A \alpha$$
$$- A \rightarrow \beta$$

$$A \rightarrow \beta R$$

$$R \rightarrow \alpha R$$

 $R \rightarrow \epsilon$

New Parse Tree

Old Parse Tree





R is a new nonterminal

Hacked Grammar

Original Grammar

Fragment

Term → Term * Int

Term → Term / Int

Term → Int

New Grammar Fragment

Term → Int Term'

Term' → * Int Term'

Term' → / Int Term'

Term' $\rightarrow \epsilon$

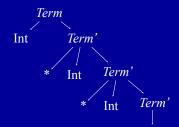
Parse Tree Comparisons

Original Grammar

Term

Int Int

New Grammar



Eliminating Left Recursion

- Changes search space exploration algorithm
 - Eliminates direct infinite recursion
 - But grammar less intuitive
- Sets things up for predictive parsing

Predictive Parsing

- Alternative to backtracking
- Useful for programming languages, which can be designed to make parsing easier
- Basic idea

 - Look ahead in input stream
 Decide which production to apply based on next tokens in input stream
 - · We will use one token of lookahead

Predictive Parsing Example Grammar

Start → Expr Term → Int Term' Expr → Term Expr' Term′ → * Int Term′ Expr' → + Term Expr' Term′ → / Int Term′ Expr' → - Term Expr' Term' $\rightarrow \epsilon$ $Expr' \rightarrow \varepsilon$

Choice Points

- Assume Term' is current position in parse tree
- Have three possible productions to apply Term' → * Int Term Term' → / Int Term'
- Use next token to decide
 - If next token is *, apply Term' → * Int Term'
 If next token is /, apply Term' → / Int Term'
 Otherwise, apply Term' → ε

Predictive Parsing + Hand Coding = Recursive Descent

- One procedure per nonterminal NT
 - Productions NT $\rightarrow \beta_1$, ..., NT $\rightarrow \beta_n$
 - Procedure examines the current input symbol T to determine which production to apply
 - If $T \in First(\beta_k)$
 - Apply production k
 - Consume terminals in β_k (check for correct terminal)
 - Recursively call procedures for nonterminals in β_k
 - Current input symbol stored in global variable token
- · Procedures return
 - true if parse succeedsfalse if parse fails

Example

```
if (token = Int n) token = NextToken(); return(TermPrime())
  else return(false)
Boolean TermPrime()
  if (token = *)
       token = NextToken();
       if (token = Int n) token = NextToken(); return(TermPrime())
       else return(false)
  else if (token = /)
       token = NextToken();
       if (token = Int n) token = NextToken(); return(TermPrime())
       else return(false)
  else return(true)
                                  Term → Int Term'
                                  Term' → * Int Term'
                                  Term' → / Int Term'
```

Term' $\rightarrow \epsilon$

Multiple Productions With Same Prefix in RHS

 Example Grammar $NT \rightarrow \text{if then}$ $NT \rightarrow \text{if then else}$

- Assume NT is current position in parse tree, and if is the next token
- Unclear which production to apply
 - Multiple k such that $T \in First(\beta_k)$
 - if ∈ First(if then)
 - if ∈ First(if then else)

Solution: Left Factor the Grammar

• New Grammar Factors Common Prefix Into Single Production

```
NT → if then NT'
NT' → else
```

- · No choice when next token is if!
- All choices have been unified in one production.

Nonterminals

• What about productions with nonterminals?

$$NT \rightarrow NT_1 \alpha_1$$

 $NT \rightarrow NT_2 \alpha_2$

- Must choose based on possible first terminals that NT₁ and NT₂ can generate
- What if NT₁ or NT₂ can generate ε?
 - Must choose based on α_1 and α_2

NT derives ε

- Two rules
 - NT $\rightarrow \epsilon$ implies NT derives ϵ
 - NT \rightarrow NT₁ ... NT_n and for all $1 \le i \le n$ NT_i derives ϵ implies NT derives ϵ

Fixed Point Algorithm for Derives ε

for all nonterminals NT set NT derives ε to be false for all productions of the form NT $\rightarrow \epsilon$ set NT derives ε to be true while (some NT derives ε changed in last iteration) for all productions of the form $NT \rightarrow NT_1 \dots NT_n$ if (for all $1 \le i \le n$ NT; derives ϵ) set NT derives ε to be true

$First(\beta)$

- T∈ First(β) if T can appear as the first symbol in a derivation starting from β

 - 1) T = First(T)2) $First(S) \subseteq First(S \beta)$ 3) NT derives ϵ implies $First(\beta) \subseteq First(NT \beta)$ 4) $NT \rightarrow S \beta$ implies $First(S \beta) \subseteq First(NT)$
- Notation
 - T is a terminal, NT is a nonterminal, S is a terminal or nonterminal, and β is a sequence of terminals or nonterminals

Rules + Request Generate System of Subset **Inclusion Constraints**

Grammar

Request: What is First(Term')? Term' → * Int Term' Term' → / Int Term' Constraints Term' $\rightarrow \epsilon$ First(* Int Term') ⊆ First(Term') First(/ Int Term') ⊆ First(Term') Rules First(*) ⊆ First(* Int Term') 1) T∈First(T) First(/) ⊆ First(/ Int Term') 2) First(S) \subseteq First(S β) *∈First(*) 3) NT derives ε implies / ∈First(/) $First(\beta) \subseteq First(NT \beta)$ 4) NT \rightarrow S β implies First(S β) \subseteq First(NT)

Constraint Propagation Algorithm

```
Constraints
                                                      Solution
First(* Int Term') ⊆ First(Term')
                                          First(Term') = {}
First(/ Int Term') ⊆ First(Term')
                                         First(* Int Term') = {}
First(*) ⊆ First(* Int Term')
                                          First(/ Int Term') = {}
First(/) \subseteq First(/ Int Term')
                                          First(*) = {}
*∈First(*)
                                          First(/) = {}
/ ∈First(/)
                                          Initialize Sets to {}
           Grammar
    Term' → * Int Term'
     Term' → / Int Term'
     Term' \rightarrow \epsilon
```

Constraint Propagation Algorithm

```
Constraints
                                                    Solution
First(* Int Term') ⊆ First(Term')
                                        First(Term') = {}
First(/ Int Term') ⊆ First(Term')
                                        First(* Int Term') = {}
First(*) \subseteq First(* Int Term')
                                        First(/ Int Term') = {}
First(/) \subseteq First(/ Int Term')
                                        First(*) = {*}
*∈First(*)
                                        First(/) = {/}
/ ∈First(/)
                                        Propagate Constraints Until
           Grammar
                                           Fixed Point
    Term' → * Int Term'
    Term' → / Int Term'
    Term' → ε
```

Constraint Propagation Algorithm

```
Constraints
                                                    Solution
First(* Int Term') ⊆ First(Term')
                                        First(Term') = {}
First(/ Int Term') ⊆ First(Term')
                                        First(* Int Term') = {*}
First(*) ⊆ First(* Int Term')
                                        First(/ Int Term') = {/}
First(/) ⊆ First(/ Int Term')
                                        First(*) = \{*\}
*∈First(*)
                                        First(/) = {/}
/ ∈First(/)
                                        Propagate Constraints Until
          Grammar
                                           Fixed Point
    Term' → * Int Term'
    Term' → / Int Term'
    \text{Term}' \to \epsilon
```

Constraint Propagation Algorithm

```
Constraints
                                                      Solution
First(* Int Term') ⊆ First(Term')
                                          First(Term') = {*,/}
First(/ Int Term') ⊆ First(Term')
                                          First(* Int Term') = {*}
First(*) \subseteq First(* Int Term')
                                          First(/ Int Term') = {/}
First(/) \subseteq First(/ Int Term')
                                          First(*) = \{*\}
*∈First(*)
                                          First(/) = {/}
/ ∈First(/)
                                          Propagate Constraints Until
           Grammar
                                             Fixed Point
    Term' → * Int Term'
    Term' → / Int Term'
    \text{Term'} \to \epsilon
```

Building A Parse Tree

- Have each procedure return the section of the parse tree for the part of the string it parsed
- Use exceptions to make code structure clean

Building Parse Tree In Example

```
Term()

if (token = Int n)

oldToken = token; token = NextToken();

node = TermPrime();

if (node == NULL) return oldToken;

else return(new TermNode(oldToken, node);

else throw SyntaxError

TermPrime()

if (token = *) || (token = /)

first = token; next = NextToken();

if (next = Int n)

token = NextToken();

return(new TermPrimeNode(first, next, TermPrime()))

else throw SyntaxError

else return(NULL)
```

Parse Tree for 2*3*4 Desired Concrete Abstract Parse Tree Parse Tree Term Term' Int Term 2 Int **Term** Int Int Term' Int 4

Why Use Hand-Coded Parser?

- Why not use parser generator?
- What do you do if your parser doesn't work?
 - Recursive descent parser write more code Parser generator Hack grammar

 - But if parser generator doesn't work, nothing you can do
- If you have complicated grammar
 - Increase chance of going outside comfort zone of parser generator
 Your parser may NEVER work

Bottom Line

- Recursive descent parser properties
 - Probably more work
 - But less risk of a disaster you can almost always make a recursive descent parser work
 - May have easier time dealing with resulting code
 - Single language system
 - No need to deal with potentially flaky parser generator
 - No integration issues with automatically generated code
- If your parser development time is small compared to rest of project, or you have a really complicated language, use hand-coded recursive descent parser

Summary

- Top-Down Parsing
- · Use Lookahead to Avoid Backtracking
- Parser is

Term()

- Hand-Coded Set of Mutually Recursive Procedures

Direct Generation of Abstract Tree

- TermPrime builds an incomplete tree
 - Missing leftmost child
 - Returns root and incomplete node
- (root, incomplete) = TermPrime()
 - Called with token = 3
 - Remaining tokens = 3 * 4

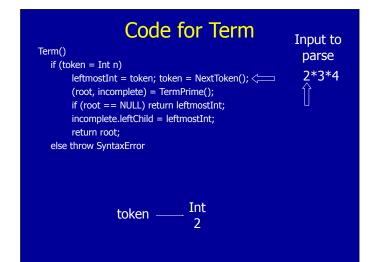


Code for Term

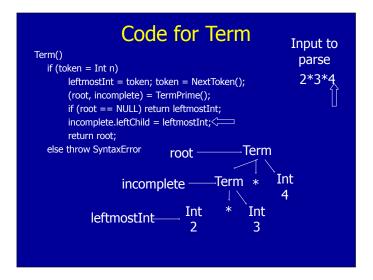
if (token = Int n) < leftmostInt = token; token = NextToken(); (root, incomplete) = TermPrime(); if (root == NULL) return leftmostInt; incomplete.leftChild = leftmostInt; return root; else throw SyntaxError

token -

Input to parse 2*3*4



```
Code for Term
                                                     Input to
Term()
                                                      parse
  if (token = Int n)
                                                       2*3*4
       leftmostInt = token; token = NextToken();
       (root, incomplete) = TermPrime();
       if (root == NULL) return leftmostInt; <==
       incomplete.leftChild = leftmostInt;
       return root;
  else throw SyntaxError
                            root —
                  incomplete ·
                                     -Term ∗
                                            Int
                               Int
           leftmostInt-
```



```
Code for Term
                                                     Input to
Term()
                                                      parse
  if (token = Int n)
       leftmostInt = token; token = NextToken();
       (root, incomplete) = TermPrime();
       if (root == NULL) return leftmostInt;
       incomplete.leftChild = leftmostInt;
       return root; <
  else throw SyntaxError
                                          -Term
                           root —
                                   —Term ∗
                 incomplete -
           leftmostInt-
```

```
Code for TermPrime
TermPrime()
   if (token = *) || (token = /)
op = token; next = NextToken();
                                                                  Missing left child
                                                                  to be filled in by
         if (next = Int n)
                                                                        caller
                   token = NextToken();
                   (root, incomplete) = TermPrime();
                   if (root == NULL)
                             root = new ExprNode(NULL, op, next);
                             return (root, root);
                             newChild = new ExprNode(NULL, op, next);
incomplete.leftChild = newChild;
                             return(root, newChild);
         else throw SyntaxError
   else return(NULL,NULL)
```