## SOLUTION of 3:

## 3.1

- a) Angry(I)  $\Rightarrow \forall x(\neg MakesHappy(x,I) \Leftrightarrow \neg Cake(x))$
- b)  $\forall x (WentToParty(x) \Leftrightarrow x \neq I)$
- c)  $\forall x (\neg AllowedOnFloor(x) \Leftrightarrow (\neg Manager(x) \lor \neg SeniorResearcher(x)))$

If an object x is an exception to a property P, this means that being x is equivalent to not enjoying property P, or that not being x is equivalent to enjoying property P.

Modelling a sentence like this:

Angry(I)  $\Rightarrow \forall x(\neg MakesHappy(x,I) \Rightarrow \neg Cake(x))$ , with a simple conditional instead of a double conditional is a mistake, because the formula has models where there is something which is not a cake and yet it makes me happy.

## 3.2

If I catch the train, then either I'm on time or the train is late.

 $CT \Rightarrow (OT \vee TL) \text{ (hyp 1)}$ 

If I wake up late, I must run to be on time.

 $WL \Rightarrow (OT \Rightarrow R)$  (hyp 2) (running is necessary for being on time, if I wake up late)

I'm out of shape

OS (hyp 3)

which [being out of shape] means that if I run I end up heavy breathing

 $OS \Leftrightarrow (R \Rightarrow HB) \text{ (hyp 4)}$ 

Today the train was on time, while I woke up late, but I managed to catch it.

 $\neg TL \wedge WL \wedge CT \text{ (hyp 5)}$ 

That's why I'm heavy breathing.

HB (thesis)

## Proof:

 $OS \Rightarrow (R \Rightarrow HB)$  (6: from 4 with  $\Leftrightarrow$ -elim and  $\land$ -elim)

 $R \Rightarrow HB$  (7: from 3 and 6 with MP)

WL (8: from 5 with  $\land$ -elim)

 $OT \Rightarrow R$  (9: from 2 and 8 with MP)

CT (10: from 5 with  $\land$ -elim)

OT vTL (11: from 1 and 10 with MP)

 $\neg TL$  (12: from 5 with  $\land$ -elim)

OT (13: from 11 and 12 with resolution)

R (14: from 9 and 13 with MP)

HB (thesis: from 7 and 14 with MP).