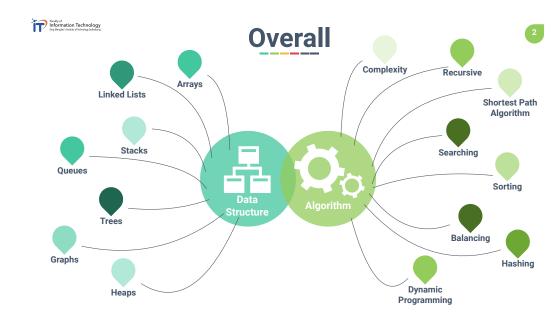


# Introduction to Data Structures and Algorithms

Dr. Sirasit Lochanachit













# What is "Data Structure"?







- Strengths and limitations
- Time and space complexity



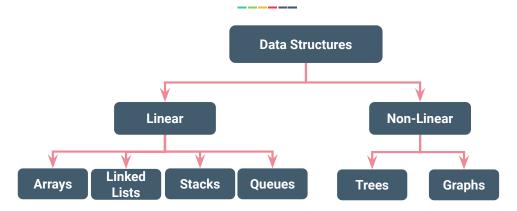


# **Abstract Data Type**

- A data type, where only behavior is defined but not implementation.
- Similar to a black box where input and output are known, but not how.
- Examples: Array, List, Map, Queue, Set, and etc.



# **Type of Data Structure**



Check out for a comprehensive list of data structures at <a href="https://en.wikipedia.org/wiki/List">https://en.wikipedia.org/wiki/List</a> of data structures



# What is "Algorithm"?

- Well-defined procedure or set of instructions to accomplish a task
- Sequence of steps that transform input into output
- Tool to solve a well-specified computational problem



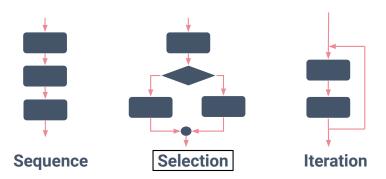
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# **Example: Sorting numbers**

- 1. Input:
  - A sequence of n numbers: <a1, a2, ..., an>
  - <31, 41, 59, 26, 41>
- 2. Sorting Algorithms
- 3. Output:
  - A permutation (reordering) <a'1, a'2, ..., a'n>
     of input sequence such that a'1 <= a'2 <= ... <= a'n</li>
  - <26, 31, 41, 41, 59>

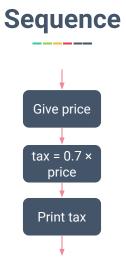
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# **Control Structure**





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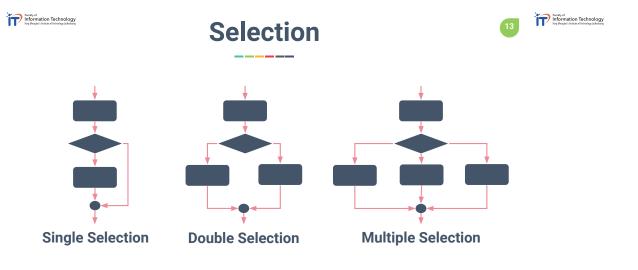


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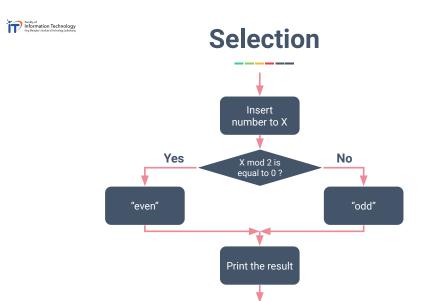
# **Exercise: Sequence**

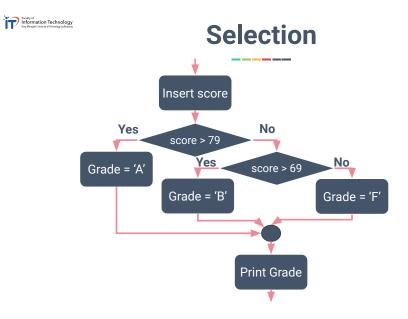
Write a flowchart that converts USD currency to Thai baht. At the end of the flowchart, print the Thai baht. (Exchange rate USD to Thai baht is 32.00)

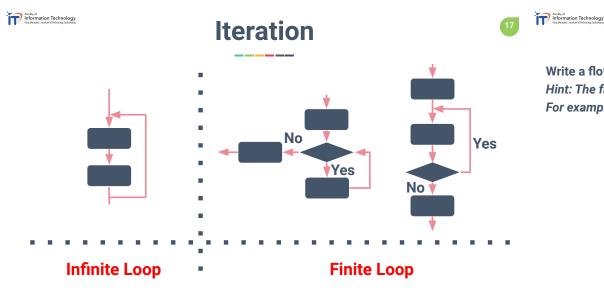












### **Exercise: Control Flow**

Write a flowchart describing the logic of factorial function.

Hint: The factorial n!, is the product of all positive integers less than or equal to n. For example: 5! = 5 \* 4 \* 3 \* 2 \* 1 = 120

# What kind of problems are solved by algorithms?

- Human Genome Project
  - o identifying all genes of human beings
- Internet: Routing, searches, and security
  - Shortest path, search engines, encrypted communication
- E-commerce
  - Ads, recommendations, authentications
- Commercial enterprises
  - Resource allocation:
    - crew assignment on flights, package delivery route

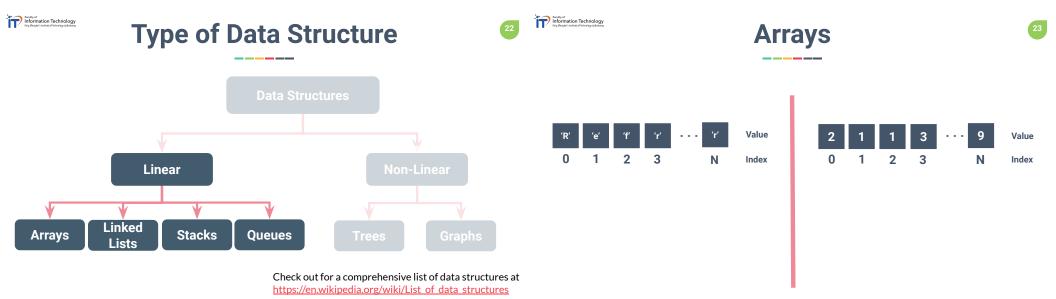


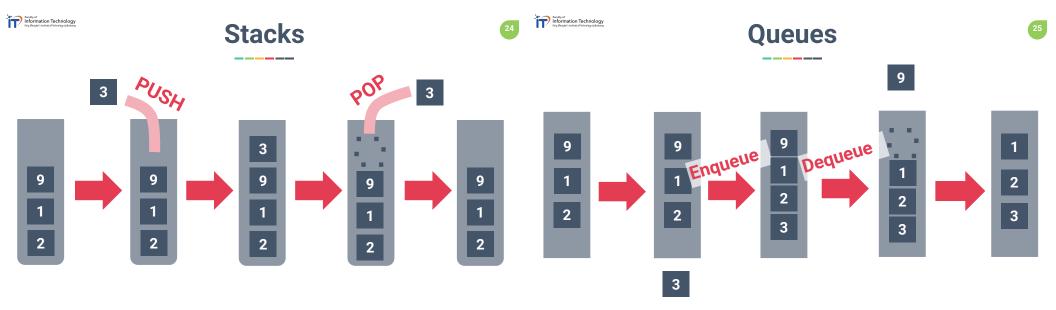
# **Data Structures and Algorithms**



- Way to store and organise data
- Algorithms
  - Sequence of steps performed on data structures to perform a task











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**Linked Lists** 

Linked Lists





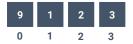


# **Linked Lists VS Arrays**

Linked Lists

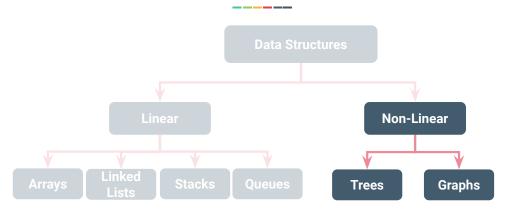


Arrays





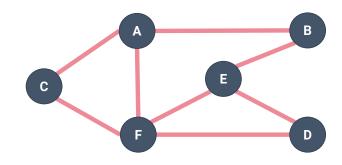
# **Type of Data Structure**



Check out for a comprehensive list of data structures at <a href="https://en.wikipedia.org/wiki/List">https://en.wikipedia.org/wiki/List</a> of data structures









# **Algorithm Analysis**



- If computers were infinitely fast, **any correct method** for solving a problem would do.
- Computing time and space in memory are a limited resource.
- The solution should run as fast as possible.
- For the same problem, it can be solved by different algorithms but they are often differ in their efficiency.
- Algorithms that are efficient in terms of time or space are preferred.

# Algorithm Analysis

- How do we measure algorithm **efficiency** or **performance**?
  - Use running time as an indicator.

# **Benchmark Analysis**





# **Algorithm Analysis**



- Example: Summation of *n* integers
  - Time required for the iterative solution seems to increase as we increase the value of *n*.
- Running time depends on many factors
  - o Hardware (CPU, RAM, etc.)
  - o Software (OS, Programming language, etc.)
- Need an alternative way for analysing algorithms with respect to running time

- How do we measure algorithm **efficiency** or **performance**?
  - Use running time as an indicator.
- Running time can be expressed as the number of operations or steps executed.
  - o theSum = 0

-> 1 step/time

Time

- $\Rightarrow$  for i in range(1,n+1):
  - theSum = theSum + i
- -> <mark>n</mark> steps/time:

### T(n) = 1 + 1



# **Algorithm Analysis**







- The running time of an algorithm or data structure operation increases with the input size.
- Running time as a function of the input size f(n)
- As *n* gets larger, the constant will become less significant.
- Order of magnitude/growth describes the running time that is most important.

- Example:
  - Suppose an algorithm runs on an input size n.
  - Times required to execute is  $T(n) = 2n^2 + n + 1$
  - The **n**<sup>2</sup> terms become larger when **n** gets larger.
  - The running time of this algorithm grows as **n**<sup>2</sup>.
- Asymptotic notation represents algorithm's complexity
  - o Ignores constant factors and slower growing terms.
  - o Focus on the main components that affect the growth.
  - Big-O notation



### Big-O notation (Order)

- Example:
  - Given T(n) = 1+n, then T(n) = O(n)
  - Given  $T(n) = 2n^2 + n + 1$ , then  $T(n) = O(n^2)$
- •O(n) means time complexity will never exceed n.

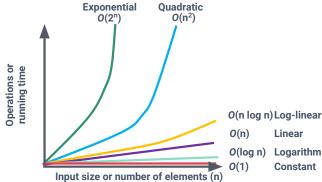
### Big-O notation (Order)

- Common f(n):
  - O(1): constant
  - O(log n): logarithm
  - O(n): Linear
  - O(n log n): Log linear
  - O(n2): Quadratic
  - O(2<sup>n</sup>): Exponential
  - O(n!): Factorial



# **Time Complexity**

In general, the standard functions of input size n are shown in figure.

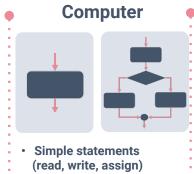


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# **Calculating Time Complexity**

### **Mathematic**

f(n) = 3



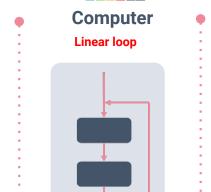
Simple operations (+ - \* / == > >= < <=)

Big-0





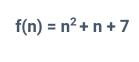
f(n) = n-3

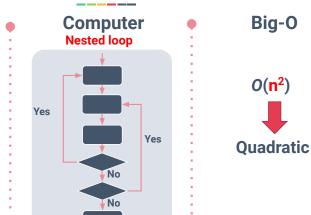


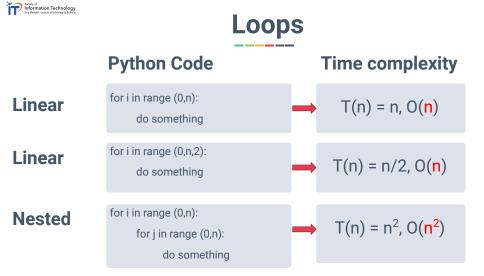
Big-O

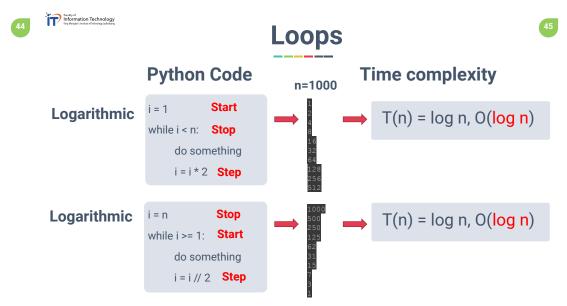


Mathematic











Linear

logarithmic

# Loops

log n

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# Loops

### **Python Code**

for i in range (0,n): n

while j < n:

j = j\*2

do something

j = 1

### Time complexity

T(n) = nlog n, O(nlog n)

**Dependent Nested** 

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Time complexity

for i in range (0,n): **n**  $T(n) = n(n+1)/2, O(n^2)$ for j in range(0, i+1):(n+1)/2 do something

Number of iterations of the inner loop depends on the outer loop

For the inner loop, the number of iterations is (n+1)/2

For example, 
$$n = 3$$
,  $i = 0$  then  $j = [0]$ ,  $i = 1$  then  $j = [0, 1]$ ,  $i = 2$  then  $j = [0, 1, 2]$ 

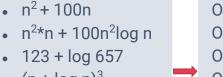
**Python Code** 

# Faculty of Information Technology

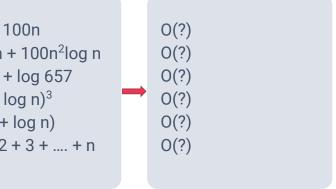
### **Exercise**

### **Exercise**

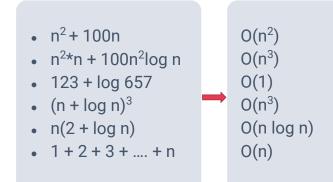
# **Time complexity**



• 
$$(n + \log n)^3$$
  $0(3)$   
•  $n(2 + \log n)$ 



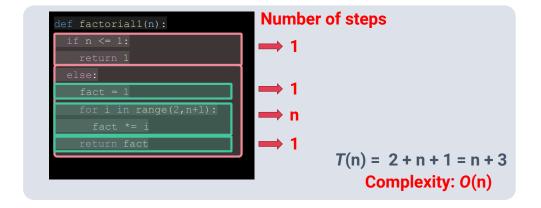
# **Time complexity**





# **Calculating Time Complexity**

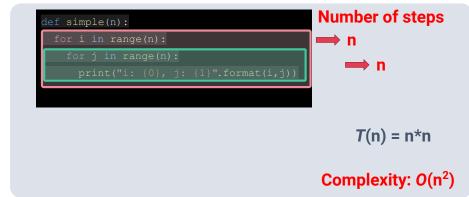
Python Code: Factorial





# **Calculating Time Complexity**

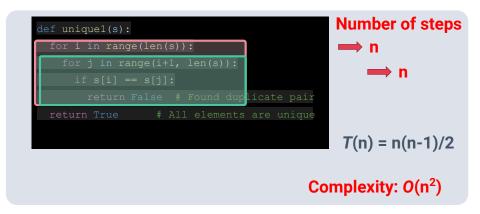
**Python Code: Simple nested loops** 





# **Calculating Time Complexity**

Python Code: Element uniqueness v1



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# **Calculating Time Complexity**

Python Code: Element uniqueness v2

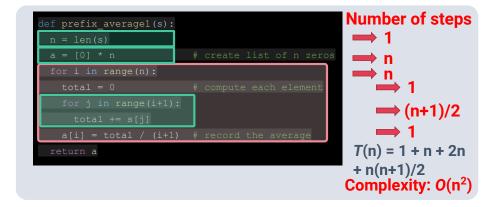




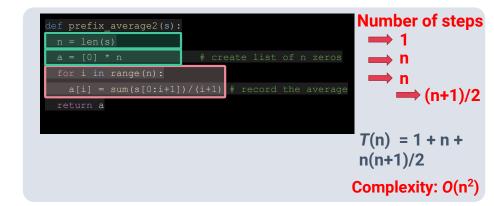
# **Calculating Time Complexity**

**Calculating Time Complexity** 

Python Code: Prefix averages v1



Python Code: Prefix averages v2





# **Calculating Time Complexity**

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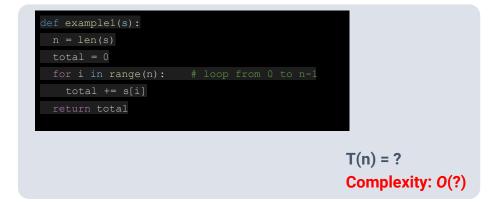
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### Exercise 1

Python Code: Prefix averages v3



**Python Code** 

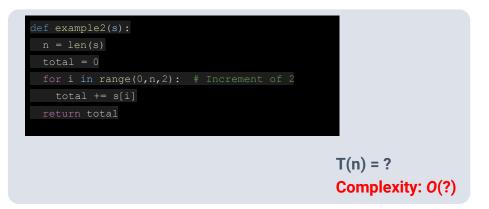


### **Exercise 2**



### **Exercise 3**

### **Python Code**



### **Python Code**

```
def example3(s):
    n = len(s)
    total = 0
    for i in range(n):  # loop from 0 to n-1
        for k in range(1+i):  # loop from 0 to i
            total += s[k]
    return total

T(n) = ?
Complexity: O(?)
```



### **Exercise 4**

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### **Exercise 5**

### **Python Code**



# **Python Code**

```
# Assume that A and B have equal length of n
def example5(A,B):
    n = len(A)
    count = 0
    for i in range(n):  # loop from 0 to n-1
        total = 0
        for j in range(n):  # loop from 0 to n-1
            for k in range(1+j):  # loop from 0 to j
                total += A[k]
        if B[i] == total:
            count += 1
        return count
T(n) = ?
Complexity: O(?)
```

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