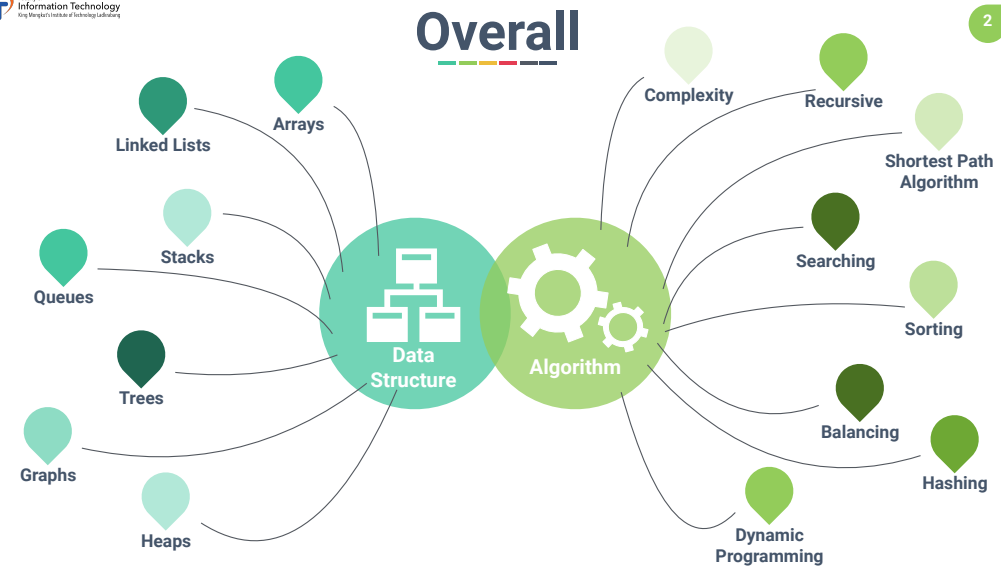


# Introduction to Data Structures and Algorithms

Dr. Sirasit Lochanachit



## Overall



## What is “Data Structure” ?



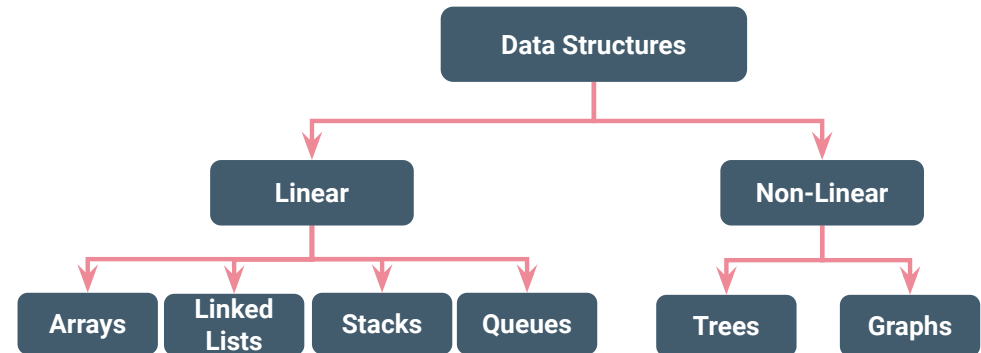
- Way to store and organise data
- Enable efficient access and modification of data
- Designed for a specific algorithm
  - Strengths and limitations
  - Time and space complexity

## Abstract Data Type

- A data type, where only behavior is defined but not implementation.
- Similar to a black box where input and output are known, but not how.
- Examples: Array, List, Map, Queue, Set, and etc.

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## Type of Data Structure



Check out for a comprehensive list of data structures at [https://en.wikipedia.org/wiki/List\\_of\\_data\\_structures](https://en.wikipedia.org/wiki/List_of_data_structures)

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## What is “Algorithm” ?

- Well-defined procedure or set of instructions to accomplish a task
- Sequence of steps that transform input into output
- Tool to solve a well-specified computational problem



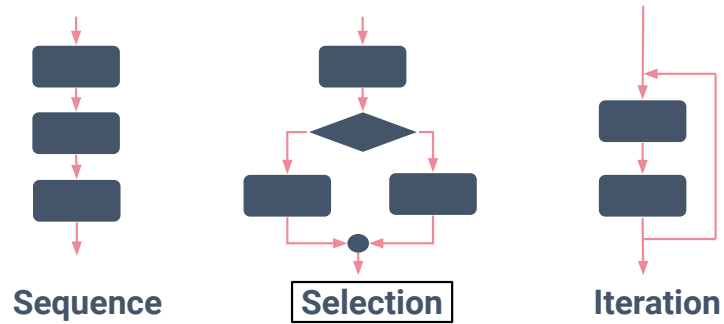
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## Example: Sorting numbers

1. Input:
  - A sequence of n numbers:  $\langle a_1, a_2, \dots, a_n \rangle$
  - $\langle 31, 41, 59, 26, 41 \rangle$
2. Sorting Algorithms
3. Output:
  - A permutation (reordering)  $\langle a'_1, a'_2, \dots, a'_n \rangle$  of input sequence such that  $a'_1 \leq a'_2 \leq \dots \leq a'_n$
  - $\langle 26, 31, 41, 41, 59 \rangle$

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## Control Structure



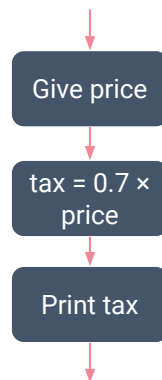
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## Sequence



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## Sequence



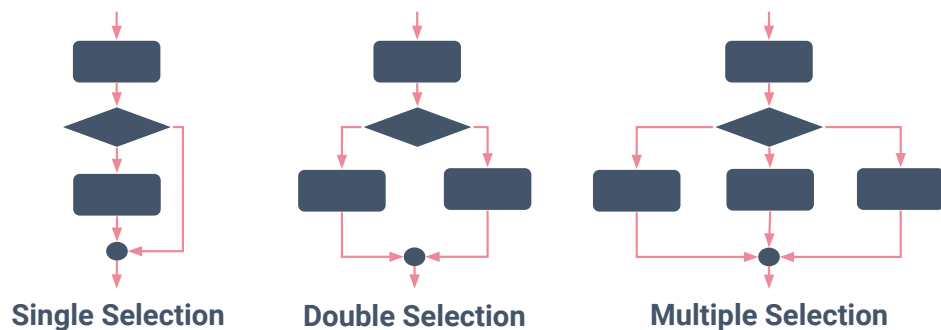
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## Exercise: Sequence

Write a flowchart that converts **USD currency** to **Thai baht**. At the end of the flowchart, print the **Thai baht**. (Exchange rate USD to Thai baht is 32.00)

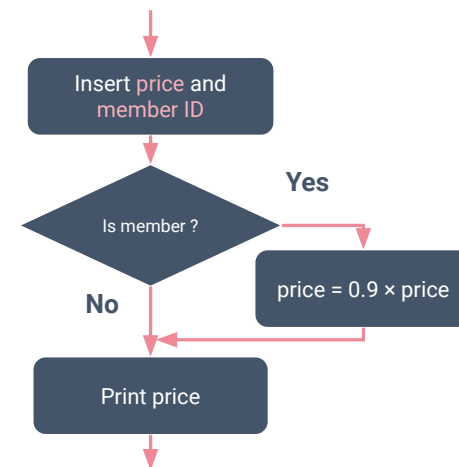
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## Selection



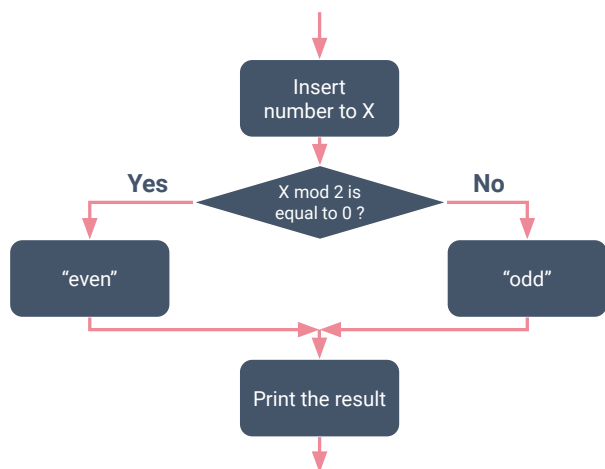
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## Selection



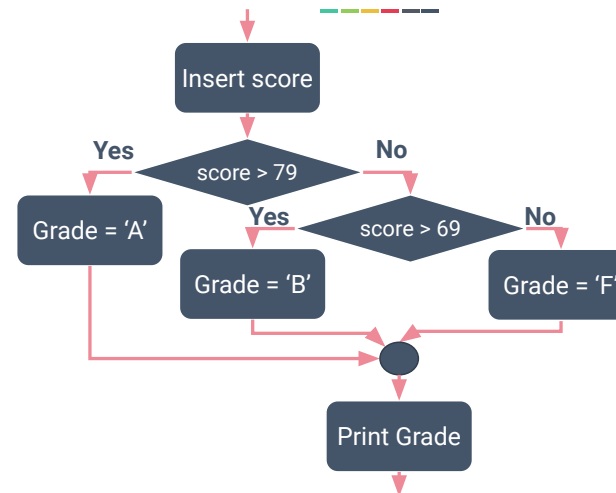
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## Selection



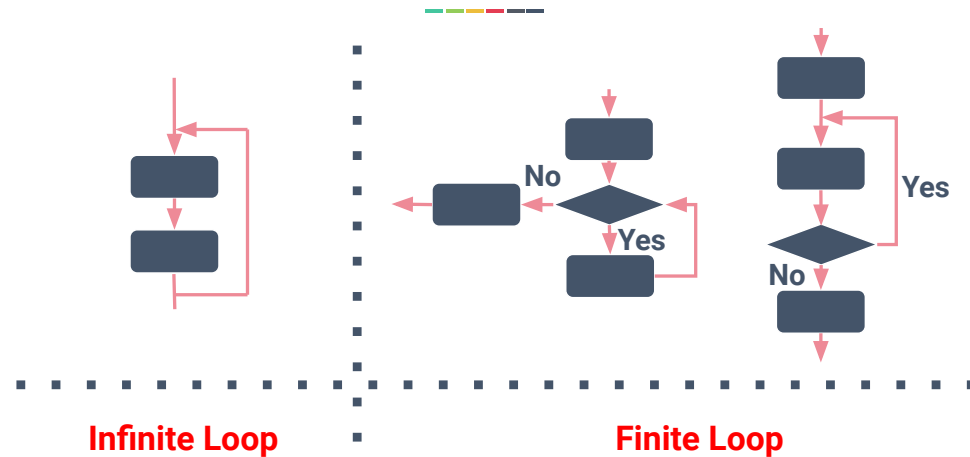
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## Selection



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## Iteration



## Exercise: Control Flow

Write a flowchart describing the logic of factorial function.

Hint: The factorial  $n!$ , is the product of all positive integers less than or equal to  $n$ .

For example:  $5! = 5 * 4 * 3 * 2 * 1 = 120$

## What kind of problems are solved by algorithms?

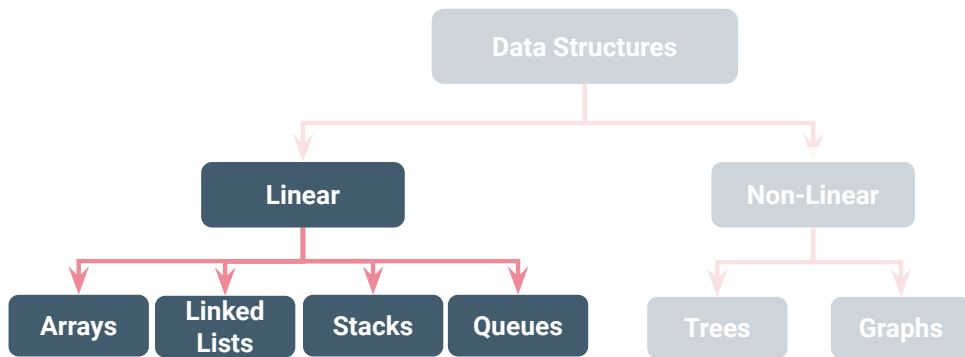
- Human Genome Project
  - identifying all genes of human beings
- Internet: Routing, searches, and security
  - Shortest path, search engines, encrypted communication
- E-commerce
  - Ads, recommendations, authentications
- Commercial enterprises
  - Resource allocation:
    - crew assignment on flights, package delivery route

## Data Structures and Algorithms

- Data Structures
  - Way to store and organise data
- Algorithms
  - Sequence of steps performed on data structures to perform a task

# Type of Data Structure

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Check out for a comprehensive list of data structures at  
[https://en.wikipedia.org/wiki/List\\_of\\_data\\_structures](https://en.wikipedia.org/wiki/List_of_data_structures)

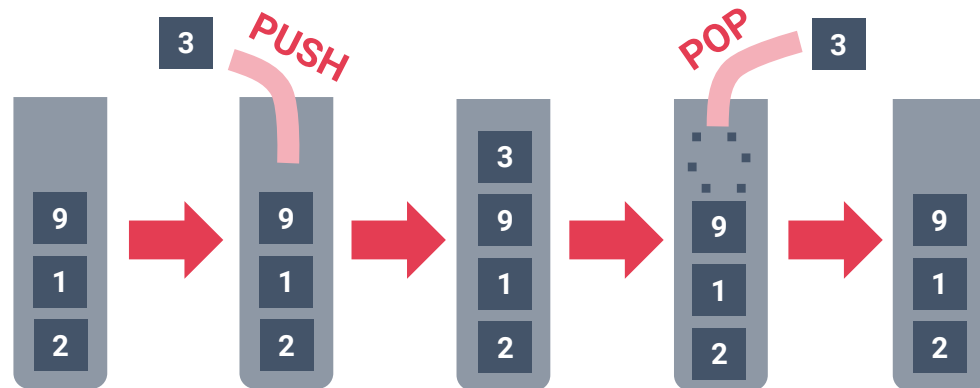
# Arrays

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'R'	'e'	'f'	'r'	...	'r'	Value	2	1	1	3	...	9	Value
0	1	2	3		N	Index	0	1	2	3		N	Index

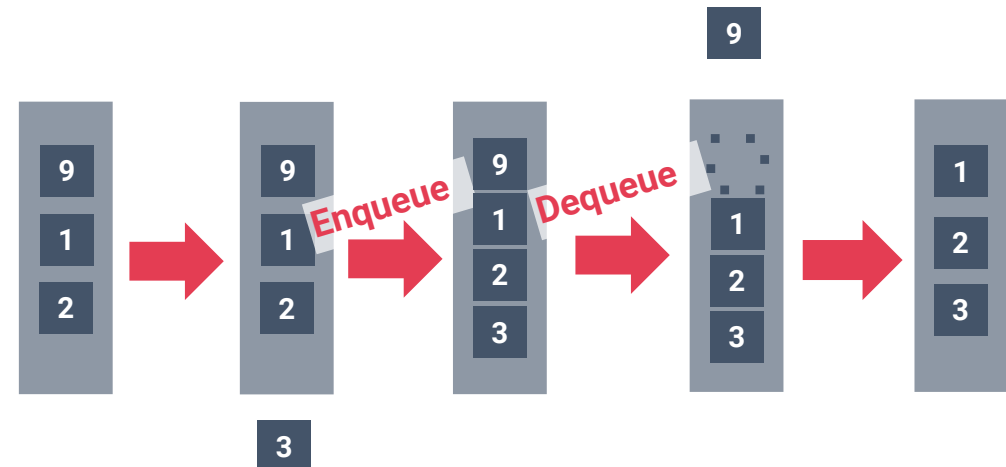
# Stacks

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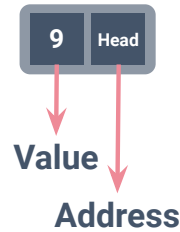


# Queues

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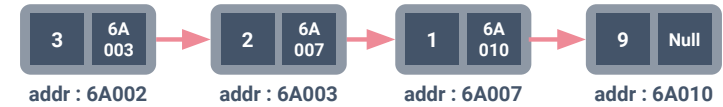
# Linked Lists



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# Linked Lists

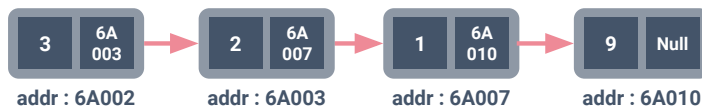
## • Linked Lists



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# Linked Lists VS Arrays

## • Linked Lists

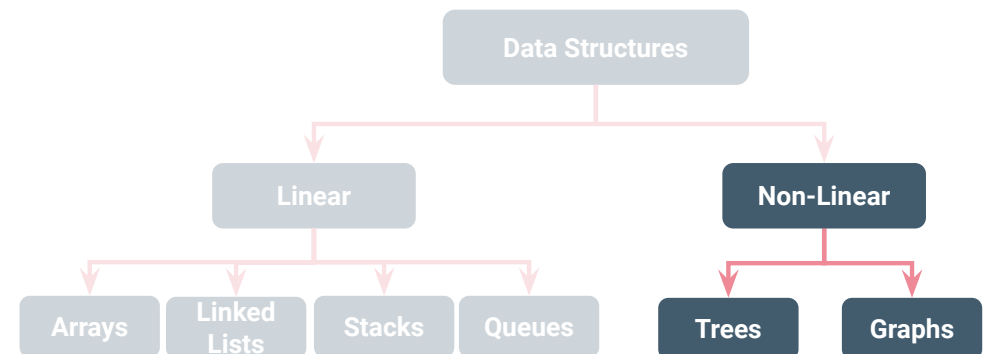


## • Arrays



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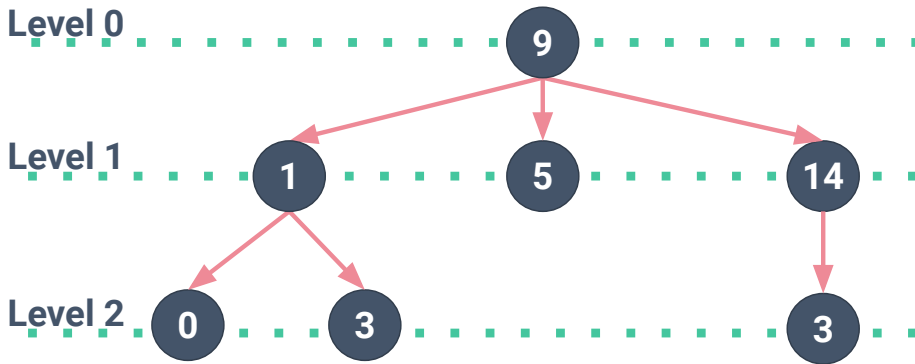
# Type of Data Structure



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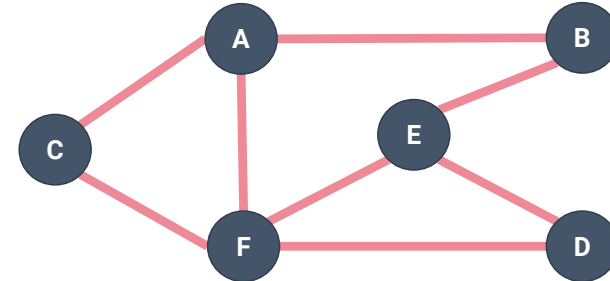
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## Trees



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## Graphs



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## Algorithm Analysis

- If computers were infinitely fast, **any correct method** for solving a problem would do.
- Computing time and space in memory are a limited resource.
- The solution should run as fast as possible.
- For the same problem, it can be solved by different algorithms but they are often differ in their efficiency.
- **Algorithms that are efficient in terms of time or space are preferred.**

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## Algorithm Analysis

- How do we measure algorithm **efficiency** or **performance**?
  - Use **running time** as an indicator.

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## Benchmark Analysis

- Example: Summation of  $n$  integers
  - Time required for the iterative solution seems to increase as we increase the value of  $n$ .
- Running time depends on many factors
  - Hardware (CPU, RAM, etc.)
  - Software (OS, Programming language, etc.)
- Need an alternative way for analysing algorithms with respect to running time

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## Algorithm Analysis

- How do we measure algorithm **efficiency** or **performance**?
  - Use **running time** as an indicator.
- Running time can be expressed as the number of operations or steps executed.
  - `theSum = 0` → 1 step/time
  - `for i in range(1,n+1):`  
`theSum = theSum + i` →  $n$  steps/times

Time  
complexity  
 $T(n) = 1+n$

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## Algorithm Analysis

- The parameter  $n$  is often referred as “**size of the problem**” or **input size**
- The running time of an algorithm or data structure operation **increases** with the input size.
- Running time as a function of the input size -  $f(n)$
- As  $n$  gets larger, the constant will become less significant.
- **Order of magnitude/growth** describes the running time that is most important.

## Asymptotic Notation

- Example:
  - Suppose an algorithm runs on an input size  $n$ .
  - Times required to execute is  $T(n) = 2n^2 + n + 1$
  - The  $n^2$  terms become **larger** when  $n$  gets larger.
  - The running time of this algorithm grows as  $n^2$ .
- Asymptotic notation represents algorithm's complexity
  - Ignores constant factors and slower growing terms.
  - Focus on the main components that affect the growth.
  - **Big-O notation**

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## Big-O notation

### •Big-O notation (Order)

#### •Example:

- Given  $T(n) = 1+n$ , then  $T(n) = O(n)$
- Given  $T(n) = 2n^2 + n + 1$ , then  $T(n) = O(n^2)$

• **$O(n)$  means time complexity will never exceed  $n$ .**

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## Big-O notation

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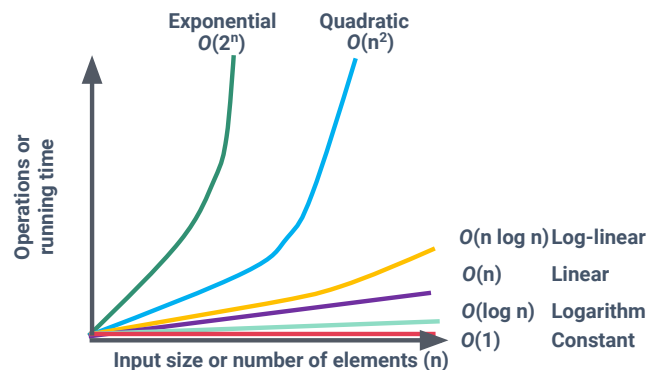
### •Big-O notation (Order)

#### •Common $f(n)$ :

- $O(1)$ : constant
- $O(\log n)$ : logarithm
- $O(n)$ : Linear
- $O(n \log n)$ : Log linear
- $O(n^2)$ : Quadratic
- $O(2^n)$ : Exponential
- $O(n!)$ : Factorial

## Time Complexity

In general, the standard functions of input size  $n$  are shown in figure.



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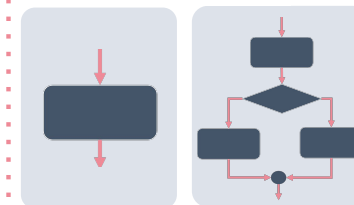
## Calculating Time Complexity

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### Mathematic

$$f(n) = 3$$

### Computer



- Simple statements (read, write, assign)
- Simple operations (+ - \* / == > >= < <=)

### Big-O

$$O(1)$$

↓  
**Constant**

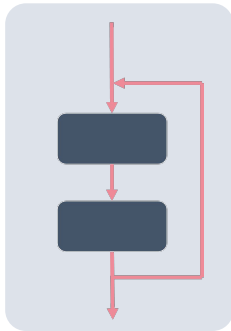
# Calculating Time Complexity

Mathematic

$$f(n) = n - 3$$

Computer

Linear loop



Big-O

$$O(n)$$

Linear

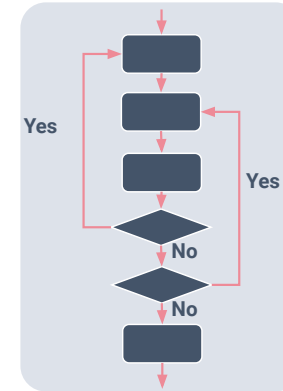
# Calculating Time Complexity

Mathematic

$$f(n) = n^2 + n + 7$$

Computer

Nested loop



Big-O

$$O(n^2)$$

Quadratic

## Loops

Python Code

Time complexity

Linear

```
for i in range(0,n):
    do something
```

$$T(n) = n, O(n)$$

Linear

```
for i in range(0,n/2):
    do something
```

$$T(n) = n/2, O(n)$$

Nested

```
for i in range(0,n):
    for j in range(0,n):
        do something
```

$$T(n) = n^2, O(n^2)$$

## Loops

Python Code

Time complexity

Logarithmic

```
i = 1
while i < n:
    do something
    i *= 2
```

n=1000

1  
2  
4  
8  
16  
32  
64  
128  
256  
512

$$T(n) = \log n, O(\log n)$$

Logarithmic

```
i = n
while i >= 1:
    do something
    i //= 2
```

1000  
500  
250  
125  
62  
31  
15  
7  
3  
1

$$T(n) = \log n, O(\log n)$$

## Loops

### Python Code

```
for i in range(0, n):
    j = 1
    while j < n:
        do something
        j *= 2
```

### Time complexity

$$T(n) = n \log n, O(n \log n)$$

Linear  
logarithmic

## Loops

### Python Code

```
for i in range(0, n):
    for j in range(0, i+1):
        do something
```

### Time complexity

$$T(n) = n(n+1)/2, O(n^2)$$

Dependent  
Nested

Number of iterations of the inner loop depends on the outer loop

For the inner loop, the number of iterations is  $(n+1)/2$

## Exercise

### Time complexity

- $n^2 + 100n$
- $n^2 * n + 100n^2 \log n$
- $123 + \log 657$
- $(n + \log n)^3$
- $n(2 + \log n)$
- $1 + 2 + 3 + \dots + n$

- $O(?)$
- $O(?)$
- $O(?)$
- $O(?)$
- $O(?)$
- $O(?)$

## Exercise

### Time complexity

- $n^2 + 100n$
- $n^2 * n + 100n^2 \log n$
- $123 + \log 657$
- $(n + \log n)^3$
- $n(2 + \log n)$
- $1 + 2 + 3 + \dots + n$

- $O(n^2)$
- $O(n^3)$
- $O(1)$
- $O(n^3)$
- $O(n \log n)$
- $O(n)$

# Calculating Time Complexity

## Python Code: Factorial

```
def factorial1(n):
```

```
    if n <= 1:
        return 1
```

```
    else:
```

```
        fact = 1
```

```
        for i in range(2, n+1):
```

```
            fact *= i
```

```
        return fact
```

→  $T(1)$

→  $T(1)$

→  $T(n)$

→  $T(1)$

$$T(n) = 2 + n + 1 = n + 3$$

**Complexity:  $O(n)$**

# Calculating Time Complexity

## Python Code: Simple nested loops

```
def simple(n):
```

```
    for i in range(n):
```

```
        for j in range(n):
```

```
            print("i: {0}, j: {1}".format(i, j))
```

→  $T(n)$

→  $T(n)$

$$T(n) = n * n$$

**Complexity:  $O(n^2)$**

# Calculating Time Complexity

## Python Code: Element uniqueness v1

```
def unique1(s):
```

```
    for i in range(len(s)):
```

```
        for j in range(i+1, len(s)):
```

```
            if s[i] == s[j]:
```

```
                return False # Found duplicate pair
```

```
    return True # All elements are unique
```

→  $T(n)$

→  $T(n)$

$$T(n) = n(n-1)/2$$

**Complexity:  $O(n^2)$**

# Calculating Time Complexity

## Python Code: Element uniqueness v2

```
def unique2(s):
```

```
    temp = sorted(s) # create a sorted copy of s
```

```
    for i in range(1, len(temp)):
```

```
        if temp[i-1] == temp[i]:
```

```
            return False # Found duplicate pair
```

```
    return True # All elements are unique
```

→  $T(n \log n)$

→  $T(n)$

$$T(n) = n \log n + n$$

**Complexity:  $O(n \log n)$**

# Calculating Time Complexity

## Python Code: Prefix averages v1

```
def prefix_average1(s):
    n = len(s)
    a = [0] * n # create list of n zeros
    for i in range(n):
        total = 0 # compute each element
        for j in range(i+1):
            total += s[j]
        a[i] = total / (i+1) # record the average
    return a
```

→  $T(1)$

→  $T(n)$

→  $T(n)$

→  $T(n)$

$$T(n) = 1 + n + 2n + n(n+1)/2$$

**Complexity:  $O(n^2)$**

# Calculating Time Complexity

## Python Code: Prefix averages v2

```
def prefix_average2(s):
    n = len(s)
    a = [0] * n # create list of n zeros
    for i in range(n):
        a[i] = sum(s[0:i+1]) / (i+1) # record the average
    return a
```

→  $T(1)$

→  $T(n)$

→  $T(n)$

→  $T(n)$

$$T(n) = 1 + n + n(n+1)/2$$

**Complexity:  $O(n^2)$**

# Calculating Time Complexity

## Python Code: Prefix averages v3

```
def prefix_average3(s):
    n = len(s)
    a = [0] * n # create list of n zeros
    total = 0
    for i in range(n):
        total += s[i] # update total sum to include s[i]
        a[i] = total / (i+1) # compute average based on
    return a
```

→  $T(1)$

→  $T(n)$

→  $T(1)$

→  $T(n)$

$$T(n) = 2 + n + 2n$$

v3 is asymptotically better than v2 and v1 **Complexity:  $O(n)$**

# Exercise 1

## Python Code

```
def example1(s):
    n = len(s)
    total = 0
    for i in range(n): # loop from 0 to n-1
        total += s[i]
    return total
```

**Complexity:  $O(?)$**

## Exercise 2

### Python Code

```
def example2(s):
    n = len(s)
    total = 0
    for i in range(0,n,2): # Increment of 2
        total += s[i]
    return total
```

Complexity:  $O(?)$

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## Exercise 3

### Python Code

```
def example3(s):
    n = len(s)
    total = 0
    for i in range(n): # loop from 0 to n-1
        for k in range(1+i): # loop from 0 to i
            total += s[k]
    return total
```

Complexity:  $O(?)$

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## Exercise 4

### Python Code

```
def example4(s):
    n = len(s)
    prefix = 0
    total = 0
    for i in range(n):
        prefix += s[i]
        total += prefix
    return total
```

Complexity:  $O(?)$

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## Exercise 5

### Python Code

```
# Assume that A and B have equal length of n
def example5(A,B):
    n = len(A)
    count = 0
    for i in range(n): # loop from 0 to n-1
        total = 0
        for j in range(n): # loop from 0 to n-1
            for k in range(1+j): # loop from 0 to j
                total += A[k]
            if B[i] == total:
                count += 1
    return count
```

Complexity:  $O(?)$

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