

# TRAINED TERNARY QUANTIZATION

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# Overview

- **two quantization factors** for positive and negative weights
- trained quantization by back propagating **two gradients**

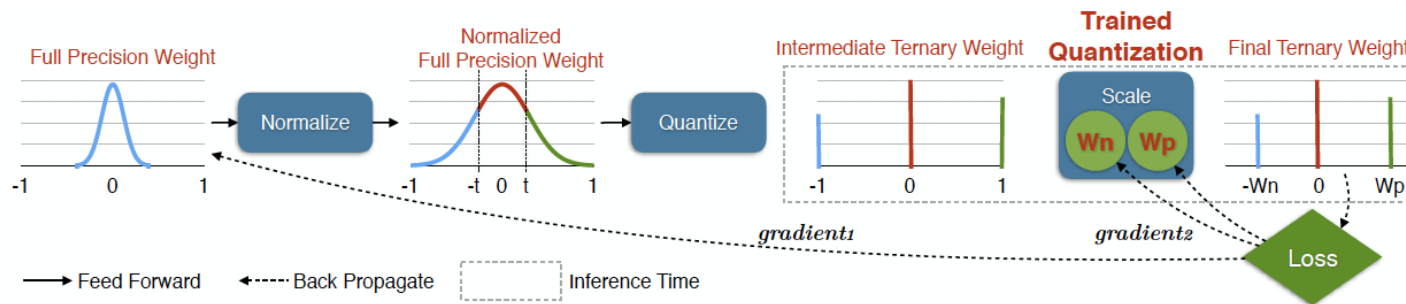


Figure 1: Overview of the trained ternary quantization procedure.

TTQ

$$w_l^t = \begin{cases} W_l^p : \tilde{w}_l > \Delta_l \\ 0 : |\tilde{w}_l| \leq \Delta_l \\ -W_l^n : \tilde{w}_l < -\Delta_l \end{cases} \quad (6)$$

$$\frac{\partial L}{\partial W_l^p} = \sum_{i \in I_l^p} \frac{\partial L}{\partial w_l^t(i)}, \frac{\partial L}{\partial W_l^n} = \sum_{i \in I_l^n} \frac{\partial L}{\partial w_l^t(i)} \quad (7)$$

Here  $I_l^p = \{i | \tilde{w}_l(i) > \Delta_l\}$  and  $I_l^n = \{i | \tilde{w}_l(i) < -\Delta_l\}$ .

$$\frac{\partial L}{\partial \tilde{w}_l} = \begin{cases} W_l^p \times \frac{\partial L}{\partial w_l^t} : \tilde{w}_l > \Delta_l \\ 1 \times \frac{\partial L}{\partial w_l^t} : |\tilde{w}_l| \leq \Delta_l \\ W_l^n \times \frac{\partial L}{\partial w_l^t} : \tilde{w}_l < -\Delta_l \end{cases} \quad (8)$$

# QUANTIZATION HEURISTIC

different heuristics: 1) use the maximum absolute value of the weights as a reference to the layer's threshold and maintain a constant factor  $t$  for all layers:

$$\Delta_l = t \times \max(|\tilde{w}|) \quad (9)$$

and 2) maintain a constant sparsity  $r$  for all layers throughout training. By adjusting the hyperparameter  $r$  we are able to obtain ternary weight networks with various sparsities. We use the first method and set  $t$  to 0.05 in experiments on CIFAR-10 and ImageNet dataset and use the second one to explore a wider range of sparsities in section 5.1.1.

# Experiments

Model	Full resolution	Ternary (Ours)	Improvement
ResNet-20	8.23	<b>8.87</b>	<b>-0.64</b>
ResNet-32	7.67	<b>7.63</b>	<b>0.04</b>
ResNet-44	7.18	<b>7.02</b>	<b>0.16</b>
ResNet-56	6.80	<b>6.44</b>	<b>0.36</b>

Table 1: Error rates of full-precision and ternary ResNets on Cifar-10

Error	Full precision	1-bit (DoReFa)	2-bit (TWN)	2-bit (Ours)
Top1	42.8%	46.1%	45.5%	<b>42.5%</b>
Top5	19.7%	23.7%	23.2%	<b>20.3%</b>

Table 2: Top1 and Top5 error rate of AlexNet on ImageNet

Error	Full precision	1-bit (BWN)	2-bit (TWN)	2-bit (Ours)
Top1	30.4%	39.2%	34.7%	<b>33.4%</b>
Top5	10.8%	17.0%	13.8%	<b>12.8%</b>

Table 3: Top1 and Top5 error rate of ResNet-18 on ImageNet