PEKING UNIVERSITY

Answer Key 13

▼ 袁磊祺

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P148

10 Let
$$\eta = \sum_{i=1}^{n} \frac{(-1)^{i-1}}{n} x_i dx_1 \wedge \cdots \wedge d\hat{x}_i \wedge \cdots \wedge dx_n$$
 and verify that $d\eta = \omega$

11 Let ω be k-form

$$\therefore d(\omega \wedge \eta) = d\omega \wedge \eta + (-1)^k \omega \wedge d\eta = 0$$

12 Let ω be k-form and $\eta = d\varphi$

$$d[(-1)^k\omega\wedge\varphi]=(-1)^kd\omega\wedge\varphi+\omega\wedge d\varphi=\omega\wedge\eta$$