Al6122 Text Data Management & Analysis

Topic: tokenization, morphology, stem, lemmatization

What to be covered

- Token and Tokenization
- Stop words
- English Morphology
- Stemming and Lemmatization
- Edit Distance

Token

- A token is an instance of a sequence of characters in some document that are grouped together as a useful semantic unit for processing.
 - Often loosely referred to as words (or terms)
 - May include punctuations or emojis
- Tokenization: Identifying the tokens in a text that we may want to deal with
 - Also called word segmentation, word tokenization
 - Pretty much a prerequisite to doing anything interesting
- Example input: "Friends, Romans and Countrymen"
 - tokens: Friends, Romans, Countrymen
- Tokenization is language dependent, e.g., English, Chinese

Tokenization

- For English, why not just use white-space?
 - Mr. Sherwood said reaction to Sea Containers' proposal has been "very positive." In New York Stock Exchange composite trading yesterday, Sea Containers closed at \$62.625, up 62.5 cents.
 - "I said, 'what're you? Crazy?' " said Sadowsky. "I can't afford to do that."
- Using white-space gives you words like:
 - cents.
 - said,
 - positive."
 - Crazy?'

Tokenization: issues

- Word-internal punctuation
 - M.P.H. Ph.D. AT&T Google.com Yahoo!
- Other Examples:
 - Finland's capital → Finland? Finlands? Finland's?
 - Hewlett-Packard → Hewlett and Packard as two tokens?
 - state-of-the-art: break up hyphenated sequence.
 - co-education, lowercase, lower-case, lower case?
- How about names?
 - San Francisco: one token or two?
 - How do you decide it is one token? Then how about "San Francisco Airport"?
- What about numbers?
 - 3/20/91 Mar. 12, 1991 20/3/91
 - 55 B.C., B-52, My PGP key is 324a3df234cb23e
 - This is my number: (800) 234-2333

Tokenization: Implementation

- Tokenization needs to be run before any other language processing,
 - it needs to be very fast.
 - Standard method for tokenization is to use deterministic algorithms based on regular expressions compiled into very efficient finite state automata.
 - Example Python-based Natural Language Toolkit (NLTK)

```
>>> text = 'That U.S.A. poster-print costs $12.40...'
>>> pattern = r'''(?x)  # set flag to allow verbose regexps
... ([A-Z]\.)+  # abbreviations, e.g. U.S.A.
... | \w+(-\w+)*  # words with optional internal hyphens
... | \$?\d+(\.\d+)?%?  # currency and percentages, e.g. $12.40, 82%
... | \.\.\  # ellipsis
... | [][.,;"'?():-_']  # these are separate tokens; includes ], [
... '''
>>> nltk.regexp_tokenize(text, pattern)
['That', 'U.S.A.', 'poster-print', 'costs', '$12.40', '...']
```

Figure 2.11 A python trace of regular expression tokenization in the NLTK (Bird et al., 2009) Python-based natural language processing toolkit, commented for readability; the (?x) verbose flag tells Python to strip comments and whitespace. Figure from Chapter 3 of Bird et al. (2009).

Examples of other issues

- URL segmentation
 - www.dietsthatwork.com
 - www.choosespain.com
- Hashtag segmentation
 - #unitedbrokemyguitar
 - + manchesterunited
 - allows Twitter users to track what many people (especially people whom you aren't already following) are reporting or thinking about a particular topic or event.

What about code?



Questions

Tags

Tour

Users

Stack Overflow is a question and answer site for professional and enthusiast programmers. It's 100% free, no registration required.

EF6 - Value cannot be null. Parameter name: extent



I'm using EF6 code first to create my db. Everything was working well last night, now when i run updatedatabase command, I get the following exception:



PM> update-database
Specify the '-Verbose' flag to view the SQL statements being applied t searchcode

System.ArgumentNullException: Value cannot be null.
Parameter name: extent
 at System.Data.Entity.Utilities.Check.NotNull[T](T value, String pa

at System.Data.Entity.Core.Mapping.StorageEntitySetMapping..ctor(En at System.Data.Entity.ModelConfiguration.Edm.DbDatabaseMappingExten at System.Data.Entity.ModelConfiguration.Edm.Services.TableMappingG at System.Data.Entity.ModelConfiguration.Edm.Services.DatabaseMappi at System.Data.Entity.ModelConfiguration.Edm.Services.DatabaseMappi at System.Data.Entity.DbModelBuilder.Build(DbProviderManifest provi at System.Data.Entity.DbModelBuilder.Build(DbConnection providerCon

at System.Data.Entity.Internal.LazyInternalContext.CreateModel(Lazy
at System.Data.Entity.Internal.RetryLazy`2.GetValue(TInput input)

at System.Data.Entity.Internal.LazyInternalContext.InitializeContex at System.Data.Entity.Internal.LazyInternalContext.get CodeFirstMod earchcode binarytree lang:Java

Run searchcode locally? Want to run your own version of searchcode

About 419 results

BinaryTree.java in rose_backup https://github.com/dpick/rose_backup.git | 171 lines | Java

1. // BinaryTree class; stores a binary tree.

```
8. // Also, the following tricky method:
9. // void merge( Object root, BinaryTree t1, BinaryTree t2 )
10. // --> Construct a new tree
```

14. /**

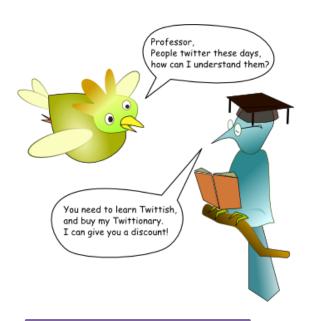
2.//

15. * BinaryTree class that illustrates the calling of BinaryNode recursive 16. * routines and merge.

17. */

18. public class BinaryTree {

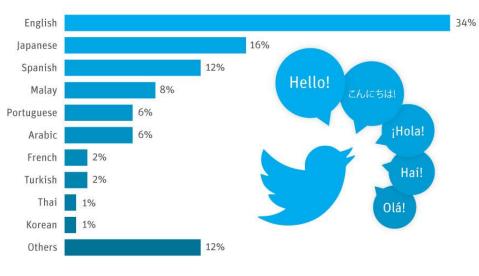
Is language really an issue here?



shd, ishould, shudd, shuld, shoud, shud, shld, sould, shouldd

Only 34% of All Tweets Are in English

Distribution of languages used in Tweets around the world (September 2013)



statista Mashable
The Statistics Portal

Source: Semiocast

http://languagetime.files.wordpress.com/2013/12/131217_twitter_sprachen_mashable_n.jpg

Words grouping by Brown Clustering

^ <u>01110111001</u> (43)	everything everythin everthing evrything everything everything everything everything everything everything errthing errthing errthing errthing errthing errthing errything errything errything everything everyth
^ <u>01110111010</u> (85)	nothing nothin nun nuthin nuttin nuffin 10x noting nthn nowt nuthn nuthing 100x nothingg nothn nothinq nutin notin nuffn nutn whatevers #nodisrespect nuttn nothinggg #dontmeantobrag 1000x zilch nothinn #nothing nothing nutting nufin nuin nout nothinqq nthng nthing nothingggg nufn nofin nothen nthin nottin nttn nought ntg nothinnn nothign n0thing nothig
^ <u>011101110110</u> (108)	something somethin sumthin sumthing sumn somthing sth sumthn sumtin smth somthin suttin sumin something summin treaters something someting sumfin smthn something summat smthng smthing sum'n sumthing smthg somn sumting something somethin
^ <u>011101110111</u> (36)	anything anythin nething anything woodsen endsmeat anything/anyone aything anything enything

Source: http://www.cs.cmu.edu/~ark/TweetNLP/cluster_viewer.html

Tokenization: language issues

- French
 - L'ensemble → one token or two?
 - L?L'?Le?
 - Want <u>l'ensemble</u> to match with <u>un ensemble</u>
- German noun compounds are not segmented
 - Lebensversicherungsgesellschaftsangestellter
 - 'life insurance company employee'
 - German retrieval systems benefit greatly from a compound splitter module
 - Can give a 15% performance boost for German

Tokenization: language issues

- Chinese and Japanese have no spaces between words:
 - 莎拉波娃现在居住在美国东南部的佛罗里达。
 - Not always guaranteed a unique tokenization
- Japanese is more complicated, with multiple alphabets intermingled
 - Dates/amounts in multiple formats

フォーチュン500社は情報不足のため時間あた\$500K(約6,000万円)

Katakana

Hiragana

Kanji

Romaji

End-user can express query entirely in hiragana!

Tokenization: language issues

- Arabic (or Hebrew) is basically written right to left, but with certain items like numbers written left to right
- Words are separated, but letter forms within a word form complex ligatures

- 'Algeria achieved its independence in 1962 after 132 years of French occupation.'
- With Unicode, the surface presentation is complex, but the stored form is straightforward

Segmentation in Chinese

- Words composed of characters; average word is 2.4 characters long.
- A simple segmentation algorithm based on dictionary:
 - Maximum Matching or Maxmatch
 - Given a lexicon of Chinese, and a string
 - Start a pointer at the beginning of the string
 - Find the longest word in dictionary that matches the string starting at pointer
 - · Move the pointer over the word in string
 - Go to 2
- State-of-the-art solutions are mostly probabilistic and deep learning
 - http://nlpprogress.com/chinese/chinese_word_segmentation.html
 - https://github.com/topics/chinese-text-segmentation
- Recent study: for most Chinese NLP tasks, take characters rather than words as input works better.
 - Characters are at a reasonable semantic level for most applications,
 - Most word standards result in a huge vocabulary with large numbers of very rare words

Maximum Matching Word Segmentation

Lexicon (Dictionary)
the
table
down
there

thetabledownthere



the table down there

Lexicon (Dictionary)
the
theta
table
down
there
bled
own

thetabledownthere

theta bled own there

Byte-Pair Encoding for (subword) Tokenization

- Data driven, and not confine to words or characters
 - Resultant **token** could be smaller than words e.g., -est, er,
 - Or larger than words, e.g., New York Times
 - Have subword tokens to deal with unknown words.
 - Proposed for machine translation, dealing with rare or new words
- Given training data (words are annotated)
 - BPE starts with the set of symbols equal to the set of characters
 - Each word is represented as a sequence of characters plus a special end-ofword symbol _
 - At each step, the most frequent pair ('A', 'B') of symbol pairs is merged, and replaced with the newly merged symbol ('AB')
 - Repeat the step, until we have done k merges (k is a parameter)
 - The final symbol vocabulary size is equal to the size of the initial vocabulary, plus the number of merge operations

BEP Example

- BPE runs inside words, we don't merge across word boundaries
 - The input is a dictionary of words together with their counts

- Count symbol pairs: r _ has highest frequency 9 (6 in newer_ and 3 in wider_)
- Then r_ is merged

After merging "r _" and then "e r_"

dictionary

- 5 low_
- 2 lowest_
- 6 newer_
- 3 wider_
- 2 new_

vocabulary

, d, e, i, l, n, o, r, s, t, w, r

dictionary

- 5 low_
- 2 lowest_
- 6 newer_
- 3 wider_
- 2 new_

vocabulary

 $_$, d, e, i, l, n, o, r, s, t, w, r $_$, er $_$

Continue merging

```
      Merge
      Current Vocabulary

      (n, ew)
      __, d, e, i, l, n, o, r, s, t, w, r__, er__, ew, new

      (l, o)
      __, d, e, i, l, n, o, r, s, t, w, r__, er__, ew, new, lo

      (lo, w)
      __, d, e, i, l, n, o, r, s, t, w, r__, er__, ew, new, lo, low, newer__

      (low, __)
      __, d, e, i, l, n, o, r, s, t, w, r__, er__, ew, new, lo, low, newer__, low__

      (low, __)
      __, d, e, i, l, n, o, r, s, t, w, r__, er__, ew, new, lo, low, newer__, low__
```

Apply BEP for (subword) tokenization

- The merging sequence is what we have learned from training data
- To apply BEP for tokenization on test data
 - We run the merges we have learned, greedily, in the order we learned them
 - The frequencies in the test data don't play a role, just the frequencies in the training data.

Follow the example:

- Segment each test sentence word into characters.
- Apply the first rule: replace every instance of "r _" in the test corpus with "r_", and then the second rule: replace every instance of "e r_" in the test corpus with "er_", and so on.
- By the end, word "n e w e r", it would be tokenized as a full word.
- a new (unknown) word like "I o w e r" would be merged into the two tokens "low" and "er"

Sentence Segmentation

- !, ? are relatively unambiguous
- Period "." is quite ambiguous
 - Sentence boundary
 - Abbreviations like Inc. or Dr.
- General idea:
 - Build a binary classifier:
 - Looks at a "."
 - Decides EndOfSentence/NotEOS
 - Could be hand-written rules, sequences of regular expressions, or machinelearning

Now we mainly focus on words

- Stop words
- English Morphology
- Stemming and Lemmatization

Stop words

- With a stop list, you exclude from the dictionary entirely the commonest words.:
 - They have little semantic content: the, a, and, to, be
 - There are a lot of them: ~30% of postings for top 30 words
- But the trend is away from doing this:
 - Good compression techniques means the space for including stopwords in a system is very small
 - Good query optimization techniques mean you pay little at query time for including stop words.
 - You need them for:
 - Phrase queries: "King of Denmark"
 - Various song titles, etc.: "Let it be", "To be or not to be"
 - "Relational" queries: "flights to London"

English Morphology

- Morphology is the study of the ways that words are built up from smaller meaningful units called morphemes
- We can usefully divide morphemes into two categories
 - Stems: The core meaning-bearing units
 - Affixes: Bits and pieces that adhere to stems to change their meanings and grammatical functions
 - Example
 - cat → cats
 - regular → irregular

English Morphology

- We can further divide morphology up into two broad classes
 - Inflectional: has the same word class as the original, cat -> cats
 - Derivational: changes of word class, care -> careless
- Word Classes
 - By word class, we have in mind familiar notions like noun and verb
 - We'll go into the details in POS tagging
 - Right now we're concerned with word classes because the way that stems and affixes combine is based to a large degree on the word class of the stem

Inflectional Morphology

- Inflectional morphology concerns the combination of stems and affixes where the resulting word:
 - Has the same word class as the original
 - Fill some syntactic function like agreement
 - Nouns are simple
 - Markers for plural and possessive
 - Example: table, tables; children, children's
 - Verbs are only slightly more complex
 - Markers appropriate to the tense of the verb
 - Example: walk, walks, walking

Regulars and Irregulars

- It is a little complicated by the fact that some words misbehave (refuse to follow the rules)
 - Mouse/mice, goose/geese, ox/oxen
 - Go/went, fly/flew
- The terms regular and irregular are used to refer to words that follow the rules and those that don't

Regular and Irregular Verbs

- Inflectional morphology in English is fairly straightforward
- But is complicated by the fact that there are irregularities
- Regulars...
 - Walk, walks, walking, walked, walked
- Irregulars
 - Catch, catches, catching, caught, caught
 - Cut, cuts, cutting, cut, cut

Derivational Morphology

- More complicated.
- Many paths are possible...
 - Start with compute
 - Computer -> computerize -> computerization
 - Computer -> computerize -> computerizable
- Meaning change
 - E.g., care -- careless
- Changes of word class

Derivational Examples

Nouns and Verbs → Adjectives

-al	computation	computational
-able	embrace	embraceable
-less	clue	clueless

Verbs and Adjectives → Nouns

-ation	computerize	computerization
-ee	appoint	appointee
-er	kill	killer
-ness	fuzzy	fuzziness

Normalization

- Need to "normalize" terms
 - Information Retrieval: indexed text & query terms must have same form.
 - We want to match U.S.A. and USA
- We implicitly define equivalence classes of terms
 - e.g., deleting periods in a term
- Alternative: asymmetric expansion:

Enter: windowSearch: window, windows

Enter: windows
 Search: Windows, windows, windows

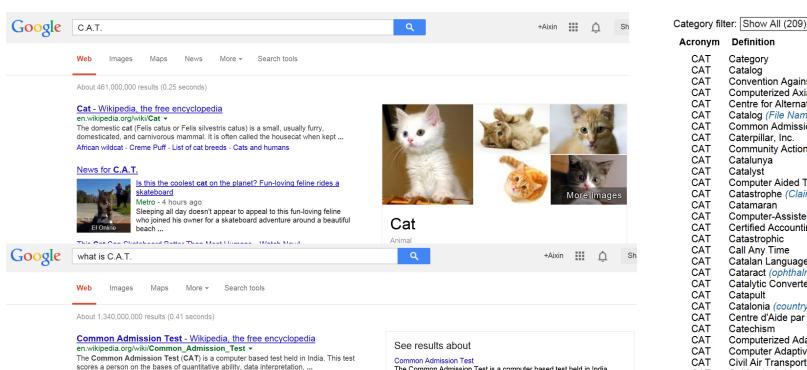
Enter: WindowsSearch: Windows

Potentially more powerful, but less efficient

Case folding

- Applications like IR: reduce all letters to lower case
 - Since users tend to use lower case
 - Possible exception: upper case in mid-sentence?
 - e.g., General Motors
 - Fed vs. fed
 - SAIL vs. sail
- For sentiment analysis, machine translation, information extraction
 - Case is helpful (US versus us is important)

Google's answer to query "C.A.T."



The Common Admission Test is a computer based test held in India.

This test scores a person on the .

The domestic cat is a small, usually furry, domesticated, and carnivorous mammal. It is often ...

Feedback/More info

Acronym Definition CAT Category CAT Catalog CAT Convention Against Torture (United Nations; CAT Computerized Axial Tomography (medical in CAT Centre for Alternative Technology (Machynlle CAT Catalog (File Name Extension) CAT Common Admission Test (India) CAT Caterpillar, Inc. CAT Community Action Team CAT Catalunva CAT Catalyst CAT Computer Aided Translation CAT Catastrophe (Claims Office) CAT Catamaran CAT Computer-Assisted Translation CAT Certified Accounting Technician CAT Catastrophic CAT Call Any Time CAT Catalan Language (ISO 639-2 Code) CAT Cataract (ophthalmology) CAT Catalytic Converter (automobiles) CAT Catapult CAT Catalonia (country identifier) CAT Centre d'Aide par le Travail (French: Center : CAT Catechism CAT Computerized Adaptive Testing CAT Computer Adaptive Test CAT Civil Air Transport (CIA front airline during 19 CAT California Achievement Test CAT Concatenate CAT Capital Area Transit (Raleigh, NC) CAT CAT Chloramphenicol Acetyltransferase

domesticated, and carnivorous mammal. It is often called the housecat when kept ...

Methcathinone - Wikipedia, the free encyclopedia en.wikipedia.org/wiki/Methcathinone -

History - Approval - Exam format - See also

Cat - Wikipedia, the free encyclopedia

en.wikipedia.org/wiki/Cat -

Methcathinone (α-methylamino-propiophenone or ephedrone) (sometimes called "cat" or "jeff") is a monoamine alkaloid and psychoactive stimulant similar to ...

The domestic cat (Felis catus or Felis silvestris catus) is a small, usually furry

What is CAT Qualification - OpenTuition

opentuition.com/fia/what-is-cat-qualification/

CAT stands for Certified Accounting Technician and the qualification provides a strong foundation of knowledge in finance and accounting. It is provided by the ...

Lemmatization

- Reduce inflections or variant forms to base form
 - am, are, is \rightarrow be
 - car, cars, car's, cars' \rightarrow car
- the boy's cars are different colors →
 - the boy car be different color
- Lemmatization: have to find correct dictionary headword form
 - Determining that two words have the same root, despite their surface differences

Light-Weight Morphology

- Sometimes you just need to know the stem of a word and you don't care about the structure.
 - E.g. camera, cameras
- In fact you may not even care if you get the right stem, as long as you get a consistent string—Stemming
- Stemming for Information Retrieval
 - Run a stemmer on the documents to be indexed
 - Run a stemmer on users' queries
 - Match to the index

Porter's stemming

- No lexicon needed
- Basically a set of staged sets of rewrite rules that strip suffixes
 - ING → ε (e.g., monitoring → monitor)
 - SSES→ SS (e.g., grasses → grass)
- More Example (recursive)
 - Computerization
 - ization -> -ize computerize
 - ize -> ε computer

Porter's stemming

- Handles both inflectional and derivational suffixes
- Doesn't guarantee that the resulting stem is really a stem
 - Lack of guarantee doesn't matter for IR
- Code:
 - http://tartarus.org/martin/PorterStemmer/
 - Implementations in C, Java, Perl, Python, C#, Lisp, Ruby, VB, javascript, php,
 Prolog, Haskell, matlab, tcl, D, and erlang

Stemming used in search

- Recall: reduce false negative? (Not matching things that we should have matched)
 - Query: "dog"
 - Doc 1: I love my dog
 - Doc 2: I do not like dogs

Works in this case

- Precision: increase false positives? (Matching strings that we should not have matched)
 - Query: "policy"
 - Doc 3: Singapore policy on gum
 - Doc 4: Singapore police cool

policy—policies
police—policing

Wrong results here

Stemming

- Reduce terms to their stems in information retrieval
- Stemming is crude chopping of affixes
 - language dependent
 - e.g., automate(s), automatic, automation all reduced to automat.

for example compressed and compression are both accepted as equivalent to compress.



for exampl compress and compress ar both accept as equival to compress

Stemmer vs Dictionary

- Stemming Rules more efficient than a dictionary
 - Algorithmic stemmers can be fast (and lean): 1 Million words in 6 seconds on 500 MHz PC
- No maintenance even if things change
- Better to ignore irregular forms (exceptions) than to complicate the algorithm
 - not much lost in practice
 - 80/20 Rule

Other stemmers

- Other stemmers exist, e.g., Lovins stemmer
 - http://www.comp.lancs.ac.uk/computing/research/stemming/general/lovins.htm
 - Single-pass, longest suffix removal (about 250 rules)
- Full morphological analysis at most modest benefits for retrieval
- Do stemming and other normalizations help?
 - English: very mixed results. Helps recall for some queries but harms precision on others
 - E.g., operative (dentistry) ⇒ oper
 - Definitely useful for Spanish, German, Finnish, ...
 - 30% performance gains for Finnish!

Language-specificity

- Many of the above features embody transformations that are
 - Language-specific and
 - Often, application-specific
- These are "plug-in" addenda to the indexing process
- Both open source and commercial plug-ins are available for handling these

Normalization: other languages

- Accents: e.g., French résumé vs. resume.
- Umlauts: e.g., German: Tuebingen vs. Tübingen
 - Should be equivalent
- Most important criterion:
 - How are your users like to write their queries for these words?
- Even in languages that standardly have accents, users often may not type them
 - Often best to normalize to a de-accented term
 - Tuebingen, Tübingen, Tubingen → Tubingen

Normalization: other languages

- Normalization of things like date forms
 - 7月30日 vs. 7/30
 - Japanese use of kana vs. Chinese characters
- Tokenization and normalization may depend on the language and so is intertwined with language detection
- Crucial: Need to "normalize" indexed text and query terms into the same form



Thesauri and soundex

- Do we handle synonyms and homonyms?
 - E.g., by hand-constructed equivalence classes
 - car = automobile color = colour
 - We can rewrite to form equivalence-class terms
 - When the document contains *automobile*, index it under *car-automobile* (and vice-versa)
 - Or we can expand a query
 - When the query contains automobile, look under car as well
- What about spelling mistakes?
 - One approach is soundex, which forms equivalence classes of words based on phonetic heuristics

Basic concepts: Phrase Detection

- Important for English
 - New York City Police Department
 - Bill Gates spoke on the benefits of Windows
- Essential for CJK (Chinese, Japanese, Korean)
 - <u>新加坡</u>是个<u>美丽的城市 [Singapore is a beautiful city]</u>
- Approaches
 - Dictionary Based
 - Most Accurate; Needs maintenance (by humans)
 - Learnt/Extracted from Corpus
 - Hidden Markov Model; N-Grams; Statistical Analysis
 - Suffix Tree Phrase Detection (via statistical counting)

Example of Extracted Phrases on 20 Newsgroup dataset

south south africa south africa internet south africa po south african south african government south african intelligence south african libertarian south america south atlantic south dakota south dakota writes south georgia south georgia island south pacific south pacific island

san diego
san diego ca
san francisco
san francisco bay
san francisco chronicle
san francisco giants
san francisco police
san francisco police inspector
san francisco police inspector ron
san francisco police intelligence
san francisco police intelligence unit
san francisco police officer
san jose
san jose ca
san jose mercury

high density high end high enough high frequency high hockey high just high level high performance high power high quality high ranking high ranking crime high ranking initiate high resolution high school high school students high speed high speed collision high sticking high tech high voltage highend higher

high

united
united kingdom
united nations
united nations quite
united states
united states attempt
united states code
united states government
united states holocaust
united states officially
united states senate

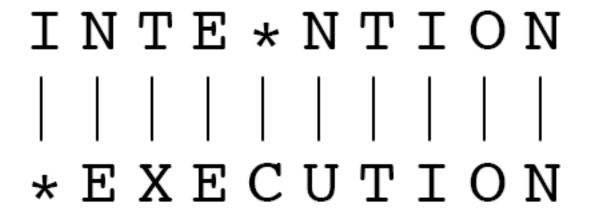
Edit Distance

- The minimum edit distance between two strings is the minimum number of editing operations needed to transform one into the other
 - Insertion
 - Deletion
 - Substitution

- Spell correction
 - The user typed "graffe"
 - Which is closest?
 - graf
 - graft
 - grail
 - giraffe

Minimum Edit Distance

Two strings and their alignment:



Minimum Edit Distance

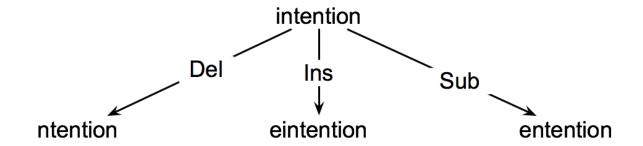
- If each operation has cost of 1
 - Distance between these is 5
- If substitutions cost 2 (Levenshtein)
 - Distance between them is 8

Other uses of Edit Distance in NLP

- Evaluating Machine Translation and speech recognition
 - Spokesman confirms senior government adviser was shot
 - Spokesman said the senior adviser was shot deadS I D I
- Named Entity Extraction and Entity Coreference
 - IBM Inc. announced today
 - IBM profits
 - Stanford President John Hennessy announced yesterday
 - for Stanford University President John Hennessy

How to find the Min Edit Distance?

- Searching for a path (sequence of edits) from the start string to the final string:
 - Initial state: the word we're transforming
 - Operators: insert, delete, substitute
 - Goal state: the word we're trying to get to
 - Path cost: what we want to minimize: the number of edits



Minimum Edit as Search

- But the space of all edit sequences is huge!
 - We can't afford to navigate naïvely
 - Lots of distinct paths wind up at the same state.
 - We don't have to keep track of all of them
 - Just the shortest path to each of those re-visted states.

Defining Min Edit Distance

- For two strings
 - -X of length n
 - -Y of length m
- We define D(i,j) to be the edit distance between X[1..i] and Y[1..j], i.e., the first i characters of X and the first j characters of Y
 - The edit distance between X and Y is thus D(n, m)

Dynamic Programming for Minimum Edit Distance

- Dynamic programming: A tabular computation of D(n,m)
 - Solving problems by combining solutions to subproblems.
- Bottom-up
 - We compute D(i,j) for small i,j, then compute larger D(i,j) based on previously computed smaller values
 - That is: we compute D(i,j) for all i (0 < i < n) and j (0 < j < m)

Defining Min Edit Distance (Levenshtein)

Initialization

$$-D(i,0) = i$$
$$-D(0,j) = j$$

Recurrence Relation:

For each
$$i = 1 \dots M$$

For each $j = 1 \dots N$

$$D[i,j] = \min \left\{ \begin{array}{l} D[i-1,j] + \text{del-cost}(source[i]) \\ D[i,j-1] + \text{ins-cost}(target[j]) \\ D[i-1,j-1] + \text{sub-cost}(source[i], target[j]) \end{array} \right.$$

- Termination:
 - D(N,M) is distance

$$D[i,j] = \min \begin{cases} D[i-1,j]+1 \\ D[i,j-1]+1 \\ D[i-1,j-1]+ \begin{cases} 2; & \text{if } source[i] \neq target[j] \\ 0; & \text{if } source[i] = target[j] \end{cases}$$

The Edit Distance Table

N	9									
0	8									
Ι	7									
Т	6									
N	5									
Е	4									
Т	3									
N	2									
Ι	1									
#	0	1	2	3	4	5	6	7	8	9
	#	Е	Χ	Е	С	U	Т	I	0	N

The Edit Distance Table

N	9										
0	8										
I	7				$\bigcap D[i]$	[-1, j]	+1				l
Т	6		$D[i \ i]$] — mir	$\int D[i]$,j-1	+1				
N	5		$igspace{igspace} oldsymbol{\mathcal{D}}[\iota, J]$	_ mm	D[i]	-1, j	$-1]+\langle$	$\begin{cases} 2; & \text{if } \\ 0 & \text{if } \end{cases}$	source	$e[i] \neq te$	arget[j]
Е	4					[-1, j] + 1 [-1, j - 1] + 1 [-1, j - 1] + 1		(U; 1I	source[i] = to		arget[J]
Т	3										
N	2										
I	1										
#	0	1	2	3	4	5	6	7	8	9	
	#	Е	Χ	Е	С	U	Т	Ι	0	N	

The Edit Distance Table

N	9	8	9	10	11	12	11	10	9	8
0	8	7	8	9	10	11	10	9	8	9
I	7	6	7	8	9	10	9	8	9	10
Т	6	5	6	7	8	9	8	9	10	11
N	5	4	5	6	7	8	9	10	11	10
Е	4	3	4	5	6	7	8	9	10	9
Т	3	4	5	6	7	8	7	8	9	8
N	2	3	4	5	6	7	8	7	8	7
I	1	2	3	4	5	6	7	6	7	8
#	0	1	2	3	4	5	6	7	8	9
	#	Е	X	E	С	U	Т	I	0	N

Computing alignments

- Edit distance isn't sufficient
 - We often need to align each character of the two strings to each other
- We do this by keeping a "backtrace"
- Every time we enter a cell, remember where we came from
- When we reach the end,
 - Trace back the path from the upper right corner to read off the alignment

MinEdit with Backtrace

n	9	↓ 8	<u>√</u>	<u> </u>	∠←↓ 11	∠←↓ 12	↓ 11	↓ 10	↓9	∠8	
0	8	↓ 7	∠ ←↓8	∠←↓ 9	<u> </u>	<u> </u>	↓ 10	↓9	/ 8	← 9	
i	7	↓ 6	∠ ←↓ 7	∠ ←↓8	∠ ←↓9	∠ ←↓ 10	↓9	/ 8	← 9	← 10	
t	6	↓ 5	∠ ←↓6	∠←↓ 7	∠ ←↓8	∠ ←↓9	∠ 8	← 9	← 10	← ↓ 11	
n	5	↓ 4	∠ ←↓ 5	∠←↓ 6	∠←↓ 7	∠ ←↓ 8	<u>/</u> ←↓9	∠ ←↓ 10	∠ ←↓ 11	∠ ↓ 10	
e	4	∠ 3	← 4	√ ← 5	← 6	← 7	<i>←</i> ↓ 8	∠ ←↓9	∠ ←↓ 10	↓9	
t	3	∠ ←↓4	∠ ←↓ 5	∠←↓ 6	∠←↓ 7	∠←↓ 8	∠ 7	<i>←</i> ↓ 8	∠ ←↓9	↓8	
n	2	∠ ←↓ 3	∠ ←↓4	∠ ←↓ 5	∠←↓ 6	∠←↓ 7	<u> </u>	↓ 7	∠←↓ 8	∠7	
i	1	∠ ←↓ 2	∠ ←↓ 3	∠ ←↓ 4	∠←↓ 5	∠←↓ 6	∠←↓ 7	∠ 6	← 7	← 8	
#	0	1	2	3	4	5	6	7	8	9	
	#	e	X	e	c	u	t	i	0	n	

Result of Backtrace

Two strings and their alignment:

Topics covered

- Token and Tokenization
- Stop words
- English Morphology
- Stemming and Lemmatization
- Edit Distance