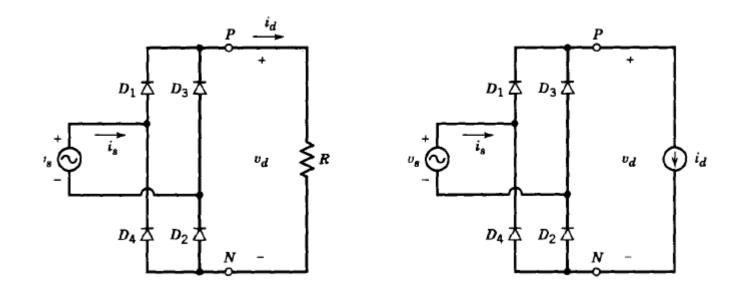
### Chapter 4 Power Converters

#### Learning Objectives

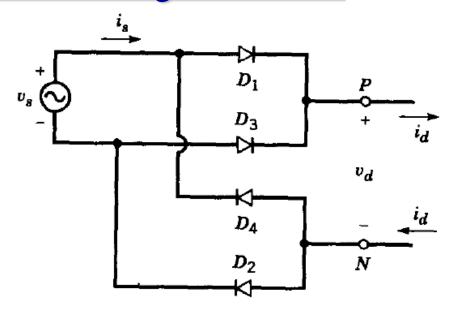
- Understand waveforms of various circuits
- Distinguish single- and three-phase converters
- Realize effects of firing angle
- Understand operating principles of different DC/DC converters





- An idealized bridge circuit with no line inductance are analysed
- A pure resistive load is very unlikely to be realized in practical case
- A constant dc current is a very good approximation in a situation when a large inductor may be connected in the circuit





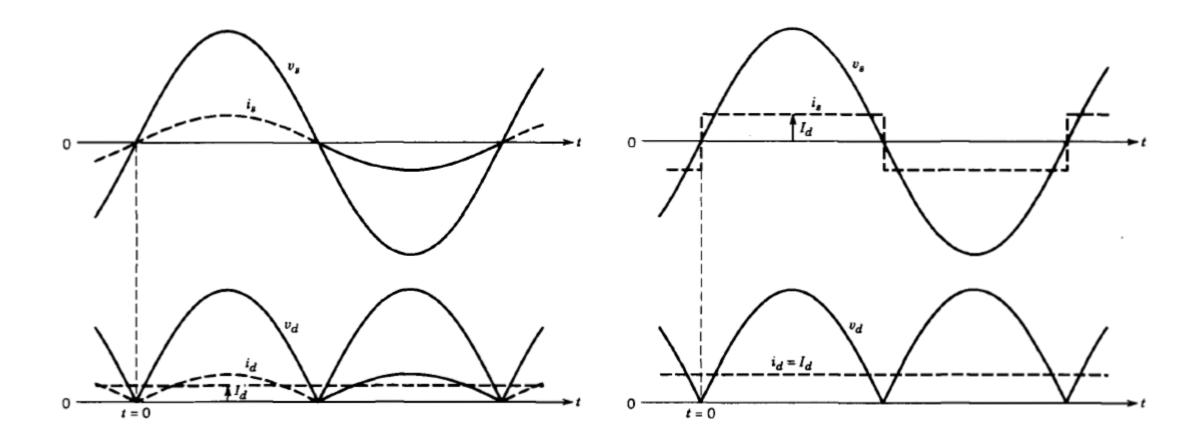
At anytime, the dc-side output voltage is

$$v_d(t) = |v_s|$$

Similarly, the ac-side current is

$$i_S = \begin{cases} i_d & v_S > 0 \\ -i_d & v_S < 0 \end{cases}$$







The average output voltage is

$$V_{d0} = \frac{1}{T/2} \int_0^{T/2} \sqrt{2} \, V_S \sin(\omega t) \, dt = \frac{\sqrt{2} V_S}{\omega \, T/2} (\cos \omega t) \Big|_{T/2}^0 = \frac{2}{\pi} \sqrt{2} V_S$$

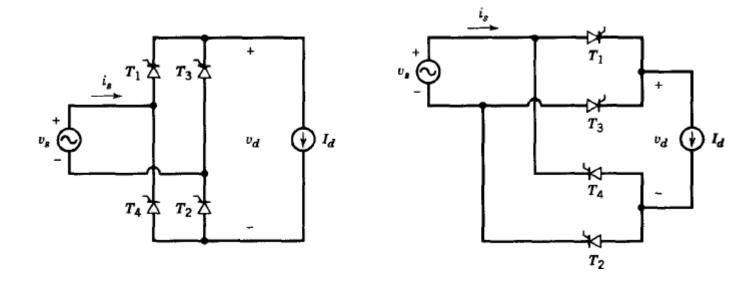
Hence

$$V_{d0} = \frac{2}{\pi} \sqrt{2} V_s = 0.9 V_s$$

where  $V_s$  is the rms value of the input voltage



### 4.2 Single-Phase Converter



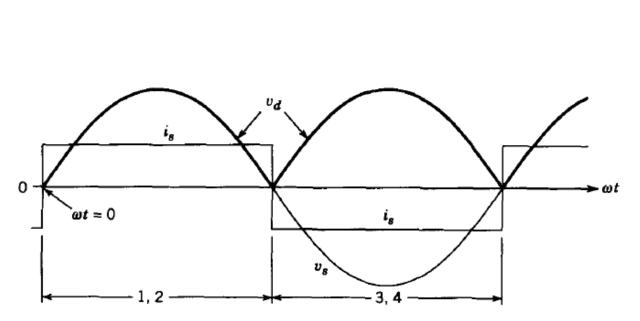
Output voltage can be found by finding the difference between the time integral when  $\alpha = 0$  and the shaded area  $A_{\alpha}$ 

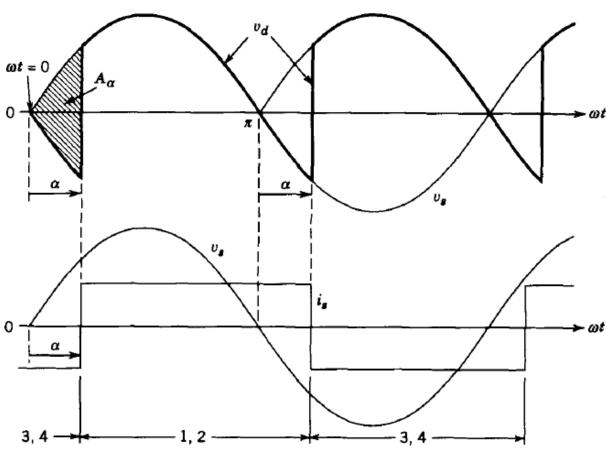
$$V_{d\alpha} = \frac{1}{\pi} \int_{\alpha}^{\alpha + \pi} \sqrt{2} V_s \sin(\omega t) d(\omega t) = \frac{2\sqrt{2}}{\pi} V_s \cos\alpha = 0.9 V_s \cos\alpha$$

Power delivered to a constant current load can also be worked out in terms of  $\alpha$ 



### 4.2 Single-Phase Converter







A separately excited DC motor, 10 hp, 220 V, 1200 rpm, is connected with an ideal single-phase full converter. Its rated armature current is 40 A with armature resistance of 0.25  $\Omega$  and armature inductance of 10 mH. The AC supply voltage is 265 V while the motor constant is 0.18 V/rpm. Assume motor current is continuous and ripple-free. If a firing angle is 30°, find

(a) Speed of the motor (Ans: 1092.2 rpm)

(b) Motor torque (Ans: 68.8 Nm)

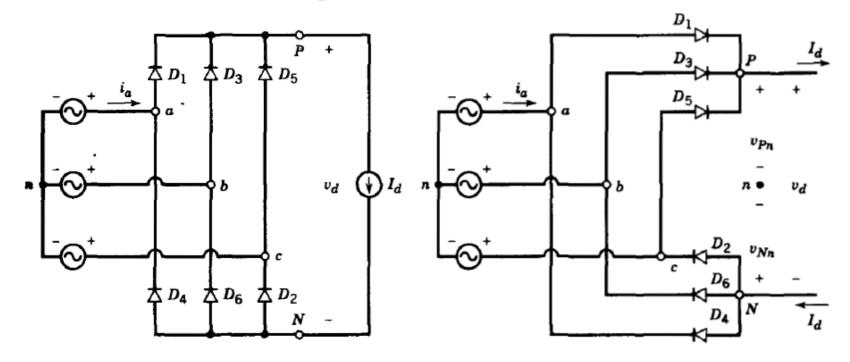
(c) Power to the motor (Ans: 8264 W)







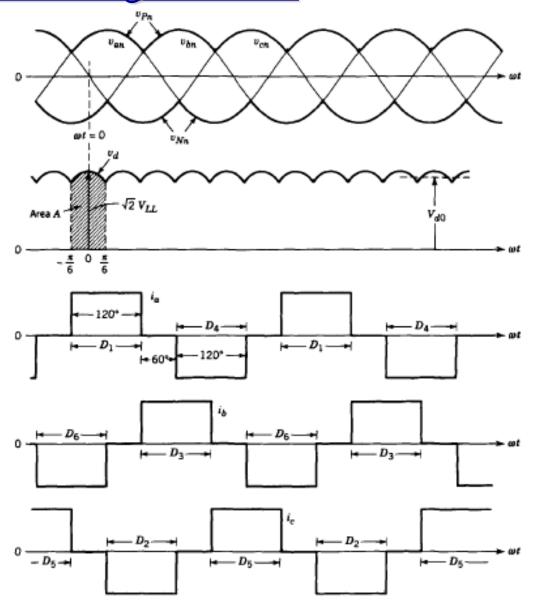
### 4.3 Three-Phase, Full-Bridge Rectifier



- Consider the case with no line inductance
- A 3-phase rectifier circuit somehow is similar to the case of 1-phase circuit
- A pair of diodes conduct at one time with voltage waveform across the load with respect to point n



### 4.3 Three-Phase, Full-Bridge Rectifier





### 4.3 Three-Phase, Full-Bridge Rectifier

If the same voltage waveform is modified with point N, the dc-side voltage becomes

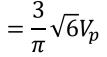
$$v_d = v_{Pn} - v_{Nn}$$

- The instantaneous voltage waveform consists of six segment per cycle of line frequency so that it is often known as six-pulse rectifier
- Consider one of the six segment

$$v_d = v_{ab} = \sqrt{2}V_{LL}\cos(\omega t)$$
 for  $-\frac{1}{6}\pi < \omega t < \frac{1}{6}\pi$ 

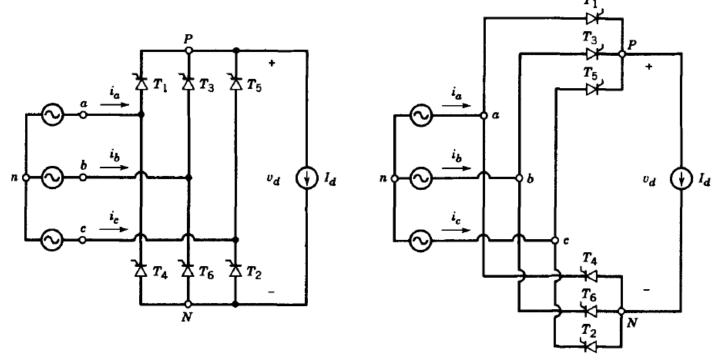
• By integrating  $v_{ab}$  and dividing it by  $\pi/3$ , it yields

$$V_{d0} = \frac{1}{\pi/3} \int_{-\pi/6}^{\pi/6} \sqrt{2} V_{LL} cos(\omega t) d(\omega t) = \frac{3}{\pi} \sqrt{2} V_{LL}$$





#### 4.4 Three-Phase Converter

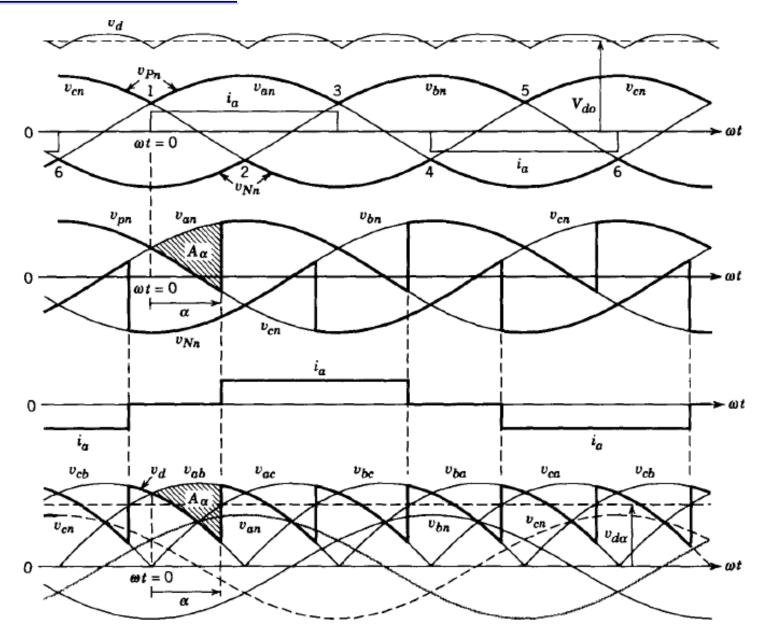


- Firing angle  $\alpha$  results in reduction of output voltage
- Based on previous derivation

$$V_{do} = \frac{3\sqrt{2}}{\pi} V_{LL} = 1.35 V_{LL}$$



#### 4.4 Three-Phase Converter





#### 4.4 Three-Phase Converter

Consider reduction in the average ac voltage with a delay angle

$$V_{d\alpha} = V_{do} - \frac{A_{\alpha}}{\pi/3}$$

With reference to the waveform

$$A_{\alpha} = \int_{0}^{\alpha} \sqrt{2} V_{LL} \sin(\omega t) d(\omega t)$$

$$V_{d\alpha} = \frac{3\sqrt{2}}{\pi} V_{LL} cos\alpha = 1.35 V_{LL} cos\alpha$$

A separately excited DC motor, 125 hp, 600 V, 1800 rpm, is connected with a three-phase full converter. The converter is operated from a three-phase, 480 V, 60 Hz supply. The rated armature current of the motor is 165 A with armature resistance of 0.0874  $\Omega$ , armature inductance of 6.5 mH and motor constant is 0.33 V/rpm. Assume the converter and AC supply are ideal. If a firing angle is 30°, find

- (a) Assume at no-load condition, the armature current is 10 % of the rated current. Find no-load speeds at firing angles of 0° and 30° (Ans: 1959 rpm; 1696 rpm)
- (b) Find the firing angle for rated speed of 1800 rpm at rated motor current (Ans: 20.1°)
- (c) Find the speed regulation for the firing angle obtained in (b) (Ans: 2.18 %)

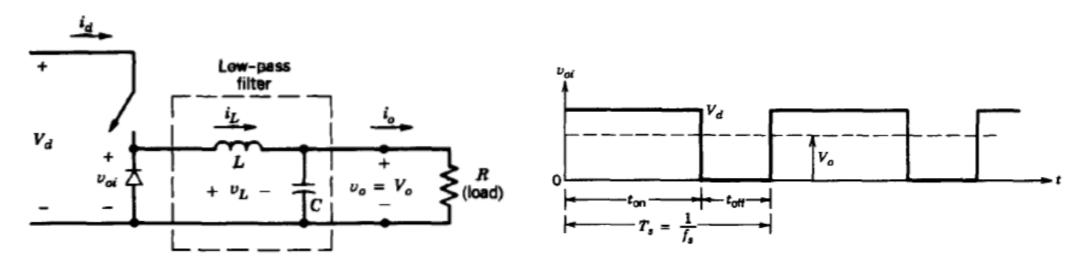








### 4.5 Step-Down (Buck) Converter



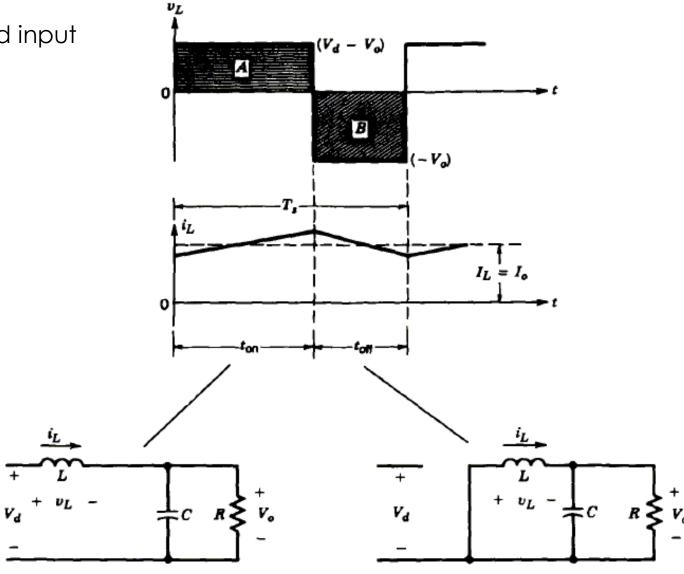
- Pulse Width Modulation (PWM) is used to control duty ratio
- Average output voltage is obtained by taking average waveform across the diode
- There are two operating modes, namely continuous conduction mode (CCM) and discontinuous conduction mode (DCM)
- In CCM, current in the inductor does not go to zero at any time



### 4.5 Step-Down (Buck) Converter

Relation between output and input

$$\frac{V_o}{V_d} = D$$





A separately excited DC motor is controlled by a chopper with DC supply of 120 V. The motor consists of armature resistance of 0.5  $\Omega$ , armature inductance of 20 mH and motor constant is 0.05 V/rpm. The motor drives a constant-torque load that needs an average armature current of 20 A. Assume the motor current is continuous.

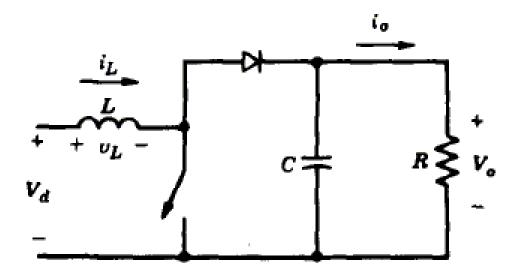
- (a) Find the range of speed control (Ans: 0 < N < 2200 rpm)
- (b) Find the duty cycle (Ans: 1/12 < D < 1)







### 4.6 Step-Up (Boost) Converter



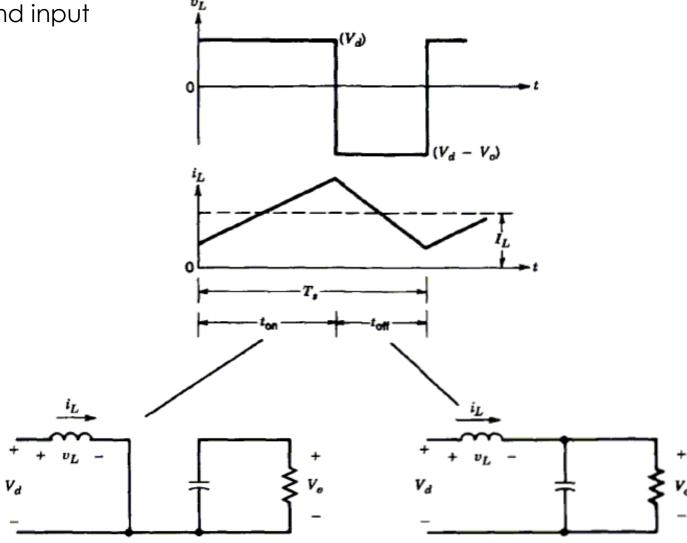
- Same as buck converter, PWM is used to control duty ratio
- Boost converter is able to produce an output voltage higher than its input
- Similar as buck converter, boost converter can also provide CCM and DCM



### 4.6 Step-Up (Boost) Converter

Relation between output and input

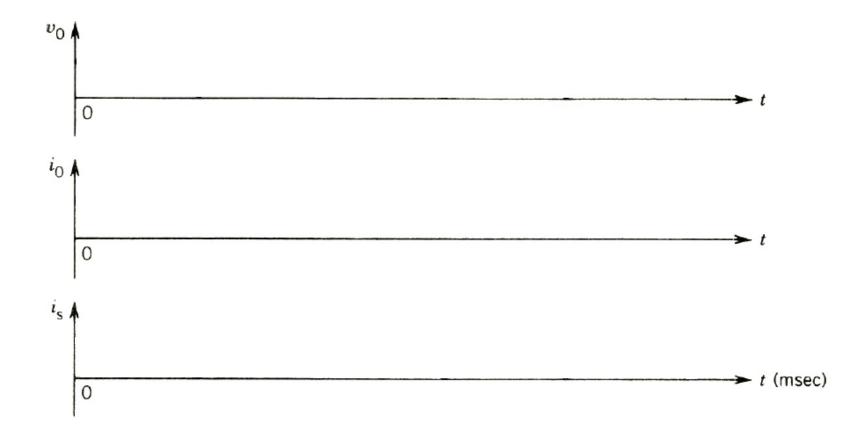
$$\frac{V_o}{V_d} = \frac{1}{1 - D}$$



A step-up converter is used to control a motor during regenerative braking mode. The motor consists of voltage constant of 0.3 V/rpm and DC bus voltage of 600 V. When the motor is at 800 rpm, it draws average motor current of 300 A.

- (a) Draw the waveforms of output voltage, output current and supply current.
- (b) Find the duty ratio of the converter.
- (c) Find the power fed back to the supply.



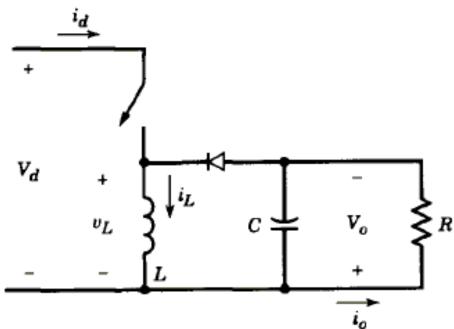








#### 4.7 Buck-Boost Converter



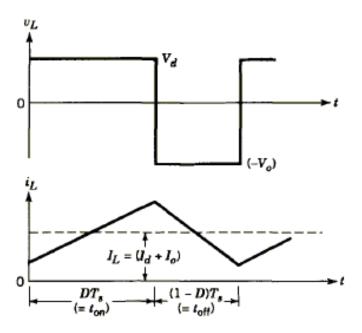
- A buck-boost converter is able to produce an output voltage higher or lower than its input with the polarity reversed
- When switch is closed, input provides energy to inductor and diode is reversed biased
- When the switch is open, the stored energy is transferred to the output
- No energy is supplied by the input during this interval

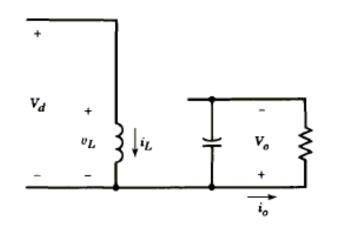


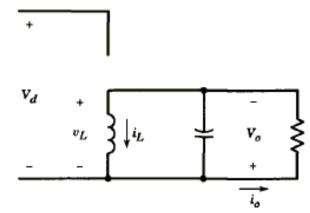
### 4.7 Buck-Boost Converter

Relation between output and input

$$\frac{V_o}{V_d} = \frac{D}{1 - D}$$

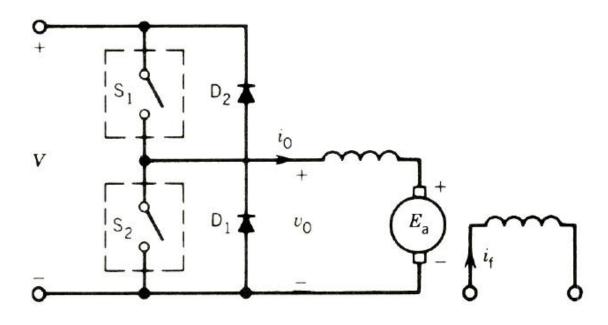








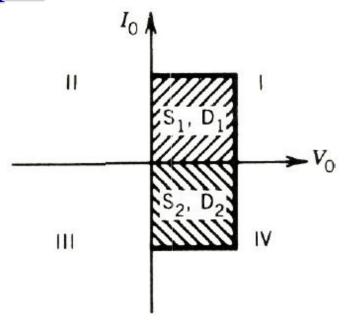
### 4.8 Two-Quadrant Chopper



- Two-quadrant chopper is formed by combination of buck and boost converters
- If  $S_1$  and  $D_1$  are operated, the system will operate as a buck converter and the DC machine as a motor
- If  $S_2$  and  $D_2$  are operated, the system will operate as a boost converter and the DC machine as a generator



#### 4.8 Two-Quadrant Chopper



- When the chopper is as a buck converter, its output voltage is either V or zero
- Its average voltage output is positive with output current flows in positive direction
- When the chopper is as a boost converter, its output voltage is either zero or V
- Its average voltage output is positive with output current flows in negative direction

