

Homework 9

1. Thevenin Circuit

$$R_{\text{new}} = \frac{3 \cdot (4.5 + 1.5)}{3 + 4.5 + 1.5}$$

$$= \frac{18}{9} = 2$$

$$V_A = \frac{2}{2+3} \cdot V_S = \boxed{4V}$$

$$V_B = \frac{1.5}{4.5+1.5} \cdot V_A = \frac{1.5}{6} \cdot 4 = \boxed{1V}$$

$$\therefore V_A - V_B = 4 - 1$$

$$= \underline{3V}$$

Norton Circuit

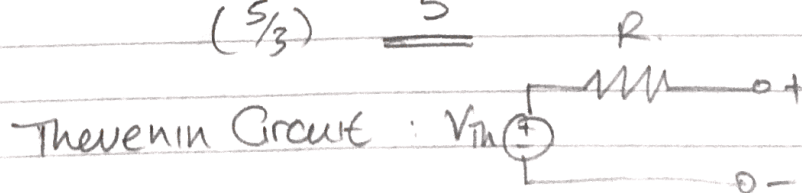
$$R_{\text{new}} = \frac{(1.5)(3)}{1.5+3} = \underline{1 \Omega}$$

$$V_C = \frac{1}{3+1} \cdot V_S = 2.5$$

$$\therefore I_{R4} = \frac{2.5}{1.5} = \underline{\underline{\frac{5}{3} A}}$$

$$\therefore R_{\text{Th}} = \frac{3}{(\frac{5}{3})} = \underline{\underline{\frac{9}{5} \Omega}}$$

Thevenin Circuit :

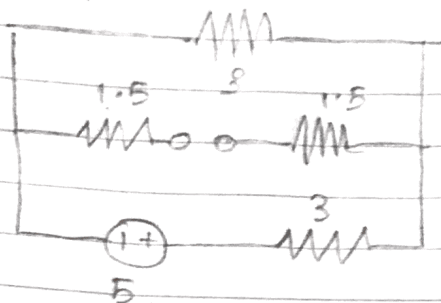


Norton Circuit :



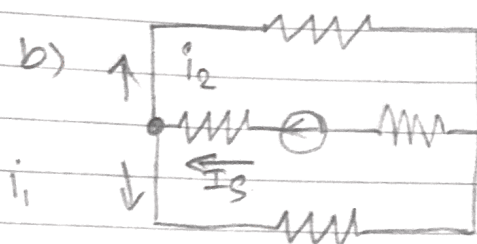
2.

a) Turn of current source:



$$V = IR$$

$$I = \frac{5}{3+3} = \frac{5}{6} \text{ A.}$$



KCL

$$I_s = i_1 + i_2$$

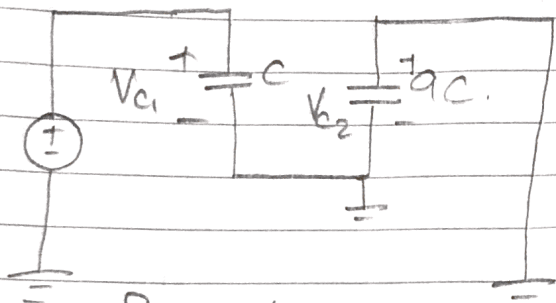
$$2i_2 = +1$$

$$i_2 = \frac{1}{2} \text{ A}$$

By superposition, $\frac{-5}{6} + \frac{1}{2} = \underline{\underline{\frac{-1}{3} \text{ A}}}$

3.

a)



Phase 1

$$V_{c1,1} = V_{\text{source}} - 0 = V_{\text{source}}$$

$$V_{c2,1} = 0 - 0 = 0$$

$$Q_{C1,1} = V_{c1,1} C_1 = C V_{\text{source}}$$

$$Q_{C2,1} = V_{c2,1} C_2 = 0$$

4. $Q = VC$

$$I = \frac{dQ}{dt} = C \frac{dV}{dt}$$

$$I = \frac{V_{init} - V_{min}}{t_{store}} C_{bit}$$

$$= \frac{(1.2 - 0.9) \cdot 28f}{1 \times 10^{-3}}$$

$$= \underline{8.4 \mu A}$$

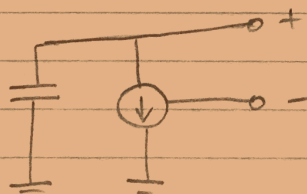
5. $I_S = C_2 \frac{dV_{out}(t)}{dt}$

$$V_{out} = \int \frac{I_S}{C_2} dt$$

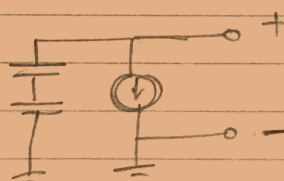
$$= \frac{I_S t}{C_2} + V_{out}(0)$$

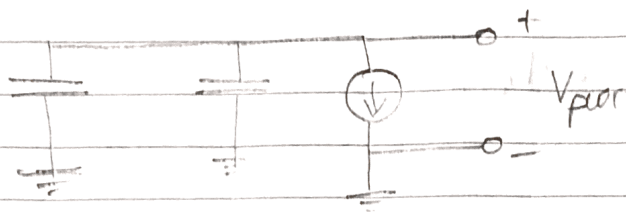
$$= \frac{I_S t}{C_2}$$

6.
a) Config 1



b) Config 2





b) Case 1 :

$$\begin{aligned}
 V_{pwr} &= \frac{Q}{C_{sc}} \\
 &= \frac{Q_{init} - i_{load}t}{C_{sc}} \\
 &= \frac{V_{init}C_{sc} - i_{load}t}{C_{sc}} \\
 &= V_{init} - \frac{i_{load}t}{C_{sc}}
 \end{aligned}$$

Case 2 :

$$\begin{aligned}
 V_{pwr} &= \frac{Q}{C_{eq}} \\
 &= \frac{Q_{init} - i_{load}t}{C_{eq}} \\
 &= \frac{V_{init}C_{sc} - i_{load}t}{C_{eq}} \\
 &= 2V_{init} - \frac{2i_{load}t}{C_{sc}}
 \end{aligned}$$

Case 3 :

$$\begin{aligned}
 V_{pwr} &= \frac{Q}{C_{eq}} \\
 &= \frac{Q_{init} - i_{load}t}{C_{eq}} \\
 &= \frac{2V_{init}C_{sc} - i_{load}t}{C_{eq}} \\
 &= V_{init} - \frac{i_{load}t}{2C_{sc}}
 \end{aligned}$$

7.

$$a) C_{full} = \frac{\epsilon_{H_2O} h \cdot \omega}{\omega} = 81 \cdot \epsilon \cdot h_{H_2O}$$

$$C_{empty} = \frac{\epsilon_{air} h \cdot \omega}{\omega} = \epsilon h_{tot}$$

$$b) C_{water} = \frac{\epsilon_{H_2O} h_{H_2O} \omega}{\omega} = 81 \epsilon h_{H_2O}$$

$$C_{air} = \frac{\epsilon_{air} (h_{tot} - h_{H_2O}) \omega}{\omega} = \epsilon (h_{tot} - h_{H_2O})$$

$$C_{tank} = C_{water} + C_{air} = \epsilon (h_{tot} + 80 h_{H_2O})$$

$$c) I_c = C_{tank} \frac{dV_c}{d\epsilon}$$

$$I_c = I_s$$

$$\frac{dV_c}{d\epsilon} = \frac{I_s}{C_{tank}}$$

$$V_c = \frac{I_s}{C_{tank}} t$$

$$d) C_{tank} = \frac{I_s \cdot t}{V_c(t)}$$

$$h_{H_2O} = \frac{C_{tank} - h_{tot} \cdot \epsilon}{80 \epsilon}$$

$$e) V_c = \frac{I_s}{C_{tank}} \cdot t$$

$$C_{tank} = \frac{I_s \cdot T_i}{V_{ref}}$$

$$h_{H_2O} = \frac{C_{tank} - h_{tot} \cdot \epsilon}{80 \epsilon}$$

10. I worked alone for this resubmission using the
Solutions that were released over the weekend