## The Manopt Toolbox, Optimization on manifolds in 3 minutes

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www.manopt.org

## A Matlab toolbox to solve optimization problems

## $\min_{X \in \mathcal{M}} f(X)$

 ${\cal M}$  is a Riemannian manifold f is sufficiently smooth on  ${\cal M}$ 

based on a generalization of unconstrained nonlinear optimization

Most well-known algorithms work just as well on important manifolds:

Steepest descent, conjugate gradients, BFGS, Newton, trust-regions, and many more.

And they come with essentially all the standard convergence guarantees.

## under a wide class of constraints

Many natural constraints in applications exhibit a Riemannian geometry.

Optimization of rotations, orthonormal matrices or fixed-rank matrices (symmetric or not, positive or not) and even optimization of linear subspaces are but a few examples.

The framework is well suited for large-scale computational engineering.

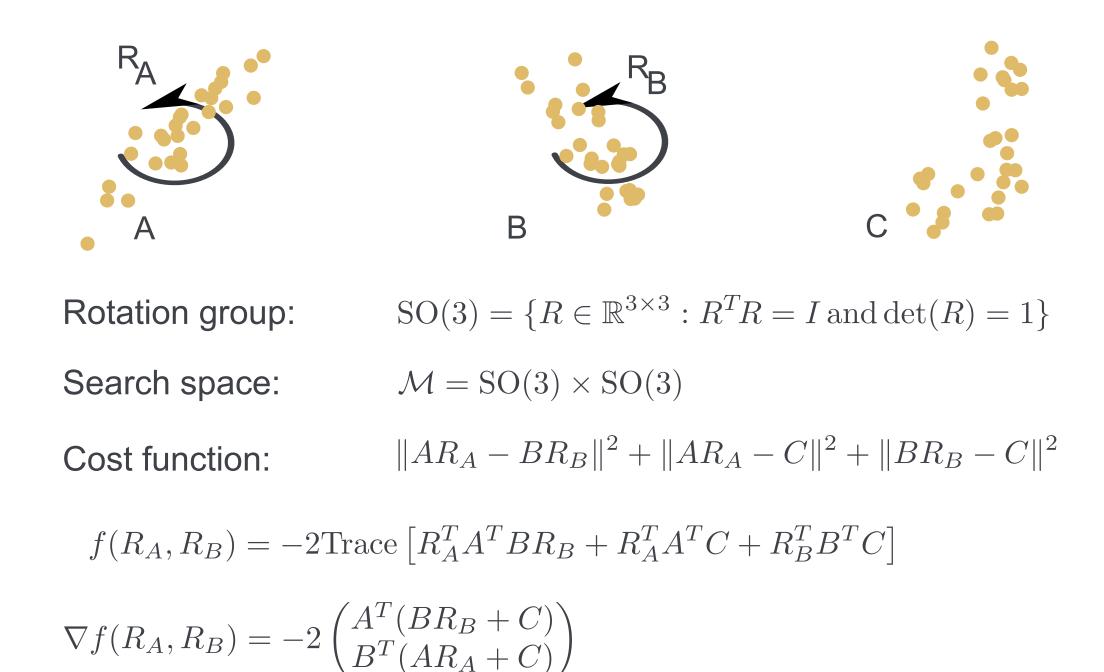
with mature theory and a friendly design

The toolbox keeps it simple:

Automatic conversion of Euclidean derivatives to their Riemannian counterpart, automatic Hessian approximation when needed, default values for all parameters, derivative checks, ...

Manopt is open source and documented.

Example: rotate clouds of points for best alignment



import manopt.solvers.trustregions.\*; import manopt.manifolds.rotations.\*; % Create the problem structure. manifold = rotationsfactory(n, 2); problem.M = manifold; % Define the problem cost function and its gradient. problem.cost = @cost; function f = cost(R)RA = R(:, :, 1); RB = R(:, :, 2); $\|\operatorname{grad} f\|$  $f = norm(A*RA-B*RB, 'fro')^2 + norm(A*RA-C, 'fro')^2 ...$ + norm(B\*RB-C, 'fro')^2; end problem.grad = @(R) manifold.egrad2rgrad(R, grad(R)); function G = grad(R)RA = R(:, :, 1); RB = R(:, :, 2);G = zeros(n, n, 2);G(:, :, 1) = -2\*A'\*(B\*RB+C);G(:, :, 2) = -2\*B'\*(A\*RA+C);% Solve. [R Rcost info] = trustregions(problem); 8 iterations % Display some statistics. semilogy([info.iter], [info.gradnorm], '.-');