

# 基于融合的滤波方法II



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# 第八章作业思路分享

相对于第七章的作业，第八章的作业相对比较简单。加入运动约束后，车体的yz轴的速度观测值为零，x轴的观测值未知（也可理解为没有x轴的观测值），因此需要去除 $G_t, C_t$ 矩阵关于速度误差状态的第一行。融合运动约束的方法比较简单，就不详细阐述。

$$G_t = \begin{bmatrix} I_3 & 0 & 0 & 0 & 0 \\ 0 & [R_{bw}]_{yz} & [[v^b]_{\times}]_{yz} & 0 & 0 \\ 0 & 0 & I_3 & 0 & 0 \end{bmatrix}$$

$$C_t = \begin{bmatrix} I_3 & 0 & 0 \\ 0 & I_2 & 0 \\ 0 & 0 & I_3 \end{bmatrix}$$

```
//YPoseVelCons是一个8维列向量
YPoseVelCons.block<3,0>(0,0) = YPoseVel_.block<3,1>(0,0);
YPoseVelCons.block<2,1>(3,0) = YPoseVel_.block<2,1>(4,0);
YPoseVelCons.block<3,1>(5,0) = YPoseVel_.block<3,1>(6,0);

Y = YPoseVelCons;
//GPoseVelCons是一个8*15的矩阵
GPoseVelCons.setZero();
GPoseVelCons.block<3,3>(0,0) = Eigen::Matrix3d::Identity();
GPoseVelCons.block<3,3>(5,6) = Eigen::Matrix3d::Identity();
GPoseVelCons.block<2,15>(3,0) = GPoseVel_.block<2,15>(4,0);

G = GPoseVelCons; |
MatrixRPoseVel R = GPoseVelCons*P_*GPoseVelCons.transpose() + RPoseVel_;
K = P_*GPoseVelCons.transpose()*R.inverse();
```

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接下来就是融合编码器，编码器的融合主要是增加了车身坐标系下的速度观测值。观测方程的 $G_t$ 、 $C_t$ 推导大家可以查看课程PPT，主要实现如下：

```
Eigen::Vector3d P_nn_obs = pose_.block<3, 1>(0,3) - T_nb.block<3, 1>(0,3);
Eigen::Matrix3d C_nn_obs = T_nb.block<3, 3>(0,0).transpose()* pose_.block<3, 3>(0,0);
Eigen::Vector3d v_bb_obs = pose_.block<3, 3>(0,0).transpose()*vel_ - v_b;

YPoseVel_.block<3, 1>(0, 0) = P_nn_obs;
YPoseVel_.block<3, 1>(3, 0) = Sophus::SO3d::vee(C_nn_obs - Eigen::Matrix3d::Identity() );
YPoseVel_.block<3, 1>(6, 0) = v_bb_obs;

Y = YPoseVel_;

// set measurement equation:
GPoseVel_.block<3, 3>(6, kIndexErrorVel) = pose_.block<3, 3>(0,0).transpose();
GPoseVel_.block<3, 3>(6, kIndexErrorOri) = Sophus::SO3d::hat(pose_.block<3, 3>(0,0).transpose()*vel_

G = GPoseVel_;

MatrixRPoseVel R = GPoseVel_*P_*GPoseVel_.transpose() + RPoseVel_;
K = P_*GPoseVel_.transpose()*R.inverse();
```

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框架中里程计的更新函数实现如下：

```
// get deltas:  
Eigen::Vector3d angular_delta;  
GetAngularDelta(1, 0, angular_delta, angular_vel_mid);
```

```
// get velocity delta:  
Eigen::Matrix3d R_curr, R_prev;  
UpdateOrientation(angular_delta, R_curr, R_prev);
```

```
double T;  
Eigen::Vector3d velocity_delta;  
GetVelocityDelta(  
    1, 0,  
    R_curr, R_prev,  
    T, velocity_delta, linear_acc_mid  
);
```

```
// update position:  
UpdatePosition(T, velocity_delta);
```

框架中函数SetProcessEquation实现如下：

```
// a. set process equation for delta vel:  
F_.block<3, 3>(kIndexErrorVel, kIndexErrorOri) = -C_nb*Sophus::SO3d::hat(f_n).matrix();  
  
F_.block<3, 3>(kIndexErrorVel, kIndexErrorAccel) = -C_nb;  
  
F_.block<3, 3>(kIndexErrorOri, kIndexErrorOri) = -Sophus::SO3d::hat(w_b).matrix();  
  
// b. set process equation for delta ori:  
B_.block<3, 3>(kIndexErrorVel, 0) = C_nb;
```

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框架中UpdateErrorEstimation函数实现如下：  
实现如下：

```
UpdateProcessEquation(linear_acc_mid, angular_vel_mid);

F_1st = T*F_;
F_2nd = 0.5*T*F_*F_1st;

MatrixF F = MatrixF::Identity() + F_1st + F_2nd;

MatrixB B;
B.block<9, 6>(0, 0) = T*B_.block<9, 6>(0, 0);

B.block<6, 6>(9, 6) = sqrt(T)*B_.block<6, 6>(9, 6);

X_ = F*X_; // fix this

P_ = F*P_*F.transpose() + B*Q_*B.transpose(); // fix this
```



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框架中CorrectErrorEstimationPose函数实现如下：

```
Eigen::Vector3d P_nn_obs = pose_.block<3, 1>(0,3) - T_nb.block<3, 1>(0,3);
Eigen::Matrix3d C_nn_obs = T_nb.block<3, 3>(0,0).transpose()* pose_.block<3, 3>(0,0);
Eigen::Vector3d v_bb_obs = pose_.block<3, 3>(0,0).transpose()*vel_ - v_b;

YPoseVel_.block<3, 1>(0, 0) = P_nn_obs;
YPoseVel_.block<3, 1>(3, 0) = Sophus::SO3d::vee(C_nn_obs - Eigen::Matrix3d::Identity() );
YPoseVel_.block<3, 1>(6, 0) = v_bb_obs;

Y = YPoseVel_;

// set measurement equation:
GPoseVel_.block<3, 3>(6, kIndexErrorVel) = pose_.block<3, 3>(0,0).transpose();
GPoseVel_.block<3, 3>(6, kIndexErrorOri) = Sophus::SO3d::hat(pose_.block<3, 3>(0,0).transpose()*vel_

G = GPoseVel_;

MatrixRPoseVel R = GPoseVel_*P_*GPoseVel_.transpose() + RPoseVel_;
K = P_*GPoseVel_.transpose()*R.inverse();
```

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框架中CorrectErrorEstimation函数实现如下：

```
case MeasurementType::POSI_VEL:  
    //  
    CorrectErrorEstimationPosiVel(  
        measurement.T_nb, measurement.v_b, measurement.w_b,  
        Y, G, K  
    );  
    break;
```

最后，误差消除函数EliminateError实现如下：

```
// a. position:  
pose_.block<3, 1>(0, 3) = pose_.block<3, 1>(0, 3) - X_.block<3, 1>(kIndexErrorPos, 0);  
// b. velocity:  
vel_ = vel_ - X_.block<3, 1>(kIndexErrorVel, 0);  
// c. orientation:  
Eigen::Matrix3d C_nn = Sophus::SO3d::exp(X_.block<3, 1>(kIndexErrorOri, 0)).matrix();  
pose_.block<3, 3>(0, 0) = C_nn*pose_.block<3, 3>(0, 0);
```

Q&A



感谢各位聆听！  
Thanks for Listening

