Assignment-2

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Problem 1(x):

If events A and B are independent such that $P(A) = \frac{3}{5}$, $P(B) = \frac{2}{3}$, find $P(A \cup B)$.

Solution:

The given input probabilities and desired values are given in the Table 1,

Event	Probability	Value
A	P(A)	$\frac{3}{5}$
В	P(B)	$\frac{2}{3}$
A + B	P(A+B)	?

Table 1:

Using the above two formulas, (1) and (2), we can use the modified probability addition rule for independent sets as,

$$P(A + B) = P(A) + P(B) - P(A) \cdot P(B)$$
(3)

By substituting the respective values in (3), we get,

$$P(A+B) = \frac{3}{5} + \frac{2}{3} - \frac{3}{5} \cdot \frac{2}{3}$$
$$= \frac{3}{5} + \frac{2}{3} - \frac{2}{5}$$
$$= \frac{13}{15}$$

So, the desired probability P(A + B) is found to be,

$$P(A+B) = \frac{13}{15} = 0.8667$$

It is also given that events A and B are independent which means,

$$P(AB) = P(A) \cdot P(B) \tag{1}$$

And from the general probability addition rule for the union of two events, we get,

$$P(A + B) = P(A) + P(B) - P(AB)$$
(2)