Assignment-6 (Papoulis Chapter 4 Example 4.2)

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Question

In a die roll experiment the six outcomes are denoted as f_i and for each outcome, a random variable is assigned as $x(f_i) = 10i$. Using these find the set of favourable outcomes for each of the conditions givn below.

- (i) $\{x \le 35\}$
- (ii) $\{x \le 5\}$
- (iii) $\{20 \le x \le 35\}$
- (iv) $\{x = 40\}$
- (v) $\{x = 35\}$



Given that the random variables of the outcomes of a die roll experiment are given as $x(f_i) = 10i$, where f_i , i = 1, 2, ...6 are the outcomes.

Then for each of the conditions imposed for the random variabes, the favourable outcomes set:



(i) Given condition,

$${x \le 35}$$

This can be written as,

$$x(f_i) \le 35$$
$$10i \le 35$$
$$i \le 3.5$$

Then the outcome set would be,

$$A = \{f_1, f_2, f_3\}$$



(ii) Given condition,

$${x \le 5}$$

This can be written as,

$$x(f_i) \le 5$$
$$10i \le 5$$
$$i \le 0.5$$

But i can only take the values from 1 to 6. So the outcome set would be empty.

$$B = \phi = \{\}$$

(iii) Given condition,

$${20 \le x \le 35}$$

This can be written as,

$$20 \le x(f_i) \le 35$$

 $20 \le 10i \le 35$
 $2 \le i \le 3.5$

So the outcome set would be,

$$C = \{f_2, f_3\}$$



(iv) Given condition,

$${x = 40}$$

This can be written as,

$$x(f_i) = 40$$
$$10i = 40$$
$$i = 4$$

So the outcome set would be,

$$D = \{f_4\}$$



(v) Given condition,

$${x = 5}$$

This can be written as,

$$x(f_i) = 5$$
$$10i = 5$$
$$i = 0.5$$

But i can only take the values from 1 to 6. So the outcome set would be empty.

$$E = \phi = \{\}$$

