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LAB 1 - PRINCIPAL COMPONENT ANALYSIS.

Objective

In this lab we are going to perform the factor reduction for the company of a diaper which has certain criteria(variables/factors) that they consider to define their product quality. For them the measures are (count, price, value, unisex, style, absorben). These variables need to be lower down so that we can arrange 2 or more of them into simpler groups as per the relationship among them.

For that purpose we will use the Principal Component Analysis to reduce 6 variable into less variable(≤ 3)generally. Although it is not predefined to choose exactly 3 or less we will consider those variables which account for more variation explained by them.

| Correlation Matrix | | | | | | | | | |
|--------------------|-------|-------|-------|--------|-------|----------|---------|---------|--------|
| | count | price | value | unisex | style | absorben | leakage | comfort | taping |
| count | 1.000 | .864 | .692 | .508 | .459 | .447 | .412 | .395 | .321 |
| price | .864 | 1.000 | .730 | .492 | .464 | .422 | .387 | .360 | .321 |
| value | .692 | .730 | 1.000 | .381 | .346 | .395 | .357 | .322 | .248 |
| unisex | .508 | .492 | .381 | 1.000 | .894 | .486 | .486 | .396 | .324 |
| style | .459 | .464 | .346 | .894 | 1.000 | .465 | .460 | .404 | .317 |
| absorben | .447 | .422 | .395 | .486 | .465 | 1.000 | .942 | .731 | .540 |
| leakage | .412 | .387 | .357 | .486 | .460 | .942 | 1.000 | .753 | .576 |
| comfort | .395 | .360 | .322 | .396 | .404 | .731 | .753 | 1.000 | .654 |
| taping | .321 | .321 | .248 | .324 | .317 | .540 | .576 | .654 | 1.000 |

Correlation Matrix

- **High Correlations:** There are strong correlations between variables such as absorben and leakage (0.942), indicating that these two variables are highly related. Other high correlations include comfort and leakage (0.753) and price and value (0.730).
- **Moderate to Low Correlations:** Variables such as count and taping (0.321) show a lower correlation, suggesting weaker relationships compared to others.

| KMO and Bartlett's Test | | |
|--|--------------------|----------|
| Kaiser-Meyer-Olkin Measure of Sampling Adequacy. | | .803 |
| Bartlett's Test of Sphericity | Approx. Chi-Square | 2404.021 |
| | df | 36 |
| | Sig. | .000 |

Kaiser-Meyer-Olkin Measure (KMO): The KMO value is 0.803, which is considered good and indicates that the sample size is adequate for PCA. **Bartlett's Test of Sphericity:** The chi-square statistic is significant ($p < 0.000$), which suggests that correlations between items are sufficient to proceed with PCA.

Communalities

- **Initial vs. Extraction Values:** Communalities represent the proportion of each variable's variance that is accounted for by the extracted components. Variables like unisex (0.944) and style (0.943) have high extraction values, meaning they are well represented by the components. Variables like taping (0.616) have lower communalities, indicating less variance is explained by the components.

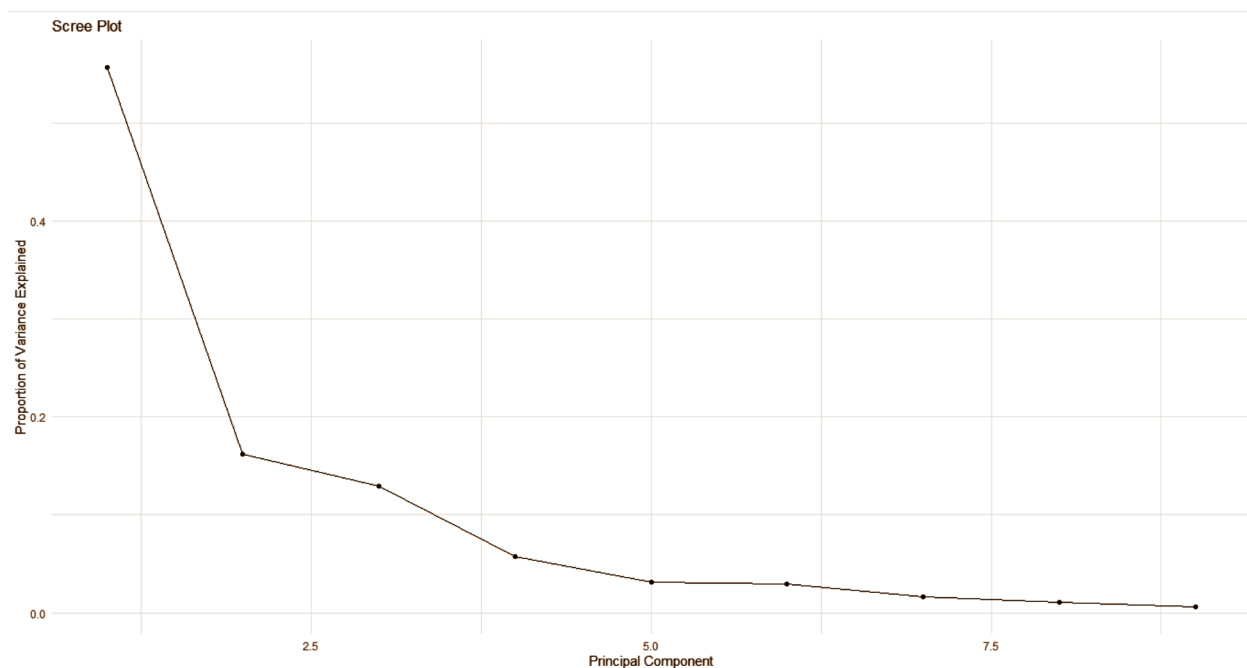
| Communalities | | |
|---------------|---------|------------|
| | Initial | Extraction |
| count | 1.000 | .862 |
| price | 1.000 | .890 |
| value | 1.000 | .786 |
| unisex | 1.000 | .944 |
| style | 1.000 | .943 |
| absorben | 1.000 | .842 |
| leakage | 1.000 | .871 |
| comfort | 1.000 | .801 |
| taping | 1.000 | .616 |

| Total Variance Explained | | | | | | | | | |
|--------------------------|---------------------|-----------|----------|-------------------------------------|---------------|--------------|----------------------------------|-----------|----------|
| Component | Initial Eigenvalues | | | Extraction Sums of Squared Loadings | | | Rotation Sums of Squared Loading | | |
| | Total | % of Var. | Cumul. % | Total | % of Variance | Cumulative % | Total | % of Var. | Cumul. % |
| 1 | 4.973 | 55.254 | 55.254 | 4.973 | 55.254 | 55.254 | 3.066 | 34.061 | 34.061 |
| 2 | 1.534 | 17.043 | 72.297 | 1.534 | 17.043 | 72.297 | 2.543 | 28.260 | 62.321 |
| 3 | 1.050 | 11.662 | 83.959 | 1.050 | 11.662 | 83.959 | 1.947 | 21.638 | 83.959 |

| Total Variance Explained | | | | | | | | | |
|--------------------------|---------------------|-------|---------|-------------------------------------|--|--|----------------------------------|--|--|
| Component | Initial Eigenvalues | | | Extraction Sums of Squared Loadings | | | Rotation Sums of Squared Loading | | |
| 4 | .556 | 6.180 | 90.140 | | | | | | |
| 5 | .326 | 3.622 | 93.762 | | | | | | |
| 6 | .272 | 3.025 | 96.787 | | | | | | |
| 7 | .135 | 1.503 | 98.290 | | | | | | |
| 8 | .099 | 1.102 | 99.392 | | | | | | |
| 9 | .055 | .608 | 100.000 | | | | | | |

Total Variance Explained

- Initial Eigenvalues:** The first component explains 55.25% of the variance, the second component explains 17.04%, and the third component explains 11.66%. Together, the first three components explain 83.96% of the variance.
- Rotation Sums of Squared Loadings:** After rotation, the variance explained by the first three components is slightly different: 34.06%, 28.26%, and 21.64%, respectively. This suggests that the rotated components provide a clearer interpretation of the variance.



Scree Plot

From the above scree plot we can see that at the three dots(that is on the third principal component) we are getting lesser values afterward for the proportion of variance explained so we will consider only the first three principal components which are addressing about 84% variations of all remaining variables.

| Component Matrix ^a | | | |
|-------------------------------|-----------|-------|-------|
| | Component | | |
| | 1 | 2 | 3 |
| count | .761 | .485 | .219 |
| price | .750 | .524 | .230 |
| value | .661 | .488 | .334 |
| unisex | .744 | .162 | -.604 |
| style | .719 | .137 | -.638 |
| absorben | .826 | -.393 | .082 |
| leakage | .817 | -.447 | .067 |
| comfort | .756 | -.456 | .147 |
| taping | .636 | -.424 | .178 |

| |
|---|
| Extraction Method: Principal Component Analysis. ^a |
| a. 3 components extracted. |

| Rotated Component Matrix | | | |
|--------------------------|-----------|------|------|
| | Component | | |
| | 1 | 2 | 3 |
| count | .224 | .865 | .251 |
| price | .193 | .891 | .243 |
| value | .183 | .862 | .105 |
| unisex | .244 | .266 | .902 |
| style | .237 | .220 | .916 |
| absorben | .850 | .232 | .256 |
| leakage | .879 | .182 | .257 |
| comfort | .863 | .177 | .157 |
| taping | .768 | .145 | .079 |

| |
|---|
| Extraction Method: Principal Component Analysis. Rotation Method: Varimax with Kaiser Normalization. ^a |
| a. Rotation converged in 4 iterations. |

Component Matrix

- **Component Loadings:**
 - **Component 1:** Strong loadings for count, price, value, absorben, leakage, and comfort suggest that this component might represent overall product quality or functionality.
 - **Component 2:** Strong loadings for price, value, and weaker for unisex and style indicate a potential dimension related to product pricing and perceived value.
 - **Component 3:** Strong loadings for unisex and style suggest this component might represent product attributes related to gender neutrality and style.

Rotated Component Matrix

- **Component 1:** High loadings for absorbency, leakage, and comfort indicate that this component is primarily associated with the performance attributes of the diaper (absorbency, leakage control, and comfort).
- **Component 2:** High loadings for price and value suggest it is related to the economic aspects of the product, such as cost and perceived value.
- **Component 3:** High loadings for unisex and style indicate that this component represents design features related to product appearance and target audience.

Summary

The PCA results suggest that the factors influencing the diaper product can be broadly categorized into three main components:

1. **Performance Attributes:** This includes variables like absorbency, leakage, and comfort.
2. **Economic Factors:** This component relates to price and value.
3. **Design and Target Audience:** This involves unisex and style.

The analysis indicates that these components collectively explain a significant portion of the variance in the dataset, allowing for a clearer understanding of the underlying factors affecting the diaper product's attributes.