



V2X Platooning Optimal Control

CE 295: Data Science for Energy, Fall 2021

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Outline

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 - 3-Vehicle Platooning Optimal Control
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- Future Work

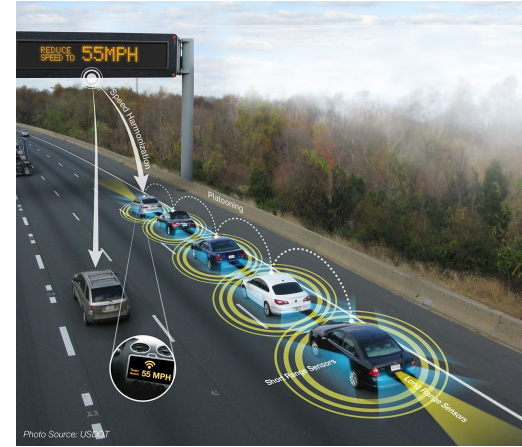
Introduction & Background

What is Vehicle Platooning?

- Vehicle fleet automation with integrated sensor array, active safety systems, and controllers to synchronize platoon acceleration and braking
- Vehicle-to-vehicle (V2V) communication [2]
- Vehicle-to-everything (V2X) communication [1]
- Emerging area of research in control and optimization: save time, money, energy
- Common scenarios this could apply to:
 - Trucks in highway driving
 - Cars in highway driving
 - **Cars in urban driving - our selection**

[1] "Platoon (automobile)" (5 Oct 2021). Wikipedia. Retrieved on 06 Nov 2021, 13:46, from [https://en.wikipedia.org/wiki/Platoon_\(automobile\)](https://en.wikipedia.org/wiki/Platoon_(automobile)).

[2] Ashley, Steven (18 Nov 2014). "Robot truck platoons roll forward." BBC. Retrieved on 06 Nov 2021, 13:49, from <https://www.bbc.com/future/article/20130409-robot-truck-platoons-roll-forward>



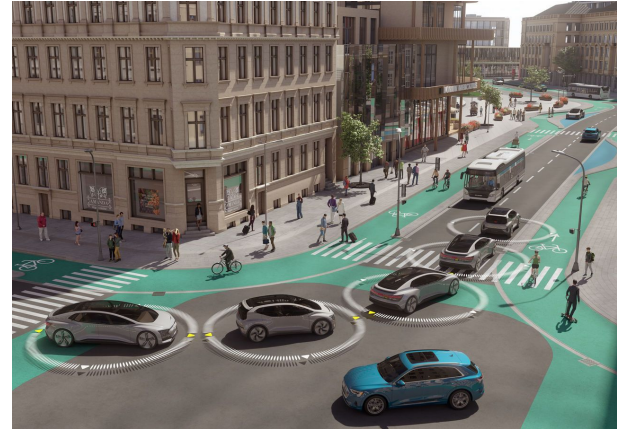
[1]



[2]

Focus of the Study

- Cars platooning in an urban area
 - More obstacles and more powertrain varieties
- Focus on battery electric vehicle (BEV) platoons
- Optimal platoon trajectory
 - Given timed traffic lights and spacing in an urban area
 - Output: optimal trajectory for the car to save time *and* energy



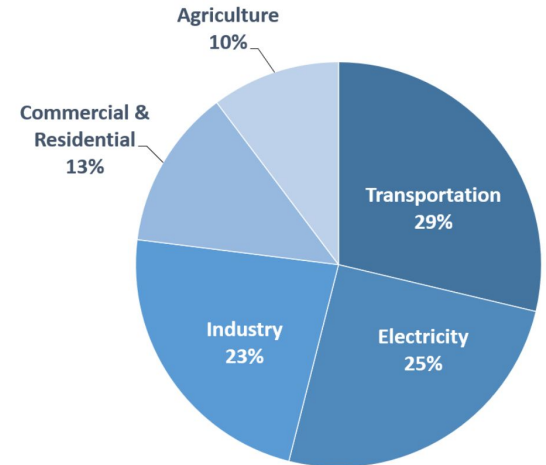
[3]

[3] Schneider, Tilman (16 Sept 2018). "Audi Study: No Congestion in the City of the Future." Audi MediaCenter. Retrieved on 06 Nov 2021, 13:52, from <https://www.audi-mediacenter.com/en/press-releases/audi-study-no-congestion-in-the-city-of-the-future-10736>.

Why Does This Matter?

- Energy saved → reduced emissions!
 - Transportation is largest emissions sector
 - Electricity second - electric vehicles
 - Reducing carbon emissions benefits the planet and its occupants
- Time saved is a huge advantage for people...
 - Traveling to and from work → more free time or family time
 - Traveling to and from a destination → time saved in the vehicle
 - Transporting goods → quicker shipping time, can sell more

Total U.S. Greenhouse Gas Emissions
by Economic Sector in 2019



[4] “Sources of Greenhouse Gas Emissions” (2021). United States Environmental Protection Agency. Retrieved on 06 Nov 2021, 14:01, from <https://www.epa.gov/ghgemissions/sources-greenhouse-gas-emissions>.

Relevant Literature



- Adaptive cruise control and cooperative adaptive cruise control can save energy [5]
- Platooning allows for closer headway → smaller drag, saves energy [6]
- Traffic lights in urban settings cause stops and delays, responsible for a large amount of emissions [7]
- Main conclusion: traffic lights increase emissions, cruise control + platooning decrease emissions
 - Can we combine the two for a more powerful energy savings effect?

[5] Wang, Z., Wu, G., & Barth, M. J. (2018, November). A review on cooperative adaptive cruise control (CACC) systems: Architectures, controls, and applications. In 2018 21st International Conference on Intelligent Transportation Systems (ITSC) (pp. 2884-2891). IEEE.

[6] Ma, F., Yang, Y., Wang, J., Liu, Z., Li, J., Nie, J., ... & Wu, L. (2019). Predictive energy-saving optimization based on nonlinear model predictive control for cooperative connected vehicles platoon with V2V communication. *Energy*, 189, 116120.

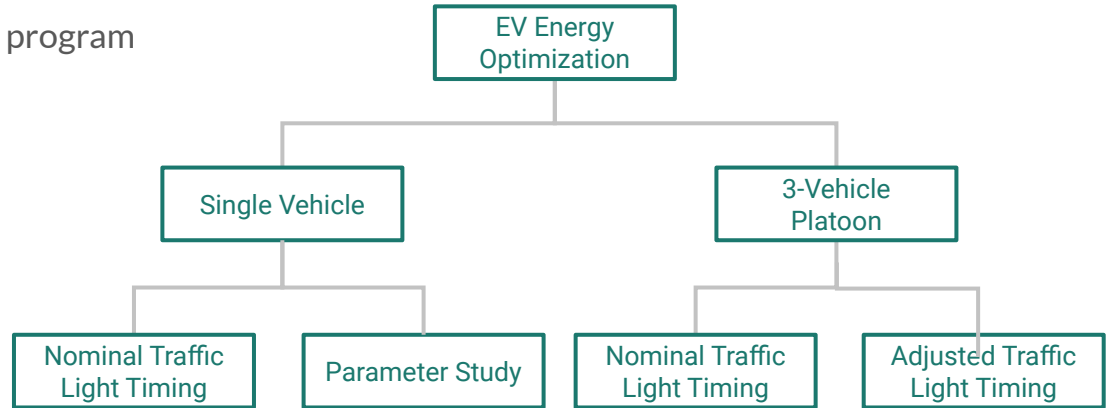
[7] C. Sun, J. Guanetti, F. Borrelli and S. J. Moura, "Optimal Eco-Driving Control of Connected and Autonomous Vehicles Through Signalized Intersections," in *IEEE Internet of Things Journal*, vol. 7, no. 5, pp. 3759-3773, May 2020, doi: 10.1109/JIOT.2020.2968120.



Methods

Problem Structure

- Mixed-integer second order cone program (MISOCP)
- Modeling language: CVXPY
- Optimization solver: MOSEK
- Two cases
 - Single Vehicle
 - 3-Vehicle Platoon



Single Vehicle Optimal Control

- Longitudinal vehicle dynamics modeled
 - Nonlinear dynamics create need for second order cone constraints
- Traffic lights using the Big-M method
 - Creates need for a mixed-integer program

TABLE II: Drive Cycle Constraints

Constraint	Value	Units
Travel Distance	3000	m
Travel Time	380	sec
Velocity Lower Bound	0	m/s
Velocity Upper Bound	17.5	m/s
Acceleration Magnitude Bound	1.5	m/s ²
Jerk Magnitude Bound	1	m/s ³

$$\min_{z(t), u(t)} \int_{t_0}^{t_f} \frac{d}{dt} E(t) dt \quad (23a)$$

$$\text{subject to } p(t) = p(t_0) + \int_{t_0}^t v(\tau) d\tau \quad (23b)$$

$$v(t) = v(t_0) + \int_{t_0}^t a(\tau) d\tau \quad (23c)$$

$$ma(t) = F(t) - F_{loss}(t) \quad (23d)$$

$$F(t) = \frac{1}{mR_{wheel}r_{final}\eta} T(t) \quad (23e)$$

$$F_{loss}(t) \geq C_{rr}mg + C_k v(t) + \frac{1}{2} \rho C_d A_f v(t)^2 \quad (23f)$$

$$P_{mot}(t) = P_{batt}(t) - P_{loss}(t) \quad (23g)$$

$$P_{batt}(t) = V_{oc} I(t) \quad (23h)$$

$$P_{loss}(t) \geq I(t) R_{int}^2 \quad (23i)$$

$$v_{min} \leq v(t) \leq v_{max} \quad (23j)$$

$$-a_{max} \leq a(t) \leq a_{max} \quad (23k)$$

$$-j_{max} \leq \frac{d}{dt} a(t) \leq j_{max} \quad (23l)$$

$$-P_{max} \leq P_{batt}(t) \leq P_{max} \quad (23m)$$

$$E(t) = E(t_0) + \int_{t_0}^t V_{oc} I(\tau) d\tau \quad (23n)$$

$$0.2 \leq SOC(t) \leq 0.8 \quad (23o)$$

$$p(L_{i,start}) - L_{i,pos} \geq -M(1 - L_{i,bool}) \quad (23p)$$

$$p(L_{i,end}) - L_{i,pos} \leq M(L_{i,bool}) \quad (23q)$$

$$z(t) = \begin{bmatrix} p(t) \\ v(t) \\ a(t) \\ E(t) \\ L_{i,bool} \end{bmatrix}, \quad u(t) = \begin{bmatrix} F(t) \\ F_{loss}(t) \\ I(t) \\ P_{mot}(t) \\ P_{batt}(t) \\ P_{loss}(t) \end{bmatrix}$$

$$p(L_{i,start}) \geq L_{i,pos} \quad \text{or} \quad p(L_{i,end}) \leq L_{i,pos}$$

Application of
Big-M method

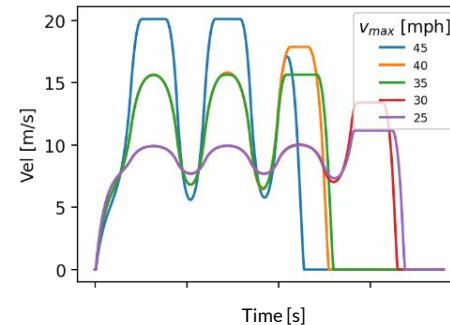
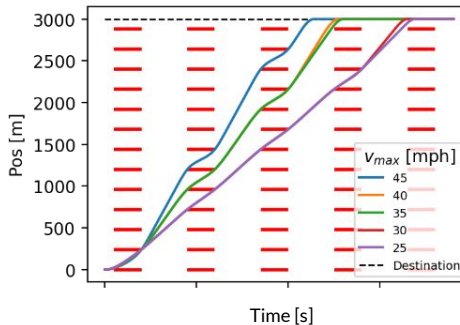
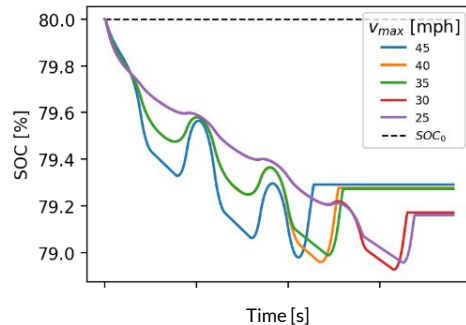


$$p(L_{i,start}) - L_{i,pos} \geq -M(1 - L_{i,bool})$$

$$p(L_{i,end}) - L_{i,pos} \leq M(L_{i,bool})$$

Single Vehicle Parameter Study Example

- Independent variable: Speed limit
- Dependent variable: Energy consumption
- Higher speed leads to a lower energy consumption*
 - *Savings eventually plateau likely due to higher aerodynamic drag at higher speeds

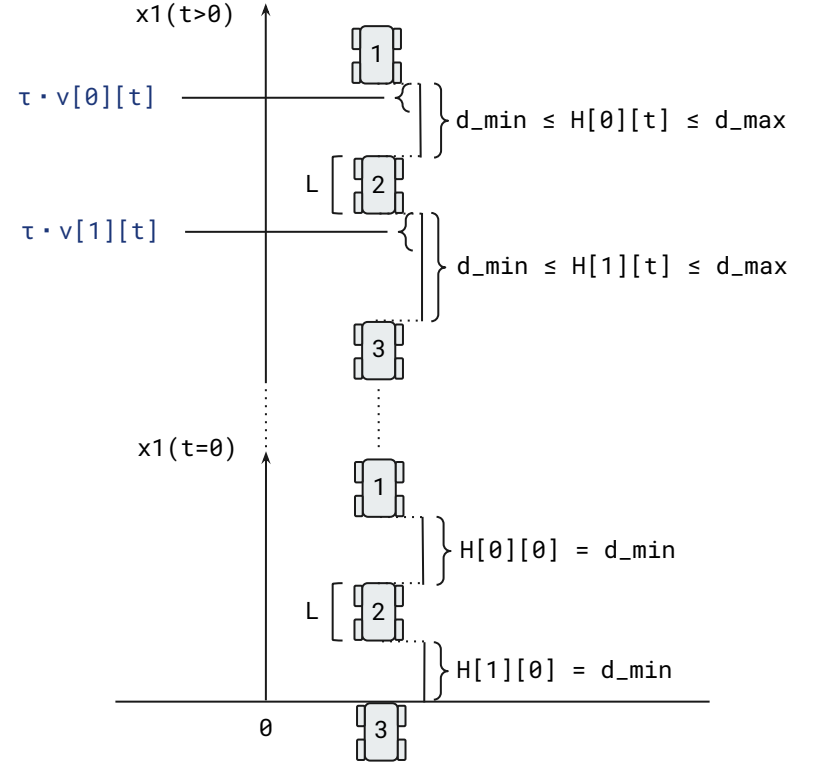


3-Vehicle Platoon Optimal Control

- Trajectory copying of the leading vehicle with constraints on:
 - Initial state, $\mathbf{x1}[\mathbf{veh}][0]$,
 - Following distance, $\mathbf{H}[\mathbf{veh}][t]$,
 - Reaction and actuation time delay, τ
- Assumes no vehicle overtaking and turning,
- Allows for 'breakaway' from the leading vehicles in light of red phase

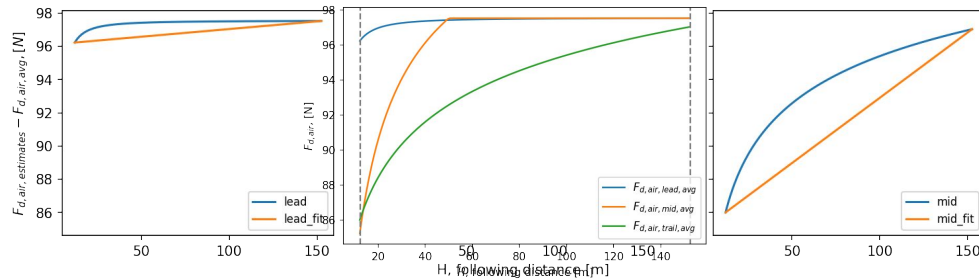
TABLE III: Vehicle Platooning Constraints

Constraint	Value	Units
Number of Vehicles, N	3	Unitless
Reaction and Actuation Time Delay, τ	0.2	sec
Minimum Following Distance, d_{min}	40	ft
Maximum Following Distance, d_{max}	500	ft

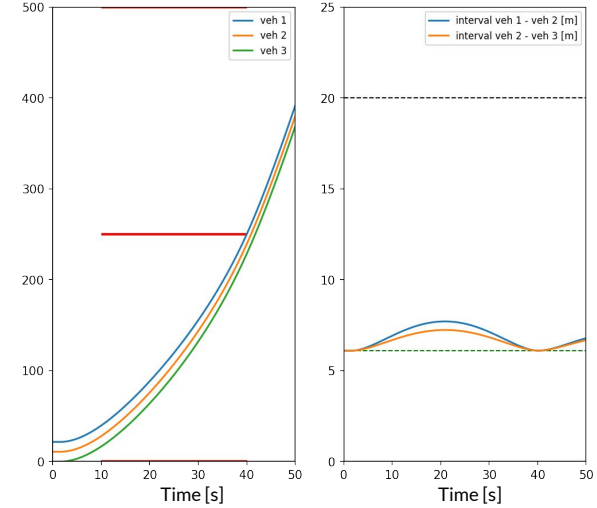


Aerodynamic Drag

- $F_{air}(\mathbf{v}, C_d(\mathbf{h})) \rightarrow$ non-convex in formulation (27) for each vehicle in the platoon,
- Using the velocity upper bound, we fixed the value of \mathbf{v}_{avg} to estimate an average drag value and linearly fitted and adjusted for \mathbf{h} (29)



Vehicle trajectory and following distance for $t \leq 50$ s



$$F_{air,k,i}(\mathbf{h}, \mathbf{v}) = \frac{g(\mathbf{h}_{k,i})}{2} \rho C_d v_{k,i}^2, \quad k = 0, 1, \dots, N, i = 0, 1 \quad (27)$$

$$g(\mathbf{h}_{k,i})(\mathbf{h}) = \alpha h_{k,i}^\beta + c \quad (28)$$

$$F_{air,approx,k,i}(\mathbf{h}, \mathbf{v}) = \frac{1}{2} \rho C_d v_{k,i}^2 - b h_{k,i}, \quad k = 0, 1, \dots, N, i = 0, 1 \quad (29)$$

Results

Traffic Light Simulation

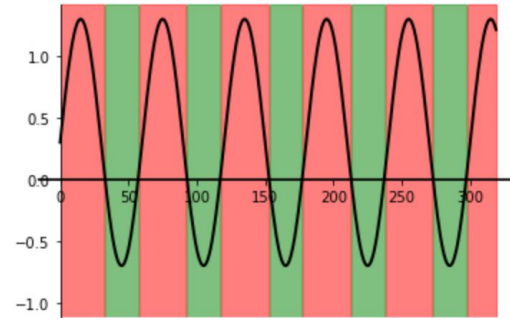
$$f(t) = \sin(\omega t + \phi) + h$$

$f(t) < 0$: green light

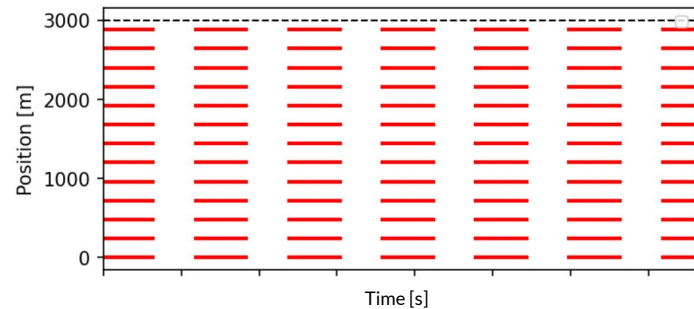
ω : traffic light cycle period

ϕ : phase shift

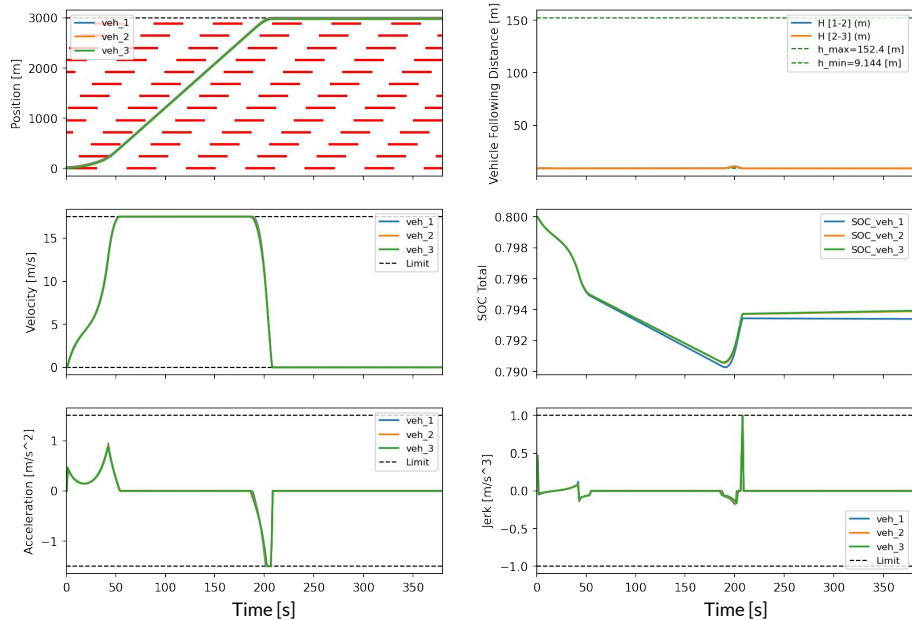
h : controls green-light duration



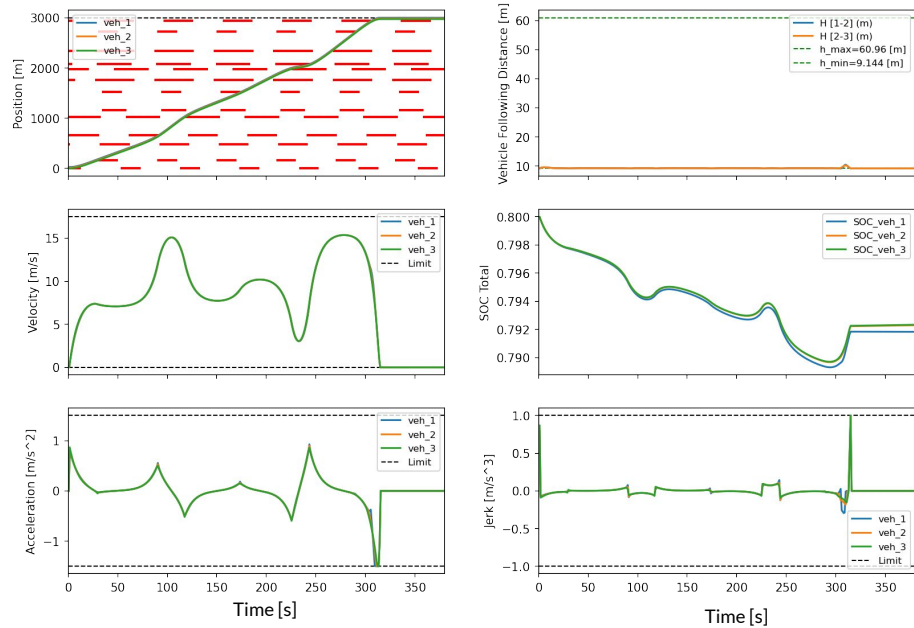
$T = 60\text{s}$
 $\omega = 2\pi/T$
 $\phi = 0$
 $h = 0.3$



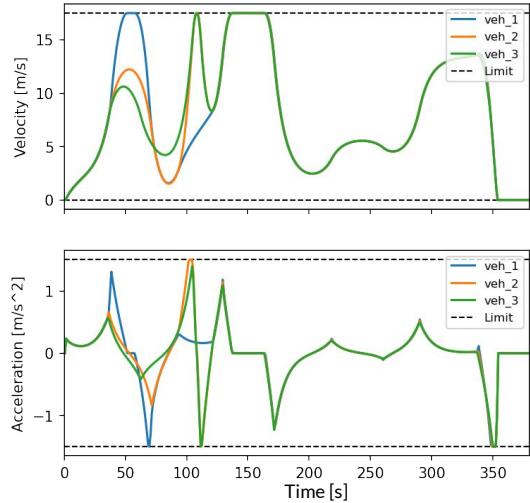
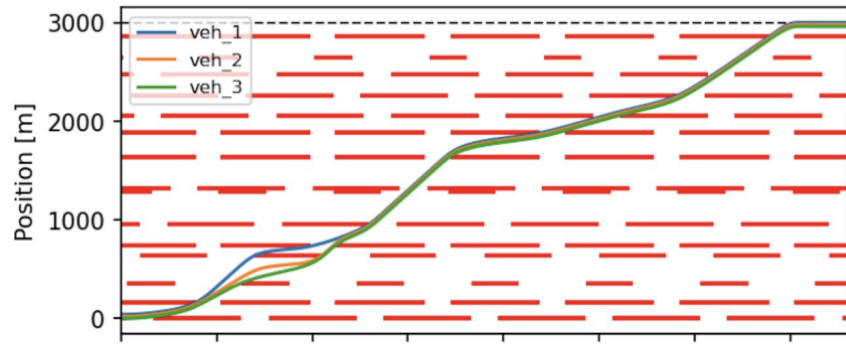
Uniform phase shift



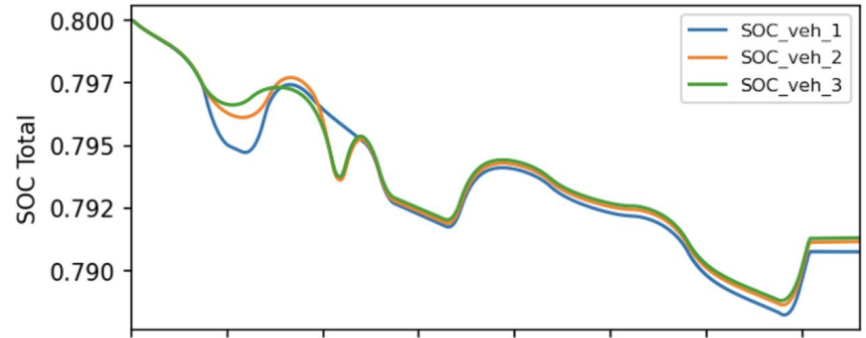
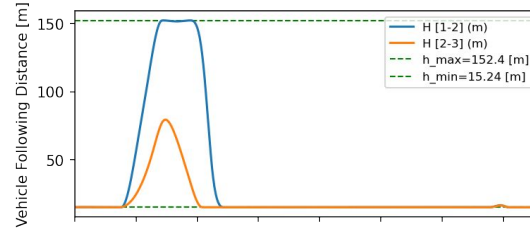
Random parameters



Results: Traffic Light Simulation Parameter Study



Random parameters + following distance

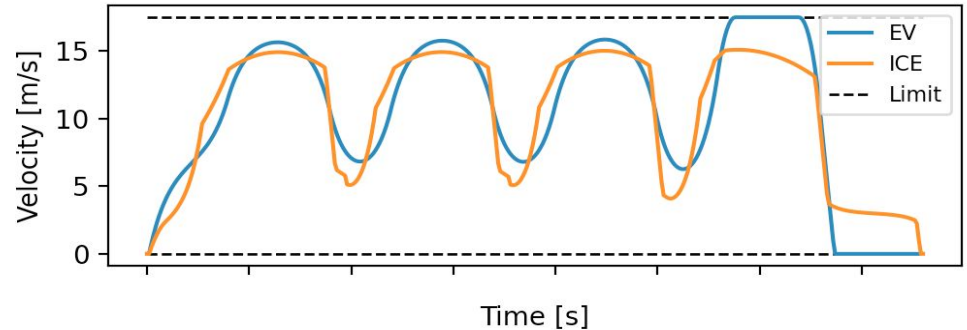


Results: Traffic Light Simulation Parameter Study

Future Work

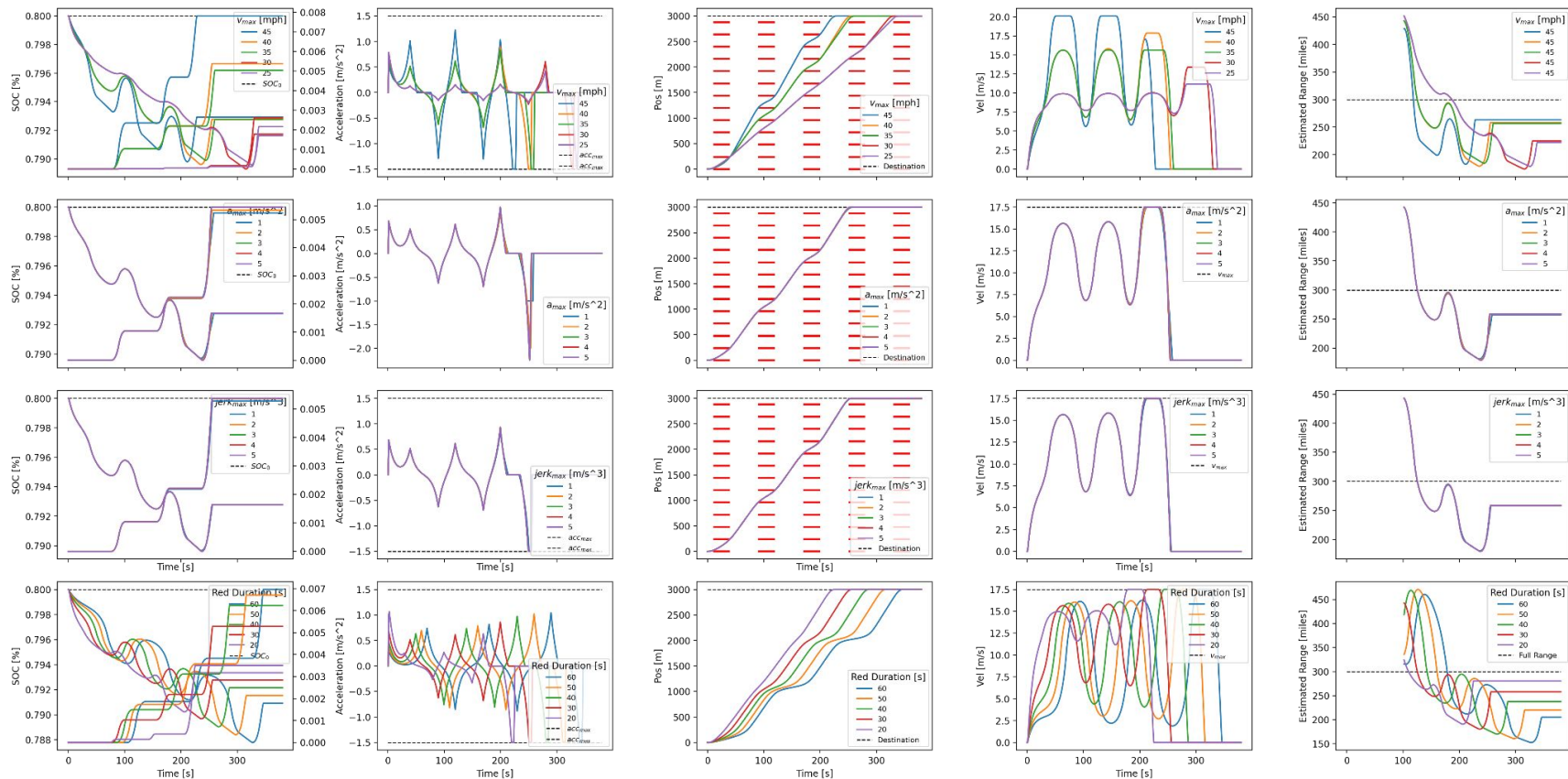
Future Work

- ICE, PHEV powertrains
- Add traffic lights as a decision variable with constraints
 - Anticipation of the length and position of platoons
- Partial knowledge of traffic light parameters
- Background traffic (non-V2X)





Thank You!



Results: Single Vehicle (BEV) Parameter Study