1) Solve
$$\frac{dy}{dx} + 2xy^2 = 0$$
, $y(2) = \frac{1}{5}$.
 $\frac{dy}{dx} = -2xy^2$.
 $\frac{dy}{dx} = -2x dx$.
 $\int \frac{dy}{y^2} = -\int 2x dx$.
 $-\frac{1}{3} = -x^2 + C$.
 $y = \frac{1}{-x^2 + C}$.
Since $y(2) = \frac{1}{5}$, $\frac{1}{-(\frac{1}{5})^2 + C}$.
 $-\frac{1}{25} + C = -5$.
 $C = \frac{1}{25} - 5$.
 $C = -\frac{124}{25}$.
 $= -\frac{1}{-x^2 - 124/25}$.

2)
$$\frac{dy}{dt} = e^{y}(10-3y-y^{2})$$
.

a) Find equilibrium points: set $e^{y}(10-3y-y^{2})=0$

phase line

- b) Since -5 < -4 = y(0) < 2, $\lim_{t \to \infty} \phi(t) = 2$.
- \$(t) is an increasing function
- 3). Solve $t^2 \frac{dy}{dt} + t(t+2)y = 0 e^t$, t>0 $\frac{dy}{dt} + \frac{t+2}{t}y = \frac{e^t}{t^2}.$

integrating factor:
$$\int \frac{t+2}{t} dt = e^{\int 1+\frac{2}{t}} dt + \frac{t+2\ln t}{t} = \frac{t^2 + t}{t^2 + t} = \frac{\int e^{2t} dt + C}{t^2 + t} =$$

4) a)
$$x - y^3 + y^2 \sin x = (3\pi y^2 + 2y \cos x)y'$$

$$(x - y^3 + y^2 \sin x) + (-3\pi y^2 - 2y \cos x) \frac{dy}{dx} = 0.$$

$$M(x,y) = x - y^3 + y^2 \sin x$$

$$N(x,y) = -3xy^2 - 2y \cos x.$$

$$\frac{\partial M}{\partial y} = -3y^2 + 2y \sin x.$$

$$\frac{\partial M}{\partial x} = -3y^2 + 2y \sin x.$$

$$\frac{\partial M}{\partial x} = -3y^2 + 2y \sin x.$$

$$\frac{\partial M}{\partial x} = x^2 y^3 - \frac{1}{1+x^2} dx + (x^3 y^2 + \sin y) dy = 0.$$

$$M(x,y) = x^3 y^3 + \sin y.$$

$$W(x,y) = x^3 y^3 + \sin y.$$

$$W(x,y) = x^3 y^3 + \sin y.$$

$$W(x,y) = x^3 y^3 - \tan^3(x) + h(y).$$

$$W(x,y) = x^3 y^3 + \sin^3(x) + \sin^3(x) + h(y).$$

$$W(x,y) = x^3 y^3 + \sin^3(x) + \sin^3(x) + h(y).$$

$$W(x,y) = x^3 y^3 + \sin^3(x) + \sin^3(x) + h(y).$$

$$W(x,y) = x^3 y^3 + \sin^3(x) + \sin^3(x) + h(y).$$

$$W(x,y) = x^3 y^3 + \sin^3(x) + \sin$$