Quiz 3, Section D03

MATH 20D, LECTURE D00, FALL 2017

NAME:

UID:

There are two problems. Write your name on the back too. No CHEATSHEETS or any electronic devices are allowed. Write your answer as clearly as possible to receive full credits. You have 20 mins to finish this quiz.

Problem 1.(5 points.) Transform the following second order ODE to a system of ODEs.

$$y' = x_1 \qquad \text{Ipt for introducing}$$

$$y' = x_2 \qquad \text{new variables } x_1, x_2$$

$$y' = x_2 = x_1' \qquad \text{Ipt}$$

$$\Rightarrow x_1' = x_2$$

$$2x_2' + 7x_2 + 5x_1 = 0$$

$$\Rightarrow x_2' = -\frac{7}{2}x_2 - \frac{5}{2}x_1$$

$$x_1' = x_2$$

$$x_2' = -\frac{5}{2}x_1 - \frac{7}{2}x_2$$

$$x_2' = -\frac{5}{2}x_1 - \frac{7}{2}x_2$$

$$\text{Correct answer}$$

NAME:

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Problem 2.(5 points.) Given

$$\vec{x}' = A\vec{x}$$
, where $A = \begin{pmatrix} 4 & -2 \\ 8 & -4 \end{pmatrix}$.

Let
$$\vec{x}^{(1)} = \begin{pmatrix} 2 \\ 4 \end{pmatrix}$$
 and $\vec{x}^{(2)} = \begin{pmatrix} 2 \\ 4 \end{pmatrix} t - \begin{pmatrix} 0 \\ 1 \end{pmatrix}$.

- a) Show that $\vec{x}^{(1)}$ and $\vec{x}^{(2)}$ are solutions of the system $\vec{x}' = A\vec{x}$.
- b) Show that $\vec{x}^{(1)}$ and $\vec{x}^{(2)}$ form a fundamental set of solutions.
- c) What is the general solution of $\vec{x}' = A\vec{x}$.

what is the general solution of
$$\vec{x} = A\vec{x}$$
.

a) $\vec{z}^{(1)} = \frac{d}{dz} \left(\frac{2}{4}\right) = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$

$$A \vec{x}^{(1)} = \begin{bmatrix} 4 & -2 \\ 8 & -4 \end{bmatrix} \begin{bmatrix} 2 \\ 4 \end{bmatrix} = \begin{bmatrix} 8 - 9 \\ 16 - 16 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$$

$$\therefore \vec{x}^{(2)} = A \vec{x}^{(1)} \quad \text{ipt}$$

$$= \begin{bmatrix} 8t - 8t + 2 \\ 16t - 16t + 4 \end{bmatrix} = \begin{bmatrix} 2 \\ 4 \end{bmatrix}$$

$$\therefore \vec{x}^{(2)} = A \vec{x}^{(2)} \quad \text{form a bundamental Solutions}$$

$$\therefore \vec{x}^{(1)}, \vec{x}^{(2)} = A \vec{x}^{(2)} \quad \text{form a bundamental Solutions}$$

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