

# HW04

MATH 20D, LECTURE D00, FALL 2017

DUE TUESDAY, OCT 31

NAME:

1. Find the general solution of the given differential equation.

(a)  $4y'' - 4y' - 3y = 0$ .

(b)  $16y'' + 24y' + 9y = 0$ .

2. Solve the given initial value problem. Sketch the graph of the solution and describe its behavior for increasing  $t$ .

(a)  $9y'' - 12y' + 4y = 0, y(0) = 2, y'(0) = -1$ .

(b)  $y'' - 6y' + 9y = 0, y(0) = 0, y'(0) = 2$ .

(c)  $y'' + 4y' + 4y = 0, y(-1) = 2, y'(-1) = 1$ .

3. Use the method of reduction of order to find a second solution of the given differential equation.

(a)  $t^2y'' - 4ty' + 6y = 0, t > 0; y_1(t) = t^2$ .

(b)  $t^2y'' + 2ty' - 2y = 0, t > 0; y_1(t) = t$ .

4. Find the general solution of the given differential equation.

(a)  $y'' - 2y' - 3y = 3e^{2t}$ .

(b)  $y'' + 2y' + y = 2e^{-t}$ .

(c)  $y'' - 2y' - 3y = -3te^{-t}$ .