

St.JOSEPH'S COLLEGE OF ENGINEERING, CHENNAI-119
St.JOSEPH'S INSTITUTE OF TECHNOLOGY, CHENNAI-119
B.E/B.TECH (COMMON TO ALL BRANCHES)-FIRST SEMESTER
MA6151/ MATHEMATICS – I

ASSIGNMENT – II UNIT-III APPLICATIONS OF DIFFERENTIAL CALCULUS

PART – A

1.	Find the radius of curvature of $y = e^x$ at the point at (0,1)
2.	Find the curvature of the curve $x^2 + y^2 - 2x - 4y - 4 = 0$
3.	Find the evolute of the curve whose centre of curvature of the curve is $\bar{x} = 2a + 3at^2, \bar{y} = -2at^3$
4.	Define Evolutes and Involutes.
5.	Find the centre of curvature of the curve $y = x^2$ at the point (1,-1)
6.	Find the envelope of the family of lines $\frac{x}{t} + yt = 2c, t$ being the parameter.
7.	Find the envelope of the family of straight lines $y = mx + \frac{a}{m}, m$ being the parameter
8.	Find the envelope of the family of circles $(x - \alpha)^2 + y^2 = r^2, \alpha$ being the parameter.

PART – B

1(a)	Find the radius of curvature of the curve $y^2 = 4x$ at (1,2)
1(b)	Find the envelope of $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ given $a^n + b^n = c^n$, where c is a known constant
2(a)	Find the radius of curvature at any point θ of the cycloid $x = a(\theta + \sin \theta); y = a(1 - \cos \theta)$
2(b)	Find the circle of curvature of the curve $\sqrt{x} + \sqrt{y} = \sqrt{a}$ at $\left(\frac{a}{4}, \frac{a}{4}\right)$.
3(a)	Find the envelope of the system of lines $\frac{x}{l} + \frac{y}{m} = 1$, where l and m are connected by the relation $\frac{l}{a} + \frac{m}{b} = 1$, l and m are the parameters.

3(b)	Find the equation of the circle of curvature of the rectangular hyperbola $xy = 12$ at the point $(3,4)$
4(a)	Find the evolute of the curve $x^{2/3} + y^{2/3} = a^{2/3}$
4(b)	Find the evolute of the parabola $x^2 = 4ay$ considering it as the envelope of its normal