The AbinitioD Γ A Project v1.0: Non-local correlations beyond and susceptibilities within dynamical mean-field theory: README (January 2018)

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Preprint: arXiv:1710.06651 **Github**: AbinitioDGA/ADGA

1 Introduction

Diagrammatic extensions of dynamical mean field theory (DMFT) such as the dynamical vertex approximation (D Γ A) allow us to include non-local correlations beyond DMFT on all length scales and proved their worth for model calculations. Here, we detail the implementation of an AbinitioD Γ A approach. We go through each major step in the workflow and discuss the input and output data files (including their structure).

2 DMFT data

Starting point of any calculation is a converged DFT+DMFT solution, which we obtain, e.g. from the package w2dynamics. The latter writes all output data into an HDF5 file, from which we extract the datasets siw, dc, mu, beta, giw (self-energy, double counting correction, chemical potential, inverse temperature, Green's function) and—depending on the run options—also hk (Hamiltonian). The data structure of the w2dynamics output is shown in Listing 1. In order to keep these instructions as concise as possible, only the parts relevant for ADGA are shown. (Information about the full contents and structure of an HDF5 file can usually be retrieved via h51s -lr. For a basic HDF5 introduction please visit /documentation/hdf5_intro.pdf) In order to use input from another (DMFT) program, it is necessary to convert it into the group structure shown in Listings 1 and 2. Examplary HDF5 templates with the existing structures can be found in /documentation/hdf5_templates/.

Listing 1: HDF5-structure of the DMFT output

```
/.axes/
                                  Group
/.axes/iw
                                  Dataset {2*NIW}
/.config
                                  Group
/ dmft -001/
                                  Group
/dmft - 001/ineq - 001/
                                  Group
/dmft-001/ineq-001/siw
                                  Group
/dmft-001/ineq-001/siw/value
                                  Dataset {NBANDS, NSPINS, 2*NIW}
/dmft - 001/ineq - 001/giw
                                  Group
/dmft-001/ineq-001/giw/value
                                  Dataset {NBANDS, NSPINS, 2*NIW}
/dmft - 001/ineq - 001/dc
                                  Group
/dmft-001/ineq-001/dc/value
                                  Dataset {NBANDS, NSPINS}
/dmft - 001/mu
                                  Group
/dmft -001/mu/value
                                  Dataset {SCALAR}
```

Please note that instead of actual numbers, we use upper-case variables here in order to keep the description general. NIW is the number of positive fermionic frequencies of the one-particle quantities, NBANDS is the number of correlated orbitals of the inequivalent atom ineq-001, and NSPINS is equal to 2.

On top of this DMFT solution, the impurity two-particle Green's function ("vertex") is computed, e.g. within w2dynamics, which has the following structure: (again, groups not necessary for ADGA are omitted here.)

Listing 2: HDF5-structure of the worm-sampled vertex

```
/.axes/
                                                    Group
                                                    Dataset \{2*N4IWB+1\}
/.axes/iwb-g4
/.axes/iwf-g4
                                                    Dataset {2*N4IWF}
/ \text{worm} - 001/
                                                    Group
/ worm - 001 / ineq - 001 /
                                                    Group
/worm-001/ineq-001/g4iw-worm/
                                                    Group
/ worm - 001/ineq - 001/g4iw - worm/00001/
                                                    Group
/worm-001/ineq-001/g4iw-worm/00001/value
                                                    Dataset \{2*N4IWF, 2*N4IWF, 2*N4IWB+1\}
/ worm - 001/ineq - 001/g4iw - worm/00001/error
                                                    Dataset \{2*N4IWF, 2*N4IWF, 2*N4IWB+1\}
/\text{worm} - 001/\text{ineq} - 001/\text{g4iw} - \text{worm}/\text{NGRPS}/
                                                    Group
/ worm -001/ in eq -001/ g4iw - worm / NGRPS / value
                                                    Dataset \{2*N4IWF, 2*N4IWF, 2*N4IWB+1\}
/ worm - 001/ineq - 001/g4iw - worm/NGRPS/error
                                                    Dataset \{2*N4IWF, 2*N4IWF, 2*N4IWB+1\}
```

N4IWF and N4IWB are the number of positive fermionic and bosonic Matsubara frequencies of the two-particle Green's function, respectively. NGRPS is the maximal number of band-spin combinations, $(2n_{dim})^4$. The group names in front of the value and error groups are integers from from 1 to NGRPS and represent a one-to-one mapping from a *band-spin combination* to an integer, e.g. $00001 \rightarrow (1\uparrow, 1\uparrow, 1\uparrow, 1\uparrow)$. In general, the transformation of band-spin combination to an index $(b_i \in [1, n_{dim}], s_i \in [1, 2] = [\uparrow, \downarrow])$

$$b_1s_1, b_2s_2, b_3s_3, b_4s_4 \rightarrow index,$$

is achieved via

$$\mathrm{index} = 2^3 n_{dim}^3 (2b_1 + s_1 - 3) + 2^2 n_{dim}^2 (2b_2 + s_2 - 3) + 2n_{dim} (2b_3 + s_3 - 3) + 2b_4 + s_4 - 2,$$

where n_{dim} represents the number of correlated bands whithin the atom under consideration. The number of existing groups can be calculated via

```
density – density interactions : N = n_{dim}^2 \times 6

Kanamori parametrization : N = \left[3n_{dim}^2 - 2n_{ndim}\right] \times 6,
```

where the factor 6 comes from all the possible SU(2) combinations allowed for a given band combination.

3 Fully nonlocal V(q) data

The $V(\mathbf{q})$ file creation is currently completely independent of the ADGA package but it must respect a certain HDF5 structure, which will be explained by considering an example of a three-band system (a template can be found in /documentation/hdf5_templates/):

Listing 3: V(q) file structure

```
      / axes
      Group

      /. axes/Q-points
      Dataset {8000, 3}

      /00001
      Dataset {8000}

      /00005
      Dataset {8000}

      ...
      Dataset {8000}

      /00077
      Dataset {8000}

      /00081
      Dataset {8000}
```

The Q-points dataset contains all q-point vectors starting from (0,0,0) and going through all other points in the following manner (e.g., for a 20x20x20 q-mesh of the Brillouin zone):

$$i = 0 \quad q = (0, 0, 0)$$

$$i = 1 \quad q = (0, 0, 0.05)$$

$$\vdots$$

$$i = 19 \quad q = (0, 0, 0.95)$$

$$i = 20 \quad q = (0, 0.05, 0)$$

$$i = 21 \quad q = (0, 0.05, 0.05)$$

$$\vdots$$

$$i = 399 \quad q = (0, 0.95, 0.95)$$

$$i = 400 \quad q = (0.05, 0, 0)$$

$$i = 401 \quad q = (0.05, 0, 0.05)$$

$$\vdots$$

$$i = 7999 \quad q = (0.95, 0.95, 0.95)$$

in units of 2π /lattice constant. The other groups then contain the $V(\mathbf{q})$ information along this list of points for the specific band combinations. The transformation of band combination to an index

$$i_1, i_2, i_3, i_4 \rightarrow index,$$

is achieved via

index =
$$n_{dim}^3(i_1 - 1) + n_{dim}^2(i_2 - 1) + n_{dim}(i_3 - 1) + i_4$$
,

where n_{dim} represents the number of correlated bands. Please note that the $V(\mathbf{q})$ implementation at the moment only supports one impurity.

4 setupvertex - symmetrizing the vertex

In order to use the vertex it must first be symmetrized and transformed into the density and magnetic channels according to

$$G_d = rac{1}{2} \left[G_{\uparrow \uparrow \uparrow \uparrow} + G_{\downarrow \downarrow \downarrow \downarrow} + G_{\uparrow \uparrow \downarrow \downarrow} + G_{\downarrow \downarrow \uparrow \uparrow}
ight]$$
 $G_m = rac{1}{2} \left[G_{\uparrow \downarrow \downarrow \uparrow} + G_{\downarrow \uparrow \uparrow \downarrow}
ight],$

where we additionally used the SU(2) symmetry. This symmetrization can be done with the setupvertex program. One simply has to execute this program, with \$ADGA_DIR as your ADGA parent directory, and follow the instructions given (colored text represents user input).

Listing 4: exemplary setupvertex execution

```
$ $ADGA_DIR/bin/setupvertex
Number of inequivalent atoms: 1
Vertex file: srvo3-2pg-repo.hdf5
Number of correlated bands for inequivalent atom 1: 3
Outputfile for symmetrized Vertex: srvo3-2pg-symmetrized.hdf5

SU2 symmetry only (s) or SU2 AND orbital symmetry (o)?: o
```

This produces an HDF5 file of the following structure:

Listing 5: symmetrized vertex structure

```
Group
/ineq-001
                                           Group
/ineq -001/dens
                                           Group
/ineq -001/dens/00000
                                           Group
/ineq -001/dens/00000/00001
                                           Group
/ineq -001/dens/00000/00001/value
                                            Dataset {2*N4IWF}
/ineq -001/magn
                                           Group
/ineq -001/magn/00000
                                           Group
/ineq -001/magn/00000/00001
                                           Group
/ineq -001/magn/00000/00001/value
                                            Dataset {2*N4IWF}
```

which is the centerpiece of the ADGA input. The group names in front of the value groups again represent a one-to-one mapping from a *band combination* to an integer. $(00001 \rightarrow (1, 1, 1, 1))$. The group before that represents a bosonic frequency which is shifted so we start at 0 (00000) and go to 2*N4IWB.

5 abinitiodga - main program

The last preparational step is the configuring of ADGA. The main program's input options are contained in a config file (of arbitrary name). This config file is segmented into groups marked by squared braces. Subgroups are marked by double squared braces.

In the [General] group we define what we want to calculate: equation of motion (calc-eom) and/or susceptibilities (calc-susc), how we want to calculate these quantities: along paths (KDataFile, QDataFile) or on a grid (q-grid) and how large our calculation should be: number of atoms (NAt), frequency box (N4iwf, N4iwb), momentum-space grid (k-grid). We also provide here the Hamiltonian (HkFile) and possibly a Umatrix file (UFile) and the nonlocal interaction file (VqFile).

Important comments on the different quantities:

k-grid represents the Hamiltonian grid and should therefore never be changed once set for a specific case. A default eom run (without KDataFile) evaluates the selfenergy on the the whole k-grid (independently of the q-points specification). Providing KDataFile accordingly evalutes the selfenergy only on the given k-points. This is especially useful if one deals with smaller box sizes (cue different scaling of the inversion and the eom) or if one is only interested in specific points and/or paths.

q-grid on the other hand describes part of the outer parallelized loop of abinitiodga. It is constrained by the Hamiltonian grid (k-grid) in that it can't be larger. Furthermore if one chooses a smaller grid each component must be divisable without remainder: $\mod(k_i, q_i) \stackrel{!}{=} 0$ (e.g. k-grid = 20 9 9; q-grid = 5 3 3).

The momentum-dependent susceptibilities are then calculated along these points (i.e. one point in the loop $q = (\vec{q}, \omega)$ equates to exactly one susceptibility value χ^q). Contrary the equation of motion is evaluated by **summing over** these points. For that reason an eom calculation only makes sense on a homogeneous q-grid over the full Brillouin zone. Therefore providing QDataFile disables the eom-feature making them mutually exclusive.

Summarized there are six (6) different major run options:

- calc-eom = T, calc-susc = T, KDataFile empty, QDataFile empty
 - → eom-evaluation on the k-grid with summation over q-grid and the bosonic frequencies (N4iwb).
 - \rightarrow susc-evaluation on the q-grid.
- calc-eom = T, calc-susc = T, KDataFile exists, QDataFile empty
 - → eom-evaluation along given k-points with summation over q-grid and the bosonic frequencies (N4iwb).
 - \rightarrow susc-evaluation on the q-grid.
- calc-eom = T, calc-susc = F, KDataFile empty, QDataFile empty
 - → eom-evaluation on the k-grid with summation over q-grid and the bosonic frequencies (N4iwb).
 - \rightarrow no susc-evaluation.
- calc-eom = T, calc-susc = F, KDataFile exists, QDataFile empty
 - → eom-evaluation along given k-points with summation over q-grid and the bosonic frequencies (N4iwb).
 - \rightarrow no susc-evaluation.
- calc-eom = F, calc-susc = T, KDataFile empty, QDataFile empty
 - \rightarrow no eom evaluation.
 - \rightarrow susc-evaluation on the q-grid.
- calc-eom = F, calc-susc = T, KDataFile empty, QDataFile exists
 - \rightarrow no eom evaluation.
 - \rightarrow susc-evaluation along the given q-points.

As a side note: If one does an eom calculation there is almost no computational penalty in also calculating the susceptibilities along the way. However full susceptibilities might need a lot of storage space.

In the [Atoms] group we define our local interactions (Udd, Vdd, Jdd, ...) and give information about the number of bands (Nd, Np). The band specification is the only mandatory configuration in this group. If we provide UFile above the interactions provided here get ignored.

In the [One-Particle] and [Two-Particle] groups we define our DMFT files. Here we must include the one particle file (1PFile) with the structure presented in Section 2 and the **symmetrized** vertex file (2PFile) together with its type (vertex-type).

In the *optional* group [Output] we may define additional output parameters. (There are also the *optional* groups [Debug] and [Verbose] available for configuration. Please check /documentation/configspec and the source code for further information)

One important thing to mention is that this config file is read by routines written in Fortran. Any kind of typos will not produce errors unless a check is imposed on that variable (Checks are mainly done for the existence of files and crucial run options).

Listings 7 and 8 contain example config files with the first and the sixth run option from the [General] group respectively. For a complete overview over all input options please check out /documentation/configspec where all options are described in detail.

Once the config file is prepared, we can run the program with the following commands, depending on whether the compilation was performed with or without MPI (colored text as user input).

Listing 6: abinitiodga run commands

```
with MPI:

$ mpirun -np #cores $ADGA_DIR/bin/abinitiodga config_file
without MPI:

$ $ADGA_DIR/bin/abinitiodga config_file
```

A recommendation for real (large) calculations: First start a full calculation on a single core in order to check whether the config file is complete and to get an estimation of the full run time. After one loop the out file (see Listing 9) prints the necessary time per loop together with the number of necessary loops. This gives an estimation of the full run time and the amount of parallelization necessary.

Listing 7: config file for q-grid calculation

```
[General]
# calculate the momentum-dependent susceptibilities
# calculate the dga-selfenergy via the equation of motion
calc-eom = T
NAt = 1 \# Number of atoms
# number of positive f/b frequencies used from the vertex
N4iwf = -1 \# full box
N4iwb = -1 \# full box
HkFile = srvo3_k20.hk # Wannier Hamiltonian
k-grid = 20 20 20 # Wannier Hamiltonian and eom grid - must be fixed at all times
q-grid = 20 20 20 # Grid we run our calculation on and susc grid
[Atoms] # fully local interaction parameters
[[1]]
Interaction = Kanamori
Nd = 3 \# number of d-bands
Np = 0 \# number of p-bands
Udd = 5.0
Vdd = 3.5
Jdd = 0.75
[One-Particle]
1 \text{ PFile} = \text{srvo} 3 - 1 \text{pg. hdf5} \# \text{DMFT} 1 \text{PG}
orb-sym = T
[Two-Particle]
2PFile = srvo3-2pg-symmetrized.hdf5 # symmetrized vertex
vertex - type = 0 \# 0: 2PGF, 1: chi_con, 2: chi
[Output]
text-output = T # additionally output the data in form of text-files
```

Listing 8: config file for q-path calculation

```
[General]
# calculate the momentum-dependent susceptibilities
calc-eom = F # must be turned off for q-path calculation
NAt = 1 \# Number of atoms
# number of positive f/b frequencies used from the vertex
N4iwf = -1 \# full fermionic box
N4iwb = 0 # only at w=0
HkFile = srvo3_k20.hk # Wannier Hamiltonian
k-grid = 20 20 20 # Wannier Hamiltonian and eom grid - must be fixed all times
# q-grid = 20 20 20 -- this gets ignored if we run with QDataFile
QDataFile = qpath_template
# this file can be found in /documentation/examples/qpath_template
Output = output-qpath
[Atoms] # fully local interaction parameters
[[1]]
Interaction = Kanamori
Nd = 3 \# number of d-bands
Np = 0 \# number of p-bands
Udd = 5.0
Vdd = 3.5
Jdd = 0.75
[One-Particle]
1 \text{ PFile} = \text{srvo} 3 - 1 \text{pg. hdf} 5 \# \text{DMFT 1PG}
orb-sym = T
[Two-Particle]
2PFile = srvo3-2pg-symmetrized.hdf5 # symmetrized vertex
vertex-type = 0 # 0: 2PGF, 1: chi_con, 2: chi
[Output]
text-output = T # additionally output the data in form of text-files
```

6 abinitiodga - output

The first thing created by abinitiodga is a log file called out in the output directory. This text file represents a basic log file, contains most of the run options and shows the progress of the calculation.

Listing 9: ADGA log file

```
Ab initio dynamical vertex approximation program (abinitiodga)
                        2 core(s) with
                                        20
                                                 20
                                                        20 k-points
   Running on
      time
                       date
                                      host
  114824.952
                   20171220
                                     132
one particle quantities in
srvo3-1pg.hdf5
two particle quantities in
srvo3-2pg-symmetrized.hdf5
Calculating with maximum number of fermionic frequencies =
                                                                 30
orb_symmetry = T
        10.00000000000000
beta=
      1.73411511496015
mu=
dc = (0.000000000000000E + 000, 0.0000000000000E + 000)
(0.000000000000000E+000,0.000000000000E+000)
(0.000000000000000E+000.0.0000000000000E+000)
(0.000000000000000E+000,0.000000000000E+000)
(0.000000000000000E+000,0.0000000000000E+000)
(0.000000000000000E+000,0.0000000000000E+000)
Reading giw from file. (The QMC green's function)
Creating U matrix from input parameters.
Running the calculation without V(q)
Frequency information:
iwmax=
 (number of fermionic matsubara frequencies of one-particle quantities)
iwfmax=
                 30 iwfmax_small=
                                           30
(number of fermionic matsubara frequencies of two-particle quantities)
                 30 iwbmax_small=
(number of bosonic matsubara frequencies of two-particle quantities)
k-point information:
       8000 \text{ k-points} in the mesh
         41 q-points in the q-path
mpi_distribute: average number of iqw points per rank (floored):
Constructing the local (frequency summed) susceptibilities from chi^{qvv'}_loc.
Writing hdf5 output to
output-qpath/adga-20171220-114824.952-output.hdf5
Starting the main loop:
To supress the progress indicator, use the verbose keyword Noprogress.
Core: 0 Completed qw-point:
                                                   20)
                                1 (from
                                            1 to
                                                       Time per point:
                                                                          0.7421
                                9 (from
Core: 0 Completed qw-point:
                                           1 to
                                                       Time per point:
                                                                          0.5335
                                                   20)
End of Program
```

Unless otherwise specified by text-output = T in the [Output] group the data produced by abinitiodga is put exclusively into a partially compressed HDF5 file (for a basic HDF5 introdution please visit /documentation/hdf5_intro.pdf). This data file contains, depending on the run options calc-eom and calc-susc, the following datasets:

Listing 10: ADGA HDF5 output format for a q-grid

Listing 10. ADOA THE Soutput format for a q-grid						
/input	Group					
/input/beta	Dataset	{SCALAR}				
/input/dc	Dataset	{NBANDS,	NSPINS }			
/input/giw	Dataset	{NBANDS,	2*NIW}			
/input/hk	Dataset	{NBANDS,	NBANDS,	NKX, N	NKY, NKZ}	
/input/iwbmax	Dataset	{SCALAR}				
/input/iwbmax_small	Dataset	{SCALAR}				
/input/iwfmax	Dataset	{SCALAR}				
/input/iwfmax_small	Dataset	{SCALAR}				
/input/iwmax	Dataset	{SCALAR}				
/input/mu	Dataset	{SCALAR}				
/input/n_dmft	Dataset	{NBANDS}				
/input/n_dmft_k	Dataset	{NBANDS,	NBANDS,	NKX, N	NKY, NKZ}	
/input/nkp	Dataset	{SCALAR}				
/input/nkpxyz	Dataset	{NBANDS}				
/input/nqp	Dataset	{SCALAR}				
/input/nqpxyz	Dataset	{NBANDS}				
/input/siw	Dataset	{NBANDS,	2*NIW}			
/occupation	Group					
/occupation/n_dga	Dataset	{NBANDS}				
/occupation/n_dga_k	Dataset	{NBANDS,	NBANDS,	NKX, N	NKY, NKZ}	
/ selfenergy	Group					
/selfenergy/loc	Group					
/selfenergy/loc/dga_ksum	Dataset	{NBANDS,	NBANDS,	2*N4IW	VF}	
/selfenergy/loc/dmft	Dataset	{NBANDS,	NBANDS,	2*N4IW	VF}	
/selfenergy/nonloc	Group					
/ selfenergy / nonloc / dga	Dataset	{NBANDS,	NBANDS,	NKX, N	NKY, NKZ,	2*N4IWF}
/selfenergy/nonloc/hartree_fock	Dataset	{NBANDS,	NBANDS,	NKX, N	NKY, NKZ,	2*N4IWF}
/ susceptibility	Group					
/susceptibility/loc	Group					
/susceptibility/loc/bubble_loc	Dataset	{NBANDS,	NBANDS,	2*N4IW	VB+1	
/susceptibility/loc/dens	Dataset	{NBANDS,	NBANDS,	2*N4IWB+1}		
/susceptibility/loc/magn	Dataset	{NBANDS,	NBANDS,	2*N4IWB+1}		
/susceptibility/nonloc	Group					
/susceptibility/nonloc/bubble_nl	Dataset	{NBANDS,	NBANDS,	NQX, N	NQY, NQZ,	2*N4IWB+1
/susceptibility/nonloc/dens	Dataset	{NBANDS,	NBANDS,	NQX, N	NQY, NQZ,	2*N4IWB+1
/susceptibility/nonloc/magn	Dataset	{NBANDS,	NBANDS,	NQX, N	NQY, NQZ,	2*N4IWB+1

Since full generalized susceptibilities have four orbital indices, they consume a massive amount of storage space. However, the physical spin and charge susceptibilities consist only of terms which have two pairs of equal indices, (i, i, j, j), which reduces the number of components from n_{dim}^4 to n_{dim}^2 . If nevertheless the output of all components is required, one has to set susc-full-output = T in the config group [Output]. If susceptibilities are calculated only for certain q-points, as specified in QDataFile, the q-points are written explicitly to /input/qpath and the susceptibility datasets have only one q-dimension.

The susceptibility output formats are shown in the following Listing:

Listing 11: susceptibility output comparison

```
Q-Path calculation - reduced (QDataFile = qpath)
/input/qpath
                                  Dataset {NQP}
/ susceptibility
                                  Group
/ susceptibility / loc
                                  Group
                                  Dataset {NBANDS, NBANDS, 2*N4IWB+1}
/ susceptibility /loc/bubble_loc
                                  Dataset {NBANDS, NBANDS, 2*N4IWB+1}
/ susceptibility / loc / dens
/susceptibility/loc/magn
                                  Dataset {NBANDS, NBANDS, 2*N4IWB+1}
/susceptibility/nonloc
                                  Group
/susceptibility/nonloc/bubble_nl Dataset {NBANDS, NBANDS, NQP, 2*N4IWB+1}
/susceptibility/nonloc/dens
                                  Dataset {NBANDS, NBANDS, NQP, 2*N4IWB+1}
                                  Dataset~\{NBANDS,~NBANDS,~NQP,~2*N4IWB+1\}
/susceptibility/nonloc/magn
Q-Path calculation - full (QDataFile = qpath)
                                  Dataset {NQP}
/input/qpath
/ susceptibility
                                  Group
/susceptibility/loc
                                  Group
/ susceptibility / loc / bubble_loc
                                  Dataset {NBANDS, NBANDS, NBANDS, NBANDS, 2*N4IWB+1}
/ susceptibility / loc / dens
                                  Dataset {NBANDS, NBANDS, NBANDS, NBANDS, 2*N4IWB+1}
/ susceptibility / loc/magn
                                  Dataset {NBANDS, NBANDS, NBANDS, NBANDS, 2*N4IWB+1}
/ susceptibility / nonloc
                                  Group
/susceptibility/nonloc/bubble_nl Dataset {NBANDS, NBANDS, NBANDS, NBANDS, NQP, 2*N4IWB+1}
/ susceptibility / nonloc / dens
                                  Dataset {NBANDS, NBANDS, NBANDS, NPANDS, NQP, 2*N4IWB+1}
                                  Dataset {NBANDS, NBANDS, NBANDS, NPANDS, NQP, 2*N4IWB+1}
/ susceptibility/nonloc/magn
Q-Grid calculation - reduced (q-grid = nqx, nqy, nqz)
/ susceptibility
                                  Group
/susceptibility/loc
                                  Group
/susceptibility/loc/bubble_loc
                                  Dataset {NBANDS, NBANDS, 2*N4IWB+1}
/susceptibility/loc/dens
                                  Dataset {NBANDS, NBANDS, 2*N4IWB+1}
/susceptibility/loc/magn
                                  Dataset {NBANDS, NBANDS, 2*N4IWB+1}
/ susceptibility / nonloc
                                  Group
/susceptibility/nonloc/bubble_nl Dataset {NBANDS, NBANDS, NQX, NQY, NQZ, 2*N4IWB+1}
                                  Dataset {NBANDS, NBANDS, NQX, NQY, NQZ, 2*N4IWB+1}
/ susceptibility / nonloc / dens
                                  Dataset {NBANDS, NBANDS, NQX, NQY, NQZ, 2*N4IWB+1}
/susceptibility/nonloc/magn
Q-Grid calculation - full (q-grid = nqx, nqy, nqz)
/ susceptibility
                                  Group
/susceptibility/loc
                                  Group
                                  Dataset {NBANDS, NBANDS, NBANDS, NBANDS, 2*N4IWB+1}
/ susceptibility / loc / bubble_loc
/susceptibility/loc/dens
                                  Dataset {NBANDS, NBANDS, NBANDS, NBANDS, 2*N4IWB+1}
/susceptibility/loc/magn
                                  Dataset {NBANDS, NBANDS, NBANDS, NBANDS, 2*N4IWB+1}
/ susceptibility / nonloc
                                  Group
/susceptibility/nonloc/bubble_nl Dataset {NBANDS, NBANDS, NBANDS, NBANDS, NQX, NQX, NQX, 2*N4IWB+1}
                                  Dataset {NBANDS, NBANDS, NBANDS, NBANDS, NQX, NQY, NQZ, 2*N4IWB+1}
/ susceptibility/nonloc/dens
/susceptibility/nonloc/magn
                                  Dataset {NBANDS, NBANDS, NBANDS, NBANDS, NQX, NQY, NQZ, 2*N4IWB+1}
```

Calculating the equation of motion on a given k-path (i.e. providing KDataFile) also changes the HDF5 output. In doing so, the k-summed quantities are not written to the output and the three k directions get collapsed down to one dimension:

Listing 12: equation of motion output comparison

```
K-Path calculation (KDataFile = kpath)
/input/kpath_eom
                                  Dataset {NKP_EOM}
/occupation
                                  Group
/occupation/n_dga_k
                                  Dataset {NBANDS, NBANDS, NKP_EOM}
/ selfenergy
                                  Group
/selfenergy/loc
                                  Group
/selfenergy/loc/dmft
                                  Dataset {NBANDS, NBANDS, 2*N4IWF}
/selfenergy/nonloc
                                  Group
/selfenergy/nonloc/dga
                                  Dataset {NBANDS, NBANDS, NKP_EOM, 2*N4IWF}
/selfenergy/nonloc/hartree_fock Dataset {NBANDS, NBANDS, NKP_EOM, 2*N4IWF}
K-Grid calculation (k-grid = nkx, nky, nkz)
/occupation
                                  Group
/occupation/n_dga
                                  Dataset {NBANDS}
/occupation/n_dga_k
                                  Dataset {NBANDS, NBANDS, NKX, NKY, NKZ}
/ selfenergy
                                  Group
/selfenergy/loc
                                  Group
                                  Dataset {NBANDS, NBANDS, 2*N4IWF}
/selfenergy/loc/dga_ksum
/selfenergy/loc/dmft
                                  Dataset {NBANDS, NBANDS, 2*N4IWF}
/selfenergy/nonloc
                                  Group
/selfenergy/nonloc/dga
                                  Dataset {NBANDS, NBANDS, NKX, NKY, NKZ, 2*N4IWF}
/ selfenergy / nonloc / hartree_fock
                                  Dataset {NBANDS, NBANDS, NKX, NKY, NKZ, 2*N4IWF}
```

7 abinitiodga - SrVO₃ test results

Finally, we present the results for the test data from the repository (/srvo3-testdata/). Using the config files in Listings 7 and 8, as well as the plot scripts found in /documentation/scripts/, we obtain the following results:

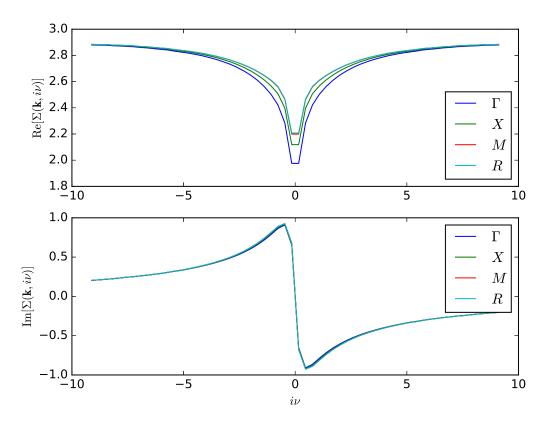


Figure 7.1: Selfenergy results for a q-qrid calculation evaluated at high symmetry points. The plot script can be found in /documentation/scripts/1D_plot_selfenergy.py

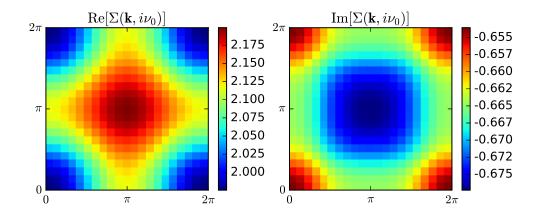


Figure 7.2: Selfenergy results for a q-qrid calculation in the $k_z=0$ plane. Please note that the Γ point is located at the bottom left corner. The plot script can be found in /documentation/scripts/2D_plot_selfenergy_plane.py

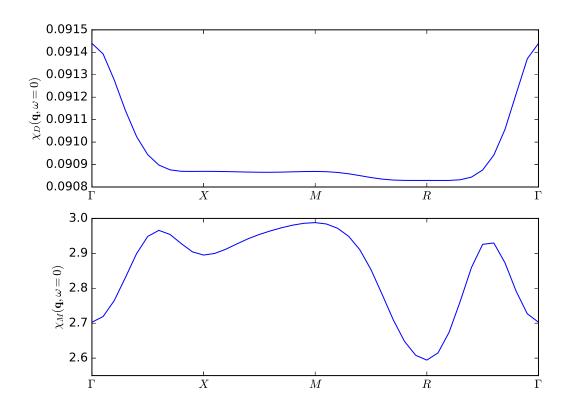


Figure 7.3: Susceptibility results for a q-path calculation. Please note that a prefactor of 2 is necessary to get the actual magnetic susceptibility. The plot script can be found in /documentation/scripts/1D_plot_qpath.py

Please note that these results are not identical to the ones found in arXiv:1710.06651, where we used much larger box sizes in combination with asymptotic vertex behaviour.