The AbinitioDΓA Project v1.0: Non-local correlations beyond and susceptibilities within dynamical mean-field theory: README (December 2017)

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1 Introduction

Diagrammatic extensions of dynamical mean field theory (DMFT) such as the dynamical vertex approximation (DΓA) allow us to include non-local correlations beyond DMFT on all length scales and proved their worth for model calculations. Here, we detail the implementation of an AbinitioDΓA approach. We go through each major step in the workflow and discuss the input and output data files (including their structure).

2 `w2dynamics` data

Starting point of any calculation is a converged DFT+DMFT solution, which we obtain from the package `w2dynamics`. The latter writes all output data into an HDF5 file, from which we extract the datasets `siw`,`dc`,`mu`, `beta` (self-energy, double counting correction, chemical potential, inverse temperature) and—depending on the run options—`giw` and/or `hk` (Green's function, Hamiltonian). The data structure of the `w2dynamics` output is shown in Listing 1. In order to keep these instructions as concise as possible, only the parts relevant for AbinitioDGA are shown. (Information about the full contents and structure of an HDF5 file can usually be retrieved via `h5ls -lr`.)

Listing 1: HDF5-structure of the DMFT output

```
/.axes/                              Group
/.axes/iw                            Dataset {2*NIW}
/.config                             Group
/dmft-001/                           Group
/dmft-001/ineq-001/                  Group
/dmft-001/ineq-001/siw               Group
/dmft-001/ineq-001/siw/value         Dataset {NBANDS, NSPINS, 2*NIW}
/dmft-001/ineq-001/giw               Group
/dmft-001/ineq-001/giw/value         Dataset {NBANDS, NSPINS, 2*NIW}
/dmft-001/ineq-001/dc                Group
/dmft-001/ineq-001/dc/value          Dataset {NBANDS, NSPINS}
/dmft-001/mu                         Group
/dmft-001/mu/value                   Dataset {SCALAR}
...
```

Please note that instead of actual numbers, we use upper-case variables here in order to keep the description general. `NIW` is the number of positive fermionic frequencies of the one-particle quantities, `NBANDS` is the number of correlated orbitals of the inequivalent atom `ineq-001`, and `NSPINS` is equal to 2.
On top of this DMFT solution, the impurity two-particle Green's function ("vertex") is computed within `w2dynamics`, which has the following structure: (again, groups not necessary for AbinitioDΓA are omitted here.)

Listing 2: worm-sampled vertex structure

```
/.axes/                                          Group
/.axes/iwb-g4                                    Dataset {2*N4IWB}
/.axes/iwf-g4                                    Dataset {2*N4IWF}
/worm-001/                                       Group
/worm-001/ineq-001/                              Group
/worm-001/ineq-001/g4iw-worm/                    Group
/worm-001/ineq-001/g4iw-worm/00001/              Group
/worm-001/ineq-001/g4iw-worm/00001/value         Dataset {2*N4IWF,2*N4IWF,2*N4IWB+1}
/worm-001/ineq-001/g4iw-worm/00001/error         Dataset {2*N4IWF,2*N4IWF,2*N4IWB+1}
...
/worm-001/ineq-001/g4iw-worm/NGRPS/              Group
/worm-001/ineq-001/g4iw-worm/NGRPS/value         Dataset {2*N4IWF,2*N4IWF,2*N4IWB+1}
/worm-001/ineq-001/g4iw-worm/NGRPS/error         Dataset {2*N4IWF,2*N4IWF,2*N4IWB+1}
...
```

`N4IWF` and `N4IWB` are the number of positive fermionic and bosonic Matsubara frequencies of the two-particle Green's function, respectively. `NGRPS` is the maximal number of band-spin combinations, $(2n_{dim})^4$. The group names in front of the `value` and `error` groups are integers from from 1 to NGRPS and represent a one-to-one mapping from a *band-spin combination* to an integer. ($00001 \rightarrow 1\uparrow, 1\uparrow, 1\uparrow, 1\uparrow,$) The number of existing groups can be calculated via

$$\text{density} - \text{density interactions}: \; N = n_{dim}^2 \times 6$$
$$\text{Kanamori parametrization}: \; N = \left[3n_{dim}^2 - 2n_{ndim}\right] \times 6,$$

where the factor 6 comes from all the possible SU(2) combinations allowed for a given band combination.

3 Fully nonlocal V(q) data

The $V(q)$ file creation is currently completely independent of the AbinitioDΓA package but it must respect a certain HDF5 structure, which will be explained by considering an example of a three-band system:

Listing 3: $V(q)$ file structure

```
/                          Group
/.axes                     Group
/.axes/Q-points            Dataset {8000, 3}
/00001                     Dataset {8000}
/00005                     Dataset {8000}
...
/00077                     Dataset {8000}
/00081                     Dataset {8000}
```

The `Q-points` dataset contains all q-point vectors starting from $(0, 0, 0)$ and going through all other points in the following manner (e.g., for a 20x20x20 q-mesh of the Brillouin zone):

$$
\begin{aligned}
i = 0 \quad & q = (0, 0, 0) \\
i = 1 \quad & q = (0, 0, 0.05) \\
& \vdots \\
i = 19 \quad & q = (0, 0, 0.95) \\
i = 20 \quad & q = (0, 0.05, 0) \\
i = 21 \quad & q = (0, 0.05, 0.05) \\
& \vdots \\
i = 399 \quad & q = (0, 0.95, 0.95) \\
i = 400 \quad & q = (0.05, 0, 0) \\
i = 401 \quad & q = (0.05, 0, 0.05) \\
& \vdots \\
i = 7999 \quad & q = (0.95, 0.95, 0.95)
\end{aligned}
$$

in units of 2π/lattice constant. The other groups then contain the V(q) information along this list of points for the specific band combinations. The transformation of band combination to an index

$$i_1, i_2, i_3, i_4 \rightarrow \text{index},$$

is achieved via

$$\text{index} = n_{dim}^3(i_1 - 1) + n_{dim}^2(i_2 - 1) + n_{dim}(i_3 - 1) + i_4,$$

where n_{dim} represents the number of correlated bands.

4 `setupvertex` - symmetrizing the vertex

In order to use the vertex it must first be symmetrized and transformed into the density and magnetic channels according to

$$G_d = \frac{1}{2}\left[G_{\uparrow\uparrow\uparrow\uparrow} + G_{\downarrow\downarrow\downarrow\downarrow} + G_{\uparrow\uparrow\downarrow\downarrow} + G_{\downarrow\downarrow\uparrow\uparrow}\right]$$

$$G_m = \frac{1}{2}\left[G_{\uparrow\downarrow\downarrow\uparrow} + G_{\downarrow\uparrow\uparrow\downarrow}\right],$$

where we additionally used the SU(2) symmetry. This symmetrization can be done with the `setupvertex` program. One simply has to execute this program and follow the instructions given.

Listing 4: exemplary setupvertex execution

```
$ $ADGA_DIR/bin/setupvertex
Number of inequivalent atoms: 1
Vertex file : srvo3-2pg-repo.hdf5
Number of correlated bands for inequivalent atom 1: 3
Outputfile for symmetrized Vertex: srvo3-2pg-symmetrized.hdf5

SU2 symmetry only (s) or SU2 AND orbital symmetry (o)?: o
```

This produces an HDF5 file of the following structure:

Listing 5: symmetrized vertex structure

```
/ineq-001                                Group
/ineq-001/dens                           Group
/ineq-001/00000                          Group
/ineq-001/00000/00001                    Group
/ineq-001/00000/00001/value              Dataset {2*N4IWF}
...
/ineq-001/magn                           Group
/ineq-001/00000                          Group
/ineq-001/00000/00001                    Group
/ineq-001/00000/00001/value              Dataset {2*N4IWF}
...
```

which is the centerpiece of the ADGA input. The group names in front of the `value` groups again represent a one to one mapping from a *band combination* to an integer. (00001 $\rightarrow$ (1, 1, 1, 1)). The group before that represents a bosonic frequency which is shifted so we start at 0 (00000) and go to 2*`N4IWB`.

5 abinitiodga - main program

The last preparational step is the configuring of ADGA. The main program's input options are contained in a config file (of arbitrary name). This config file is segmented into groups marked by squared braces. Subgroups are marked by double squared braces. In the [General] group we define what we want to calculate and how large our calculation should be (i.e. frequency box, momentum-space grid). In the [Atoms] group we define our local interactions and give information about the number of bands. In the [One-Particle] and [Two-Particle] group we define our files and in the [Output] group we define additional output parameters. One important thing to mention is that this config file is read by routines written in Fortran. Any kind of typos will not produce errors unless a check is imposed on that variable (Checks are mainly done for the existance of files and crucial run options).
Listing 7 contains an example config file. For a complete overview for all options please check out ADGA/documentation/configspec where all options are described in detail. Once the config file is prepared, we can run the program with the following commands, depending on whether the compilation was performed with or without MPI.

Listing 6: abinitiodga run commands

```
with MPI:
$ mpirun -np 3 $ADGA_DIR/bin/abinitiodga config_file
without MPI:
$ $ADGA_DIR/bin/abinitiodga config_file
```

Listing 7: example abinitiodga config file

```
[General]
# calculate the momentum-dependent susceptibilities
calc-susc = T
# calculate the dga-selfenergy via the equation of motion
calc-eom  = T

NAt = 1 # Number of atoms

# number of positive f/b frequencies used from the vertex
N4iwf = 30
N4iwb = 30

HkFile = srvo3_k20.hk # Wannier Hamiltonian

# hdf5 file with fully non-local interaction datasets
# the number of q-points must coincide with the q-grid argument
VqFile = vq_q20.hdf5

k-grid = 20 20 20 # Wannier Hamiltonian grid
q-grid = 20 20 20 # Grid we want to run our calculation on

[Atoms] # fully local interaction parameters
[[1]]
Interaction = Kanamori
Nd = 3 # number of d-bands
Np = 0 # number of p-bands
Udd = 5.0
Vdd = 3.5
Jdd = 0.75

[One-Particle]
1PFile = srvo3-1pg.hdf5 # DMFT 1PG
orb-sym = T

[Two-Particle]
2PFile = srvo3-2pg-symmetrized.hdf5 # symmetrized vertex
vertex-type = 0 # 0: 2PGF, 1: chi_con, 2: chi

[Output]
text-output = T # additionally output the data in form of text-files
```

6 abinitiodga - output

Unless otherwise specified by `text-output = T` in the [Output] group the data produced by abinitiodga is put into a partially compressed HDF5 file. This data file contains, depending on the run options `calc-eom` and `calc-susc`, the following datasets:

Listing 8: ADGA output format

```
/input                                  Group
/input/beta                             Dataset {SCALAR}
/input/dc                               Dataset {NBANDS, NSPINS}
/input/giw                              Dataset {NBANDS, 2*NIW}
/input/hk                               Dataset {NBANDS, NBANDS, NKX, NKY, NKZ}
/input/iwbmax                           Dataset {SCALAR}
/input/iwbmax_small                     Dataset {SCALAR}
/input/iwfmax                           Dataset {SCALAR}
/input/iwfmax_small                     Dataset {SCALAR}
/input/iwmax                            Dataset {SCALAR}
/input/mu                               Dataset {SCALAR}
/input/n_dmft                           Dataset {NBANDS}
/input/n_dmft_k                         Dataset {NBANDS, NBANDS, NKX, NKY, NKZ}
/input/nkp                              Dataset {SCALAR}
/input/nkpxyz                           Dataset {NBANDS}
/input/nqp                              Dataset {SCALAR}
/input/nqpxyz                           Dataset {NBANDS}
/input/siw                              Dataset {NBANDS, 2*NIW}
/occupation                             Group
/occupation/n_dga                       Dataset {NBANDS}
/occupation/n_dga_k                     Dataset {NBANDS, NBANDS, NKX, NKY, NKZ}
/selfenergy                             Group
/selfenergy/loc                         Group
/selfenergy/loc/dga_ksum                Dataset {NBANDS, NBANDS, 2*N4IWF}
/selfenergy/loc/dmft                    Dataset {NBANDS, NBANDS, 2*N4IWF}
/selfenergy/nonloc                      Group
/selfenergy/nonloc/dga                  Dataset {NBANDS, NBANDS, NKX, NKY, NKZ, 2*N4IWF}
/selfenergy/nonloc/hartree_fock         Dataset {NBANDS, NBANDS, NKX, NKY, NKZ, 2*N4IWF}
/susceptibility                         Group
/susceptibility/loc                     Group
/susceptibility/loc/bubble_loc          Dataset {NBANDS, NBANDS, 2*N4IWB+1}
/susceptibility/loc/dens                Dataset {NBANDS, NBANDS, 2*N4IWB+1}
/susceptibility/loc/magn                Dataset {NBANDS, NBANDS, 2*N4IWB+1}
/susceptibility/nonloc                  Group
/susceptibility/nonloc/bubble_nl        Dataset {NBANDS, NBANDS, NQX, NQY, NQZ, 2*N4IWB+1}
/susceptibility/nonloc/dens             Dataset {NBANDS, NBANDS, NQX, NQY, NQZ, 2*N4IWB+1}
/susceptibility/nonloc/magn             Dataset {NBANDS, NBANDS, NQX, NQY, NQZ, 2*N4IWB+1}
```

Since full generalized susceptibilities have four orbital indices, they consume a large amount of often unused storage space. However, the physical spin and charge susceptibilities consist only of terms which have two pairs of equal indices, (i, i, j, j), which reduces the number of components from n_{dim}^4 to n_{dim}^2. If nevertheless the output of all components is required, one has to set `susc-full-output = T` in the config group `[Output]`. If susceptibilities are calculated only for certain q-points, as specified in `QDataFile`, the q-points are written explicitly to `/input/qpath` and the susceptibility datasets have only one q-dimension.