



# Reference Manual for **I**nteracting **Q**uantum **I**mpurity **S**ystems Simulating **T**oolkit

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To my lovely wife X. Zhao

*L. H*

To my lovely girlfriend X.Y. Mao

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