

Reference Manual for Interacting Quantum Impurity Systems Simulating Toolkit

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To my lovely wife X. Zhao

L. H

To my lovely girlfriend X.Y. Mao

Y.L. Wang

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INTRODUCTION

1.1 What's iQIST?

The Interacting Quantum Impurity Solver Toolkit (dubbed iQIST) is an open source software package aiming to provide a full, reliable, flexible, and powerful tool chain for various quantum impurity models. It contains a few continuous-time quantum Monte Carlo impurity solvers (hybridization expansion version), a Hirsch-Fye quantum Monte Carlo impurity solver, and numerous prep-processed and post-processed tools. The iQIST is an all-in-one package. With it you can solve quantum impurity models and analyze the calculated results easily and efficiently.

1.2 Motivation

1.3 Software architecture

1.4 Main features

The iQIST is a powerful software package. It consists of many components (We just call the executable program as component in iQIST). The main components of iQIST is the continuous-time quantum Monte Carlo impurity solvers. So far these impurity solvers support the following features:

* Density-density interaction * General interaction * SOC interaction * Hubbard model and Hubbard-Holstein model * Frequency-dependent interaction * Orthogonal polynomial representation * Kernel polynomial representation * Improved estimator for self-energy * Single-particle Greens function $G(i\omega_n)$ * Two-particle correlation function $\chi(\omega,\omega',\nu)$ * Local irreducible

2 INTRODUCTION

vertex function $\Gamma(\omega, \omega', \nu)$ * Self-energy function $\Sigma(i\omega_n)$ * Histogram of perturbation expansion order * Kinetic and potential energies * (Double) occupation numbers, magnetic moment * Atomic state probability * Spin-spin correlation function * Orbital-orbital correlation function * Autocorrelation function and autocorrelation time * Divide-and-conquer algorithm * Sparse matrix multiplication * Good quantum numbers * Skip listing trick * Lazy trace evaluation * Dynamical truncation approximation

1.5 Development history

```
v0.2.0 // Aug ———
   * add bin/clean.sh * add doc/guide support in src/build/Makefile
   v0.1.9 // Aug 18, 2014 —
   * make new building/compiling system (src/build). * make setup shell script (bin/). * update
CSSL code (src/common/s_vector.f90). * refine azalea code (src/ctqmc/azalea). * refine ctqmc api
(src/ctqmc/api).
   v0.1.8 // Aug 4, 2014 —
   * add pansy code (experimental). * add manjushaka code (experimental). * add jasmine code
(experimental). * implement CSSL and CSML codes (experimental).
   v0.1.7 // Jul 2, 2014 —
   * add entropy code. * add stochastic code. * add swing code. * add toolbox code.
   v0.1.6 // Jul 2, 2014 —
   * add iris code.
   v0.1.5 // Jul 2, 2014 —
   * add daisy code.
   v0.1.4 // Jul 2, 2014 —
   * add lavender code.
   v0.1.3 // Jul 2, 2014 -
   * add begonia code.
   v0.1.2 // Jul 2, 2014 —
   * change the file mode for gardenia code.
   v0.1.1 // Jul 2, 2014 ——
   * change the file mode for azalea code.
   v0.1.0 // Jul 2, 2014 -
   * init the whole directory structure.
   v0.0.0 // Jul 2, 2014 —
   * init the project.
```

1.6 Policy and licences

The iQIST software package is released under the General Public Licence 3.0 (GPL) or later version. We are sorry. We DO NOT provide any technical support now. If you meet some problems when you are using iQIST. You can write a letter to us. But we can not guarantee we will reply you.

INSTALLATION

- 2.1 Obtain
- 2.2 Uncompress
- 2.3 Directory structures
- 2.4 Compiling environment

2.5 Compiling system

In order to compile and install iQIST correctly, you should ensure the following softwares are correctly installed and configured in your OS.

* Intel Fortran compiler * MPICH2 or OpenMPI * BLAS * LAPACK * Python 2.X * scipy, numpy, and f2py

The downloaded iQIST software package is likely a compressed file with zip or tar.gz suffix. The users should uncompress it at first. And then go to the iqist/src/build directory, edit the make.sys file to configure the compiling environment. Once the compiling environment is configured, please run the make command in the top-level directory of iQIST. After a few minutes (depending on the performance of compiling platform), the iQIST is ready for you. Note that all of the executable programs will be copied into the iqist/bin directory automatically. Please add this directory into the system environment variable PATH.

6 INSTALLATION

- 2.6 Build impurity solvers
- 2.7 Build auxiliary tools
- 2.8 Build documents
- 2.9 Build application programming interfaces

RUNNING

- 3.1 Configure your system
- 3.2 Create input files
- 3.3 Execute codes
- 3.4 Monitor and Profile

STANDARD INPUT FILES

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- 4.2 solver.eimp.in
- 4.3 solver.hyb.in
- 4.4 solver.anydos.in
- 4.5 solver.ktau.in
- 4.6 atom.cix

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- 5.2.2 solver.green.bin
- 5.2.3 solver.weiss.dat
- 5.2.4 solver.hybrid.dat
- 5.2.5 solver.grn.dat
- 5.2.6 solver.wss.dat
- 5.2.7 solver.hyb.dat
- 5.2.8 solver.sgm.dat
- 5.2.9 solver.hub.dat
- 5.2.10 solver.nmat.dat
- 5.2.11 solver.schi.dat
- 5.2.12 solver.ochi.dat
- 5.2.13 solver.twop.dat
- 5.2.14 solver.vrtx.dat

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- 6.3 isspn
- 6.4 isbin
- 6.5 isort
- 6.6 isvrt
- **6.7** isscr
- 6.8 nband
- 6.9 nspin
- 6.10 norbs
- 6.11 ncfgs
- 6.12 nzero
- **6.13** nvect
- C 1 4 mlarant

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AUXILIARY TOOLS

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7.3 Parquet component

APPLICATION PROGRAMMING INTERFACES

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- 8.2 Python binding
- 8.3 iqist.py

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*i*QIST IN ACTION

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9.5 Practical exercises

- 9.5.1 Orbital-selective Mott transition in two-band Hubbard model
- 9.5.2 Orbital Kondo and spin Kondo effects in three-band Anderson impurity

 $\underline{22} \hspace{2cm} \textit{INSIDE } i\textit{QIST}$

Chapter 10

${\bf INSIDE} \ \ {\it iQIST}$

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10.2.6	Truncation approximation
10.2.7	Lazy trace evaluation
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Appendix

A.1 TODO