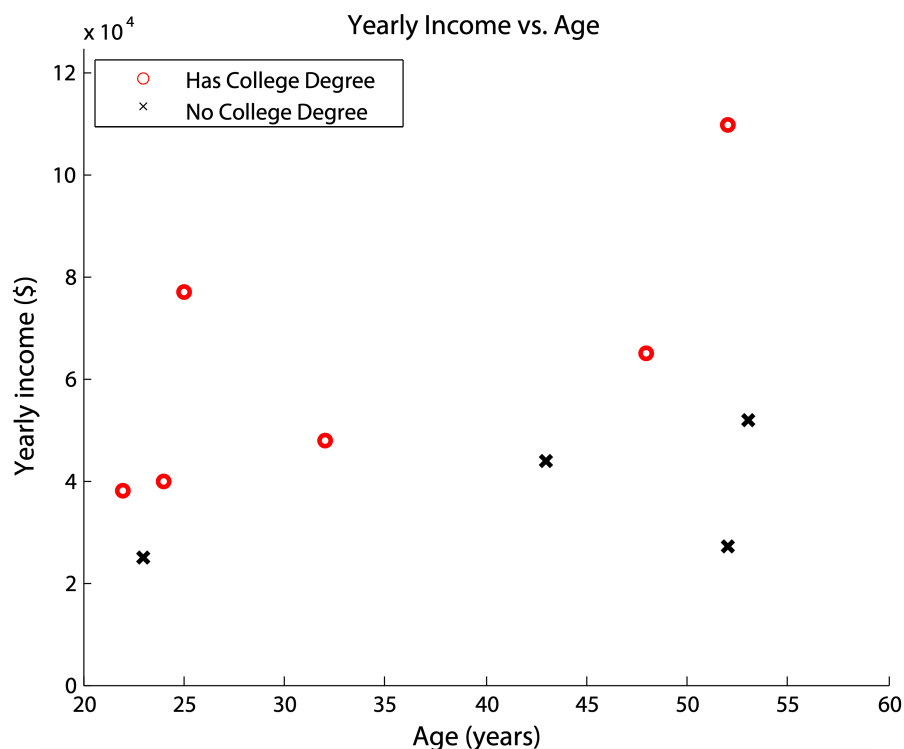


1. Consider the problem of predicting if a person has a college degree based on age and salary. The table and graph below contain training data for 10 individuals.

| Age | Salary | College Degree |
|-----|---------|----------------|
| 24 | 40,000 | Yes |
| 53 | 52,000 | No |
| 23 | 24,000 | No |
| 25 | 77,000 | Yes |
| 32 | 48,000 | Yes |
| 52 | 108,000 | Yes |
| 22 | 38,000 | Yes |
| 43 | 44,000 | No |
| 52 | 27,000 | No |
| 48 | 67,000 | Yes |



a. (3 points) Build a decision tree for classifying whether a person has a college degree by **greedily splitting attributes that maximize information gain** (Assume that the threshold for each split is **the middle value of the attribute in the current subset**). Show the information gain at each split and draw the decision boundary of your learned tree in the figure.

b. (2 points) A multivariate decision tree is a generalization of univariate decision trees, where more than one attribute can be used in the decision rule for each split. That is, splits need not be orthogonal to a feature's axis.

For the same data, provide a multivariate decision tree where each decision rule is a linear classifier that makes decisions **based on the sign of $\alpha x_{\text{age}} + \beta x_{\text{income}} - 1$** .

Draw your tree including the α , β and the information gain for each split. Draw the decision boundary.

c. (1 points) Draw the decision boundaries for the 1-nearest neighbor classifier assuming that we are using standard Euclidean distance to compute the nearest neighbors.

2. In this problem we'll use Naive Bayes to predict whether a person has a cold given the symptoms Headache, Cough, Sore Throat. Imagine we have observed the following data:

| Disease | Headache | Cough | Sore Throat |
|--------------------|----------|-------|-------------|
| <i>Cold</i> | T | T | T |
| <i>Cold</i> | T | T | T |
| <i>Cold</i> | T | F | F |
| \neg <i>Cold</i> | F | F | F |
| \neg <i>Cold</i> | F | F | F |
| \neg <i>Cold</i> | T | T | T |

- (2 points) Remember that when using Naive Bayes, we make the assumption that all features are conditionally independent given the target value. Factorize the joint probability $P(\text{Cold}, \text{Headache}, \text{Cough}, \text{Sore Throat})$ using this assumption.
- (2 points) Using no Laplacian smoothing, what is $P(\text{Cold} | \neg \text{Headache}, \text{Cough}, \text{Sore Throat})$?