# Writing Programs in Stata and Using them for the gmm Command

Roy Mill

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#### Motivation

- So, you know how to run OLS in Stata, but it's not enough for the job market.
- Programs are used to encapsulate code
  - Instead of rewriting the code for every program that needs the same functionality.
  - To be used by programs that leave "black boxes".
- Example: OLS. What you actually do is:
  - 1. Take all independent variables and put them under X.
  - 2. Take the dependent variable and put it in Y.
  - Remove observations that have a missing value in either variables.
  - 4. Calculate  $b = (X'X)^{-1} X'Y$ , the variance covariance matrix, t-tests, CI, and other statistics.
  - 5. Report everything.

But instead of having you write all this by yourself, it was encapsulated in a program called regress.

# Functions in Math and in Programming

- Just like programs, functions too encapsulate stuff.
  - Instead of writing  $\frac{c^{1-\sigma}}{1-\sigma}$  we write u(c).
  - If we think  $\sigma$  might vary, we write  $u(c, \sigma)$  (or  $u_{\sigma}(c)$  which is the same)
- Functions take arguments  $(c, \sigma)$  and return a value. In between they perform various operations.
- In programming, you do the same. Define the function, then you can call it and assign the returned value in the same line of code:

• Programs in Stata are not functions in the sense that you can't assign them to a value:

$$local R2 = r(R2)$$

#### What's in a Program?

• Suppose we define a CRRA function in pseudocode (not aimed at a programming language syntax):

```
function utility(consumption, sigma) {
   if (sigma == 1) {
      utils = log(consumption)
   } else {
      utils = consumption ^ (1-sigma) / (1-sigma)
   }
   return utils
}
```

- As always, whenever we write a function or a program we do three things:
  - 1. Define our list of arguments (our  $(c, \sigma)$ )
  - 2. Do something that depends on the arguments (calculate utility, regress variables, make coffee)
  - 3. Return something (or report to the user).

# What's in a Program?

• Some programs don't return anything:

#### compress

• Others don't take any arguments:

#### count

- Actually, count can take arguments, but they are optional:
   count if south == 1
  - We will now write a program that calculates CRRA utility and prints it to the screen.

# Our First Program (OMG!)

- Create a file named utility.ado.
  - Place it in your working directory (the one you "cd" into).
- Write the following code in it:

• Go to the command window in Stata and type: utility 4.

Utility for c=4 is -.25

#### Small ado-files notes

- When you type in the command utility. Stata:
  - 1. Looks for a program named utility that is already loaded into Stata's memory.
  - 2. If there is no program called utility in memory, Stata looks for a utility.ado file under a list of folders. One of them is the folder you "cd"-ed to.
- To see the list of folders Stata looks for the ado file in, type adopath
  - To add a folder to the list of folders, type adopath + <added folder>
- Note that after Stata read your ado file in step 2, next time it will find the program in step 1.
  - If you changed the ado file, type program drop utility before the next time you run it, to throw the program from Stata's memory.

# Getting Arguments for the Program

- There are two statements that tell the program how to expect the arguments
  - The args command for an ordered list of arguments.
  - The syntax command puts more structure on the arguments and makes them more Stata-like.
- The syntax of the args command:

```
args local1 [local2 [local3 [...]]]
```

• For example:

#### args consumption sigma

• This means that after we're done with the program, when we run in Stata the command:

#### utility 41 3

• Stata will run the program utility and assign 41 to 'consumption' and 3 to 'sigma' inside utility.

## Writing Generic Code

- We can write our program from above to be more generic
  - Not specific to  $\sigma = 2$ , but for any  $\sigma$ .

• Letting  $\sigma$  be determined freely by the user makes your program suit more purposes.

# Pros and Cons of Being Generic

#### • Pros:

- If you want other users to use, program solves a wider range of problems.
- If you want to change parameters to check sensitivity, no need to change the program.
  - Can loop easily over different values of  $\sigma$
- Overall, makes your code more reusable and do-files using this program easily adjustable.

#### Cons

- Input validation. What if someone runs utility 41 risky?
  - Should the program validate that the second argument is numeric?
  - When using the command syntax instead of args, Stata takes care of some validation
- Code can get cumbersome, or slower
  - We added the if condition to take care of  $\sigma = 1$ .

## Optional Arguments

- Actually, specifying k locals with args doesn't require the user to run the program with k arguments.
  - If given m > k arguments, Stata will ignore arguments k + 1 through m.
  - If given m < k arguments, Stata will have locals m+1 through k undefined (empty).
- So we can let the user only **optionally** set some arguments:

# Optional Arguments

- However, can't omit any subset of arguments. If you specified m arguments, then
  - the first m locals will have these arguments assigned to them respectively
  - the last k-m will be empty.
- In other words, can't omit consumption and specify sigma. First argument is always consumption.

# Specifying Arguments Using syntax

 Allows your program to receive input like most Stata commands

```
command [varlist | namelist | anything]
  [if] [in] [using filename]
  [= exp] [weight]
  [, options]
```

- Takes care of some input validation
  - If you say varlist, Stata will check that all arguments there are variables list
  - Can limit the number of arguments.
- Parses the user's input smartly and puts it in locals inside the program
  - If user adds a condition using if, or in
  - If the user specifies weights variable
  - If the user specifies a using file.

## An Example

- Suppose we write a program that calculates utility for each observation in our dataset. Name this program utilize.
  - It requires a variable containing consumption  $c_i$ .
  - It creates a new variable named utility containing  $u_i = \frac{c_i^{1-\sigma_i}}{1-\sigma_i}$
  - It assumes  $\sigma_i = 2$  for all observations.
- This is how the program will look like

```
program utilize
    syntax varlist(max=1)

local sigma = 2
    local newvarname = "utility"

gen 'newvarname' = 'varlist' ^ (1-'sigma') / (1-'sigma')
end
```

## An Example

- Good. Now allow the program to do more
  - Specify a different name for the generated variable.
  - Allow  $\sigma_i$  to be another (still fixed)  $\sigma$ , but not 2 necessarily.
- This is how the program will look like now

```
program utilize
    syntax varlist(max=1) [, newvarname(name) sigma(real 2)]
    if ("'newvarname'" == "") {
        local newvarname = "utility"
    }
    gen 'newvarname' = 'varlist' ^ (1-'sigma') / (1-'sigma')
end
```

• Had we wanted to make newvarname required, we could have rewriten the syntax line as follows:

```
syntax varlist(max=1) , newvarname(name) [sigma(real 2)]
```

## Tweaking it a bit more

- Now, allow the program to optionally receive a variable name containing an *i*-specific  $\sigma_i$ .
  - Only if the second variable name is missing, assume  $\sigma_i = 2$  for all observations.
  - If the  $\sigma_i$  variable is specified, assume  $\sigma_i = 2$  only for observations with missing  $\sigma_i$ .
  - Allow the user to specify a different default  $\sigma$ .
- The program now becomes a bit longer...

## Tweaking it a bit more

```
program utilize
    syntax varlist(max=2) [, newvarname(name) sigma(real 2)]
   if ("'newvarname'" == "") {
       local newvarname = "utility"
   local consumpvar : word 1 of 'varlist'
   local sigmavar : word 2 of 'varlist'
    if ("'sigmavar'" != "") {
        gen 'newvarname' = 'consumpvar' ^ (1-'sigmavar') / (1-'sigmavar') ///
                                                  if 'sigmavar' != .
        replace 'newvarname' = 'consumpvar' ^ (1-'sigma') / (1-'sigma') ///
                                                  if 'sigmavar' == .
    else {
        gen 'newvarname' = 'consumpvar' ^ (1-'sigma') / (1-'sigma')
end
```

## Passing Conditions to Your Program

• You can allow (or require) to specify a condition using if:

- The / after the if tells Stata to put inside the local if only the condition that is specified when the program is called.
- Without the / Stata will add the "if" word.
- Example: suppose I run utilize consumption if female==0
  - If I have if / in the syntax line, then 'if' contains
     "female==0"
  - If I have if in the syntax line, then 'if' contains "if female==0"

# Small Comments about Programs in General

- version # statement
  - Usually invoked before the syntax or args command
  - Tells Stata to be compatible with the version in which you wrote the program.

```
program utilize
    version 11
    syntax varlist(max=2) [, newvarname(name) sigma(real 2)]

// rest of program
end
```

- Scope (locals vs globals)
  - Locals set outside the program can't be used inside the program.
  - Locals set inside the program can't be used outside the program.
  - Globals set anywhere can be reached from anywhere.

# Small Comments about the syntax Command

- You can specify on-off options that don't take additional arguments.
  - They will contain their own names if they were specified or nothing if not

```
program savesomething
   syntax varlist using [, replace]

// 'replace' contains the string "replace" if specified. "" otherwise.
   if ("'replace'" != "") {
        di "replace option was specified."
   }
end
```

• You can specify shorthands for your options capitalizing the letters of the shorthand.

```
syntax varlist(max=2) [, Newvarname(name) SIgma(real 2)]
    // rest of program

// outside the program, we can call the program this way:
utilize consumption, n(calcuated_util) si(3)
```

# Returning Values from a Program

• We said that unlike functions, programs in Stata can't be assigned as an expression:

```
gen util = utility(consumption) // This is wrong!
```

- You can generate variables inside programs (like we did in utilize)
- You can also return values like other Stata programs do:
  - return list after you run an r-class program will show you the returned values
  - ereturn list will do the same for e-class programs.
- Perfect for returning different statistics or estimation results.
- eclass programs perform estimation. Other programs should be rclass.

## Returning Values from a Program

• Suppose now we want utility to return the result too, and not just print it out.

```
program utility, rclass
    // everything else as before (calculating the local 'utils')
    return scalar utility = 'utils'
    matrix input = ('consumption', 'sigma')
    return matrix arguments = input
end
// Outside the program
utility 41 3
di "The program returned " r(utility)
matrix list r(arguments)
```

- If the program is an e-class program, just specify eclass instead of rclass at the top, and use ereturn instead of return.
- See help return for further details.

## With a little help from my Stata

- There is no time to go through everything that syntax lets you do.
- Moreover, you will probably get the invalid syntax r(197); error hundreds of times.
- Stata is your friend. Well, maybe not. But let it help you.
  - Always work with a window of help syntax open.
  - Same for help return

#### GMM Estimation in Stata 11

- As of version 11, Stata has a gmm command that allows to directly estimate GMM models.
- You can specify your equations using either substitutable expressions or moment-evaluator programs.
- Both methods are used in other commands in Stata such as ml (maximum likelihood) or nl (nonlinear LS).
- The main focus of these slides is not the econometrics, but the ability to implementing equations to code.
- We will use what we learned about programs above to write a moment-evaluator program.
- As always, more help in help gmm.
  - Many examples and more details in the manual pages (That's the PDF file you get when you click on Manual: [R] gmm at the bottom of the Stata help window)

## GMM Quick Reminder

• A model that yields moment equations of the form:

$$\mathbb{E}\left[\mathbf{z}_{i}\cdot u_{i}\left(\beta\right)\right]=0$$

if  $u_i$  is an additive error in the model, or more generally:

$$\mathbb{E}\left[h_i\left(\mathbf{z}_i,\beta\right)\right] = 0$$

where:

- $\beta$  is a vector of parameters we're interested in estimating using these moment equations.
- $\mathbf{z}_i$  is a vector of instruments: variables that satisfy the moment condition.
- Numerically look for a  $\hat{\beta}$  that minimizes the (weighted) distance of the sample-analogues from 0.
- Use derivatives of  $\frac{\partial u_i}{\partial \beta}$  or  $\frac{\partial h_i}{\partial \beta}$  to calculate  $\widehat{Var}\left(\hat{\beta}\right)$  (and to find  $\hat{\beta}$ ).

# Estimating GMM Using Substitutable Expressions

 Suppose I try to estimate the following nonlinear (and stupid) model for cars' MPG

$$MPG_i = \alpha \left(WEIGHT_i\right)^{\beta} \left(LENGTH_i\right)^{\gamma} + u_i$$

- We have 3 parameters:  $(\alpha, \beta, \gamma)$  and 3 instruments: weight, length and a constant term.
- Let's rewrite the equation for  $u_i$  and specify  $z_i$ :

```
gmm (mpg - {alpha=1}*weight^{beta=1}*length^{gamma=1}) ///
, instruments(weight length)
```

- Parameters are in curly brackets. Initial values can be specified with =.
  - Stata will substitute the curly brackets with the current iteration's value of the parameter.
- Instruments were specified using the instruments option.

  Constant term added by default.

#### One more time

• Suppose our crazy theory says that:

$$HEADROOM_i = \exp(\beta_0 + \beta_1 TRUNK_i + \beta_2 MPG_i) + v_i$$

- Also, we think  $MPG_i$  is correlated with the error so we use  $LENGTH_i$  and  $WEIGHT_i$  as instruments.
- This means that we believe our moment conditions are:

$$\mathbb{E}\left[\begin{array}{c} v_i \\ TRUNK_iv_i \\ LENGTH_iv_i \\ WEIGHT_iv_i \end{array}\right] = 0$$

• All we need to do is to express  $v_i$  in an equation:

$$v_i = HEADROOM_i - \exp(\beta_0 + \beta_1 TRUNK_i + \beta_2 MPG_i)$$

• And then run:

```
gmm (headroom - exp({b0} + {b1}*trunk + {b2}*mpg)) ///
, instruments(trunk weight length)
```

# Another way to specify initial values for the parameters

Initial values can be specified using the from option.

- Will override any initial values set with {param=value}
- Can pass a name of a vector of values:

```
matrix initials = (.01, .2, .1)
gmm ... , instruments(...) from(initials)
```

• Alternatively, can list parameters and their values:

```
gmm ..., instruments(...) from(alpha .01 beta .2 gamma .1)
```

# Another way to specify linear combinations

Linear combinations can be specified using the: operator

• Instead of writing:

```
gmm (headroom - exp({b0} + {b1}*trunk + {b2}*mpg)), ...
can write:
gmm (headroom - exp({b0} + {xb: trunk mpg})), ...
```

- Constant terms are not included, so we added {b0}.
- The xb is just a name, can put anything there: {mylincom: trunk mpg}
- We can refer to the same linear combination again:
  - Suppose we had a model that looked like:

$$\mathbb{E}\left\{\mathbf{z}\frac{y - \exp\left(\mathbf{x}'\beta\right)}{\exp\left(\mathbf{x}'\beta\right)}\right\} = 0$$

Then we should write (assume no constants, for simplicity):

```
gmm ((y - exp({lin: x1 x2 x3}))/exp({lin:})), ...
```

# Weighing Moment Conditions

• As you remember, the actual GMM estimator looks roughly like this

$$\hat{\beta}_{GMM} = \arg\min_{\beta} \left( U(\beta)' Z \right) W(Z'U(\beta))$$

- If you're just-identified, the weighting matrix doesn't matter.
- If you're overidentified, then you need to choose a weighting matrix.
- Stata by default:
  - Runs once with  $W = (Z'Z)^{-1}$  (like 2SLS).
  - Then, using the predicted  $\hat{U}$ , Stata allows for heteroskedastic u's and re-estimates using  $W = \left(\hat{U}'ZZ'\hat{U}\right)^{-1}$
  - Stata by default reports the result of the second estimation.

# Changing the Default Weighting Scheme

- To change the initial weighting matrix from Z'Z, use the winitial option.
- To change the way the weighting matrix is recalculated, use the wmatrix option.
  - Can take heteroskedasticity and autocorrelation (HAC), or clusters, into account. Can assume homoskedasticity instead.
- To change the number of times GMM is estimated (from the default twice), use:
  - onestep for only one estimation (to replicate 2SLS, say)
  - twostep is default
  - igmm allows for more iterations. Other options are required though. See help.

# Specifying Analytical Derivatives

- Derivatives are used for minimizing the distance function and for calculating variance matrix.
- By default, Stata numerically calculates the Jacobian.
  - Basically, looking at the change in the function value following a small change of each parameter.
- Numerical derivatives are usually fine. But you can specify analytical derivatives.
  - More accurate, and makes optimization faster.
  - Can specify  $\frac{\partial u_i}{\partial \beta}$  using the derivative option.
  - If you do, need to specify all derivatives in model.
- More on this in the help file and the manual (p. 593)

# Optimization Options

- You can change the settings of the optimization gmm does each time it estimates.
- technique(nr) will change the optimization technique from Gauss Newton (default) to modified Newton-Raphson (nr).
  - dfp, bfgs also allowed for the gmm command.
- <2->conv\_maxiter(1000) will set the maximum number of iterations to 1000.
  - This is not the GMM iterations! These are the iterations in the search for the minimizing  $\hat{\beta}$ .
  - GMM iterations are the ones that update the weighting matrix after errors are estimated.
- <3->conv\_ptol(), conv\_vtol(), conv\_nrtol(), tracelevel() also available for you to set.

# Estimating Multiple Equations Simultaneously

- Estimating one equation is for kids. You will never get a good placement if you estimate just one equation.
- If we assume there's covariance between the errors of the equations, it's better to estimate them jointly:

$$\mathbb{E}\left[\begin{array}{c} z_{u}u\\ z_{v}v \end{array}\right] = \mathbb{E}\left[\begin{array}{c} z_{u}\left(MPG_{i} - \alpha\left(WEIGHT\right)^{\beta}\left(LENGTH\right)^{\gamma}\right)\\ z_{v}\left(HEADROOM - \exp\left(\beta_{0} + \beta_{1}TRUNK + \beta_{2}MPG\right)\right) \end{array}\right] = 0$$

- We can use the same instruments for all equations, or we can differ  $z_n$  from  $z_v$ .
- For now, assume the same instruments for both equations. Just add the equation.

# Initial Weighting Matrix with Simultaneous Equations

- All we did was to add the 2nd equation in a separate parentheses.
- Recall that Stata by default sets the initial weighting matrix to be  $W = \left(\frac{1}{n} \sum_{i=1}^{n} z_i' z_i\right)^{-1} = \Lambda^{-1}$ .
- When you have m equations,  $z_i$  contains all equations'  $z_i = (z_{i1}, ..., z_{im})$ 
  - They can be identical, in which case they are copied.
- $\Lambda$  now is composed of blocks according to the equation. For equations r,s we get:

$$\Lambda_{rs} = n^{-1} \sum_{i=1}^{n} z'_{ir} z_{is}$$

• If you have a common instrument in all equations,  $\Lambda$  will not be positive-definite.  $W = \Lambda^{-1}$  must be positive-definite.

# Initial Weighting Matrix with Simultaneous Equations

#### Possible solutions:

- 1. Impose  $\Lambda_{rs} = 0$  in the initial matrix by adding the independent suboption: winitial(unadjusted, independent)
- 1. Impose a different (and positive-definite) initial weighting matrix.
  - 1.1 One straightforward positive-definite matrix is the identity matrix winitial(identity)
    - 1.1.1 Usually performs badly longer convergence.
  - 1.2 Alternatively, construct any matrix and impose it:

```
matrix W = ...
gmm ... , winitial(W)
```

• In any case, the second iteration of GMM doesn't have to impose these restrictions. Weighting matrix is recalculated next iteration and usually is fine.

# Specifying Different Instruments for Different Equations

• If equations are not named  $\Rightarrow$  identified by their order.

• Alternatively, we can name the equations.

- Note how colon inside () follows equation name and colon inside {} follows linear combination name
- When specifying instruments
  - No equation specified ⇒ apply instruments to all equations
  - Can apply additional instruments to a subset of equations

# Using GMM in the Moment-Evaluating Program Mode

- We can't always express the error as a function of variables and parameters.
  - Sometimes our moments are more complicated.
- As in the manual, following Blundell, Griffith and Windmeijer (2002), we have:

$$y_{it} = \exp\left(\mathbf{x}_{it}^{'}\beta\right)\nu_i + \epsilon_{it} = \mu_{it}\nu_i + \epsilon_{it}$$

where  $\nu_i$  is a multiplicative unobservable fixed-effect and we're interested in  $\beta$ 

• We can estimate our betas by replacing  $\nu_i$  with  $\frac{\bar{y}_i}{\bar{\mu}_i}$ , creating the following moment conditions (sample analogues):

$$\sum_{i} \sum_{t} \mathbf{x}_{it} \left( y_{it} - \mu_{it} \frac{\bar{y}_i}{\bar{\mu}_i} \right) = 0$$

- You can't write a substitutable expression that will do that.
- Luckily, we already know how to write programs!

# A Moment-Evaluator Program's Possible syntax

syntax varlist if [weight], at(name) [derivatives(varlist)] [options]

- varlist will contain the variable names into which the program is supposed to save  $u_i$
- if will hold the sample of observations that enter the analysis
  - Stata will take care of removing any observations with a missing value in one of the variables.
- at will get a name of a vector of the current iteration's  $\hat{\beta}$ .
- weight allows gmm to pass pweights, fweights or aweights specified by the user.
- derivatives allows the program to save analytical derivatives in additional variables.
- options are any other options your program potentially needs from gmm.

## A Simple Moment-Evaluating Program

• Write a program to evaluate the moments of the first example:

```
MPG_i = \alpha (WEIGHT_i)^{\beta} (LENGTH_i)^{\gamma} + u_i
```

- Note the use of varlist. The program is expecting one variable to hold the *u* it calculates.
- Also, 'at' contains a name of a vector that holds the values of the current  $\hat{\alpha}, \hat{\beta}, \hat{\gamma}$

# Adding Derivatives

```
program gmm_cobbdoug
    syntax varlist if, at(name) [derivatives(varlist)]
   quietly replace 'varlist' = ( mpg - 'at'[1,1] * weight^('at'[1,2]) * ///
                              length^('at'[1,3])) 'if'
   if ("'derivatives'" == "") { // if derivatives unnecessary
        exit
   local d var 1 : word 1 of 'derivatives'
   local d var 2 : word 2 of 'derivatives'
   local d_var_3 : word 3 of 'derivatives'
    qui replace 'd_var_1' = -1 * weight^('at'[1,2]) * length^('at'[1,3]) 'if'
    qui replace 'd_var_2' = -1 * 'at'[1,1] * log(weight) * ///
                               weight^('at'[1,2]) * length^('at'[1,3]) 'if'
    qui replace 'd_var_3' = -1 * 'at'[1,1] * log(length) * ///
                               weight^('at'[1,2]) * length^('at'[1,3]) 'if'
end
// outside the program
matrix initial = (1, 1, 1)
gmm gmm_cobbdoug, nequations(1) parameters(alpha beta gamma) ///
     instruments(weight length) from(initial) hasderivatives
```

## Generalizing our Program

• We can make the program estimate any equation of the form:

$$y = \beta_0 x_1^{\beta_1} x_2^{\beta_2} \cdot \dots \cdot x_k^{\beta_k} + u$$

```
program gmm_cobbdoug
    syntax varlist if, at(name) lhs(varname) rhs(varlist) [derivatives(varlist)]
    local j = 2 // 'at'[1,1] is the multiplicative term, start with 'at'[1,2]
    local factor str ""
    foreach var of varlist 'rhs' {
        if ('i' > 2) {
             local factor str "'factor str' * "
        local factor_str "'factor_str', 'var', ('at', [1, 'i'])"
        local '++j' // equivalent to local j = 'j' + 1
    quietly replace 'varlist' = 'lhs' - 'at'[1,1] * 'factor_str' 'if'
    // Derivatives part on next slide...
```

## Generalizing our Program

```
// continued from last slide ...
   if ("'derivatives'" == "") { // if derivatives unnecessary
         exit
   local j = 1
    foreach var of varlist 'derivatives' { '
        if ('i' == 1) {
            qui replace 'var' = -1 * 'factor_str' 'if'
        else {
            local rhs_counter = 'j' - 1
            local curvar : word 'rhs_counter' of 'rhs'
            qui replace 'var' = -1 * 'at'[1,1] * log('curvar') * 'factor_str' '
       local '++j' // equivalent to local j = 'j' + 1
end
```

# Summary

- Programs allow you to encapsulate code and use it from multiple do-files or the command line.
- The new gmm command lets you estimate GMM models flexibly.
  - With substitutable expression you can estimate a system of equations with one (long) line of code.
  - With moment-evaluating programs you can increase functionality.
- Two help files will be your best guides, except for these magnificent slides
  - help syntax for how to get inputs to your program.
  - help gmm (but mainly the manual page) for how to translate your GMM model to code.