



Figure 1: elliptic curves examples

Notes of a presentation.
All prime factors of $n! + 1$ is greater than n

$$\begin{aligned}\Pi(x) &= \{p \leq x, p \in Prime\} \quad x \rightarrow \infty \\ \Pi(x) &\sim \frac{x}{\ln x} \text{ as } x \rightarrow \infty \\ \text{Riemann } \zeta \\ \xi(s) &= \Gamma(s/2 + 1)(s - 1)\Pi^{-s/2}\zeta(s) \tag{0-0-1}\end{aligned}$$

狄利克莱积分
perron formula

Selberg’s identity

$$\sum_{p \leq x} \log p + \sum_{pq \leq x} \frac{\log p \times \log q}{\log x} = 2x + O\left(\frac{x}{\log x}\right)$$

Erdős

$$x^n + y^n = z^n \tag{0-0-2}$$

1^{er} Case

$$xyz \equiv 0(\text{mod}n)$$

只用证明n为素数的情况

GL1, GL2

elliptic curves 整数落点

Modular form 模形式是数学上一个满足一些泛函方程与增长条件、在上半平面上的（复）解析函数。因此，模形式理论属于数论的范畴。模形式也出现在其他领域，例如代数拓扑和弦理论。

$$f\left(\frac{az+b}{cz+d}\right) = (cz+d)^k f(z) \tag{0-0-3}$$

$$a^n + b^n = z^n$$

$$y^2 = x(x - a)(x - b)$$

不存在module form

Andrew Wiles

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